

Matrix2D

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# Chapter 1

## Class Index

### 1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

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| <a href="#">Mat2D_Minor</a>  | A minor "view" into a reference matrix | 7 |
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# Chapter 2

## File Index

### 2.1 File List

Here is a list of all files with brief descriptions:

|                            |   |                    |
|----------------------------|---|--------------------|
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| <a href="#">temp.c</a>     |   | <a href="#">59</a> |



# Chapter 3

## Class Documentation

### 3.1 Mat2D Struct Reference

Dense row-major matrix of double.

```
#include <Matrix2D.h>
```

#### Public Attributes

- size\_t `rows`
- size\_t `cols`
- size\_t `stride_r`
- double \* `elements`

#### 3.1.1 Detailed Description

Dense row-major matrix of double.

- `rows` Number of rows (height).
- `cols` Number of columns (width).
- `stride_r` Number of elements between successive rows in memory. For contiguous storage, `stride_r == cols`.
- `elements` Pointer to a contiguous buffer of `rows * cols` doubles.

#### Note

This type is a shallow handle; copying `Mat2D` copies the pointer, not the underlying data.

Definition at line 117 of file [Matrix2D.h](#).

#### 3.1.2 Member Data Documentation

### 3.1.2.1 cols

```
size_t Mat2D::cols
```

Definition at line 119 of file [Matrix2D.h](#).

Referenced by [mat2D\\_add\(\)](#), [mat2D\\_add\\_col\\_to\\_col\(\)](#), [mat2D\\_add\\_row\\_time\\_factor\\_to\\_row\(\)](#), [mat2D\\_add\\_row\\_to\\_row\(\)](#), [mat2D\\_alloc\(\)](#), [mat2D\\_calc\\_norma\(\)](#), [mat2D\\_copy\(\)](#), [mat2D\\_copy\\_mat\\_to\\_mat\\_at\\_window\(\)](#), [mat2D\\_cross\(\)](#), [mat2D\\_det\(\)](#), [mat2D\\_det\\_2x2\\_mat\(\)](#), [mat2D\\_dot\(\)](#), [mat2D\\_dot\\_product\(\)](#), [mat2D\\_fill\(\)](#), [mat2D\\_fill\\_sequence\(\)](#), [mat2D\\_get\\_col\(\)](#), [mat2D\\_get\\_row\(\)](#), [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), [mat2D\\_make\\_identity\(\)](#), [mat2D\\_mat\\_is\\_all\\_digit\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_mult\(\)](#), [mat2D\\_mult\\_row\(\)](#), [mat2D\\_offset2d\(\)](#), [mat2D\\_print\(\)](#), [mat2D\\_print\\_as\\_col\(\)](#), [mat2D\\_rand\(\)](#), [mat2D\\_row\\_is\\_all\\_digit\(\)](#), [mat2D\\_set\\_identity\(\)](#), [mat2D\\_set\\_rot\\_mat\\_x\(\)](#), [mat2D\\_set\\_rot\\_mat\\_y\(\)](#), [mat2D\\_set\\_rot\\_mat\\_z\(\)](#), [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#), [mat2D\\_sub\(\)](#), [mat2D\\_sub\\_col\\_to\\_col\(\)](#), [mat2D\\_sub\\_row\\_time\\_factor\\_to\\_row\(\)](#), [mat2D\\_sub\\_row\\_to\\_row\(\)](#), [mat2D\\_swap\\_rows\(\)](#), [mat2D\\_transpose\(\)](#), and [mat2D\\_upper\\_triangulate\(\)](#).

### 3.1.2.2 elements

```
double* Mat2D::elements
```

Definition at line 121 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\(\)](#), [mat2D\\_free\(\)](#), and [mat2D\\_print\\_as\\_col\(\)](#).

### 3.1.2.3 rows

```
size_t Mat2D::rows
```

Definition at line 118 of file [Matrix2D.h](#).

