

# *Computer Simulation of Liquids*

## Michael P. Allen and Dominic J. Tildesley

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List of errata up to March 21, 2023

Line numbers below do not include section headings, equations, figures etc.  
Negative line numbers are counted up from the bottom of the page.

### Chapter 1

**p11**  $\ell -16$  ‘It quite possible’  $\rightarrow$  ‘It is quite possible’.

F Perez  
2017-10-07  
MPA  
2017-04-04

**p14** In eqn (1.15) the signs of the odd-order terms are wrong:

$$+T_\alpha \rightarrow -T_\alpha \quad \text{and} \quad +\frac{1}{3}T_{\alpha\beta\gamma} \rightarrow -\frac{1}{3}T_{\alpha\beta\gamma}.$$

**p15** In eqn (1.20),  $T_{\alpha\beta} \rightarrow T_{\alpha\beta}^{ab}$ . In eqn (1.21),  $A_{\alpha\beta} \rightarrow A_{\alpha\beta}^{ab}$ .

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**p17** In eqn (1.22),  $B_{\alpha\beta} \rightarrow B_{\alpha\beta}^{ab}$ ,  $T_{\alpha\beta} \rightarrow T_{\alpha\beta}^{ab}$ ,  $(\alpha^a)^{-1} \rightarrow (\alpha^a)_{\alpha\beta}^{-1}$ .

In eqn (1.23) and  $\ell 15$ ,  $\tilde{T}_{\alpha\beta} \rightarrow \tilde{T}_{\alpha\beta}^{ab}$ . Also in this equation the factor  $4\pi\epsilon_0$  should be omitted for consistency with eqn (1.17).

MPA  
2019-07-30  
Bian Li  
2022-04-02

**p35**  $\ell 11$ , ‘see Chapter 13’  $\rightarrow$  ‘see Chapter 14’.

**p36**  $\ell 7$ ,  $v(r) \sim r^3 \rightarrow v(r) \sim r^{-3}$ .

$\ell 8$ , ‘Chapter 5’  $\rightarrow$  ‘Chapter 6’.

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2019-07-30  
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2019-07-30

**p42**  $\ell 3$  Remove sentence ‘Some of these methods ... Appendix A.’

### Chapter 2

**p55** In eqn (2.35),  $N_n \rightarrow N_c$ ; in eqns (2.35), (2.36) and  $\ell -4$ ,  $\mu_n \rightarrow \mu_c$ .

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2019-07-22

**p66**  $\ell 19$ ,  $k_B T/V\beta_T \rightarrow k_B T/V\beta_S$ .

**p67**  $\ell 2$ , ‘(eqn (2.82))’  $\rightarrow$  ‘(eqn (2.62))’.

$\ell 8$ , between eqns (2.85) and (2.86), ‘viral’  $\rightarrow$  ‘virial’.

MPA  
2019-08-13  
MPA  
2019-07-18

## Chapter 3

A Fleury  
2018-08-02

**p116** All the masses in eqns (3.49ab) should be raised to the power  $-1$ :

$$\begin{aligned}\mathbf{r}_{12}(t + \delta t) &= \mathbf{r}'_{12}(t + \delta t) + (m_1^{-1} + m_2^{-1})\lambda_{12}^{(r)}\mathbf{r}_{12}(t) - m_2^{-1}\lambda_{23}^{(r)}\mathbf{r}_{23}(t) \\ \mathbf{r}_{23}(t + \delta t) &= \mathbf{r}'_{23}(t + \delta t) - m_2^{-1}\lambda_{12}^{(r)}\mathbf{r}_{12}(t) + (m_2^{-1} + m_3^{-1})\lambda_{23}^{(r)}\mathbf{r}_{23}(t).\end{aligned}$$

The same correction should be applied to eqns (3.53ab); in addition, all the bond vectors in eqns (3.53ab) should be evaluated at  $t + \delta t$ :

$$\begin{aligned}\mathbf{v}_{12}(t + \delta t) &= \mathbf{v}'_{12}(t + \delta t) + (m_1^{-1} + m_2^{-1})\lambda_{12}^{(v)}\mathbf{r}_{12}(t + \delta t) - m_2^{-1}\lambda_{23}^{(v)}\mathbf{r}_{23}(t + \delta t) \\ \mathbf{v}_{23}(t + \delta t) &= \mathbf{v}'_{23}(t + \delta t) - m_2^{-1}\lambda_{12}^{(v)}\mathbf{r}_{12}(t + \delta t) + (m_2^{-1} + m_3^{-1})\lambda_{23}^{(v)}\mathbf{r}_{23}(t + \delta t)\end{aligned}$$

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**p120**  $\ell$  14 ‘eqn (2.161)’  $\rightarrow$  ‘eqn (2.167)’.

MPA  
2023-02-11

**p131**  $\ell$  19, the sentence should read: ‘It is relatively straightforward to combine it with constraint algorithms (Ryckaert and Ciccotti, 1986); see, however, Peters et al. (2014).’

MPA  
2023-03-21

**p139**  $\ell$  –3, the last 3 sentences of section 3.8, beginning with ‘Also...’, should be replaced by: ‘Also, the distribution is not canonical (it may tend to isokinetic as  $\tau \rightarrow 0$  and microcanonical as  $\tau \rightarrow \infty$  (Morishita, 2000)). Recently it has been shown that these equations of motion do not preserve *any* distribution (Petersen and Searles, 2022). The Berendsen thermostat is quite widely used, but in view of the risk of generating incorrect results (see e.g. Braun et al., 2018), alternatives are to be preferred.’

