# Package 'fnets'

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<b>Description</b> Implements methods for network estimation and forecasting of high-dimensional time series exhibiting strong serial and cross-sectional correlations under a factor-adjusted vector autoregressive model.										
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common.predict

Forecasting the factor-driven common component

# Description

Produces forecasts of the common component for a given forecasting horizon by estimating the best linear predictors

#### Usage

```
common.predict(
  object,
  x,
  h = 1,
  common.method = c("restricted", "unrestricted"),
  r = NULL
)
```

#### **Arguments**

object fnets object

x input time series matrix, with each row representing a variable

h forecasting horizon

common.method a string specifying the method for common component forecasting; possible values are:

• "restricted" performs forecasting under a restrictive static factor model

• "unrestricted" performs forecasting under an unrestrictive, blockwise VAR representation of the common component

number of static factors; if common.method = "restricted" and r = NULL, it is estimated as the maximiser of the ratio of the successive eigenvalues of the estimate of the common component covariance matrix, see Ahn and Horenstein (2013)

# Value

r

#### a list containing

is in-sample estimator of the common component
 fc forecasts of the common component for a given forecasting horizon h
 r static factor number
 h forecast horizon

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#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

Ahn, S. C. & Horenstein, A. R. (2013) Eigenvalue ratio test for the number of factors. Econometrica, 81(3), 1203–1227.

Forni, M., Hallin, M., Lippi, M. & Reichlin, L. (2005). The generalized dynamic factor model: one-sided estimation and forecasting. Journal of the American Statistical Association, 100(471), 830–840.

Forni, M., Hallin, M., Lippi, M. & Zaffaroni, P. (2017). Dynamic factor models with infinite-dimensional factor space: Asymptotic analysis. Journal of Econometrics, 199(1), 74–92.

### **Examples**

fnets

Factor-adjusted network estimation

# **Description**

Operating under factor-adjusted vector autoregressive (VAR) model, the function estimates the spectral density and autocovariance matrices of the factor-driven common component and the idiosyncratic VAR process, the impulse response functions and common shocks for the common component, and VAR parameters, innovation covariance matrix and long-run partial correlations for the idiosyncratic component.

#### **Usage**

```
fnets(
    x,
    center = TRUE,
    q = NULL,
    ic.op = 5,
    kern.const = 4,
    common.args = list(var.order = NULL, max.var.order = NULL, trunc.lags = 20, n.perm = 10),
    idio.var.order = 1,
    idio.method = c("lasso", "ds"),
```

