# Reinforcement learning Episode 1

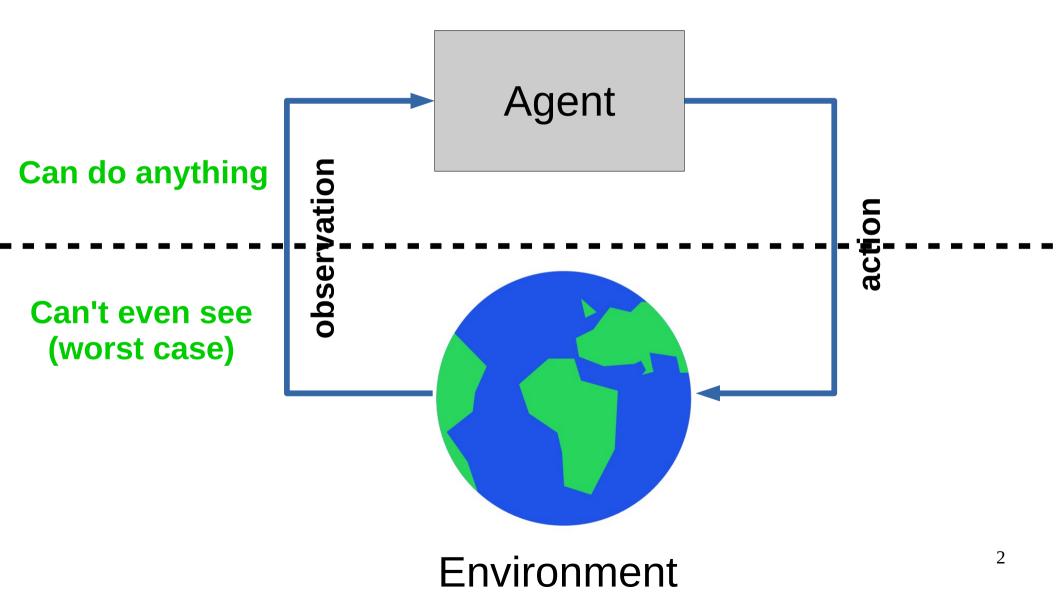
## Temporal Difference







# Recap: reinforcement learning



## Monte-carlo methods

R(z) – evaluated at the very end

Metaheuristics (genetic algorithm, etc.)

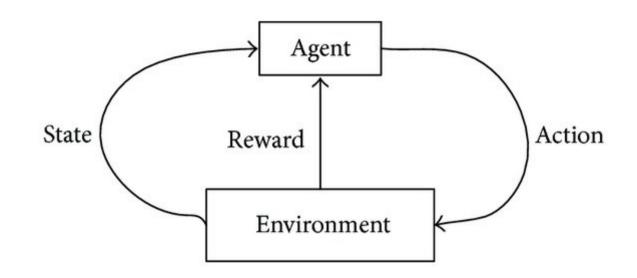
Stochastic optimization (crossentropy method)

#### Monte-carlo: drawbacks

- Both need a full session to start learning
- Requires a lot of interaction
  - A lot of crashed robots / simulations



## MDP formalism: reward on each tick



# Classic MDP(Markov Decision Process) Agent interacts with environment

- Environment states:  $s \in S$
- Agent actions:  $a \in A$
- State transition:  $P(s_{t+1}|s_t, a_t)$
- Reward:  $r_t = r(s_t, a_t)$



Objective:

Total action value

$$R_{t} = r_{t} + \gamma \cdot r_{t+1} + \gamma^{2} \cdot r_{t+2} + \dots + \gamma^{n} \cdot r_{t+n}$$

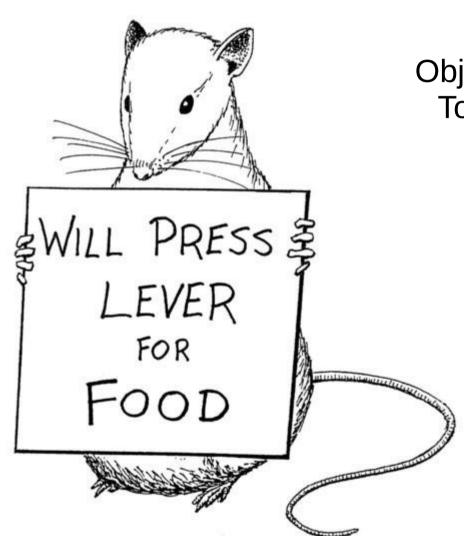
$$R_{t} = \sum_{i} \gamma^{i} \cdot r_{t+i} \quad \gamma \in (0,1) const$$