Referenced by [mat2D\\_add\(\)](#), [mat2D\\_add\\_col\\_to\\_col\(\)](#), [mat2D\\_add\\_row\\_to\\_row\(\)](#), [mat2D\\_alloc\(\)](#), [mat2D\\_calc\\_norma\(\)](#), [mat2D\\_col\\_is\\_all\\_digit\(\)](#), [mat2D\\_copy\(\)](#), [mat2D\\_copy\\_mat\\_to\\_mat\\_at\\_window\(\)](#), [mat2D\\_cross\(\)](#), [mat2D\\_det\(\)](#), [mat2D\\_det\\_2x2\\_mat\(\)](#), [mat2D\\_dot\(\)](#), [mat2D\\_dot\\_product\(\)](#), [mat2D\\_fill\(\)](#), [mat2D\\_fill\\_sequence\(\)](#), [mat2D\\_get\\_col\(\)](#), [mat2D\\_get\\_row\(\)](#), [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), [mat2D\\_make\\_identity\(\)](#), [mat2D\\_mat\\_is\\_all\\_digit\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_mult\(\)](#), [mat2D\\_offset2d\(\)](#), [mat2D\\_print\(\)](#), [mat2D\\_print\\_as\\_col\(\)](#), [mat2D\\_rand\(\)](#), [mat2D\\_set\\_identity\(\)](#), [mat2D\\_set\\_rot\\_mat\\_x\(\)](#), [mat2D\\_set\\_rot\\_mat\\_y\(\)](#), [mat2D\\_set\\_rot\\_mat\\_z\(\)](#), [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#), [mat2D\\_sub\(\)](#), [mat2D\\_sub\\_col\\_to\\_col\(\)](#), [mat2D\\_sub\\_row\\_to\\_row\(\)](#), [mat2D\\_transpose\(\)](#), and [mat2D\\_upper\\_triangulate\(\)](#).

### 3.1.2.4 stride\_r

```
size_t Mat2D::stride_r
```

Definition at line 120 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\(\)](#), and [mat2D\\_offset2d\(\)](#).

The documentation for this struct was generated from the following file:

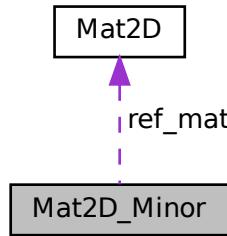
- [Matrix2D.h](#)

## 3.2 Mat2D\_Minor Struct Reference

A minor "view" into a reference matrix.

```
#include <Matrix2D.h>
```

Collaboration diagram for Mat2D\_Minor:



### Public Attributes

- `size_t rows`
- `size_t cols`
- `size_t stride_r`
- `size_t * rows_list`
- `size_t * cols_list`
- `Mat2D ref_mat`

#### 3.2.1 Detailed Description

A minor "view" into a reference matrix.

Represents a minor by excluding one row and one column of a reference matrix. The minor does not own the reference matrix data; instead it stores two index arrays (`rows_list`, `cols_list`) mapping minor coordinates to the reference matrix coordinates.

Memory ownership:

- `rows_list` and `cols_list` are heap-allocated by the minor allocators and must be freed with `mat2D_minor_free()`.
- `ref_mat.elements` is not owned by the minor and must not be freed by `mat2D_minor_free()`.

Definition at line 152 of file [Matrix2D.h](#).

#### 3.2.2 Member Data Documentation

### 3.2.2.1 cols

```
size_t Mat2D_Minor::cols
```

Definition at line 154 of file [Matrix2D.h](#).

Referenced by [mat2D\\_det\(\)](#), [mat2D\\_det\\_2x2\\_mat\\_minor\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#), [mat2D\\_minor\\_det\(\)](#), and [mat2D\\_minor\\_print\(\)](#).

### 3.2.2.2 cols\_list

```
size_t* Mat2D_Minor::cols_list
```

Definition at line 157 of file [Matrix2D.h](#).

Referenced by [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#), and [mat2D\\_minor\\_free\(\)](#).

### 3.2.2.3 ref\_mat

```
Mat2D Mat2D_Minor::ref_mat
```

Definition at line 158 of file [Matrix2D.h](#).

Referenced by [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), and [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#).

### 3.2.2.4 rows

```
size_t Mat2D_Minor::rows
```

Definition at line 153 of file [Matrix2D.h](#).

Referenced by [mat2D\\_det\(\)](#), [mat2D\\_det\\_2x2\\_mat\\_minor\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#), [mat2D\\_minor\\_det\(\)](#), and [mat2D\\_minor\\_print\(\)](#).

### 3.2.2.5 rows\_list

```
size_t* Mat2D_Minor::rows_list
```

Definition at line 156 of file [Matrix2D.h](#).

Referenced by [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#), and [mat2D\\_minor\\_free\(\)](#).

### 3.2.2.6 stride\_r

```
size_t Mat2D_Minor::stride_r
```

Definition at line 155 of file [Matrix2D.h](#).

