

$\left. \begin{matrix} LR(1) \\ LR(0) \\ LALR(1) \end{matrix} \right\}$ bottom-up parsing
yacc \leftarrow

$\left. \begin{matrix} \text{leftmost derivation} \\ \text{rightmost} \end{matrix} \right\}$
lookahead(k)

Section 4.4 Top Down Parsing

example:

$E \rightarrow E + T \mid T$
 $T \rightarrow T * F \mid F$
 $F \rightarrow (E) \mid ID$

remove
① left-recursive
② left-factoring

Alg 4.1 p179
① $A \rightarrow A\alpha \mid \beta$
 \Downarrow
 $A \rightarrow \beta A'$
 $A' \rightarrow \alpha A' \mid \epsilon$
② $A \rightarrow \alpha B \mid \alpha C$
 \Downarrow
 $A \rightarrow \alpha A'$
 $A' \rightarrow B \mid C$

Alg 4.2 p178

$A \rightarrow \alpha A'$
 $A' \rightarrow B \mid C$

$E' \rightarrow \epsilon$ p189
 $E \rightarrow TE'$
 $E' \rightarrow +TE' \mid \epsilon$
 $T \rightarrow FT'$
 $T' \rightarrow *FT' \mid \epsilon$
 $F \rightarrow (E) \mid ID$

	FIRST	FOLLOW
E	(, ID	\$,)
E'	+, ϵ	\$,)
T	(, ID	+, \$,)
T'	*, ϵ	+, \$,)
F	(, ID	*, +, \$,)

$F \rightarrow (E)$
 \uparrow
A
 α
 \uparrow
B
 β

Follow(A):

- ① $\$ \in \text{Follow}(S)$
- ② If $A \rightarrow \alpha B \beta$: place anything in $\text{FIRST}(\beta)$ except ϵ in $\text{Follow}(B)$
- ③ If $A \rightarrow \alpha B$ or $A \rightarrow \alpha B \beta$ where $\epsilon \in \text{FIRST}(\beta)$: place anything in $\text{Follow}(A)$ into $\text{Follow}(B)$

start symbol $\$$ Follow(A) =

$S \xRightarrow{*} A \xRightarrow{*} \alpha B \xRightarrow{*} \dots$

Build a Parse Table (Alg 4.4 p190)
Fig 4.15 p188

	ID	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow ID$			$F \rightarrow (E)$		

Trace pp 188 Fig 4.16
Stack Input

$\$ E$ ID + ID * ID \$
 $\$ E T$ ID + ID * ID \$
 $\$ E T F$ ID + ID * ID \$
 $\$ E T' F$ ID + ID * ID \$
 $\$ E T'$ + ID \$ ID \$
 $\$ E T'$ + ID * ID \$
 $\$ E T' +$ + ID * ID \$
 $\$ E T$ ID * ID \$
 $\$ E T' F$ ID * ID \$
 $\$ E T' ID$ ID * ID \$
 $\$ E T'$ * ID \$
 $\$ E T' F *$ * ID \$
 $\$ E T' F$ ID \$
 $\$ E T' ID$ ID \$
 $\$ E T'$ \$ \$
 $\$ E$ ACCEPT \$