γ ~ patience Cake tomorrow is γ as good as now

Reinforcement learning:

 Find policy that maximizes the expected reward

$$\pi = P(a|s) : E[R] \rightarrow max$$



Objective:

Total action value

$$R_{t} = r_{t} + \gamma \cdot r_{t+1} + \gamma^{2} \cdot r_{t+2} + \dots + \gamma^{n} \cdot r_{t+n}$$

$$R_{t} = \sum_{i} \gamma^{i} \cdot r_{t+i} \quad \gamma \in (0,1) const$$

Trivia: which y corresponds to "only current reward matters"?

Reinforcement learning:

 Find policy that maximizes the expected reward

$$\pi = P(a|s) : E[R] \rightarrow max$$



Objective:

Total reward

$$R_{t} = r_{t} + \gamma \cdot r_{t+1} + \gamma^{2} \cdot r_{t+2} + \dots + \gamma^{n} \cdot r_{t+n}$$

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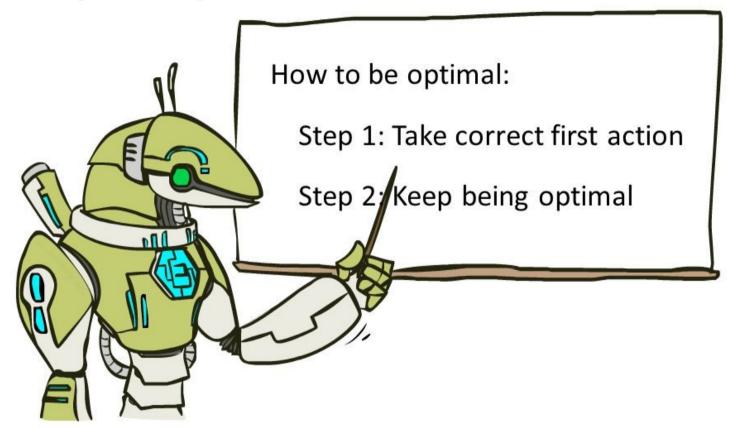
Reinforcement learning:

Find policy that maximizes the expected reward

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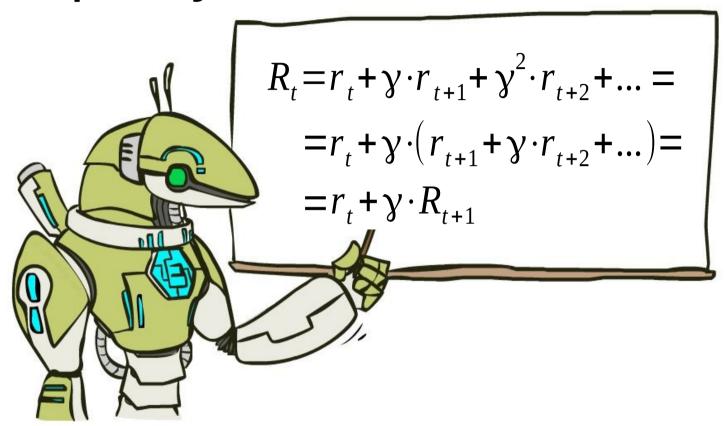
Is optimal policy same as it would be in monte-carlo (if we add-up all r\_t)?

# Optimal policy



Recurrent optimal strategy definition

# Optimal policy



We rewrite R with sheer power of math!

