

Final Project of Discrete Mathematics



Formosa OJ

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Link: <https://oj.nctu.me/groups/>

Apply “帥宏翰教授離散數學”

Formosa OJ			使用說明	Groups
#	Name	Type	Apply	
1	Public	Public	Join	
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10	帥宏翰教授離散數學	Closed	Enter	
11	謝旻錚教授競技程式設計(一)	Public	Join	
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Link: <https://oj.nctu.me/groups/10/problems/>

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帥宏翰教授離散數學

New

PID	Problem
720	RSA Implementation
721	RSA - Break the RSA cryptography
736	RSA - Encryption
744	Maximum k-core

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744 . Maximum k-core

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Description

Given a simple undirected graph, please find the maximum k-core subgraph.

Input Format


Each line contain the edge given by a pair of node numbers(0, 1, 2, ... , n, $n < 1000$), which is separated by a space.

Output Format

(Maximum number of k)-
Edges sorted by vertex n

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Select "Execute Type": C/C++/Python2/Python3

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宏翰教授離散數學

744. Maximum k-core

Execute Type:

C

From Computer

選擇檔案 未選擇任何檔案

File Name: main.c

1

Submit

Upload your source code
from your computer

Formosa OJ - Verdict

- AC: Accepted (答對)
- WA: Wrong Answer (答案錯)
- CE: Compilation Error (編譯時錯誤)
- RE: Runtime Error (執行時錯誤)
- TLE: Time Limit Exceeded (超過時間限制)
- MLE: Memory Limit Exceeded (超過記憶體限制)
- SE: System Error (系統錯誤)

Formosa OJ – IO (Python3)

Case 1

Input:

77 7 HI

Python 3:

```
s1 = input()          #s1='77 7 HI'
s2 = input().split(' ') #s2[0]='77' s2[1]='7'
                        #s2[2]='HI'
```

Output:

30,17

Python 3:

```
c = list[30,17]
code = ','.join([str(integer) for integer in c])
print(code)
```

Formosa OJ – IO (C)

Case 1

Input:

77 7 HI

Output:

30,17

C:

```
int n1, n2;  
char s[30];  
scanf("%d%d%s", &n1, &n2, s);  
//n1=77, n2=7, s=HI
```

C:

```
int n1=30, n2=17;  
printf("%d,%d", n1, n2);
```

Formosa OJ – IO (C++)

Case 1

Input:

77 7 HI

Output:

30,17

C++:

```
int n1, n2;
```

```
string s;
```

```
cin >> n1 >> n2 >> s; //n1=77, n2=7, s=HI
```

C++:

```
int n1=30, n2=17;
```

```
cout << n1 << "," << n2 << endl;
```

Formosa OJ – IO (Python3)

Case 2

Input:

0 1

0 2

1 2

1 3

.....

Python 3:

```
import sys
```

```
for line in sys.stdin:
```

```
    a=line.split(' ')
```

```
    n1=int(a[0])
```

```
    n2=int(a[1])
```

Formosa OJ – IO (C)

Case 2

Input:

0 1

0 2

1 2

1 3

.....

C:

```
int n1, n2;
```

```
while(scanf("%d%d", &n1, &n2)!=EOF){
```

```
    .....
```

```
}
```

Formosa OJ – IO (C++)

Case 2

Input:

0 1

0 2

1 2

1 3

.....

C++:

```
int n1, n2;
```

```
while(cin >> n1 >> n2){
```

```
    .....
```

```
}
```

Project Candidates: #1

RSA - Encryption

- The objective is to use Public key (n,e) and message (m) to compute ciphertext (c) .

RSA - Break the RSA

- The objective is to use Public key (n,e) and ciphertext (c) to break RSA cryptography and compute message (m) .

Tools are allowed BUT you need to implement your own modular exponentiation function ($x^y \bmod n$).

No plagiarism.