Referenced by [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), and [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#).

The documentation for this struct was generated from the following file:

- [Matrix2D.h](#)

## 3.3 Mat2D\_uint32 Struct Reference

Dense row-major matrix of uint32\_t.

```
#include <Matrix2D.h>
```

### Public Attributes

- size\_t [rows](#)
- size\_t [cols](#)
- size\_t [stride\\_r](#)
- uint32\_t \* [elements](#)

### 3.3.1 Detailed Description

Dense row-major matrix of uint32\_t.

Same layout rules as [Mat2D](#), but with uint32\_t elements.

Definition at line 130 of file [Matrix2D.h](#).

### 3.3.2 Member Data Documentation

#### 3.3.2.1 cols

```
size_t Mat2D_uint32::cols
```

Definition at line 132 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\\_uint32\(\)](#), [mat2D\\_fill\\_uint32\(\)](#), and [mat2D\\_offset2d\\_uint32\(\)](#).

### 3.3.2.2 elements

```
uint32_t* Mat2D_uint32::elements
```

Definition at line 134 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\\_uint32\(\)](#), and [mat2D\\_free\\_uint32\(\)](#).

### 3.3.2.3 rows

```
size_t Mat2D_uint32::rows
```

Definition at line 131 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\\_uint32\(\)](#), [mat2D\\_fill\\_uint32\(\)](#), and [mat2D\\_offset2d\\_uint32\(\)](#).

### 3.3.2.4 stride\_r

```
size_t Mat2D_uint32::stride_r
```

Definition at line 133 of file [Matrix2D.h](#).

Referenced by [mat2D\\_alloc\\_uint32\(\)](#), and [mat2D\\_offset2d\\_uint32\(\)](#).

The documentation for this struct was generated from the following file:

- [Matrix2D.h](#)

# Chapter 4

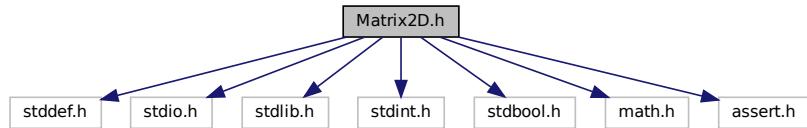
## File Documentation

### 4.1 Matrix2D.h File Reference

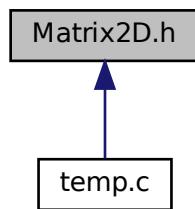
Lightweight 2D matrix helpers (double / uint32\_t).

```
#include <stddef.h>
#include <stdio.h>
#include <stdlib.h>
#include <stdint.h>
#include <stdbool.h>
#include <math.h>
#include <assert.h>
```

Include dependency graph for Matrix2D.h:



This graph shows which files directly or indirectly include this file:



## Classes

- struct `Mat2D`  
*Dense row-major matrix of double.*
- struct `Mat2D_uint32`  
*Dense row-major matrix of uint32\_t.*
- struct `Mat2D_Minor`  
*A minor "view" into a reference matrix.*

## Macros

- `#define MAT2D_MALLOC` malloc  
*Allocation function used by this library.*
- `#define MAT2D_FREE` free  
*Deallocation function used by this library.*
- `#define MAT2D_ASSERT` assert  
*Assertion macro used by this library for parameter validation.*
- `#define MAT2D_AT(m, i, j)` `(m).elements[mat2D_offset2d((m), (i), (j))]`  
*Access element (i, j) of a `Mat2D` (0-based).*
- `#define MAT2D_AT_UINT32(m, i, j)` `(m).elements[mat2D_offset2d_uint32((m), (i), (j))]`  
*Access element (i, j) of a `Mat2D_uint32` (0-based).*
- `#define MAT2D_PI` 3.14159265358979323846
- `#define MAT2D_EPS` 1e-15
- `#define MAT2D_IS_ZERO(x)` `(fabs(x) < MAT2D_EPS)`  
*Test whether a floating-point value is "near zero".*
- `#define MAT2D_MINOR_AT(mm, i, j)` `MAT2D_AT((mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j])`  
*Access element (i, j) of a `Mat2D_Minor` (0-based).*
- `#define MAT2D_PRINT(m)` `mat2D_print(m, #m, 0)`  
*Convenience macro to print a matrix with its variable name.*
- `#define MAT2D_PRINT_AS_COL(m)` `mat2D_print_as_col(m, #m, 0)`  
*Convenience macro to print a matrix as a single column with its name.*
- `#define MAT2D_MINOR_PRINT(mm)` `mat2D_minor_print(mm, #mm, 0)`  
*Convenience macro to print a minor with its variable name.*
- `#define mat2D_normalize(m)` `mat2D_mult((m), 1.0 / mat2D_calc_norma((m)))`  
*Normalize a matrix in-place to unit Frobenius norm.*