# Value iteration (Temporal Difference)

#### Idea:

For each state, obtain V(state)

$$V(s) = \max_{a} [r(s,a) + \gamma \cdot V(s'(s,a))]$$

**Definition** V(s) – expected total reward R that can be obtained starting from state s under optimal policy

# Value iteration (Temporal Difference)

#### Idea:

For each state, obtain V(state)

$$V(s) = \max_{a} [r(s,a) + \gamma \cdot E_{s' \sim P(s'|s,a)} V(s')]$$

$$\downarrow \bullet$$
Stochastic action outcome

**Trivia:** if we know the exact V(s) for all states, how do we determine the best actions?

#### Idea:

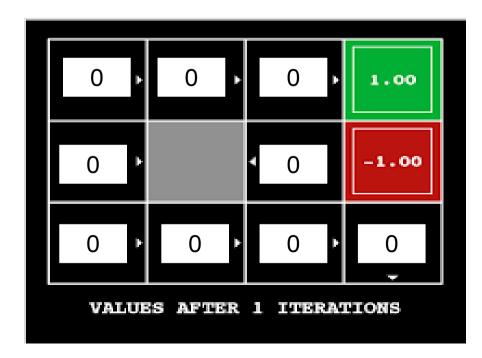
$$\forall s, V_0(s) := 0$$

$$V_{i+1}(s) := \max_{a} [r(s,a) + \gamma \cdot E_{s' \sim P(s'|s,a)} V_{i}(s')]$$

#### Idea:

$$\forall s, V_0(s) := 0$$

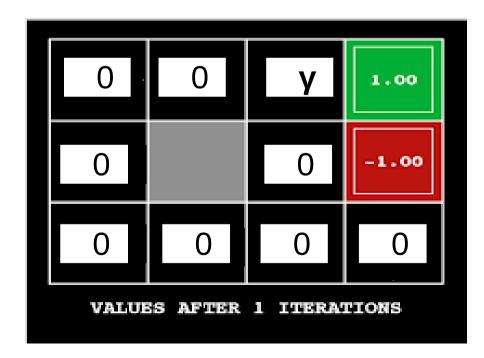
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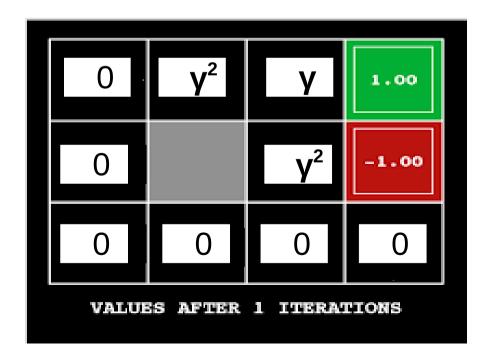
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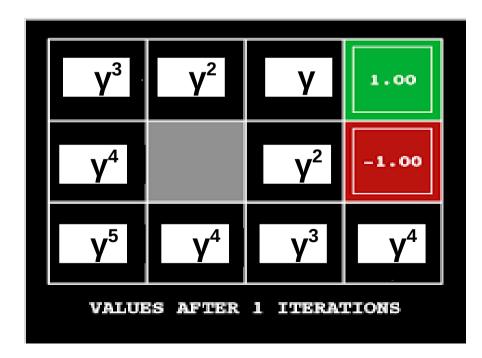
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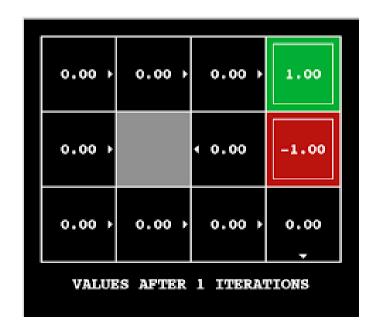
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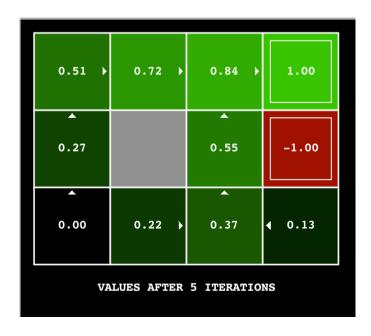


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# Voila! We've solved the reinforcement learning! Or have we?

What happens if we apply it to real world problems?

