

## Cryptography Final Review Sheet

(1) RSA - Public Key Encryption.

**Given:**

$n$  a small prime

$e$  smallest odd integer with gcd with  $\phi$  of 1

$c$  an encrypted message

**Needed:**

$p$  and  $q$  two prime numbers whose products are  $n$

$$\phi = (p - 1)(q - 1)$$

$$d = e^{-1}$$

- (a) Find the primes  $p$  and  $q$ . If you do not have a prime factorization on your calculator, then know that one of them is going to be less  $\sqrt{n}$ , knowing this, we can test all primes less than  $\sqrt{n}$ .
- (b) Calculate  $\phi = (p - 1)(q - 1)$ . From here, it should be easy to find  $e$  if it is not given. Parse through lowest odd values until you find one where  $\gcd(e, \phi) = 1$ .