





# Task

- Download the [unigram](#) and [bigram](#) data. 
  - Complete the following code to estimate  $P(w[0], \dots, w[6])$ . 
  - Submit a short report explaining how you derive this estimation. 
  - References: [IOUtils](#). 
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# Solution

```
String[] w = {"he", "came", "to", "my", "school", "to", "study"};
```

## Chain Rule

$$P(w[0], \dots, w[6]) = P(w[6] | w[0], w[1], w[2], w[3], w[4], w[5]) * P(w[5] | w[0], \dots, w[4]) * \text{etc...}$$

## Markov Assumption Method

$$P(w[0], \dots, w[6]) = P(w[0]) * P(w[1] | w[0]) * P(w[2] | w[1]) * P(w[3] | w[2]) * P(w[4] | w[3]) * P(w[5] | w[4]) * P(w[6] | w[5])$$

$P(w[0])$  is simply a unigram probability of the word “he”. Derived by counting the number of times the word he appeared in our sample (the .txt files) and divided by the total number of words observed.  $P(w[0]) = 0.0014331108804395238$  or 0.14%

$P(w[1] | w[0])$  is a bigram as  $P(w[1])$  “came” is dependent on the  $P(w[0])$  “he” appearing right before it. This is consistent with the chain rule so far but will diverge into the markov assumption in the next step as we disregard  $w[0]$  when calc  $w[2]$ .  $P(w[1] | w[0]) = 0.004758864772863373$  or 0.48% the total probability so far is  $6.819980884530863E-6$

$P(w[2] | w[1]) = 0.2169154509097054$  or 21.69% and total prob is  $1.4793592287635838E-6$

$P(w[3] | w[2]) = 0.0036468028849340603$  or 0.36% and total prob is  $5.394931503308864E-9$

$P(w[4] | w[3]) = 7.9365518615475E-4$  or 0.08% and total prob is  $4.281715366550761E-12$

$P(w[5] | w[4]) = 0.018234547310248688$  or 1.8% and total prob is  $7.807514142038865E-14$

$P(w[6] | w[5]) = 8.853309990925741E-4$  or 0.09% and total prob is  $6.91223429580067E-17$

Therefor the  $P(w[0], \dots, w[6]) = 6.91223429580067E-17$  or .000000000000006912%

**TLDR:**  $P(w[0], \dots, w[6])$  was estimated via markov’s assumption and bigrams, my commented test.java file is available in my quiz1 directory should you want to look at that.