

Merge Sort

```
mergeSort(arr):
```

```
    if len(arr) == 0:  
        return arr
```

```
    first_half ← first half of arr
```

```
    second_half ← second half of arr
```

```
    sorted ← merge(mergeSort(first_half), mergeSort(second_half))
```

```
    return sorted
```

```
merge(sorted1, sorted2):
```

```
    i, j ←
```

```
    newArr ← empty array
```

```
    while i < len(arr1) and j < len(arr2):
```

```
        if sorted1[i] ≤ sorted2[j]
```

```
            newArr[i+j] ← sorted1[i]
```

```
            i = i + 1
```

```
        else:
```

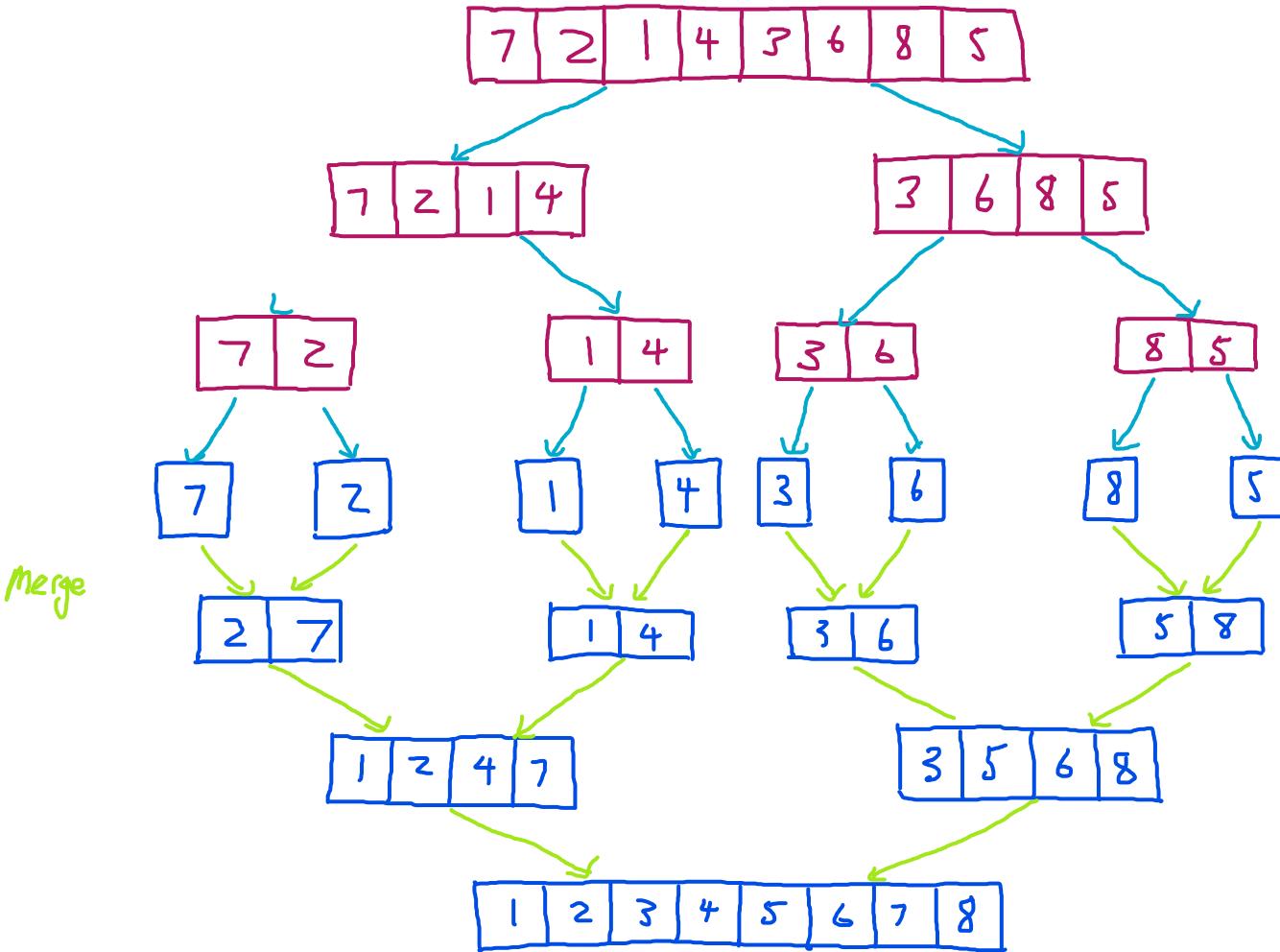
```
            newArr[i+j] ← sorted2[j]
```

```
            j = j + 1
```

```
    return newArr
```

In merge sort, we recursively divide the array by half, then call the same procedure on each half. Afterwards, both halves will be sorted (recursive leap of faith). We then merge the two halves (go thru both lists, compare leftmost unadded items of each list, then add the smaller value).

See example below on why this works.

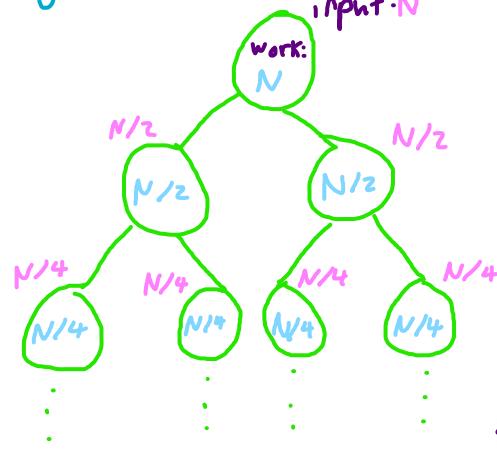


Runtime? $\Theta(N \log N)$

① Realize that Merge takes $\Theta(N)$ time.

② There are two recursive calls in mergesort, each call with $\frac{1}{2}$ the input

mergesort(arr), len(arr)=N
input:N



| Level | Work |
|----------|---|
| 0 | N |
| 1 | $\frac{N}{2} + \frac{N}{2} = N$ |
| 2 | $\frac{N}{4} + \frac{N}{4} + \frac{N}{4} + \frac{N}{4} = N$ |
| : | : |
| $\log N$ | N |

$$N \cdot \log N = \boxed{\Theta(N \log N)}$$

