

Housing and Credit Cycles

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1 INTRODUCTION

There has been an increasing interest in the study of the interaction between credit, speculation and house prices (Mian & Sufi 2011, 2018). The Great Recession caused researchers to focus on the narrative of credit, housing market and financial stability. This study will look into the short term transitory interaction between household credit and house prices.

Kishor (2020) and Mian & Sufi (2018) had detailed literature reviews on the dynamics between housing market and credit conditions. Kiyotaki & Moore (1997) modeled the fluctuation of credit condition due to credit limit and asset prices. It showed how exogenous shocks can create cycles in credit, asset prices and output. Alessi (2018) used a random forest model to identify unsustainable credit growth.

Regarding house prices cycle dynamics, Kishor (2015) studied the U.S. housing market by using a combination of Unobserved Component model and GARCH model to study the time-varying importance of permanent and transitory housing components in the U.S. housing prices. Agnello (2011, 2018) examined different variables that are likely to create a bubble in housing markets.

The dynamics of houses price and household credit can be viewed through the lens of the borrower balance sheet. An increase in home equity due to increase in house prices will allow borrower to borrow more to finance either personal consumption or more speculation housing investment. Mian & Sufi (2018) showed that speculation is a critical channel through which credit supply expansion affects the housing cycle. The crash in the housing market and following credit crunch showed the importance of housing prices for household balance sheet as well as banking sector balance sheet.

The findings in the literature motivate further examination in the structure of the relation between household credit and house prices. This study will look into the short term transitory and long term permanent components interaction between household credit and house prices. The decomposition methodology that I use in this paper to extract transitory and permanent information from a non-stationary time series is called Unobserved Components model pioneered by Beveridge & Nelson (1981). The implementation detail of the methodology is inspired by Morley (2007) and Huang & Kishor (2019). This method allows the permanent component to be shown as a random walk and the transitory or cyclical component to be a stationary process with mean zero. This

configuration is important to infer any structural linkage between the two variables of interest, household credit and house prices.

2 DATA DESCRIPTION

Our quarterly data sample periods include periods from January 1989 to January 2020. Table 1 shows the description of the data used in this paper. The sample periods were chosen based on the nature of the change in regulation of credit and housing markets beginning early 1990s. The main source of the data comes from the Bank of International Settlement (BIS). The housing price index is based on base index of 2010 as 100. The credit to household data is measured as percentage of GDP.

Table 1: Descriptive statistics

Country	Index	Mean	Max	Min	Frequency	Periods
UK	y_t	432.0829	459.1071	406.7316	Quarterly	1989:Q1-2020:Q1
	h_t	464.7302	503.8838	441.5308	Quarterly	1989:Q1-2020:Q1
US	y_t	429.0831	456.8506	395.8907	Quarterly	1989:Q1-2020:Q1
	h_t	434.0478	480.1792	378.2752	Quarterly	1989:Q1-2020:Q1

y_t is credit to household series, h_t is housing price index series. Both are log transformed.

Table 2: Correlation matrix

Country		y_t	h_t
UK	y_t	1	
	h_t	0.9359935	1
US	y_t	1	
	h_t	0.7046029	1

3 EMPIRICAL MODEL

3.1 Model specification

Series:

-Credit : Credit to non financial sector

-HPI : Housing Price Index

$$\ln \frac{Credit}{GDP} = y_t = \tau_{yt} + c_{yt} \quad (1)$$

$$\ln HPI = h_t = \tau_{ht} + c_{ht} \quad (2)$$

Trends:

A random walk drift term g_t is added in the stochastic trend inspired by Clark (1987)

$$\tau_{yt} = \tau_{yt-1} + \eta_{yt}, \quad \eta_{yt} \sim iidN(0, \sigma_{\eta_y}^2) \quad (3)$$

$$\tau_{ht} = \tau_{ht-1} + \eta_{ht}, \quad \eta_{ht} \sim iidN(0, \sigma_{\eta_h}^2) \quad (4)$$

Cycles:

$$c_{yt} = \phi_y^1 c_{yt-1} + \phi_y^2 c_{yt-2} + \phi_y^x c_{ht-1} + \varepsilon_{yt}, \quad \varepsilon_{yt} \sim iidN(0, \sigma_{\varepsilon_y}^2) \quad (5)$$

$$c_{ht} = \phi_h^1 c_{ht-1} + \phi_h^2 c_{ht-2} + \phi_h^x c_{yt-1} + \varepsilon_{ht}, \quad \varepsilon_{ht} \sim iidN(0, \sigma_{\varepsilon_h}^2) \quad (6)$$

