

6. Update operation

$$(n, S, T) + (1, x_j, x_j x_j^T) = (n+1, S+x_j, T+x_j x_j^T)$$

7. Compactness and Efficiency:

Compactness:  $\pm$ , on comparing with situation where we need to store all vectors, in this case info we just store one number, one vector (size of  $m$ ) and one matrix

Efficiency:  $\pm$ , lightweight operations for combining, and heavy operations for matrix computations

8. Minimum number  $n$  is 1