

```

import numpy as np
import tensorflow as tf
import keras
from keras import layers

class Sampling(layers.Layer):
    """Uses (mean, log(variance)) to sample z, the vector encoding a digit."""

    def call(self, inputs):
        mean, log_var = inputs
        batch = tf.shape(mean)[0]
        dim = tf.shape(mean)[1]
        epsilon = tf.keras.backend.random_normal(shape=(batch, dim))
        return epsilon * tf.exp(log_var * .5) + mean

```

```

latent_dim = 2
encoder_inputs = keras.Input(shape=(28, 28, 1))
x = layers.Conv2D(32, 3, activation="relu", strides=2, padding="same")(encoder_inputs)
x = layers.Conv2D(64, 3, activation="relu", strides=2, padding="same")(x)
x = layers.Flatten()(x)
x = layers.Dense(16, activation="relu")(x)
z_mean = layers.Dense(latent_dim, name="z_mean")(x)
z_log_var = layers.Dense(latent_dim, name="z_log_var")(x)
z = Sampling()([z_mean, z_log_var])
encoder = keras.Model(encoder_inputs, [z_mean, z_log_var, z], name="encoder")
encoder.summary()

```

Model: "encoder"

Layer (type)	Output Shape	Param #	Connected to
input_layer (InputLayer)	(None, 28, 28, 1)	0	-
conv2d (Conv2D)	(None, 14, 14, 32)	320	input_layer[0][0]
conv2d_1 (Conv2D)	(None, 7, 7, 64)	18,496	conv2d[0][0]
flatten (Flatten)	(None, 3136)	0	conv2d_1[0][0]
dense (Dense)	(None, 16)	50,192	flatten[0][0]
z_mean (Dense)	(None, 2)	34	dense[0][0]
z_log_var (Dense)	(None, 2)	34	dense[0][0]
sampling (Sampling)	(None, 2)	0	z_mean[0][0], z_log_var[0][0]

Total params: 69,076 (269.83 KB)

Trainable params: 69,076 (269.83 KB)

Non-trainable params: 0 (0.00 B)

```

latent_inputs = keras.Input(shape=(latent_dim,))
x = layers.Dense(7 * 7 * 64, activation="relu")(latent_inputs)
x = layers.Reshape((7, 7, 64))(x)
x = layers.Conv2DTranspose(128, 3, activation="relu", strides=2, padding="same")(x)
x = layers.Conv2DTranspose(64, 3, activation="relu", strides=2, padding="same")(x)
decoder_outputs = layers.Conv2DTranspose(1, 3, activation="sigmoid", padding="same") (x)
decoder = keras.Model(latent_inputs, decoder_outputs, name="decoder")
decoder.summary()