State-Space Model

Transition equation:

$$\beta_t = F \beta_{t-1} + \tilde{v}_t \quad (7)$$

Where the transitory components are:

$$\begin{bmatrix} \tau_{yt} \\ c_{yt} \\ c_{yt-1} \\ \tau_{ht} \\ c_{ht} \\ c_{ht-1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & \phi_y^1 & \phi_y^2 & 0 & \phi_y^x & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & \phi_h^x & 0 & 0 & \phi_h^1 & \phi_h^2 \\ 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \tau_{yt-1} \\ c_{yt-1} \\ c_{yt-2} \\ \tau_{ht-1} \\ c_{ht-1} \\ c_{ht-2} \end{bmatrix} + \begin{bmatrix} \eta_{yt} \\ \varepsilon_{yt} \\ 0 \\ \eta_{ht} \\ \varepsilon_{ht} \\ 0 \end{bmatrix} \quad (8)$$

The covariance matrix for \tilde{v}_t , denoted Q , is:

$$Q = \begin{bmatrix} \sigma_{\eta_y}^2 & 0 & 0 & 0 & 0 & 0 \\ 0 & \sigma_{\varepsilon_y}^2 & 0 & 0 & \sigma_{\varepsilon_y \varepsilon_h} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \sigma_{\eta_h}^2 & 0 & 0 \\ 0 & \sigma_{\varepsilon_y \varepsilon_h} & 0 & 0 & \sigma_{\varepsilon_h}^2 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad (9)$$

Measurement Equation:

$$\tilde{y}_t = A + H\beta_t \quad (10)$$

$$\begin{bmatrix} y_t \\ h_t \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} \tau_{yt} \\ c_{yt} \\ c_{yt-1} \\ \tau_{ht} \\ c_{ht} \\ c_{ht-1} \end{bmatrix}$$

3.2 Parameters constraints

The estimation of the unobserved component model uses a nonlinear log-likelihood function maximization. Estimating this function requires numerical optimization.

I did not put stationary constraints directly on the autoregressive parameters. Since such constraints on a VAR(2) system is complex to set up. However, to achieve feasible stationary transitory measurement, I implement an additional term on the objective function:

$$l(\theta) = -w1 \sum_{t=1}^T \ln[(2\pi)^2 |f_{t|t-1}|] - w2 \sum_{t=1}^T \eta'_{t|t-1} f_{t|t-1}^{-1} \eta_{t|t-1} - w3 * \sum_{t=1}^T (c_{yt}^2) + w4 * \sum_{t=1}^T (c_{ht}^2) \quad (11)$$

The last term in the objective function acts as a penalty against too much transitory deviation from zero. Without this penalty, the trend would be linear or all the movements in the measured series would be matched by transitory movements.

Regarding constraints on covariance matrix, I applied the same constraints as in Morley 2007 to imply for positive-definite covariance matrix.

3.3 Priors selection

The priors for autoregressive parameters in matrix F are taken from VAR regression of the HP filter cycle decomposition of the series.

Table 3: Parameters description

Description	Parameter
Log-likelihood value	llv
Credit to household	
Credit to household 1st AR parameter	ϕ_y^1
Credit to household 2nd AR parameter	ϕ_y^2
Credit to household 1st cross cycle AR parameter	ϕ_y^{x1}
Credit to household 2nd cross cycle AR parameter	ϕ_y^{x2}
S.D. of permanent shocks to Credit to household	σ_{ny}
S.D. of permanent shocks to Credit to household	σ_{ey}
Housing Price Index	
Housing Price Index 1st AR parameter	ϕ_h^1
Housing Price Index 2nd AR parameter	ϕ_h^2
Housing Price Index 1st cross cycle AR parameter	ϕ_h^{x1}
Housing Price Index 2nd cross cycle AR parameter	ϕ_h^{x2}
S.D. of permanent shocks to Housing Price Index	σ_{nh}
S.D. of permanent shocks to Housing Price Index	σ_{eh}
Cross-series correlations	
Correlation: Permanent credit to household/Permanent Housing Price Index	σ_{nynh}
Correlation: Transitory credit to household/Transitory Housing Price Index	σ_{nynh}

For $\beta_{0|0}$, I set $\tau_{0|0}$ as the value HP filtered trend component and omit the first observation from the regression. $c_{0|0}$ cycle components are also set to be equal to their HP filter counterpart. Variance $var(\tau_{0|0}) = 100 + 50 * random$; while other measures of the starting covariance are set to be their unconditional values.

Starting standard deviation and correlation values are randomized within reasonable range.

4 RESULTS AND INTERPRETATION

In this following section, I will apply the UC model to data from 2 countries: US and UK.