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```
idio.args = list(n.iter = 100, tol = 1e-05, n.cores = min(parallel::detectCores() -
  1, 3)),
lrpc.method = c("par", "npar", "none"),
cv.args = list(n.folds = 1, path.length = 10, do.plot = FALSE)
```

# **Arguments**

input time series matrix, with each row representing a variable Χ whether to de-mean the input x row-wise center number of factors. If q = NULL, the factor number is estimated by an information criterion-based approach of Hallin and Liška (2007), see hl.factor.number for further details choice of the information criterion, see hl.factor.number for further details ic.op kern.const constant multiplied to floor( $(\dim(x)[2]/\log(\dim(x)[2]))^{(1/3)}$ ) which determines the kernel bandwidth for dynamic PCA a list specifying the tuning parameters required for estimating the impulse recommon.args

sponse functions and common shocks. It contains:

- var. order order of the blockwise VAR representation of the common component. If var.order = NULL, it is selected blockwise by Schwarz criterion
- max.var.order maximum blockwise VAR order for the Schwarz criterion
- trunc.lags truncation lag for impulse response function estimation
- n.perm number of cross-sectional permutations involved in impluse response function estimation

idio.var.order order of the idiosyncratic VAR process; if a vector of integers is supplied, the order is chosen via cross validation

a string specifying the method to be adopted for idiosyncratic VAR process esidio.method timation; possible values are:

- "lasso" Lasso-type 11-regularised M-estimation
- "ds" Dantzig Selector-type constrained 11-minimisation

a list specifying the tuning parameters required for estimating the idiosyncratic VAR process. It contains:

- n.iter maximum number of descent steps; applicable when method = "lasso"
- tol numerical tolerance for increases in the loss function; applicable when method = "lasso"
- n.cores number of cores to use for parallel computing, see makePSOCKcluster; applicable when method = "ds"

1rpc.method

idio.args

a string specifying the type of estimator for long-run partial correlation matrix estimation; possible values are:

- "par" parametric estimator based on the VAR model assumption
- "npar" nonparametric estimator from inverting the long-run covariance matrix of the idiosyncratic component via constrained 11-minimisation
- "none" do not estimate the long-run partial correlation matrix

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cv.args

a list specifying arguments for the cross validation procedures for selecting the tuning parameters involved in VAR parameter and (long-run) partial correlation matrix estimation. It contains:

- n.folds number of folds
- path.length number of regularisation parameter values to consider; a sequence is generated automatically based in this value
- do.plot whether to plot the output of the cross validation step

#### **Details**

See Barigozzi, Cho and Owens (2021) for further details.

#### Value

an S3 object of class fnets, which contains the following fields:

q	number of factors
spec	a list containing estimates of the spectral density matrices for x, common and idiosyncratic components
acv	a list containing estimates of the autocovariance matrices for x, common and idiosyncratic components
common.irf	if $q \ge 1$ , a list containing estimators of the impulse response functions (as an array of dimension $(p,q,trunc.lags + 2)$ ) and common shocks (an array of dimension $(q,n)$ ) for the common component
idio.var	a list containing the following fields:
	<ul> <li>beta estimate of VAR parameter matrix; each column contains parameter estimates for the regression model for a given variable</li> <li>Gamma estimate of the innovation covariance matrix</li> <li>lambda regularisation parameter</li> <li>var.order VAR order</li> </ul>
lrpc	see the output of par.lrpc if lrpc.method = 'par' and that of npar.lrpc if lrpc.method = 'npar'
mean.x	if center = TRUE, returns a vector containing row-wise sample means of $x$ ; if center = FALSE, returns a vector of zeros
idio.method	input parameter
1rpc.method	input parameter
kern.const	input parameter

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

Hallin, M. & Liška, R. (2007) Determining the number of factors in the general dynamic factor model. Journal of the American Statistical Association, 102(478), 603–617.

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#### See Also

predict.fnets, plot.fnets

#### **Examples**

```
## Not run:
set.seed(123)
n <- 500
p <- 50
common <- sim.common1(n, p)
idio <- sim.var(n, p)
x <- common$\frac{1}{2}\text{data} \text{dio.}\text{var.order} = 1, idio.method = "lasso",
lrpc.method = "par", cv.args = list(n.folds = 1, path.length = 10, do.plot = TRUE))
pre <- predict(out, x, h = 1, common.method = 'unrestricted')
plot(out, type = 'granger', display = 'network', threshold = .05)
plot(out, type = 'lrpc', display = 'heatmap', threshold = .05)
## End(Not run)</pre>
```

fnets.var

11-regularised Yule-Walker estimation for VAR processes

#### **Description**

Estimates the VAR parameter matrices via 11-regularised Yule-Walker estimation and innovation covariance matrix via constrained 11-minimisation.

#### Usage

