

# What Caused The Early Millenium Slowdown? Evidenece Based on Vector Autoregressions

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## Abstract

Abstract to be written here. The abstract should not be too long and should provide the reader with a good understanding what you are writing about. Academic papers are not like novels where you keep the reader in suspense. To be effective in getting others to read your paper, be as open and concise about your findings here as possible. Ideally, upon reading your abstract, the reader should feel he / she must read your paper in entirety.

*Keywords:* Multivariate GARCH, Kalman Filter, Copula

*JEL classification* L250, L100

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## 1. Introduction

In this research assignment, I replicate a research assignment by Gert Peersman (2005), a German economist, titled “What caused the early millennium slowdown? Evidence based on vector autoregressions”. In this paper, Peersman (2005) uses a simple four-variable VAR (vector autoregressive model) and an identification based scheme based on sign restrictions to examine the effects of a supply, demand, monetary policy and oil price shocks. Peersman (2005) uses data from the United States and Euro area. However, this assignment will only focus on analyzing shocks for the USA. Peersman (2005) concludes that the millennial slowdown is not the result of one particular shock, but a combination of them. The goal of this assignment is to replicate the results of Peersman (2005) as well as preform additional robustness test to ensure the validity of Peermans (2005) results.

- summarize what robustness checks and analysis you did(including the ones that you replicate)

This paper is structured as follows: The first section will give an overview of the paper with respects to the economics, methodology and data that Peersman (2005) used. The second section will replicate

the results for the US. The third section will perform robustness checks and the forth section will conclude.

## **2. Overview of the paper**

This section gives a brief overview of the economics of Peersman (2005) and a critical evaluation of the statistical approach that Peersman (2005) choose to analyze possible causes for the economic slowdown of the US.

### *2.1. Literature Review*

The 1990s was the start of an economic boom for the United States as they experienced the unusual combination of rapid output growth and extremely low and stable inflation. From 1994 to 2002 the United States real GDP grew by an average annual rate of almost 4 percent while annual inflation was less than 2 percent. However, by the end of 2001, the US began to experience negative growth (Peersman, 2005). Since 2001, the US economy has not experienced close to the same economic growth. It is therefore important to understand what caused the slowdown.

The economic expansion that the US experienced made headlines as it was the longest expansion in economic history. Many explanations have been offered as to why the US experienced such rapid growth, but overall, it is attributed to numerous factors. Productivity growth increased tremendously which created a favorable investment environment. The private investment opportunities contributed to the advancements in technologies and inspired innovation (Weller, 2002). Furthermore, the Federal Open Market Committee (FOMC) created an environment for the Federal Reserve to keep inflation rates low and stable (Taylor, 1998).

Another possible reason is that the US economy mostly experienced positive shocks during the late 1990s. The Fed has the responsibility to responds to shocks to the economy to ensure that output, employment, and inflation remain stable. The Fed can easily respond to a demand shock as it pushed output, employment, and inflation in the same direction. Therefore, the Fed will lower interest rate which will increase money supply to combat the effects of a demand shock. However, supply shock, such as an increase in oil prices, are more complicated to respond. With the threat of a recession, the Fed will need to decide whether to prioritize inflation stability or employment stability. Which attributed the economic boom that the US experienced, is the fact that large supply shocks were uncommon during the 1990s.

After 10 years of economic growth, the US economy entered a recession. The 2001/2002 was relatively short lived. Kliesen (2003) argues that the recession was caused by shocks to investment by businesses

and households and by a decline in real net exports. However, Kleisen (2003) does recognize that it can be extremely difficult to challenging to discover the root cause of a recession. Understanding fluctuation in the growth of an economy has been research by many economists but it is still relatively poorly understood. Therefore, Peersman (2005) adds value to research by examining four shocks (oil, demand, supply, and monetary policy) to analyze the origin of the slowdown.

Peersman (2005) concludes that the slowdown of economic growth was caused by a combination of several shocks. This conclusion is non-surprising and therefore Peersman (2005) main contribution is the impressive mathematical and statistical analysis that he performed.