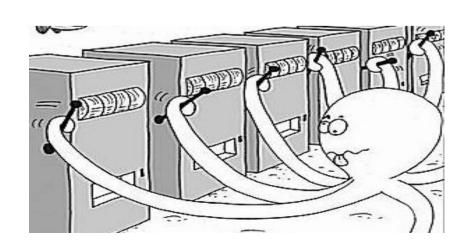
# Reality check: web

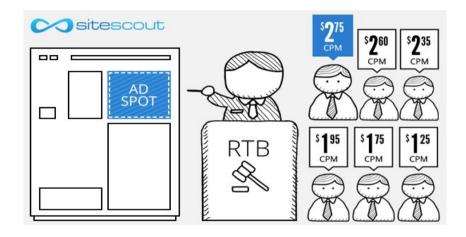
#### Cases:

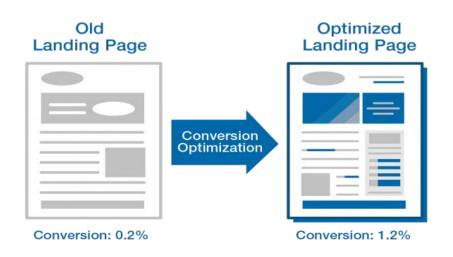
- Pick ads to maximize profit
- Design landing page to maximize user retention
- Recommend items to users

#### Common traits:

- Independent states
- Large action space





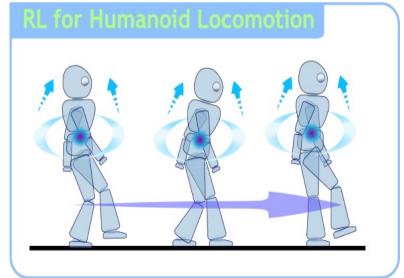


# Reality check: dynamic systems









# Reality check: MOAR

#### Cases:

- Robots
- Self-driving vehicles
- Pilot assistant
- More robots!

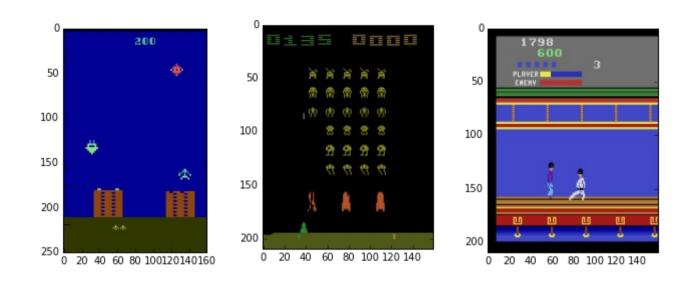
#### Common traits:

- Continuous state space
- Continuous action space
- Partially-observable environment
- LONG sessions





