CS61B Lecture #4: Simple Pointer Manipulation

Recreation Prove that for every acute angle $\alpha > 0$,

$$\tan \alpha + \cot \alpha \ge 2$$

Announcements

- Today: More pointer hacking.
- Handing in labs and homework: We'll be lenient about accepting late homework and labs for lab1, lab2, and hw0. Just get it done: part of the point is getting to understand the tools involved. We will not accept submissions by email.
- We will feel free to interpret the absence of a central repository for you or a lack of a lab1 submission from you as indicating that you intend to drop the course.
- HW1 to be released tonight (roughly).
- Project 0 to be released Friday.

Small Test of Understanding

- In Java, the keyword final in a variable declaration means that the variable's value may not be changed after the variable is initialized.
- Is the following class valid?

```
public class Issue {
     private final IntList aList = new IntList(0, null);
     public void modify(int k) {
          this.aList.head = k;
```

Why or why not?

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     private final IntList aList = new IntList(0, null);
     public void modify(int k) {
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```

Why or why not?

Answer: This is valid. Although modify changes the head variable of the object pointed to by aList, it does not modify the contents of aList itself (which is a pointer).

Destructive solutions may modify objects in the original list to save time or space:

```
/** Destructively add N to P's items. */
static IntList dincrList(IntList P, int n) {
                                               X = IntList.list(3, 43, 56);
 if (P == null)
                                               /* IntList.list from HW #1 */
   return null;
                                               Q = dincrList(X, 2);
 else {
   P.head += n;
   P.tail = dincrList(P.tail, n);
   return P;
/** Destructively add N to L's items. */
static IntList dincrList(IntList L, int n)
 // 'for' can do more than count!
 for (IntList p = L; p != null; p = p.tail)
   p.head += n;
 return L;
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 // 'for' can do more than count!
 for (IntList p = L; p != null; p = p.tail)
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If L is the list [2, 1, 2, 9, 2], we want removeAll(L,2) to be the new list [1, 9].

```
/** The list resulting from removing all instances of X from L
  * non-destructively. */
static IntList removeAll(IntList L, int x) {
  if (L == null)
    return /*( null with all x's removed )*/;
  else if (L.head == x)
    return /*( L with all x's removed (L!=null, L.head==x) )*/;
  else
    return /*( L with all x's removed (L!=null, L.head!=x) )*/;
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  if (L == null)
    return null;
  else if (L.head == x)
    return removeAll(L.tail, x);
  else
    return new IntList(L.head, removeAll(L.tail, x));
}
```

```
/** The list resulting from removing all instances
 * of X from L non-destructively. */
static IntList removeAll(IntList L, int x) {
  IntList result, last;
  result = last = null;
  for ( ; L != null; L = L.tail) {
    if (x == L.head)
      continue:
    else if (last == null)
      result = last = new IntList(L.head, null);
    else
      last = last.tail = new IntList(L.head, null);
 return result;
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 * of X from L non-destructively. */
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 IntList result, last;
 result = last = null;
 for ( ; L != null; L = L.tail) {
   if (x == L.head)
                                   result:
     continue:
                                     last:
                                                    removeAll (P, 2)
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                                                    P does not change!
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 IntList result, last;
 result = last = null;
 for ( ; L != null; L = L.tail) {
    if (x == L.head)
                                    result: -
      continue:
                                                     removeAll (P, 2)
    else if (last == null)
                                      last: l
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→ : Original
                                  ....: after Q = dremoveAll (Q,1)
                          |3| <del>|</del>
                                 →|1|-|
/** The list resulting from removing all instances of X from L.
  The original list may be destroyed. */
static IntList dremoveAll(IntList L, int x) {
  if (L == null)
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     return /*( L with all x's removed (L != null) )*/;
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 while (L != null) {
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    if (x != L.head) {
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```

Aside: How to Write a Loop (in Theory)

- Try to give a description of how things look on any arbitrary iteration of the loop.
- This description is known as a loop invariant, because it is always true at the start of each iteration.
- The loop body then must
 - Start from any situation consistent with the invariant and condition:
 - Make progress in such a way as to make the invariant true again.

```
// Invariant must be true here
while (condition) { // condition must not have side-effects.
  // (Invariant and condition are necessarily true here.)
  loop body
  // Invariant must again be true here
// Invariant true and condition false.
```

 So if our loop gets the desired answer whenever Invariant is true and condition false, our job is done!

Relationship to Recursion

 Another way to see this is to consider an equivalent recursive procedure:

```
/** Assuming Invariant, produce a situation where Inveriant
  * is true and condition is false. */
void loop() {
    // Invariant assumed true here.
    if (condition) {
        // Invariant and condition true here.
        loop body
        // Invariant must be true here.
        loop()
        // Invariant true here and condition false.
    } else { /* condition false here. */ }
}
```

- Here, the invariant is the precondition of the function loop.
- The loop maintains the invariant while making the condition false.
- Idea is to arrange that our actual goal is implied by this post-condition.

Example: Loop Invariant for dremove All

```
/** The list resulting from removing all X's from L
   destructively. */
static IntList dremoveAll(IntList L, int x) {
 IntList result, last;
 result = last = null:
                                    result:
  while ** (L != null) {
    IntList next = L.tail;
                                      last:
    if (x != L.head) {
      if (last == null)
        result = last = L;
                                                     P = dremoveAll (P, 2)
      else
        last = last.tail = L;
                                   ** Invariant:
     L.tail = null;
                                     • result points to the list of items in the
                                       final result except for those from L on-
   L = next;
```

- ward.
- L points to an unchanged tail of the original list of items in L.
- last points to the last item in result or is null if result is null.

return result;