## *2.2. Data and Methodology*

This paper used quarterly data from 1980 to 2002 on the US consumer expenditure index (CPUS), real GDP (YUS), short term nominal interest rate (SUS) as well as data on the oil price (OIL). Changes in CPUS record the rate of inflation while changes in YUS record output growth. The data is presented in figure 2.1 below.

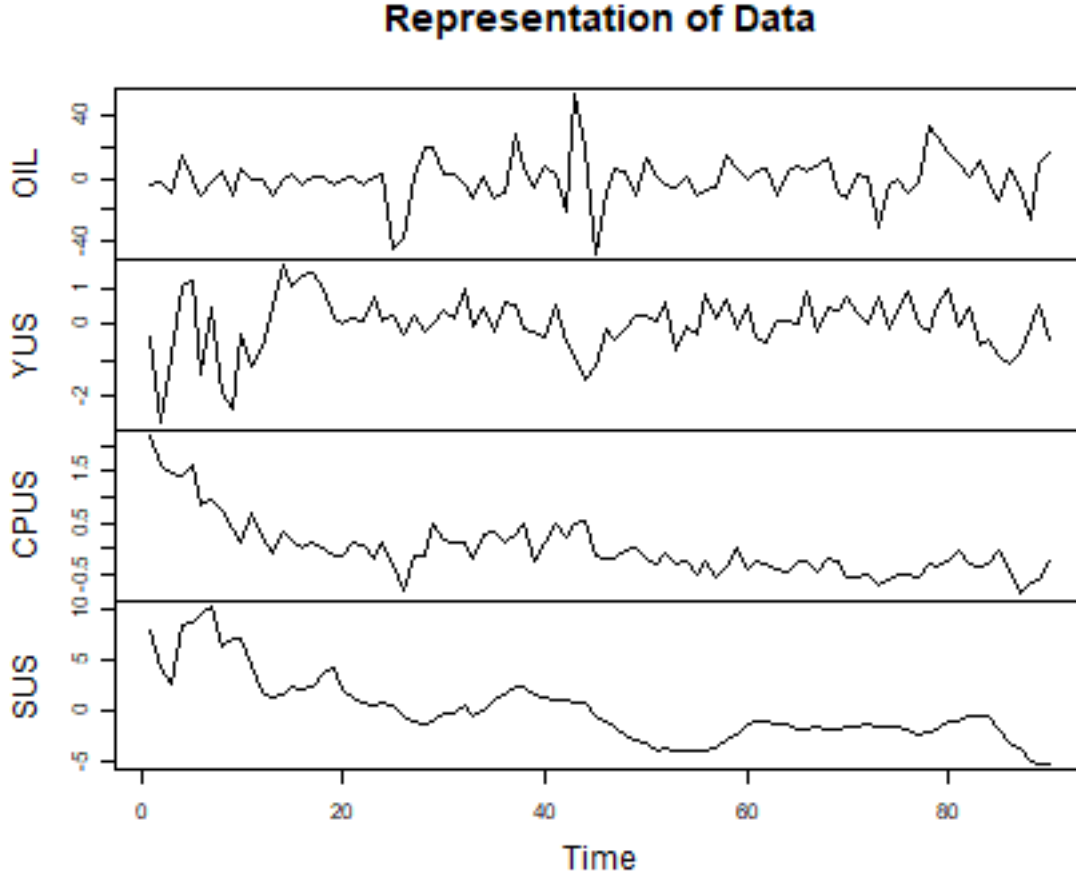


Figure 2.1: Data

Peersman (2005) makes use of a four-variable constant-coefficient VAR, with three lags and identifies four shocks. The variables included in the analysis is the first difference of oil prices, output growth measured by the real GDP index, consumer inflation measured by consumer price index and short-term nominal interest rates. The four shocks that are analyzed in this paper is an shock to oil price and an aggregate demand, aggregate supply, and monetary policy shock. Therefore, the equation can be presented as follows:

$$\begin{bmatrix} \Delta oil_t \\ \Delta y_t \\ \Delta p_t \\ s_t \end{bmatrix} = \left[ I - \sum_{i=1}^n A_i \right]^{-1} \begin{bmatrix} b_{11} & b_{12} & b_{13} & b_{14} \\ b_{21} & b_{22} & b_{23} & b_{24} \\ b_{31} & b_{32} & b_{33} & b_{34} \\ b_{41} & b_{42} & b_{43} & b_{44} \end{bmatrix} \begin{bmatrix} \epsilon_t^{oil} \\ \epsilon_t^s \\ \epsilon_t^d \\ \epsilon_t^m \end{bmatrix}$$

Where  $\Delta oil_t$ ,  $\Delta y_t$  and  $\Delta p_t$  represent the first difference of the price of oil, output growth and the

consumer prices respectively.  $s_t$  represents the short term nominal interest rate. The oil price, demand, supply and monetary shock is represented by  $\epsilon_t^{oil}$ ,  $\epsilon_t^d$ ,  $\epsilon_t^s$  and  $\epsilon_t^m$  respectively.

Peersman (2005) assumes that the variables follow a covariance stationary process. He uses the Dickey fuller test to reject the null hypothesis of the existence of a unit root at a 10 percent level for OIL, YUS and CPUS, however, the null hypothesis for interest rates cannot be rejected. Peersman (2005) makes the assumption that interest rates are stationary since the nominal rate cannot have a unit root if both the real rate and inflation are stationary. This assumption will be intensely analyzed in section xx during which I will perform numerous robustness checks.

The paper makes use of a traditional identification strategy using a combination of short-run and long-run restrictions. For the purpose of this assignment, the short-run and long-run restrictions will be discussed and modelled separately. Peersman (2005) assumes that there is a contemporaneous impact of an oil shock on all variables in the VAR, but no immediate impact of other shocks on oil prices. This assumption is consistent with previous literature. Further Peersman (2005) adds the restrictions that a monetary policy shock has no contemporaneous effect on output, since monetary policy shocks have a temporary effect on output. To model these contemporaneous effects  $b_{12} = b_{13} = b_{14} = b_{24} = 0$ . However, to accurately model the contemporaneous effects, the VAR needs  $[(k-1)-k]/2$  restrictions, where  $k$  represents the number of variables. This implies that a further two contemporaneous effects are needed to model the short-run and long run restrictions further. I will argue two more contemporaneous effects that are consistent with past literature in the next section. Taking into account only the contemporaneous effects that Peersman (2005) specifically specified in his paper, your matrix will change to:

$$\begin{bmatrix} b_{11} & 0 & 0 & 0 \\ b_{21} & b_{22} & b_{23} & 0 \\ b_{31} & b_{32} & b_{33} & b_{34} \\ b_{41} & b_{42} & b_{43} & b_{44} \end{bmatrix}$$

Peersman (2005) follows Blanchard and Quah (1989), Gali (1992) and Gerlach and Smeth (1995) to add long-run restrictions to the model. He assumes that demand and monetary shocks have no long-run impact on the level of real output. Using this approach, demand and monetary policy shocks with permanent effects are therefore labelled as supply shock.