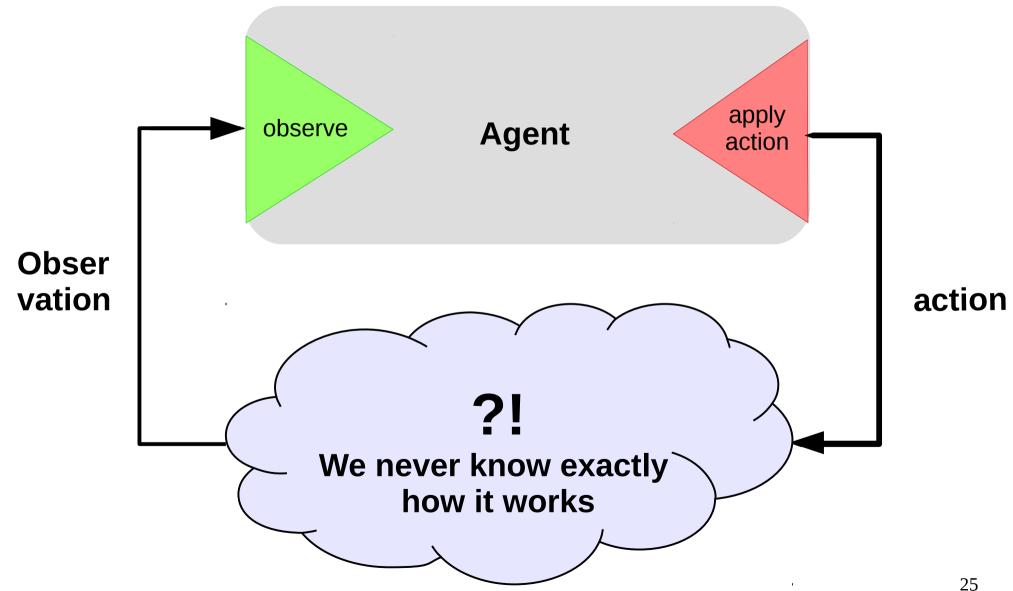
# Reality check: videogames



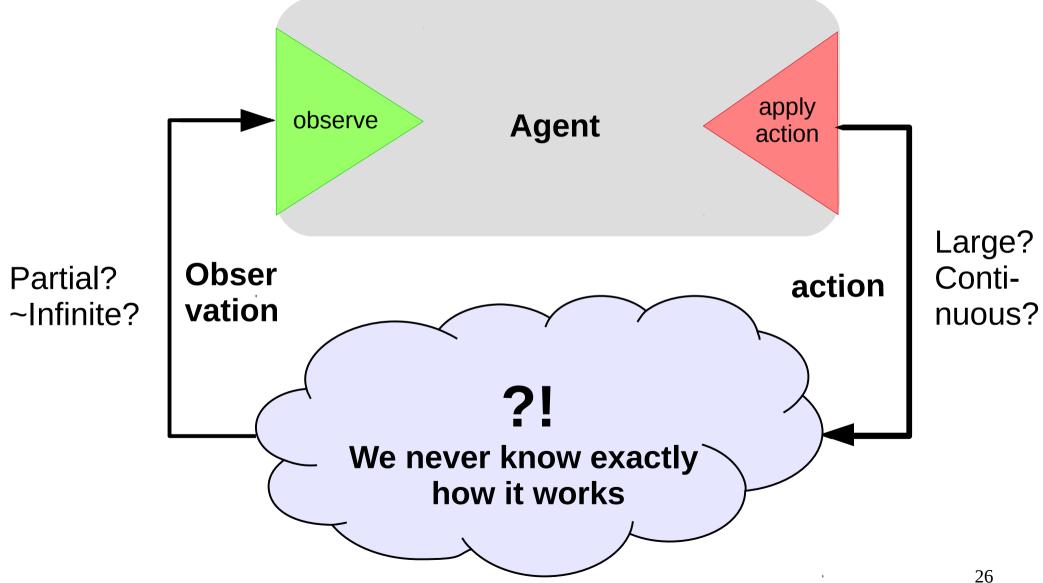


• **Trivia:** What are the states and actions? What are the problems?

## Real world



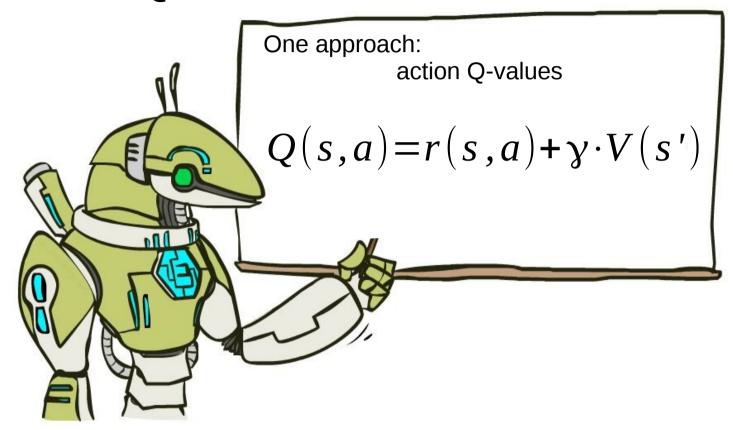
## Real world



#### Problem:

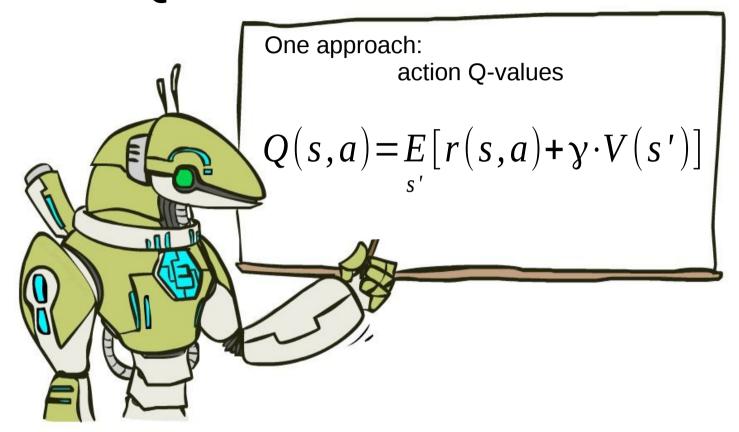
We never know actual P(s'|s,a)

Learn it?
Get rid of it?