## Functions

- `double mat2D_rand_double (void)`  
*Return a pseudo-random double in the range [0, 1].*
- `Mat2D mat2D_alloc (size_t rows, size_t cols)`  
*Allocate a rows-by-cols matrix of double.*
- `Mat2D_uint32 mat2D_alloc_uint32 (size_t rows, size_t cols)`  
*Allocate a rows-by-cols matrix of uint32\_t.*
- `void mat2D_free (Mat2D m)`  
*Free the buffer owned by a `Mat2D`.*
- `void mat2D_free_uint32 (Mat2D_uint32 m)`  
*Free the buffer owned by a `Mat2D_uint32`.*
- `size_t mat2D_offset2d (Mat2D m, size_t i, size_t j)`  
*Compute the linear offset of element (i, j) in a `Mat2D`.*

- `size_t mat2D_offset2d_uint32 (Mat2D_uint32 m, size_t i, size_t j)`  
`Compute the linear offset of element (i, j) in a Mat2D_uint32.`
- `void mat2D_fill (Mat2D m, double x)`  
`Fill all elements of a matrix of doubles with a scalar value.`
- `void mat2D_fill_sequence (Mat2D m, double start, double step)`  
`Fill a matrix with an arithmetic sequence laid out in row-major order.`
- `void mat2D_fill_uint32 (Mat2D_uint32 m, uint32_t x)`  
`Fill all elements of a matrix of uint32_t with a scalar value.`
- `void mat2D_rand (Mat2D m, double low, double high)`  
`Fill a matrix with pseudo-random doubles in [low, high].`
- `void mat2D_dot (Mat2D dst, Mat2D a, Mat2D b)`  
`Matrix product: dst = a * b.`
- `double mat2D_dot_product (Mat2D a, Mat2D b)`  
`Dot product between two vectors.`
- `void mat2D_cross (Mat2D dst, Mat2D a, Mat2D b)`  
`3D cross product: dst = a x b for 3x1 vectors.`
- `void mat2D_add (Mat2D dst, Mat2D a)`  
`In-place addition: dst += a.`
- `void mat2D_add_row_time_factor_to_row (Mat2D m, size_t des_r, size_t src_r, double factor)`  
`Row operation: row(des_r) += factor * row(src_r).`
- `void mat2D_sub (Mat2D dst, Mat2D a)`  
`In-place subtraction: dst -= a.`
- `void mat2D_sub_row_time_factor_to_row (Mat2D m, size_t des_r, size_t src_r, double factor)`  
`Row operation: row(des_r) -= factor * row(src_r).`
- `void mat2D_mult (Mat2D m, double factor)`  
`In-place scalar multiplication: m *= factor.`
- `void mat2D_mult_row (Mat2D m, size_t r, double factor)`  
`In-place row scaling: row(r) *= factor.`
- `void mat2D_print (Mat2D m, const char *name, size_t padding)`  
`Print a matrix to stdout with a name and indentation padding.`
- `void mat2D_print_as_col (Mat2D m, const char *name, size_t padding)`  
`Print a matrix as a flattened column vector to stdout.`
- `void mat2D_set_identity (Mat2D m)`  
`Set a square matrix to the identity matrix.`
- `double mat2D_make_identity (Mat2D m)`  
`Reduce a matrix to identity using Gauss-Jordan style elimination.`
- `void mat2D_set_rot_mat_x (Mat2D m, float angle_deg)`  
`Set a 3x3 rotation matrix for rotation about the X-axis.`
- `void mat2D_set_rot_mat_y (Mat2D m, float angle_deg)`  
`Set a 3x3 rotation matrix for rotation about the Y-axis.`
- `void mat2D_set_rot_mat_z (Mat2D m, float angle_deg)`  
`Set a 3x3 rotation matrix for rotation about the Z-axis.`
- `void mat2D_set_DCM_zyx (Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg)`  
`Build a 3x3 direction cosine matrix (DCM) from Z-Y-X Euler angles.`
- `void mat2D_copy (Mat2D des, Mat2D src)`  
`Copy all elements from src to des.`
- `void mat2D_copy_mat_to_mat_at_window (Mat2D des, Mat2D src, size_t is, size_t js, size_t ie, size_t je)`  
`Copy a rectangular window from src into des.`
- `void mat2D_get_col (Mat2D des, size_t des_col, Mat2D src, size_t src_col)`  
`Copy a column from src into a column of des.`
- `void mat2D_add_col_to_col (Mat2D des, size_t des_col, Mat2D src, size_t src_col)`

