

Modulus

Whole Numbers

int

+ - \*

~~÷~~

0.123

double

0 Decimal

float

123

int division  $4 \bmod 3 = 1$

$$\frac{3}{3} = 1 \qquad \frac{4}{3} = 1 \quad R: 1$$

Remainder

$$\frac{999,999}{100,000} = 9 \quad R: 99,999$$

$$999,999 \bmod 100,000 = 99,999$$

$$X \% y = n$$

$n$  can be any number from  
 $0$  to  $y-1$

$y$  is a divisor of  
 $X$  when  
 $X \% y == 0$

$$4 \% 3 = 1$$

$$5 \% 3 = 2$$

$$6 \% 3 = 0 \leftarrow$$

$$\begin{array}{l} \text{even} \quad \text{odd} \\ n \% 2 == 0 \quad (\text{even}) \\ (\text{odd}) \quad n \% 2 == 1 \quad || \quad n \% 2 != 0 \end{array}$$

$$0, 1, 2 \quad \begin{matrix} \%2 \\ \%3 \end{matrix} \quad f(s_n) =$$

$s_n$  1, 2, 3, 4, 5, 6, 7, 8, ... ↙

$f(s_n) = 1, 2, 3, 1, 2, 3, 1, 2, \dots$

propose  $f(s_n) = s_n \% 3$

Algorithm

$f(k) = 1, 2, 0, 1, 2, 0, 1, 2, \dots$

$$k = s_n - 1$$

$$(1-1) \% 3 = 0$$

$$(2-1) \% 3 = 1$$

$$(3-1) \% 3 = 2$$

$$f(s_n) = ((s_n - 1) \% 3) + 1$$

$$x \stackrel{+}{\underset{-}{*}} y = z$$

$$z \text{ — } y = x$$

$$z \text{ — } x = y$$

$$x \div y = \underline{\underline{z}}$$

$$\begin{array}{r} z \quad \underline{x} \quad = y \\ z \quad y \quad = x \end{array}$$