```

```
Model: "decoder"
```

```
class VAE(keras.Model):
    def __init__(self, encoder, decoder, **kwargs):
        super(VAE, self).__init__(**kwargs)
        self.encoder = encoder
        self.decoder = decoder
        self.total_loss_tracker = keras.metrics.Mean(name="total_loss")
        self.reconstruction_loss_tracker = keras.metrics.Mean(
            name="reconstruction_loss"
        )
        self.kl_loss_tracker = keras.metrics.Mean(name="kl_loss")

    @property
    def metrics(self):
        return [
            self.total_loss_tracker,
            self.reconstruction_loss_tracker,
            self.kl_loss_tracker,
        ]

    def train_step(self, data):
        with tf.GradientTape() as tape:
            z_mean, z_log_var, z = self.encoder(data)
            reconstruction = self.decoder(z)
            reconstruction_loss = tf.reduce_mean(
                tf.reduce_sum(
                    keras.losses.binary_crossentropy(data, reconstruction),
                    axis=(1, 2)
                )
            )
            kl_loss = -0.5 * (1 + z_log_var - tf.square(z_mean) - tf.exp(z_log_var))
            kl_loss = tf.reduce_mean(tf.reduce_sum(kl_loss, axis=1))
            total_loss = reconstruction_loss + 0.1 * kl_loss
            grads = tape.gradient(total_loss, self.trainable_weights)
            self.optimizer.apply_gradients(zip(grads, self.trainable_weights))
            self.total_loss_tracker.update_state(total_loss)
            self.reconstruction_loss_tracker.update_state(reconstruction_loss)
            self.kl_loss_tracker.update_state(kl_loss)
        return {
            "loss": self.total_loss_tracker.result(),
            "reconstruction_loss": self.reconstruction_loss_tracker.result(),
            "kl_loss": self.kl_loss_tracker.result(),
        }

    def call(self, data):
        z_mean, z_log_var, z = self.encoder(data)
        reconstruction = self.decoder(z)
        return reconstruction
```

```
(x_train, _), (x_test, _) = keras.datasets.fashion_mnist.load_data()
fashion_mnist = np.concatenate([x_train, x_test], axis=0)
fashion_mnist = np.expand_dims(fashion_mnist, -1).astype("float32") / 255
vae = VAE(encoder, decoder)
vae.compile(optimizer=keras.optimizers.Adam(),
            loss=tf.keras.losses.MeanSquaredError())
vae.fit(fashion_mnist, fashion_mnist, epochs=2, batch_size=128)
```

```
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datasets/train-labels-idx1-ubyte.gz
29515/29515          0s 0us/step
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datasets/train-images-idx3-ubyte.gz
26421880/26421880      0s 0us/step
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datasets/t10k-labels-idx1-ubyte.gz
5148/5148          0s 1us/step
Downloading data from https://storage.googleapis.com/tensorflow/tf-keras-datasets/t10k-images-idx3-ubyte.gz
4422102/4422102      0s 0us/step
Epoch 1/2
547/547          226s 406ms/step - kl_loss: 0.0000e+00 - loss: 0.0741 - reconstruction_loss: 0.0000e+00 - total_
Epoch 2/2
547/547          213s 390ms/step - kl_loss: 0.0000e+00 - loss: 0.0343 - reconstruction_loss: 0.0000e+00 - total_
<keras.src.callbacks.history.History at 0x785443985310>
```

```
import numpy as np
import matplotlib.pyplot as plt

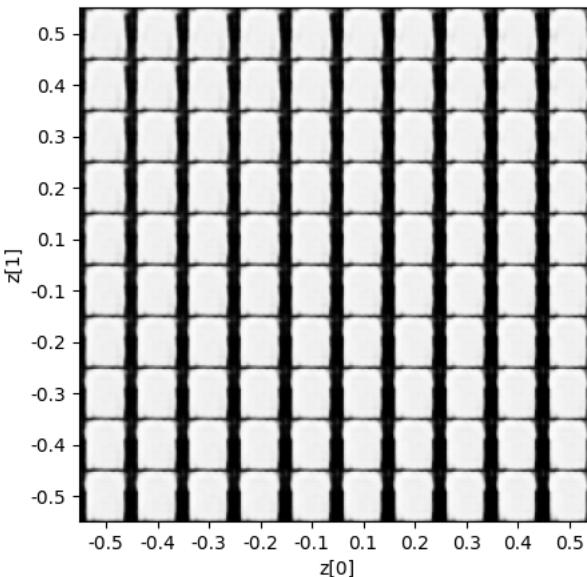
def plot_latent_space(vae, n=10, figsize=5):
    img_size = 28
    scale = 0.5
    figure = np.zeros((img_size * n, img_size * n))
    grid_x = np.linspace(-scale, scale, n)
    grid_y = np.linspace(-scale, scale, n)[::-1]
```

```

for i, yi in enumerate(grid_y):
    for j, xi in enumerate(grid_x):
        sample = np.array([[xi, yi]])
        x_decoded = vae.decoder.predict(sample, verbose=0)
        digit = x_decoded[0].reshape(img_size, img_size)
        figure[
            i * img_size: (i + 1) * img_size,
            j * img_size: (j + 1) * img_size
        ] = digit

plt.figure(figsize=(figsize, figsize))
start_range = img_size // 2
end_range = n * img_size + start_range
pixel_range = np.arange(start_range, end_range, img_size)
sample_range_x = np.round(grid_x, 1)
sample_range_y = np.round(grid_y, 1)
plt.xticks(pixel_range, sample_range_x)
plt.yticks(pixel_range, sample_range_y)
plt.xlabel("z[0]")
plt.ylabel("z[1]")
plt.imshow(figure, cmap="Greys_r")
plt.show()
plot_latent_space(vae)

```



```

import numpy as np
import matplotlib.pyplot as plt
from tensorflow import keras

labels = {
    0: "T-shirt/top",
    1: "Trouser",
    2: "Pullover",
    3: "Dress",
    4: "Coat",
    5: "Sandal",
    6: "Shirt",
    7: "Sneaker",
    8: "Bag",
    9: "Ankle boot"
}

def plot_label_clusters(encoder, data, test_labels):
    z_mean, _, _ = encoder.predict(data, verbose=0)
    plt.figure(figsize=(12, 10))
    sc = plt.scatter(z_mean[:, 0], z_mean[:, 1], c=test_labels, cmap="tab10")
    cbar = plt.colorbar(sc, ticks=range(10))
    cbar.ax.set_yticklabels([labels.get(i) for i in range(10)])
    plt.xlabel("z[0]")
    plt.ylabel("z[1]")
    plt.show()

(x_train, y_train), _ = keras.datasets.fashion_mnist.load_data()
x_train = np.expand_dims(x_train, -1).astype("float32") / 255

plot_label_clusters(encoder, x_train, y_train)

```