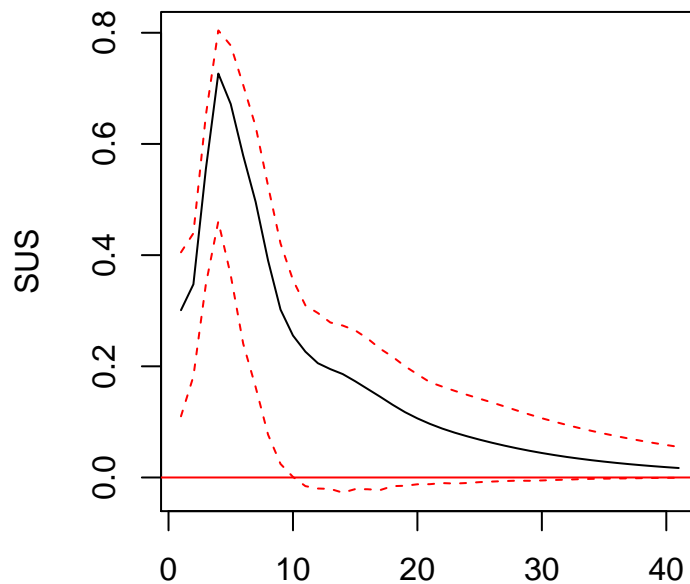
### 3. Replication

##

## SVAR Estimation Results:

```
## =====
##
## Call:
## BQ(x = var1)
##
## Type: Blanchard-Quah
## Sample size: 87
## Log Likelihood: -509.82
##
## Estimated contemporaneous impact matrix:
##           OIL      YUS   CPUS    SUS
## OIL  14.27792 -0.60992 0.5745  0.93202
## YUS   0.01323  0.46186 0.2982  0.14909
## CPUS  0.09324 -0.06909 0.1888 -0.02819
## SUS   0.10862 -0.03907 0.2478  0.78286
##
## Estimated identified long run impact matrix:
##           OIL      YUS   CPUS    SUS
## OIL  14.8451  0.00000 0.000 0.000
## YUS  -0.2685  1.15227 0.000 0.000
## CPUS  0.5088 -0.08494 1.052 0.000
## SUS   3.4184  2.47207 9.211 2.394
##
## Covariance matrix of reduced form residuals (*100):
##           OIL      YUS   CPUS    SUS
## OIL  20542.97 21.74 145.556 244.673
## YUS   21.74 32.46  2.140 17.400
## CPUS  145.56  2.14  4.989  3.754
## SUS   244.67 17.40  3.754 68.761
```

### Orthogonal Impulse Response from YUS



84 % Bootstrap CI, 100 runs

#### 4. Impulse response function

First thing I need to do is convert the data to a time series object in R. And to do this I need to create a date column.

The graph below, just shows you the dataset for the US. This is nice because you can see the pattern all the variables follow. This is not in the paper but might be nice to put in under ‘descriptive statistics’.

Now that I have a nice little graph, I can continue by creating my VAR. We first look at a simple four variable VAR. These variables are OIL, CPUS, YUS and SUS. This VAR will then be used for my impulse response functions.

## 5. Structural VAR

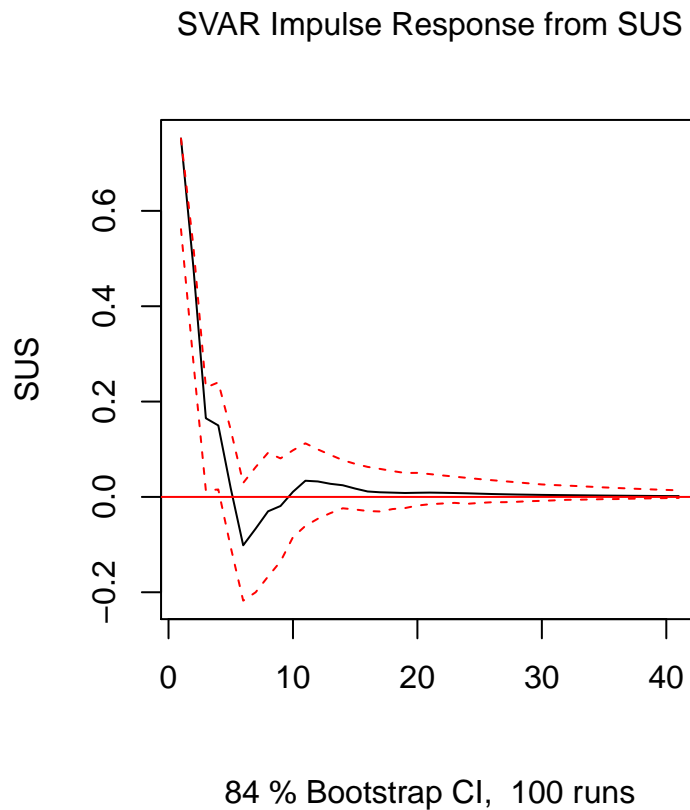
Argue that authors do not make use of a simple VAR but rather a structural VAR.