Choosing priors from an estimated VAR(2) regression on HP filtered cycle and trend series. The following likelihood function weights are selected in the manner that they make the decomposed series most stable.

The tables below show the three Unobserved Component VAR(2) models regression results with and without cross-cycle parameters.

Table 4: United Kingdom regression results

Parameters	VAR(2)		VAR(2) 1-cross-lag		VAR(2) 2-cross-lags	
	Estimate	Std. Error	Estimate	Std. Error	Estimate	Std. Error
ϕ_y^1	1.9725	0.0234	1.8820	0.0005	1.8895	0.0002
ϕ_y^2	-0.9827	0.0263	-0.8160	0.0022	-0.8743	0.0026
ϕ_y^{x1}			-0.0240	0.0004	0.1756	0.0008
ϕ_y^{x2}					-0.1964	0.0035
ϕ_h^1	1.5048	0.1019	1.5748	0.0056	1.5742	0.0643
ϕ_h^2	-0.5608	0.1252	-0.7094	0.0077	-0.7364	0.0586
ϕ_h^{x1}			0.3783	0.0171	0.7214	0.0492
ϕ_h^{x2}					-0.5959	0.0442
σ_{ny}	0.7063	0.0600	0.7017	0.0353	0.6040	0.0374
σ_{ey}	0.0004	0.0104	0.1127	0.0052	0.0160	0.0063
σ_{nh}	1.8676	0.1617	1.6429	0.1023	1.9038	0.1115
σ_{eh}	0.6568	0.2583	0.6323	0.0193	0.1289	0.0269
σ_{eyeh}	0.6888	13.1231	1.0000	7.0580×10^{-6}	0.9998	0.0061
σ_{nynh}	0.5680	0.1125				
Log-likelihood value	-454.6450		-464.0793		-456.5685	

Weights of likelihood function: $w1 = 0.6$, $w2 = 0.4$, $w3 = 0.004$, $w4 = 0.003$

$$l(\theta) = -w1 \sum_{t=1}^T \ln[(2\pi)^2 |f_t|_{t-1}|] - w2 \sum_{t=1}^T \eta'_{t|t-1} f_{t|t-1}^{-1} \eta_{t|t-1} - w3 * \sum_{t=1}^T (c_{yt}^2) + w4 * \sum_{t=1}^T (c_{ht}^2)$$

Table 5: United States regression results

Parameters	VAR(2)		VAR(2) 1-cross-lag		VAR(2) 2-cross-lags	
	Estimate	Std. Error	Estimate	Std. Error	Estimate	Std. Error
ϕ_y^1	1.8497	0.0645	1.3050	0.1048	1.5502	0.0622
ϕ_y^2	-0.8917	0.0639	-0.5099	0.0696	-0.5754	0.0642
ϕ_y^{x1}			0.0332	0.0027	0.0141	0.0083
ϕ_y^{x2}					0.0037	0.0114
ϕ_h^1	1.7847	0.0345	2.0529	0.0421	1.8338	0.0658
ϕ_h^2	-0.8034	0.0345	-1.2469	0.0731	-0.9358	0.0611
ϕ_h^{x1}			1.0795	0.2918	1.7429	0.4406
ϕ_h^{x2}					-1.6544	0.4175
σ_{ny}	0.4793	0.0244	0.4718	0.0241	0.4195	0.0206
σ_{ey}	0.0281	0.0154	0.0256	0.0136	0.0375	0.0132
σ_{nh}	0.4549	0.0440	0.4742	0.0383	0.4937	0.0367
σ_{eh}	0.2566	0.0323	0.0876	0.0756	0.0966	0.0478
σ_{eyeh}	-1.0000	0.0001	1.0000	8.5939×10^{-5}	1.0000	2.5743×10^{-6}
σ_{nynh}	0.3974	0.0721				
Log-likelihood value	-339.7258		-346.9160		-332.0706	

Weights of likelihood function: $w1 = 0.8$, $w2 = 0.2$, $w3 = 0.003$, $w4 = 0.004$

$$l(\theta) = -w1 \sum_{t=1}^T \ln[(2\pi)^2 |f_t|_{t-1}|] - w2 \sum_{t=1}^T \eta'_{t|t-1} f_{t|t-1}^{-1} \eta_{t|t-1} - w3 * \sum_{t=1}^T (c_{yt}^2) + w4 * \sum_{t=1}^T (c_{ht}^2)$$

The tables 4 and 5 shows maximum-likelihood estimates of all three Unobserved Component VAR(2) models. The first model is a parsimony UC VAR(2) model with no cross-cycle terms (ϕ_y^x and ϕ_h^x are set to be zero). The next two models introduces 1 and 2 cross-cycle lags terms respectively.