EXAMPLE

- $p = 61, q = 53$
- $n = 61 \times 53 = 3233$
- $\varphi(n) = 60 \times 52 = 3120$
- $e = 17 \Rightarrow ex + \varphi(n)y = 1$
- $17 \times 2753 - 3120 \times 15 = 1$

Public key: (n, e)

Private key: (n, d)

$$\gcd(17, 3120) = 1$$

$$\Rightarrow e = 17$$

$d = \text{inverse of } 17 \text{ mod } 3120$

$$\Rightarrow d = 2753$$

- $A = 123, A^{17} \equiv 123^{17} \equiv 855 \pmod{3233} \Rightarrow \text{encrypt}$
- $855^{2753} \equiv 123 \pmod{3233} \Rightarrow \text{decrypt}$

Description(RSA - Encryption)

Use Public key (n,e) and message (m) to compute ciphertext (c) .

Input:

A test case consists of one line, which contains two integers n , e , and a string of the message (one word without any space).

Output:

Your program must produce a single line, containing ASCII code of the message separate by comma (,).

Format (RSA - Encryption)

Input: (n e m)

77 7 HI

Output: (c)

30,17

Solve:

$H = 72 ; I = 73$

$72^{7\%77} = 30$

$73^{7\%77} = 17$

Testdata (RSA - Encryption)

Number of test cases: 8

Time Limit: 1000ms

Per test case = 3% ; All 8 test cases = 24%

Description(RSA - Break the RSA)

Use Public key (n,e) and ciphertext (c) to break RSA cryptography and compute message (m) .

Input

A test case consists of one line, which contains two integers n , e , and a string of the ciphertext (numbers separated by comma).

Output

Your program must produce a single line, containing original message.

Format (RSA - Break the RSA)

Input: (n e c)

221 5 89,99

Output: (m)

HI

Testdata (RSA - Break the RSA)

Number of test cases: 4

Time Limit: 10000ms

Per test case = 6% ; All 4 test cases = 24%

Speed of Breaking Encryption(12%)

- Top 25% : 12%
- Top 50% : 9%
- Top 75% : 6%
- The rest : 3%

Grading policy (RSA)

Correctness (48%):

- Encryption: 24%
- Breaking Encryption: 24%

Speed of Breaking Encryption(12%)

- Top 25% : 12%
- Top 50% : 9%
- Top 75% : 6%
- The rest : 3%

Report (40%)

- English/Chinese
- Novelty
- Comprehensiveness of experiments
- Theoretical results

Project Candidates: #2

Graph problem-- Maximum k-core problem

- A k-core of a graph G is a maximal subgraph of G in which all vertices have degree at least k .
- Find the maximum k-core in the simple graph G .
- Tools are allowed while existing source codes are forbidden.
- Packages for graph or network are also forbidden (Ex. NetworkX).
- No plagiarism.

Format (Maximum k-core)

Input(graph):

0 1

0 2

1 2

1 4

1 5

2 3

2 4

2 5

4 5

Output(maximum k-core):

3-core

1 2

1 4

1 5

2 4

2 5

4 5

Example

input:

0 1

0 2

1 2

1 4

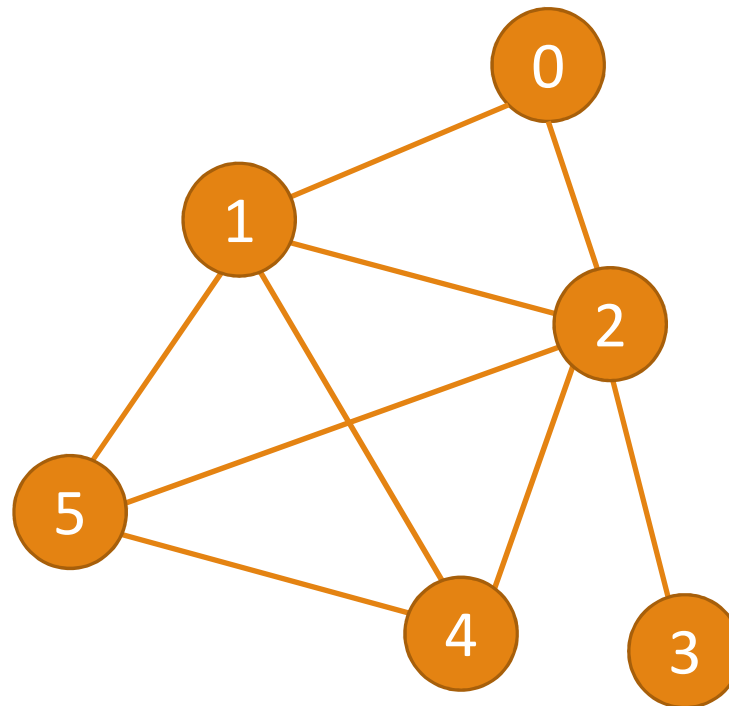
1 5

2 3

2 4

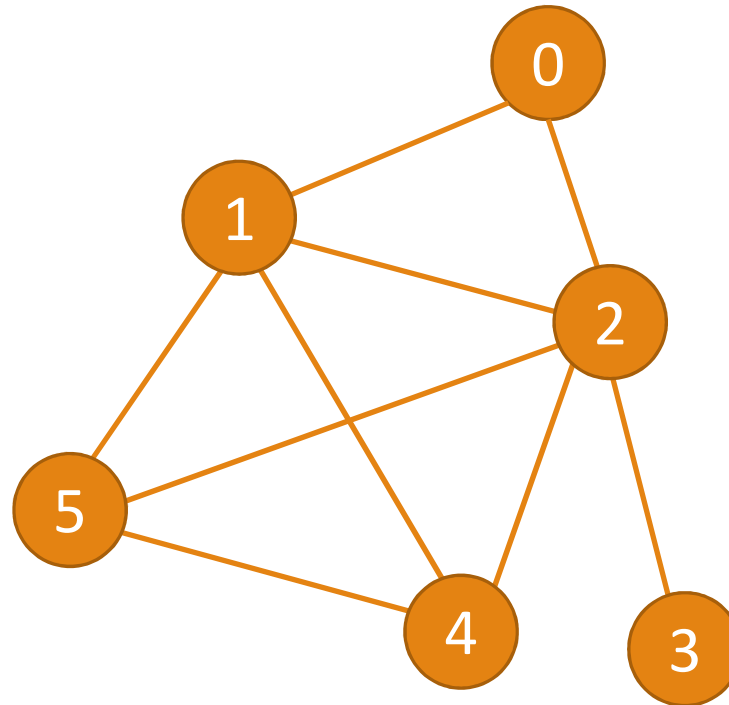
2 5

4 5



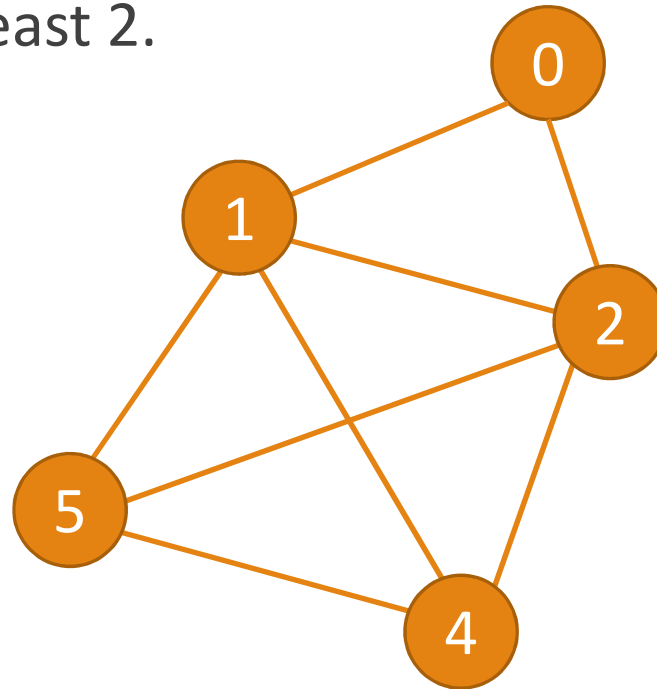
Example(create 2-core graph)

Remove the vertex with degree 1.