First VAR analysis that Peersman does is based on conventional zero contemporaneous and long run restrictions. Peersman assumes that there is a contemporaneous impact of an oil shock on all other variables in the system, but no immediate impact of the other shocks on oil

```
##      [,1] [,2] [,3] [,4]
## [1,]   NA    0    0    0
## [2,]   NA   NA    0    0
## [3,]   NA   NA   NA    0
## [4,]   NA   NA   NA   NA
```

```
##      [,1] [,2] [,3] [,4]
## [1,]   NA    0    0    0
## [2,]    0   NA    0    0
## [3,]    0    0   NA    0
## [4,]    0    0    0   NA
```





##

ACTUAL PROJECT DTAA

## 6. Test whether variables are stationary

Variables that are included in the dataset (same order): oil, output growth, consumer inflation and short-term nominal interest rate for EU and US.

Gideon suggested I only do the replication for the US, since this will be a lot of work.

In order to test whether a variable is stationary, you can use a unit root test such as the Dickey-Fuller (DF) test

Null hypothesis: There is a unit root Alternative hypothesis: Time series is stationary

If p-values is less than 0.05, it means we can reject the null hypothesis.

```
##
## Augmented Dickey-Fuller Test
##
## data: x$OIL
## Dickey-Fuller = -5.5461, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

##
## Augmented Dickey-Fuller Test
##
## data: x$YUS
## Dickey-Fuller = -4.0998, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

##
## Augmented Dickey-Fuller Test
##
## data: x$SUS
## Dickey-Fuller = -3.1218, Lag order = 4, p-value = 0.1143
## alternative hypothesis: stationary

##
## Augmented Dickey-Fuller Test
##
## data: x$CPUS
## Dickey-Fuller = -4.7117, Lag order = 4, p-value = 0.01
## alternative hypothesis: stationary

##
## Phillips-Perron Unit Root Test
##
## data: x$OIL
## Dickey-Fuller Z(alpha) = -66.677, Truncation lag parameter = 3, p-value
## = 0.01
## alternative hypothesis: stationary
```

```
##
## Phillips-Perron Unit Root Test
##
## data: x$YUS
## Dickey-Fuller Z(alpha) = -56.833, Truncation lag parameter = 3, p-value
## = 0.01
## alternative hypothesis: stationary
```

```
##
## Phillips-Perron Unit Root Test
##
## data: x$SUS
## Dickey-Fuller Z(alpha) = -15.957, Truncation lag parameter = 3, p-value
## = 0.1816
## alternative hypothesis: stationary
```

```
##
## Phillips-Perron Unit Root Test
##
## data: x$CPUS
## Dickey-Fuller Z(alpha) = -27.881, Truncation lag parameter = 3, p-value
## = 0.01
## alternative hypothesis: stationary
```

#Optimal lag length

I now determine the optimal lag length for an unrestricted VAR with a maximum lag length of 10.

According to the AIC and the FPE, the optimal lag length is 4. However, the SC and HQ criterion indicates an optimal lag length of 1. The data estimates a VAR including a constant and a trend as deterministic regressor.