The model selection criteria is to choose models with highest log-likelihood value. The parsimony UC VAR(2) models with no cross-cycle terms and the VAR(2) with 2 cross-cycle terms model have the highest likelihood values. Therefore, discussion regarding estimation results will focus mostly on these two. Additionally, because of identification problem, I will omit the cross-series correlation of trend component σ_{nynh} in the estimation results for crosscycle models.

4.1 Dynamic relationship between Credit to household and Housing Price

The results of VAR(2) model regression suggests that permanent shocks dominate transitory shocks in term of variation in both household credit and housing price variables. The standard deviation of the shocks in cycle of credit is 0.0004 in the UK and 0.0281 in the US, much smaller than standard deviation of the shocks to trend of credit in the UK of 0.7063 and in the US of 0.4793. The same applies for housing price, the standard deviation of the shocks in cycle of housing price is 0.6568 in the UK and 0.2566 in the US, smaller than standard deviation of the shocks to trend of housing price in the UK of 1.8676 and in the US of 0.4549. This result also indicates that variations in the trend components of the UK is bigger than the US, while variations in the cycle components of the UK is smaller than the US. In regard of the estimated parameters, the sum of AR parameters of the cyclical components in all 3 models are smaller although close to one. This implies that shocks to the cycle are persistent but will eventually dissipate.

The correlation analysis of the shocks to the cyclical components among the two variables suggests that cyclical variation among housing price and credit household is strongly positively correlated. Although we ran into the problem of identification or perfect collinearity with a cross-series correlation of 1 in a few estimated models. The overall results suggest that transitory shock to housing credit is closely positively correlated to transitory shock in housing price. The estimated correlation result in VAR(2) 2-cross cycle lags model is 0.9998 for the UK at 95% significant level. This implies that a transitory increase in household credit will lead to an appreciation in housing price above its long-run trend.

The correlation analysis of the shocks to the trends among the two variables reveals that there is also a long-term underlying correlation between shocks to the trend components of household credit and housing price. However, this correlation is much smaller compared to the correlation of the transitory components. The long-term components correlation estimated value is 0.568 in the UK and 0.3974 in the US. Overall, the results from the above analyses suggest that the short-run and long-run dynamics of the two variables are very different. Therefore, there is a benefit in decomposing the series into trend and cyclical components.

4.2 Trend-cycle decomposition

The following graphs shows the UC forecast series against the actual data series.

Figure 1: VAR(2) UK:

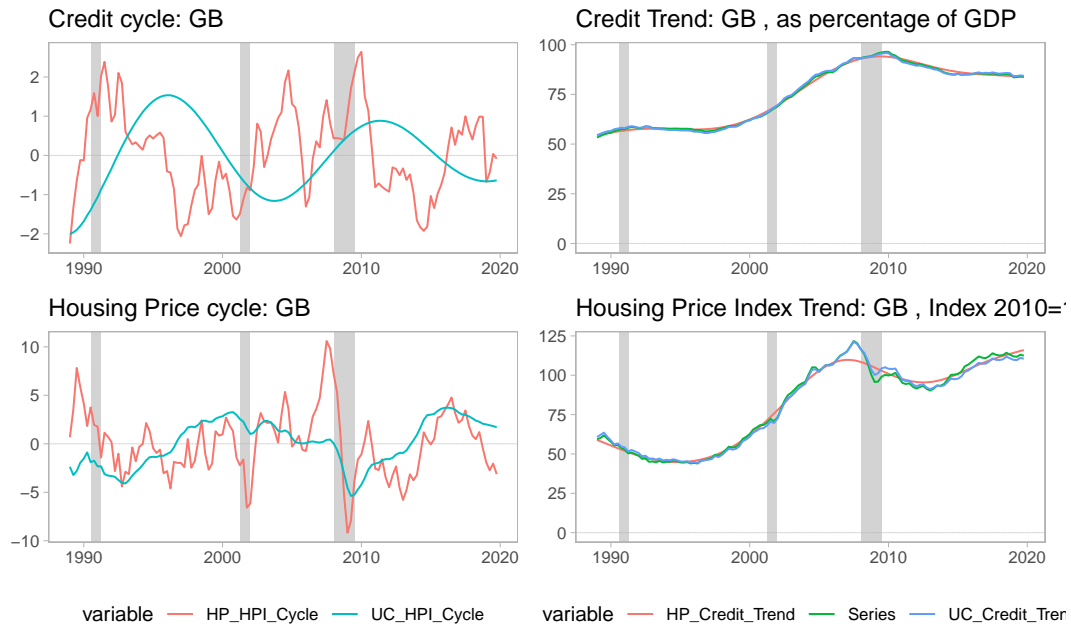


Figure 2: VAR(2) Crosscycle 1st lag only UK:

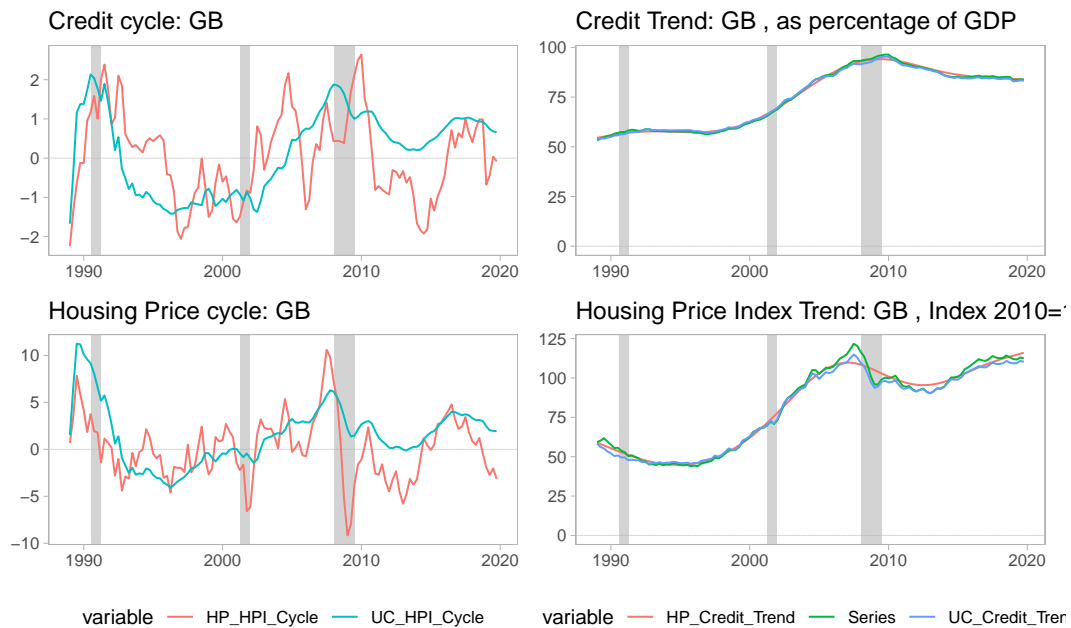


Figure 3: VAR(2) Crosscycle 2 lags UK:

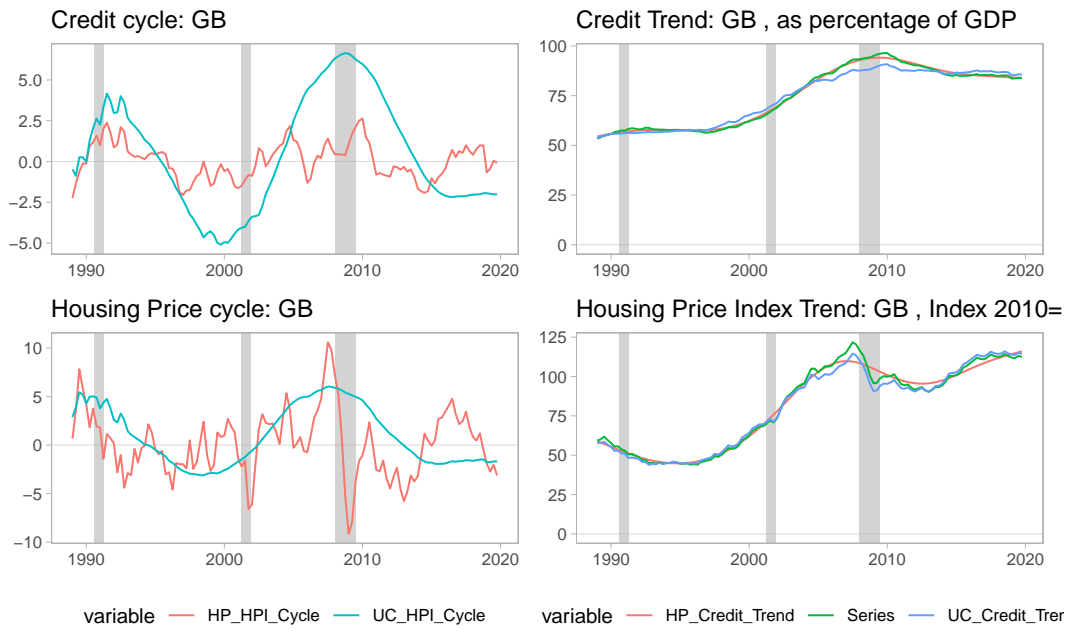


Figure 4: VAR(2) US:

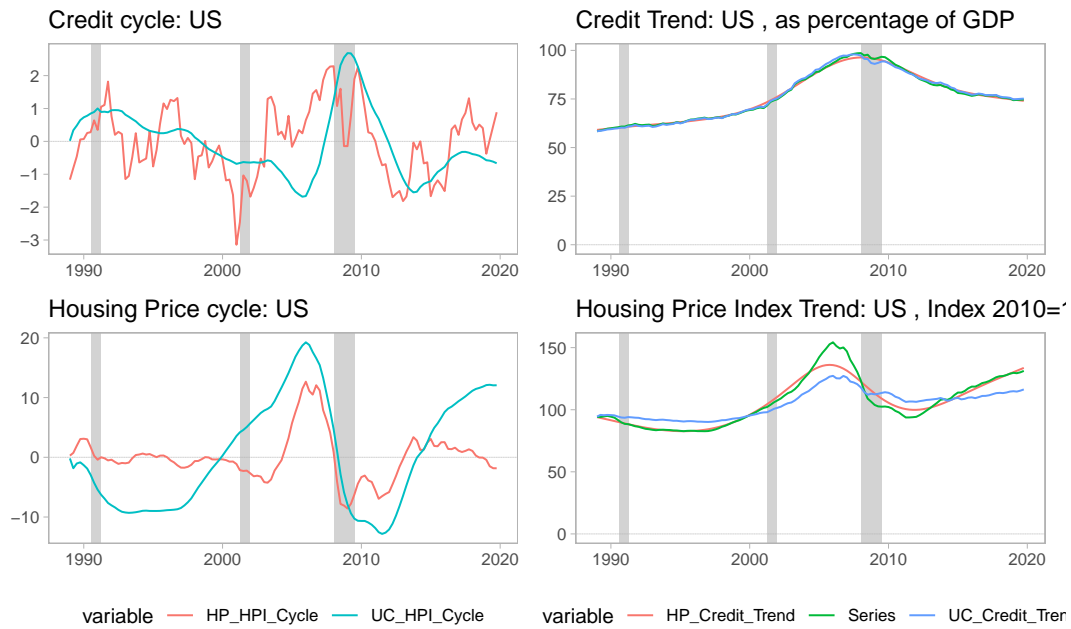


Figure 5: VAR(2) Crosscycle 1st lag only US:

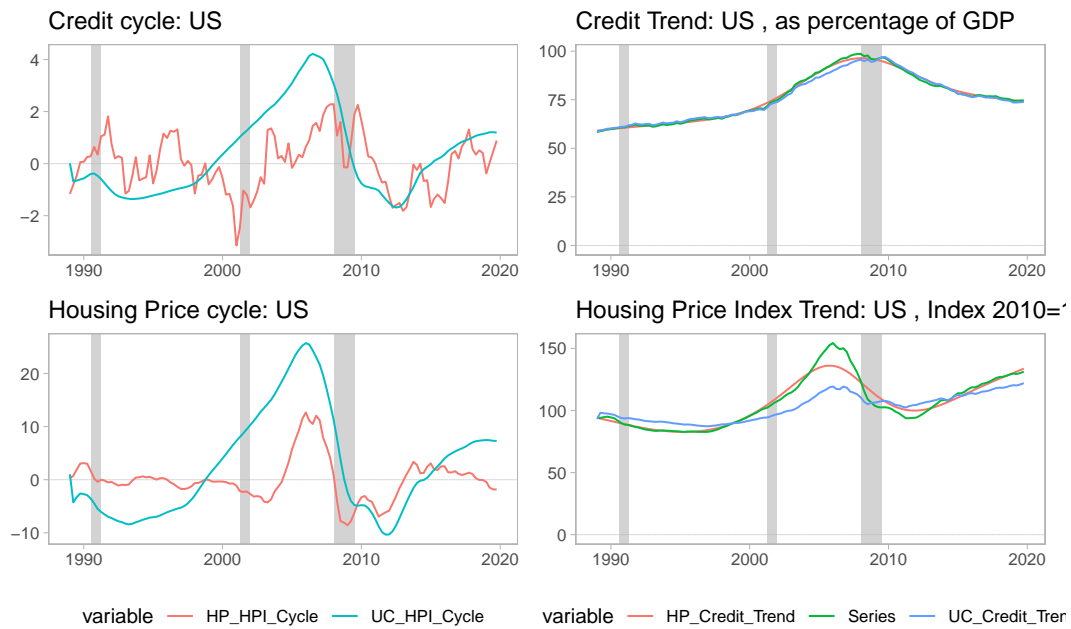
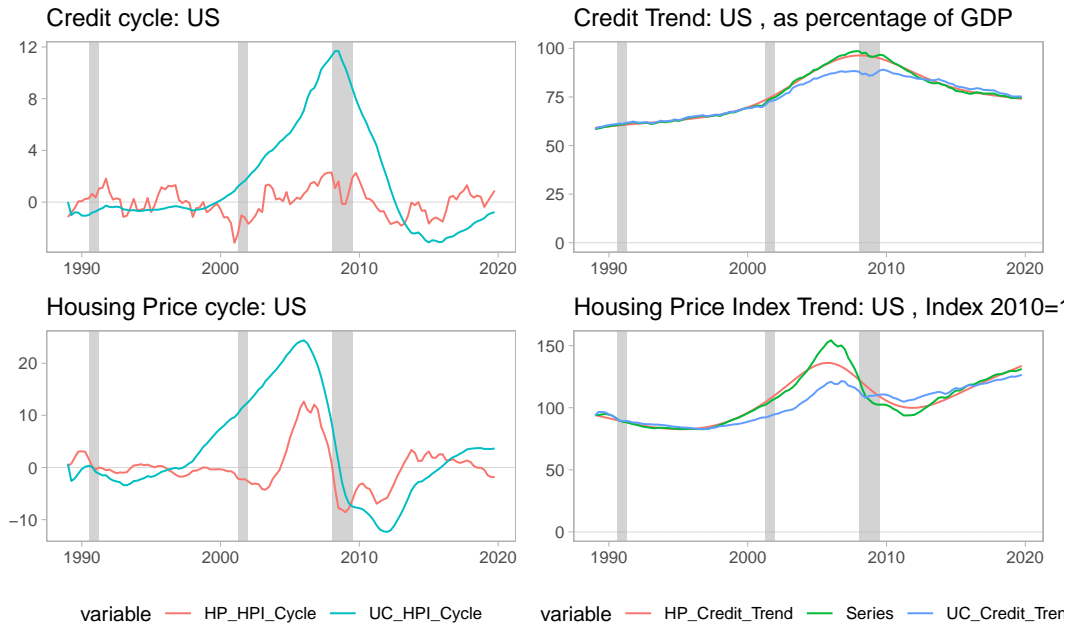


Figure 6: VAR(2) Crosscycle 2 lags US:



In this subsection, we decompose trend and cycle of household credit and housing price using the correlated unobserved component model. The stochastic trend in the multivariate UC model captures the long-run evolution in household credit, housing price, and the effect of the recent global financial crisis. In the long run, there is an increasing trend in the housing price index. The household credit trend is also increasing but since the series is credit to household as a ratio to GDP, the rate at which household credit trend increases is smaller than that of the housing price index. There is a downward movement of the trend components in both credit and housing price after the financial crisis. However, the housing price index trends made a quicker recovery than household credit did.

The cyclical components of the model capture the evolution of household credit, housing price, and their dynamic relationship. In figure 1-6, we can see that there is an increase in credit transitory component before the financial crisis of 2008-2009 happened, and there is a negative shock to the transitory component of housing price after the recession is captured in the model as well.

It is also important to point out that our models capture a significant bigger gap in transitory shock in both credit and house price than a Hodrick-Prescott (HP) filter would. This implies that when dealing with a time series of low frequency and long-term assets such as housing price, it is worthwhile to consider using the unobserved component model rather than simply applying an HP filter since it reveals more lower frequency information. The graphs indicate that the magnitude of transitory shocks the models capture is higher and the frequency of the movement of the cycles is lower than that of other methods (HP filter). The graphs also imply that the models detect a bigger credit gap in the UK (Figure 3), and also bigger gaps in household credit and house price in the US (Figure 4-6).