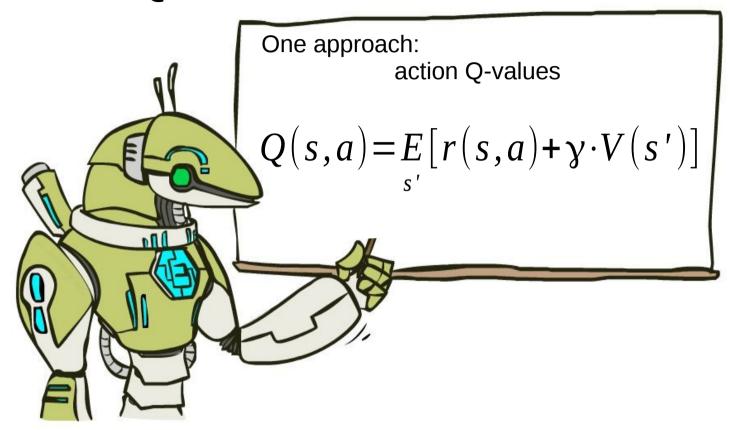
**Action value Q(s,a)** is the expected total reward **R** agent gets from state **s** by taking action **a** and following policy  $\pi$  from next state.

$$\pi(s)$$
:  $argmax_a Q(s,a)$ 



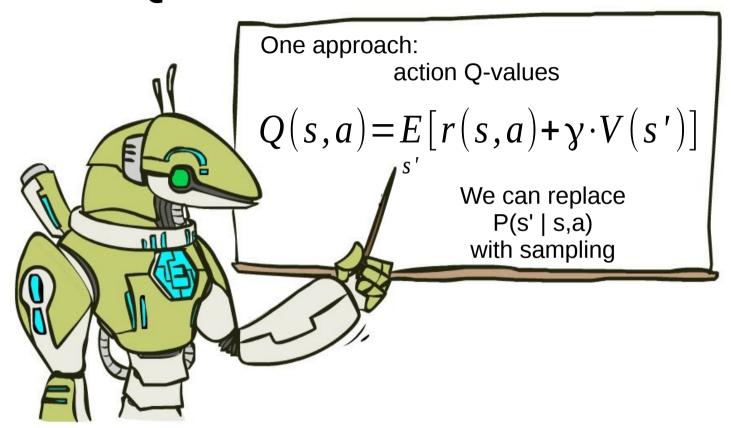
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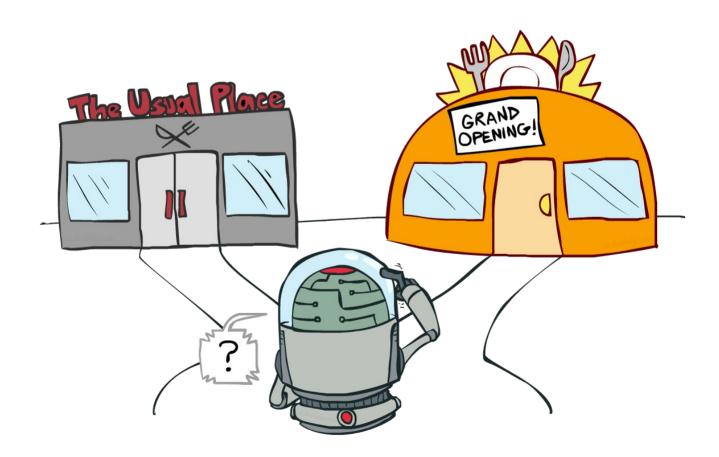


$$Q(s_t, a_t) \leftarrow \alpha \cdot (r_t + \gamma \cdot max_{a'} Q(s_{t+1}, a')) + (1 - \alpha) Q(s_t, a_t)$$

$$\pi(s)$$
:  $argmax_a Q(s,a)$ 

# **Exploration Vs Exploitation**

Balance between using what you learned and trying to find something even better



# **Exploration Vs Exploitation**

#### Strategies:

- · ε-greedy
  - · With probability ε take a uniformly random action; otherwise take optimal action.
- · Softmax