```
fnets.var(
    x,
    center = TRUE,
    method = c("lasso", "ds"),
    lambda = NULL,
    var.order = 1,
    cv.args = list(n.folds = 1, path.length = 10, do.plot = FALSE),
    n.iter = 100,
    tol = 1e-05,
    n.cores = min(parallel::detectCores() - 1, 3)
)
```

# **Arguments**

x input time series matrix, with each row representing a variable

center whether to de-mean the input x row-wise

method a string specifying the method to be adopted for VAR process estimation; possi-

ble values are:

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	<ul> <li>"lasso" Lasso-type 11-regularised M-estimation</li> </ul>
	<ul> <li>"ds" Dantzig Selector-type constrained 11-minimisation</li> </ul>
lambda	regularisation parameter; if lambda = NULL, cross validation is employed to select the parameter
var.order	order of the VAR process; if a vector of integers is supplied, the order is chosen via cross validation
cv.args	a list specifying arguments for the cross validation procedure for selecting the regularisation parameter (and VAR order). It contains:
	• n.folds number of folds
	• path.length number of regularisation parameter values to consider; a sequence is generated automatically based in this value
	• do.plot whether to plot the output of the cross validation step
n.iter	maximum number of descent steps; applicable when method = "lasso"
tol	numerical tolerance for increases in the loss function; applicable when method = "lasso" $$
n.cores	number of cores to use for parallel computing, see <pre>makePSOCKcluster</pre> ; applicable when method = "ds"

# **Details**

Further information can be found in Barigozzi, Cho and Owens (2021).

#### Value

a list which contains the following fields:

beta estimate of VAR parameter matrix; each column contains parameter estimates

for the regression model for a given variable

Gamma estimate of the innovation covariance matrix

lambda regularisation parameter

var.order VAR order

mean.x if center = TRUE, returns a vector containing row-wise sample means of x; if

center = FALSE, returns a vector of zeros

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

```
library(fnets)
set.seed(123)
n <- 500
p <- 50
```

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hl.factor.number

Factor number estimator of Hallin and Liška (2007)

# Description

Estimates the number of factors by minimising an information criterion over sub-samples of the data. Currently the three information criteria proposed in Hallin and Liška (2007) (ic.op = 1,2 or 3) and their variations with logarithm taken on the cost (ic.op = 4,5 or 6) are implemented, with ic.op = 5 recommended as a default choice based on numerical experiments.

# Usage

```
hl.factor.number(x, q.max = NULL, mm, w = NULL, do.plot = FALSE, center = TRUE)
```

#### **Arguments**

Χ	input time series matrix, with each row representing a variable
q.max	maximum number of factors; if $q.max = NULL$ , a default value is selected as $min(50,floor(sqrt(min(dim(x)[2]-1,dim(x)[1])))$
mm	integer representing the kernel bandwidth
W	vector of length $2 * mm + 1$ containing symmetric weights; if $w = NULL$ , default weights are generated using the Bartlett kernel and $mm$
do.plot	whether to plot the values of six information criteria
center	whether to de-mean the input x row-wise

### **Details**

See Hallin and Liška (2007) for further details.

#### Value

a list containing	
q.hat	a vector containing minimisers of the six information criteria
Gamma_x	an array containing the estimates of the autocovariance matrices of x at 2 $\star$ mm + 1 lags
Sigma_x	an array containing the estimates of the spectral density matrices of x at 2 $\star$ mm + 1 Fourier frequencies
sv	a list containing the singular value decomposition of Sigma_x

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#### References

Hallin, M. & Liška, R. (2007) Determining the number of factors in the general dynamic factor model. Journal of the American Statistical Association, 102(478), 603–617.

# **Examples**

```
library(fnets)

set.seed(123)
n <- 500
p <- 50
common <- sim.common2(n, p)
idio <- sim.var(n, p)
x <- common$\frac{1}{2} \text{ apply(idio$\frac{1}{2}} \text{ data}, 1, sd)/\text{ apply(common$\frac{1}{2}} \text{ data}, 1, sd) + idio$\frac{1}{2} \text{ data}

hl <- hl.factor.number(x, q.max = NULL, mm = floor(4 * (n/log(n))^*(1/3)), do.plot = TRUE)
hl$q</pre>
```

idio.predict

Forecasting idiosyncratic VAR process

#### **Description**

Produces forecasts of the idiosyncratic VAR process for a given forecasting horizon by estimating the best linear predictors

# Usage

```
idio.predict(object, x, cpre, h = 1)
```

# Arguments

object fnets object

x input time series matrix, with each row representing a variable

cpre output of common.predict

h forecast horizon

#### Value

a list containing

is in-sample estimator of the idiosyncratic component

fc forecasts of the idiosyncratic component for a given forecasting horizon h

h forecast horizon

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#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

# **Examples**

npar.lrpc

Nonparametric estimation of long-run partial correlations of factoradjusted VAR processes

# Description

Returns a nonparametric estimate of long-run partial correlations of the VAR process from the inverse of long-run covariance matrix obtained via constrained 11-minimisation.

#### Usage