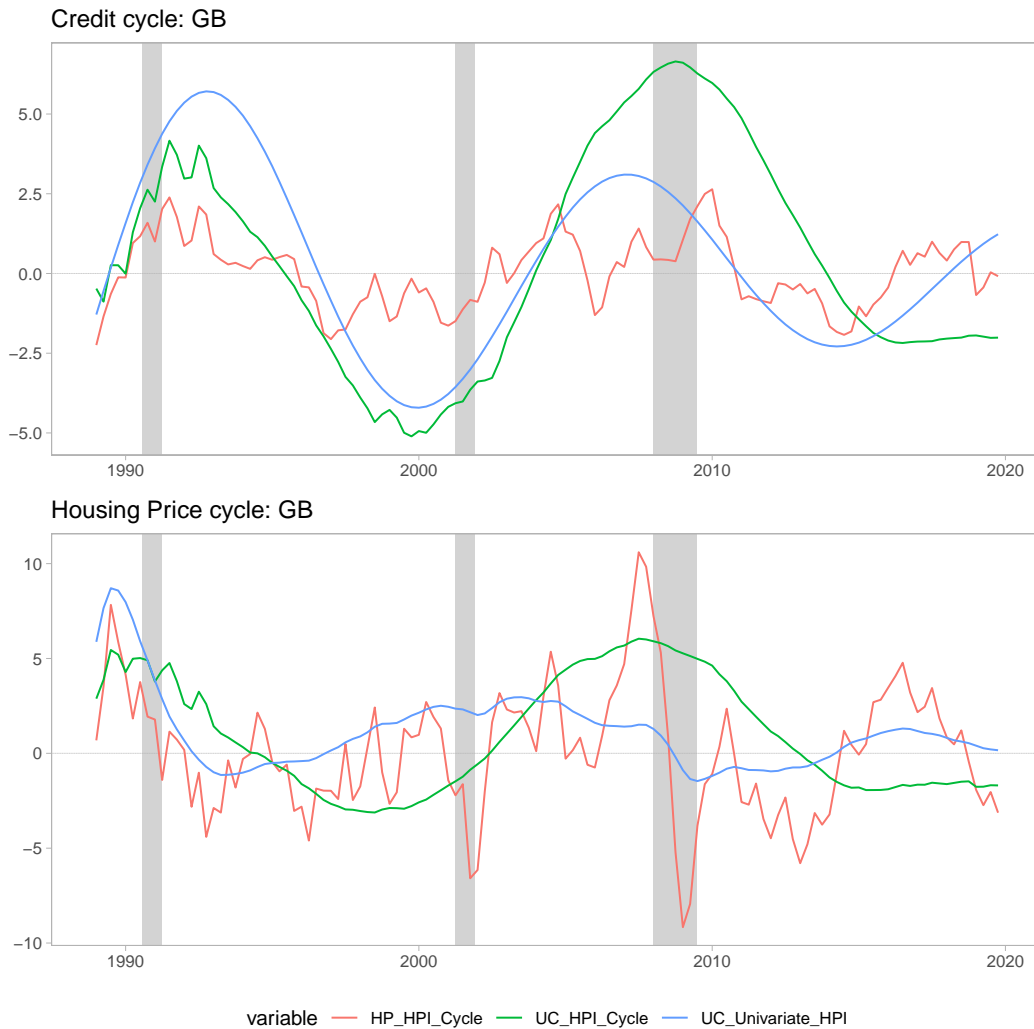
4.3 Co-movement amongn the cyclical components

A novel contribution of this paper is to introduce the cross-cycle parameter ϕ_h^{xt} and ϕ_y^{xt} in which it measures the effect of a change in last periods credit transitory component on the current housing price transitory component and vice versa. From Table 5 and 6, in both cross-cycle regressions in the UK and US, I can observe that there is a significant positive effect of last period credit cycle deviation on current housing cycle component (ϕ_h^{x1}). While the coefficients of transitory housing index deviation on household credit (ϕ_y^{x1}) are much smaller. This holds true for 2-crosscycle lags model also. This confirms that transitory shocks to household credit will cause a positive deviation in transitory housing price. However, transitory shocks to housing price have significantly smaller impact on household credit.

5 Robustness Check

5.1 Comparison with univariate trend-cycle decomposition models

Figure 7: Comparing Multivariate UC cycles with alternate decompositions: UK



The use of multivariate model in theory should provide a superior measurement of trend and cycle components as compared to the univariate models. As we allow for dynamic interaction between cycles and trends components. This provide a visual comparison between the three method of decomposition: HP filter, Multivariate Unobserved components and Univariate Unobserved components.

Figure 8: Comparing Multivariate UC cycles with alternate decompositions: US



6 CONCLUSION

Employing cross effects on the transitory components of the two series allows me to decompose the two variables of credit and housing price into short and long-term components. The models measure the causal effect of past short-term shock from household credit on current housing price and vice versa.

In this paper, the models for US and GB data show that there is a positive relationship between lags of short-term household credit to current house price.

Further development for this paper should include studying on policy implication of credit and house price gaps with higher magnitude, more robust optimal constraints on parameters to ensure stability rather than an ad-hoc approach to selecting weights. Additional examination of the multicollinearity / identification issue also needs to be addressed.