- Add a source column into a destination column.  
`void mat2D_sub_col_to_col (Mat2D des, size_t des_col, Mat2D src, size_t src_col)`  
*Subtract a source column from a destination column.*
- Swap two rows of a matrix in-place.  
`void mat2D_swap_rows (Mat2D m, size_t r1, size_t r2)`  
*Swap two rows of a matrix in-place.*
- Copy a row from src into a row of des.  
`void mat2D_get_row (Mat2D des, size_t des_row, Mat2D src, size_t src_row)`  
*Copy a row from src into a row of des.*
- Add a source row to a destination row.  
`void mat2D_add_row_to_row (Mat2D des, size_t des_row, Mat2D src, size_t src_row)`  
`void mat2D_sub_row_to_row (Mat2D des, size_t des_row, Mat2D src, size_t src_row)`  
*Subtract a source row from a destination row.*
- Compute the Frobenius norm of a matrix,  $\sqrt{\sum(m_{ij}^2)}$ .  
`double mat2D_calc_norma (Mat2D m)`
- Check if all elements of a matrix equal a given digit.  
`bool mat2D_mat_is_all_digit (Mat2D m, double digit)`  
*Check if all elements of a matrix equal a given digit.*
- Check if all elements of a row equal a given digit.  
`bool mat2D_row_is_all_digit (Mat2D m, double digit, size_t r)`  
*Check if all elements of a row equal a given digit.*
- Check if all elements of a column equal a given digit.  
`bool mat2D_col_is_all_digit (Mat2D m, double digit, size_t c)`  
*Check if all elements of a column equal a given digit.*
- Determinant of a 2x2 matrix.  
`double mat2D_det_2x2_mat (Mat2D m)`  
*Determinant of a 2x2 matrix.*
- Forward elimination to transform a matrix to upper triangular form.  
`double mat2D_upper_triangulate (Mat2D m)`  
*Forward elimination to transform a matrix to upper triangular form.*
- Determinant of a square matrix via Gaussian elimination.  
`double mat2D_det (Mat2D m)`  
*Determinant of a square matrix via Gaussian elimination.*
- Compute LUP decomposition:  $P \cdot A = L \cdot U$  with L unit diagonal.  
`void mat2D_LUP_decomposition_with_swap (Mat2D src, Mat2D l, Mat2D p, Mat2D u)`  
*Compute LUP decomposition:  $P \cdot A = L \cdot U$  with L unit diagonal.*
- Transpose a matrix:  $des = src^T$ .  
`void mat2D_transpose (Mat2D des, Mat2D src)`  
*Transpose a matrix:  $des = src^T$ .*
- Invert a square matrix using Gauss-Jordan elimination.  
`void mat2D_solve_linear_sys_LUP_decomposition (Mat2D A, Mat2D x, Mat2D B)`  
*Solve the linear system  $A \cdot x = B$  using an LUP-based approach.*
- Allocate a minor view by excluding row i and column j of ref\_mat.  
`Mat2D_Minor mat2D_minor_alloc_fill_from_mat (Mat2D ref_mat, size_t i, size_t j)`  
*Allocate a minor view by excluding row i and column j of ref\_mat.*
- Allocate a nested minor view from an existing minor by excluding row i and column j of the minor.  
`Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor (Mat2D_Minor ref_mm, size_t i, size_t j)`  
*Allocate a nested minor view from an existing minor by excluding row i and column j of the minor.*
- Free the index arrays owned by a minor.  
`void mat2D_minor_free (Mat2D_Minor mm)`  
*Free the index arrays owned by a minor.*
- Print a minor matrix to stdout with a name and indentation padding.  
`void mat2D_minor_print (Mat2D_Minor mm, const char *name, size_t padding)`  
*Print a minor matrix to stdout with a name and indentation padding.*
- Determinant of a 2x2 minor.  
`double mat2D_det_2x2_mat_minor (Mat2D_Minor mm)`  
*Determinant of a 2x2 minor.*
- Determinant of a minor via recursive expansion by minors.  
`double mat2D_minor_det (Mat2D_Minor mm)`  
*Determinant of a minor via recursive expansion by minors.*

### 4.1.1 Detailed Description

Lightweight 2D matrix helpers (double / uint32\_t).