Pick action proportional to softmax of shifted normalized Q-values.

$$P(a) = softmax(\frac{Q(a)}{\tau})$$

 Some methods have a built-in exploration strategy (e.g. A2c)

#### **P**roblem:

# State space is usually large, sometimes continuous.

And so is action space;

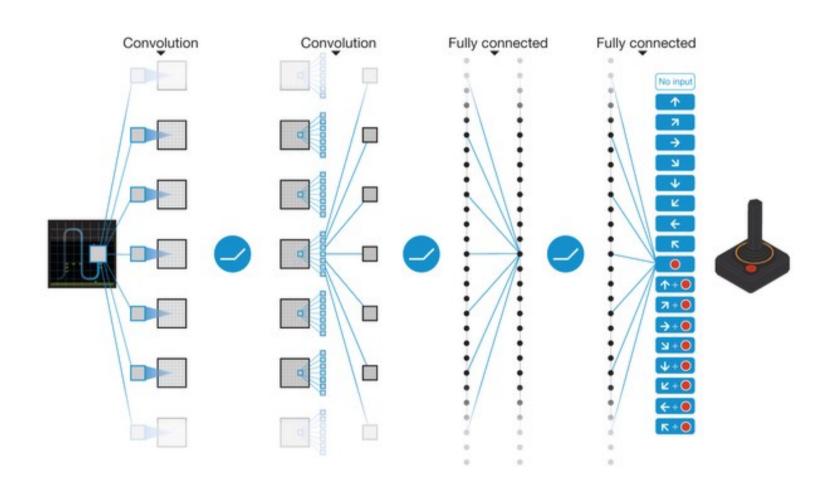
However, states do have a structure, similar states have similar action outcomes.

# From tables to approximations

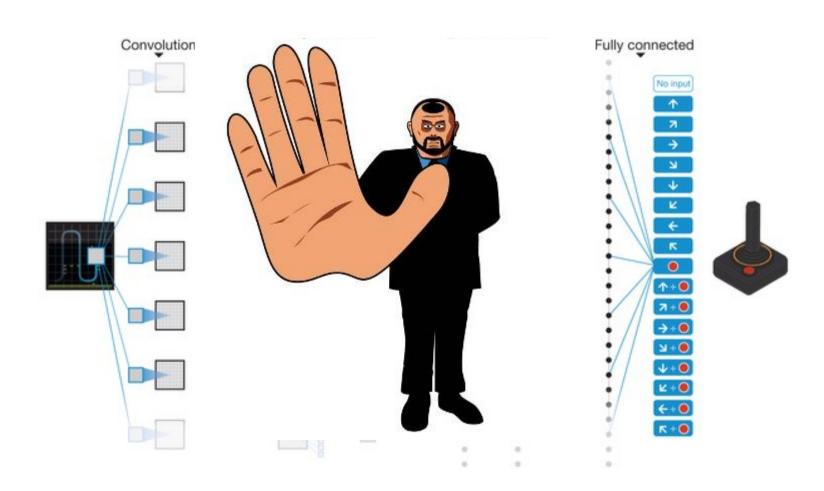
- Before:
  - For all states, for all actions, remember Q(s,a)
- Now:
  - Approximate Q(s,a) with some function
  - e.g. linear model over state features

$$argmin_{w,b}(Q(s_t,a_t)-[r_t+\gamma\cdot max_{a'}Q(s_{t+1},a')])^2$$

## Smells like a neural network



## Not so fast...





Objective:

Total reward

$$R_{t} = r_{t} + \gamma \cdot r_{t+1} + \gamma^{2} \cdot r_{t+2} + \dots + \gamma^{n} \cdot r_{t+n}$$