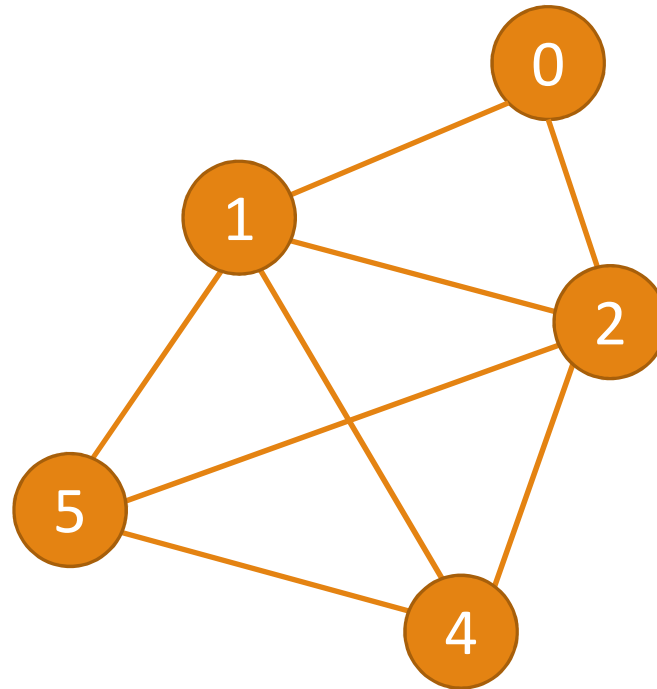
Example(2-core graph)

All vertices in 2-core graph
have degree at least 2.



Example(create 3-core graph)

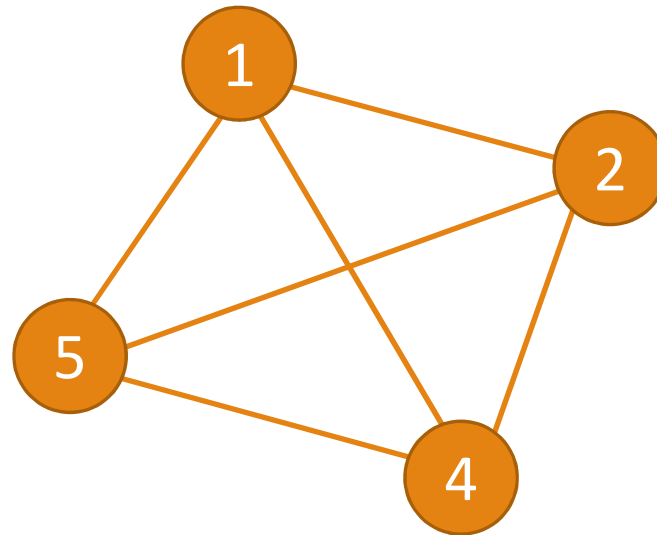
Remove the vertex with degree 2.



Example(3-core graph)

All vertices in 3-core graph
have degree at least 3.

The maximum k-core is 3-core.



Test data

Number of test cases: 10

Time Limit: 4000ms

Memory Limit: 1,000,000 (KiB)

4% for each test case, all 10 test cases = 40%

Grading policy

1. Correctness (40%)

2. Speed (20%):

- Top 25%: 20%
- Top 50%: 15%
- Top 75%: 10%
- The rest: 5%

3. Report (40%)

- English/Chinese
- Novelty
- Comprehensiveness of experiments
- Theoretical results

Deadline

1/16 23:59 | Formosa OJ關閉

1/17 23:59 | 繳交report與程式檔 (E3)