MPA  
2017-04-30  
2019-08-21

**p141** In the equation at the top of the page the sign of  $\mathbf{r} \cdot \mathbf{f}$  is wrong, and a factor  $1/dV$  was omitted from the correction term:

$$\mathcal{P}' = \mathcal{P} + (1/gV)\mathbf{p} \cdot \mathbf{p}/m = \frac{1}{dV}(\alpha\mathbf{p} \cdot \mathbf{p}/m + \mathbf{r} \cdot \mathbf{f}) - \frac{\partial\mathcal{V}}{\partial V}.$$

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2017-04-30

**p142** The expression for  $iL'_2$  should have a factor of  $d$ :

$$iL'_2 = d(\mathcal{P}' - P)V \frac{\partial}{\partial p_\epsilon}.$$

MPA  
2019-08-14

**p145** In the equations,  $T_{\alpha\beta} \rightarrow T_{\alpha\beta}^{ab}$  and  $|\mathbf{p}_{\mu^a}|^2/m_{\mu^a} \rightarrow |\mathbf{p}_{\mu^a}|^2/2m_{\mu^a}$ .

## Chapter 4

- p162** In the second part of eqn (4.34), defining the terms  $\mathcal{V}_m^{(12)}$  and  $\mathcal{V}_m^{(6)}$ , the negative sign is wrong:  $-\mathcal{V}_m^{(6)} \rightarrow +\mathcal{V}_m^{(6)}$ , giving

$$\begin{aligned}\mathcal{V}_m &= 4\epsilon \sum_i \sum_{j>i} \left( \frac{\sigma}{L_m s_{ij}^m} \right)^{12} - 4\epsilon \sum_i \sum_{j>i} \left( \frac{\sigma}{L_m s_{ij}^m} \right)^6 \\ &= \mathcal{V}_m^{(12)} + \mathcal{V}_m^{(6)}.\end{aligned}$$

J Mikhail  
2018-05-30

## Chapter 6

- p218**  $\ell - 4$  ‘(see Fig. 5.6(b))’  $\rightarrow$  ‘(see Fig. 6.2(b))’.

- p222** Equation (6.16) has the wrong sign:

$$(\mathbf{f}_{ij})_\alpha = q_i \hat{T}_{\alpha\beta} \mu_{j\beta} - q_j \hat{T}_{\alpha\beta} \mu_{i\beta}.$$

- p229**  $\ell 8$  ‘charges densities’  $\rightarrow$  ‘charge densities’.

Also, in eqn (6.43) there is a superfluous right parenthesis in the denominator, should be

$$b(k_x) = \frac{\exp(i(P-1)k_x\ell)}{\sum_{q=0}^{P-2} \exp(ik_x\ell q) M_P(q+1)}.$$

- p251** In eqn (6.106) the factor  $V$  should be  $1/V$ :

$$\mathcal{V}_{\text{correction}}^{qq} = \frac{2\pi}{V} \left( \sum_i q_i z_i \right)^2$$

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2018-04-13

## Chapter 9

- p323**  $\ell 5$  The sentence beginning ‘Smc’ should read ‘Asymptotically, the rejection rate of both smc, and FB with  $\lambda = \frac{1}{2}$ , approaches zero, proportional to the third power of the typical step size (see section 12.3 and e.g. Gupta et al., 1990; Vorselaars, 2023).’

- p333**  $\ell 14$  ‘(see Section 4.5)’  $\rightarrow$  ‘(see Section 4.4)’,  
 $\ell - 2$  ‘(eqn (4.41))’  $\rightarrow$  ‘(eqn (4.42))’.

- p337**  $\ell 21$  ‘liquid-vapour’  $\rightarrow$  ‘liquid–vapour’.

B Vorselaars  
2023-02-11

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2019-08-15

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2019-08-17

## Chapter 10

- p344** In eqn (10.2b)  $\int_{\mathbf{r} \in \mathbf{A}} \rightarrow \int_{\mathbf{r} \in \mathbf{B}}$ .

MPA  
2017-03-07

## Chapter 11

**p360**  $\ell - 7$  ‘eqn (2.153)’  $\rightarrow$  ‘eqn (2.159)’.

**p362**  $\ell 6$  ‘Fig. 9.4’  $\rightarrow$  ‘Fig. 1.15(b)’.

**p379**  $\ell - 16$  ‘Chapter 9’  $\rightarrow$  ‘Chapter 3’.

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2019-07-30

## Chapter 12

**p388**  $\ell - 5$  Before the sentence starting ‘A sample...’, insert ‘Typically, the rejection rate for a single-step HMC move is proportional to  $\delta t^3$  at small  $\delta t$  (Gupta et al., 1990).’.

B Vorselaars  
2023-02-11

## Chapter 13

**p420**  $\ell - 5$  ‘described by eqn (1.36)’  $\rightarrow$  ‘described by eqn (1.20)’.

**p443**  $\ell - 12$  ‘described in Section 13.4’  $\rightarrow$  ‘described in Section 13.2’.

**p444**  $\ell 9$  ‘described in Section 13.4’  $\rightarrow$  ‘described in Section 13.2’.

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2019-08-10  
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2019-08-01  
MPA  
2019-08-01

## Appendix D

**p502**  $\ell - 5$  ‘eqns (D.1a) and (D.2b)’  $\rightarrow$  ‘eqns (D.1a) and (D.1b)’.

**p505**  $\ell - 5$  ‘integral of eqn (D.14a)’  $\rightarrow$  ‘integral of eqn (D.14b)’.

MPA  
2019-08-19  
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2019-08-19

## Appendix E

**p510**  $\ell 12$  ‘...generating  $X_i = 1$ , but allows the possibility of  $X_i = 0$ ;’  
 $\rightarrow$  ‘...generating  $\xi_i = 1$ , but allows the possibility of  $\xi_i = 0$ ;’.

J Mikhail  
2021-09-30

## Bibliography (additional items)

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