This single-header module provides small utilities for dense row-major matrices:

- Allocation/free for `Mat2D` (double) and `Mat2D_uint32`
- Basic arithmetic and row/column operations
- Matrix multiplication, transpose, dot and cross products
- Determinant and inversion (Gaussian / Gauss-Jordan style)
- A simple LUP decomposition helper and a linear system solver
- Rotation matrix helpers (X/Y/Z) and a Z-Y-X DCM builder (as implemented)
- “Minor” views (index lists into a reference matrix) for educational determinant-by-minors computation

Storage model

- Matrices are dense and row-major (C-style).
- Element at row i and column j (0-based) is: `elements[i * stride_r + j]`
- For matrices created by `mat2D_alloc()`, `stride_r == cols`.

Usage

- In exactly one translation unit, define `MATRIX2D_IMPLEMENTATION` before including this header to compile the implementation.
- In all other files, include the header without that macro to get declarations only.

Example: `#define MATRIX2D_IMPLEMENTATION #include "matrix2d.h"`

Notes and limitations

- This one-file library is heavily inspired by Tsoding's nn.h implementation of matrix creation and operations:  
<https://github.com/tsoding/nn.h> and the video: <https://youtu.be/L1TbWe8b←VOc?list=PLpM-Dvs8t0VZPZKggcql-MmjjaBdZKeDMw>
- All APIs assume the caller provides correctly-sized destination matrices. Shape mismatches are checked with `MAT2D_ASSERT` in many routines.
- This library does not try to be numerically robust:
  - Pivoting is limited (only performed when a pivot is “near zero” per `MAT2D_EPS` in several routines).
  - Ill-conditioned matrices may produce inaccurate determinants/inverses.
- RNG uses C `rand()`; it is not cryptographically secure.

Warning

Numerical stability and correctness

- `mat2D_minor_det()` is factorial-time and is intended only for very small matrices (educational use).
- `mat2D_invert()` uses Gauss-Jordan elimination and may be unstable for ill-conditioned matrices. Consider a more robust decomposition for production use (full pivoting / QR / SVD).
- Several routines do not guard against aliasing (e.g. `dst == a`). Unless documented otherwise, assume inputs and outputs must not overlap.

Definition in file [Matrix2D.h](#).

## 4.1.2 Macro Definition Documentation

### 4.1.2.1 MAT2D\_ASSERT

```
#define MAT2D_ASSERT assert
```

Assertion macro used by this library for parameter validation.

Defaults to assert(). Override by defining MAT2D\_ASSERT before including this header to customize validation behavior.

Definition at line 101 of file [Matrix2D.h](#).

### 4.1.2.2 MAT2D\_AT

```
#define MAT2D_AT(  
    m,  
    i,  
    j ) (m).elements[mat2D_offset2d((m), (i), (j))]
```

Access element (i, j) of a [Mat2D](#) (0-based).

Expands to row-major indexing using stride\_r: (m).elements[(i) \* (m).stride\_r + (j)]

#### Warning

In the “fast” configuration this macro performs no bounds checking.

Definition at line 179 of file [Matrix2D.h](#).

### 4.1.2.3 MAT2D\_AT\_UINT32

```
#define MAT2D_AT_UINT32(   
    m,  
    i,  
    j ) (m).elements[mat2D_offset2d_uint32((m), (i), (j))]
```

Access element (i, j) of a [Mat2D\\_uint32](#) (0-based).

#### Warning

In the “fast” configuration this macro performs no bounds checking.

Definition at line 180 of file [Matrix2D.h](#).

#### 4.1.2.4 MAT2D\_EPS

```
#define MAT2D_EPS 1e-15
```

Definition at line 191 of file [Matrix2D.h](#).

#### 4.1.2.5 MAT2D\_FREE

```
#define MAT2D_FREE free
```

Deallocation function used by this library.

Defaults to `free()`. Override by defining `MAT2D_FREE` before including this header to match a custom allocator.

Definition at line 88 of file [Matrix2D.h](#).