I will use a VAR with lag length equal to one as specified by the paper.

```
## $selection
## AIC(n)  HQ(n)  SC(n) FPE(n)
##      2      2      1      2
##
```

## \$criteria

##	1	2	3	4	5	6
## AIC(n)	-0.33015958	-0.6286755	-0.5641153	-0.5631453	-0.3447481	-0.1678686
## HQ(n)	-0.04365279	-0.1511641	0.1044006	0.2963751	0.7057768	1.0736608
## SC(n)	0.38444841	0.5623378	1.1033034	1.5806787	2.2754812	2.9287660
## FPE(n)	0.71962087	0.5361090	0.5772066	0.5875388	0.7507903	0.9323487
##	7	8	9	10		
## AIC(n)	0.01651095	-0.2157611	-0.3324915	-0.5683809		
## HQ(n)	1.44904491	1.4077774	1.4820515	1.4371666		
## SC(n)	3.58955090	3.8336842	4.1933591	4.4338750		
## FPE(n)	1.18570839	1.0145723	0.9995686	0.9024505		



7. VAR

Diagram of fit and residuals for OIL

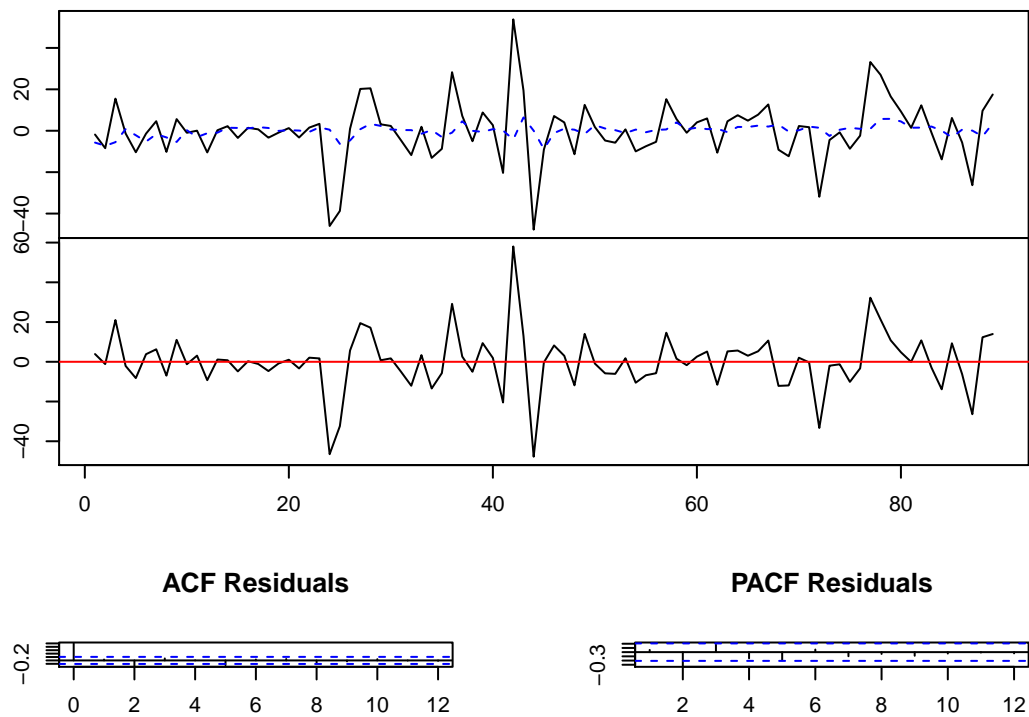
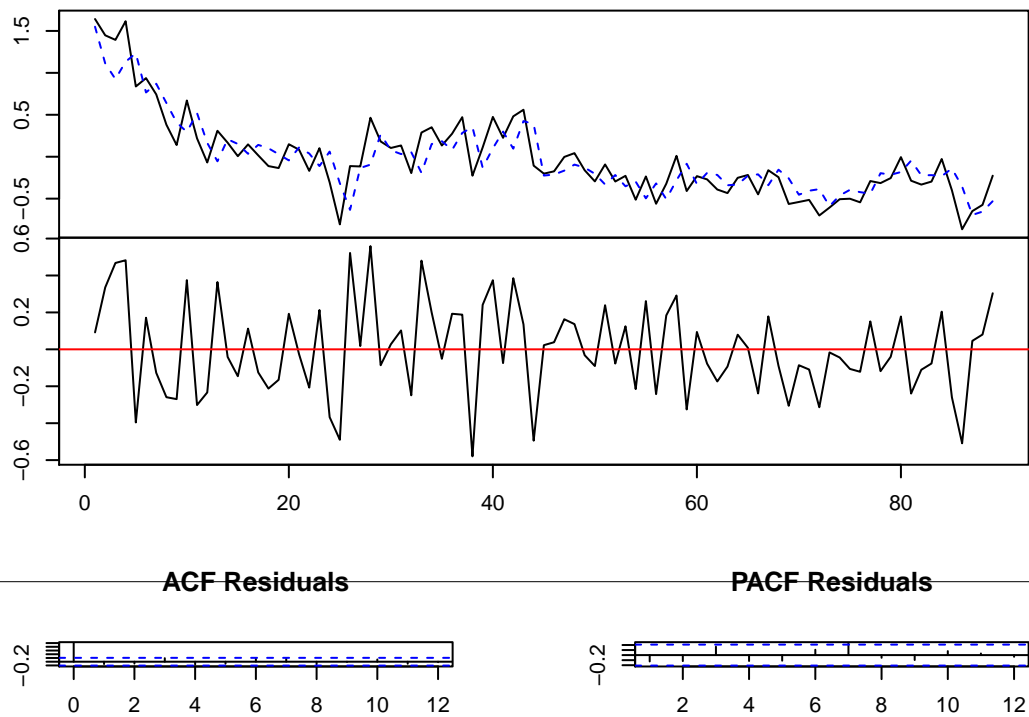