```
npar.lrpc(
  object,
  x,
  eta = NULL,
  cv.args = list(n.folds = 1, path.length = 10, do.plot = FALSE),
  do.correct = TRUE,
  n.cores = min(parallel::detectCores() - 1, 3)
)
```

# **Arguments**

```
object fnets object

x input time series matrix; with each row representing a variable

eta regularisation parameter; if eta = NULL, it is selected by cross validation

cv.args a list specifying arguments for the cross validation procedure for selecting the tuning parameter involved in long-run partial correlation matrix estimation. It contains:
```

• n.folds number of folds

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• path.length number of regularisation parameter values to consider; a sequence is generated automatically based in this value

• do.plot whether to plot the output of the cross validation step

do.correct whether to correct for any negative entries in the diagonals of the inverse of

long-run covariance matrix

n. cores number of cores to use for parallel computing, see makePSOCKcluster

#### Value

a list containing

Omega estimated inverse of the long-run covariance matrix

1rpc estimated long-run partial correlation matrix

eta regularisation parameter

### **Examples**

par.lrpc

Parametric estimation of long-run partial correlations of factoradjusted VAR processes

# **Description**

Returns a parametric estimate of long-run partial correlations of the VAR process from the VAR parameter estimates and the inverse of innovation covariance matrix obtained via constrained 11-minimisation.

par.lrpc

# Usage

```
par.lrpc(
  object,
  x,
  eta = NULL,
  cv.args = list(n.folds = 1, path.length = 10, do.plot = FALSE),
  adaptive = FALSE,
  eta.1 = NULL,
  do.correct = TRUE,
  n.cores = min(parallel::detectCores() - 1, 3)
)
```

# Arguments

object	fnets object
X	input time series matrix; with each row representing a variable
eta	regularisation parameter; if eta = NULL, it is selected by cross validation
cv.args	a list specifying arguments for the cross validation procedure for selecting the tuning parameter involved in long-run partial correlation matrix estimation. It contains:
	• n.folds number of folds
	• path.length number of regularisation parameter values to consider; a sequence is generated automatically based in this value
	• do.plot whether to plot the output of the cross validation step
adaptive	whether to use the adaptive estimation procedure
eta.1	regularisation parameter for Step 1 of the adaptive estimation procedure; if eta.1 = NULL, defaults to $2 * sqrt(log(dim(x)[1])/dim(x)[2])$
do.correct	whether to correct for any negative entries in the diagonals of the inverse of long-run covariance matrix
n.cores	number of cores to use for parallel computing, see makePSOCKcluster

#### **Details**

See Barigozzi, Cho and Owens (2021) for further details.

# Value

# a list containing

Delta estimated inverse of the innovation covariance matrix
Omega estimated inverse of the long-run covariance matrix
pc estimated innovation partial correlation matrix
lrpc estimated long-run partial correlation matrix
eta regularisation parameter
adaptive was the adaptive procedure used

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#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

#### **Examples**

plot.fnets

Plotting the networks estimated by fnets

# Description

Plotting method for S3 objects of class fnets. Produces a plot visualising three networks underlying factor-adjusted VAR processes: (i) directed network representing Granger causal linkages, as given by estimated VAR transition matrices aggregated across the lags, (ii) undirected network representing contemporaneous linkages after accounting for lead-lag dependence, as given by partial correlations of VAR innovations, (iii) undirected network summarising (i) and (ii) as given by long-run partial correlations of VAR processes.

# Usage