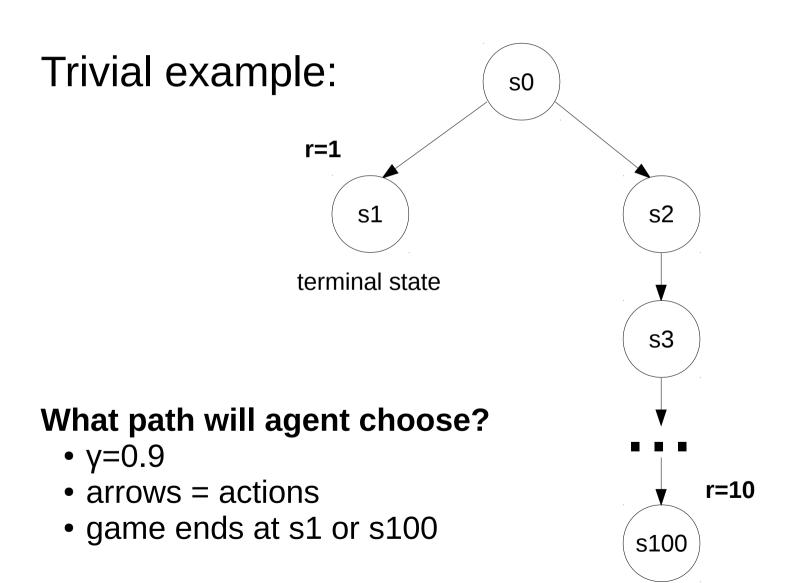
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Reinforcement learning:

Find policy that maximizes the expected reward

$$\pi = P(a|s) : E[R] \rightarrow max$$

Optimal policy isn't always maximizing monte-carlo reward!



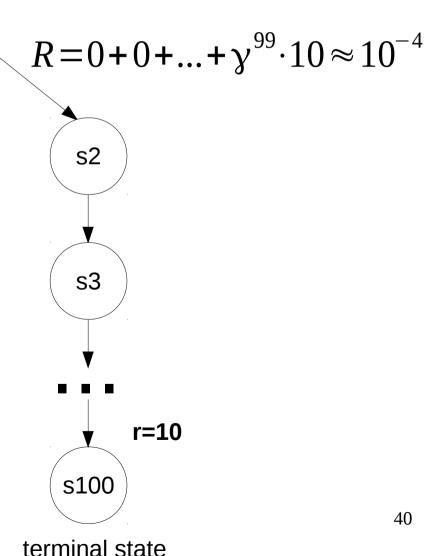
terminal state

Trivial example:

s0 R=1r=1 s1 terminal state

What path will agent choose?

- y=0.9
- arrows = actions
- game ends at s1 or s100
- left action has higher R!



#### Deephack'17 qualification round, Atari Skiing



- You steer the red guy
- Session lasts ~5k steps
- You get -3~-7 reward each tick (faster game = better score)
- At the end of session, you get up to r=-30k (based on passing gates, etc.)
- Q-learning with gamma=0.99 fails it doesn't learn to pass gates

What's the problem?

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  - Q-learning with gamma=0.99 fails

#### CoastRunner7 experiment (openAI)



- You control the boat
- Rewards for getting to checkpoints
- Rewards for collecting bonuses
- What could possibly go wrong?
- "Optimal" policy video: https://www.youtube.com/watch?v=tlOIHko8ySg

## Nuts and bolts: MC vs TD

#### Monte-carlo

- Ignores intermediate rewards doesn't need γ (discount)
- Needs full episode to learn Infinite MDP are a problem
- Doesn't use Markov property
   Works with non-markov envs

#### **Temporal Difference**

- Uses intermediate rewards trains faster under right γ
- Learns from incomplete episode Works with infinite MDP
- Requires markov property
   Non-markov env is a problem



## Nuts and bolts: discount

• Effective horizon  $1+\gamma+\gamma^2+...=\frac{1}{(1-\gamma)}$ 

Heuristic: your agent stops giving a damn in this many turns.

#### Typical values:

- y=0.9, 10 turns
- y=0.95, 20 turns
- y=0.99, 100 turns
- γ=1, infinitely long

Higher  $\gamma$  = less stable algorithm.  $\gamma$ =1 only works for episodic MDP (finite amount of turns).

## Nuts and bolts: discount

• Effective horizon  $1+\gamma+\gamma^2+...=\frac{1}{(1-\gamma)}$ 

Heuristic: your agent stops giving a damn in this many turns.

- Atari Skiing, reward was delayed by in 5k steps
- y=0.99 is not enough
- γ=1 and a few hacks works better
- Or use a better reward function



## Let's write some code!