Diagram of fit and residuals for CPUS



# Diagnostic tests and Test statistics

The results for diagnostic test for VAR(1), VAR(2) and VAR(3) are provided in the table below.

Here you look and interpret all the test to determine whether VAR(1) is too restrictive. ARGUE this as part of your robustness test for the paper.

```
##
##  Portmanteau Test (asymptotic)
##
## data:  Residuals of VAR object VAR(vardat0, p = 1, type = "const")
## Chi-squared = 232.87, df = 240, p-value = 0.6172

## $JB
##
##  JB-Test (multivariate)
##
## data:  Residuals of VAR object VAR(vardat0, p = 1, type = "const")
## Chi-squared = 202.43, df = 8, p-value < 2.2e-16
##
##
## $Skewness
##
##  Skewness only (multivariate)
##
## data:  Residuals of VAR object VAR(vardat0, p = 1, type = "const")
## Chi-squared = 20.322, df = 4, p-value = 0.0004313
##
##
## $Kurtosis
##
##  Kurtosis only (multivariate)
##
## data:  Residuals of VAR object VAR(vardat0, p = 1, type = "const")
## Chi-squared = 182.11, df = 4, p-value < 2.2e-16

##
##  ARCH (multivariate)
```

```
##  
## data: Residuals of VAR object VAR(vardat0, p = 1, type = "const")  
## Chi-squared = 615.75, df = 500, p-value = 3e-04
```

## 8. Short run restrictions

Contemporaneous parameters

There is a contemporaneous impact of an oil shock on all variables but no immediate impact of other shocks on oil

monetary policy also has no contemporaneous effect on output.

Therefore  $b_{12}=b_{13}=b_{14}=0$  and  $b_{24}=0$  (found in Gerts discussion paper)

Note restrictions on matrix  $K_2-k/2$ . This implies we need six restrictions. Gert paper gives 4 short run and two long run restrictions. Therefore we need to argue two more short run restrictions.

$b_{23}=0$  since monetary policy shocks are shocks with a temporary effect on output, and are a combination of monetary policy, money demand and possibly exchange rate shocks, as long as these shocks have an influence on short term interest rates

Monetary policy has no effect on macro economic variables (CObin, 2012). Therefore  $b_{34}=0$

## 9. Conclusion



## References

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## Appendix

### *Appendix A*

Some appendix information here

### *Appendix B*