```
## S3 method for class 'fnets'
plot(
    x,
    type = c("granger", "pc", "lrpc"),
    display = c("network", "heatmap"),
    names = NA,
    groups = NA,
    threshold = 0,
    ...
)
```

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#### **Arguments**

x fnets object type a string specifying which of the above three networks (i)–(iii) to vis

a string specifying which of the above three networks (i)–(iii) to visualise; possible values are

- "granger" directed network representing Granger causal linkages
- "pc" undirected network representing contemporaneous linkages; available when x\$1rpc.method = "par"
- "lrpc" undirected network summarising Granger causal and contemporaneous linkages; available when x\$lrpc.method = "par" or x\$lrpc.method = "npar"

display a string specifying how to visualise the network; possible values are:

- "network" as an igraph object, see plot.igraph
- "heatmap" as a heatmap, see imagePlot

names a character vector containing the names of the vertices

groups an integer vector denoting any group structure of the vertices

threshold if threshold > 0, hard thresholding is performed on the matrix giving rise to

the network of interest

... additional arguments

#### **Details**

See Barigozzi, Cho and Owens (2021) for further details.

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

#### See Also

fnets

predict.fnets Forecasting by fnets

#### **Description**

Produces forecasts of the data for a given forecasting horizon by separately estimating the best linear predictors of common and idiosyncratic components

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#### Usage

```
## S3 method for class 'fnets'
predict(
  object,
    x,
    h = 1,
    common.method = c("restricted", "unrestricted"),
    r = NULL,
    ...
)
```

#### **Arguments**

object fnets object

x input time series matrix, with each row representing a variable

h forecasting horizon

common.method a string specifying the method for common component forecasting; possible

values are:

• "restricted" performs forecasting under a restrictive static factor model

• "unrestricted" performs forecasting under an unrestrictive, blockwise

VAR representation of the common component

number of static factors; if common.method = "restricted" and r = NULL, it is estimated as the maximiser of the ratio of the successive eigenvalues of the

estimate of the common component covariance matrix, see Ahn and Horenstein

(2013)

... not used

# Value

r

a list containing

forecast for the given forecasting horizon

common.pred a list containing forecasting results for the common component a list containing forecasting results for the idiosyncratic component

mean.x mean.x argument from object

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

Ahn, S. C. & Horenstein, A. R. (2013) Eigenvalue ratio test for the number of factors. Econometrica, 81(3), 1203–1227.

#### See Also

fnets, common.predict, idio.predict

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	_
cim	common1

Simulate data from a dynamic factor model

# Description

Simulate the common component following a dynamic factor model that does not admit a static representation; see the model (C1) in the reference.

# Usage

```
sim.common1(n, p, q = 2, heavy = FALSE)
```

# **Arguments**

n	sample size
р	dimension

q number of dynamic factors

heavy if heavy = FALSE, common shocks are generated from rnorm whereas if heavy

= TRUE, from rt with df = 5 and then scaled by sqrt(3 / 5)

# Value

a list containing

data generated series
q number of factors

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

```
common <- sim.common1(500, 50)</pre>
```

sim.common2

sim.common2	Simulate data from a static factor model	

# Description

Simulate the common component following a dynamic factor model that admits a static representation; see the model (C2) in the reference.

# Usage

```
sim.common2(n, p, q = 2, heavy = FALSE)
```

# Arguments

n	sample size
р	dimension
q	number of dynamic factors; number of static factors is given by 2 * q
heavy	if heavy = FALSE, common shocks are generated from rnorm whereas if heavy = TRUE, from rt with df = 5 and then scaled by sqrt(3 / 5)

# Value

a list containing

data generated seriesq number of factorsr number of static factors

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

```
common <- sim.common2(500, 50)</pre>
```

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SI	n.	va	r

Simulate a VAR(1) process

# Description

Simulate a VAR(1) process; see the reference for the generation of the transition matrix.

# Usage

```
sim.var(n, p, Gamma = diag(1, p), heavy = FALSE)
```

# Arguments

n sample size p dimension

Gamma innovation covariance matrix; ignored if heavy = TRUE

heavy if heavy = FALSE, common shocks are generated from rnorm whereas if heavy

= TRUE, from rt with df = 5 and then scaled by sqrt(3 / 5)

#### Value

a list containing

data generated series
A transition matrix

Gamma innovation covariance matrix

#### References

Barigozzi, M., Cho, H. & Owens, D. (2021) FNETS: Factor-adjusted network analysis for high-dimensional time series.

```
idio <- sim.var(500, 50)
```

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