#### 4.1.2.6 MAT2D\_IS\_ZERO

```
#define MAT2D_IS_ZERO(  
    x ) (fabs(x) < MAT2D_EPS)
```

Test whether a floating-point value is “near zero”.

Uses `fabs(x) < MAT2D_EPS`.

Definition at line 201 of file [Matrix2D.h](#).

#### 4.1.2.7 MAT2D\_MALLOC

```
#define MAT2D_MALLOC malloc
```

Allocation function used by this library.

Defaults to `malloc()`. Override by defining `MAT2D_MALLOC` before including this header to use a custom allocator.

Definition at line 76 of file [Matrix2D.h](#).

#### 4.1.2.8 MAT2D\_MINOR\_AT

```
#define MAT2D_MINOR_AT(
    mm,
    i,
    j ) MAT2D_AT( (mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j] )
```

Access element (i, j) of a [Mat2D\\_Minor](#) (0-based).

Dereferences into the underlying reference matrix using rows\_list/cols\_list.

Definition at line [210](#) of file [Matrix2D.h](#).

#### 4.1.2.9 MAT2D\_MINOR\_PRINT

```
#define MAT2D_MINOR_PRINT(
    mm ) mat2D_minor_print(mm, #mm, 0)
```

Convenience macro to print a minor with its variable name.

Definition at line [228](#) of file [Matrix2D.h](#).

#### 4.1.2.10 mat2D\_normalize

```
#define mat2D_normalize(
    m ) mat2D_mult((m), 1.0 / mat2D_calc_norma((m)) )
```

Normalize a matrix in-place to unit Frobenius norm.

Equivalent to:  $m *= 1.0 / \text{mat2D\_calc\_norma}(m)$

##### Warning

If the Frobenius norm is 0, this performs a division by zero.

Definition at line [240](#) of file [Matrix2D.h](#).

#### 4.1.2.11 MAT2D\_PI

```
#define MAT2D_PI 3.14159265358979323846
```

Definition at line [187](#) of file [Matrix2D.h](#).

#### 4.1.2.12 MAT2D\_PRINT

```
#define MAT2D_PRINT(  
    m ) mat2D_print(m, #m, 0)
```

Convenience macro to print a matrix with its variable name.

Definition at line 216 of file [Matrix2D.h](#).

#### 4.1.2.13 MAT2D\_PRINT\_AS\_COL

```
#define MAT2D_PRINT_AS_COL(  
    m ) mat2D_print_as_col(m, #m, 0)
```

Convenience macro to print a matrix as a single column with its name.

Definition at line 222 of file [Matrix2D.h](#).

### 4.1.3 Function Documentation

#### 4.1.3.1 mat2D\_add()

```
void mat2D_add (  
    Mat2D dst,  
    Mat2D a )
```

In-place addition: dst += a.

##### Parameters

|            |                                       |
|------------|---------------------------------------|
| <i>dst</i> | Destination matrix to be incremented. |
| <i>a</i>   | Summand of same shape as dst.         |

##### Precondition

dst and a have identical shape.

Definition at line 591 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.2 mat2D\_add\_col\_to\_col()

```
void mat2D_add_col_to_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Add a source column into a destination column.

Performs:  $\text{des}[:, \text{des\_col}] += \text{src}[:, \text{src\_col}]$

##### Parameters

|                |   |
|----------------|---|
| <i>des</i>     | Destination matrix (same row count as <i>src</i> ). |
| <i>des_col</i> | Column index in destination.                        |
| <i>src</i>     | Source matrix.                                      |
| <i>src_col</i> | Column index in source.                             |

Definition at line 953 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.3 mat2D\_add\_row\_time\_factor\_to\_row()

```
void mat2D_add_row_time_factor_to_row (
    Mat2D m,
    size_t des_r,
    size_t src_r,
    double factor )
```

Row operation:  $\text{row}(\text{des\_r}) += \text{factor} * \text{row}(\text{src\_r})$ .

##### Parameters

|               |                        |
|---------------|------------------------|
| <i>m</i>      | Matrix.                |
| <i>des_r</i>  | Destination row index. |
| <i>src_r</i>  | Source row index.      |
| <i>factor</i> | Scalar multiplier.     |

##### Warning

Indices are not bounds-checked in this routine.

Definition at line 611 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D\\_AT](#).

#### 4.1.3.4 mat2D\_add\_row\_to\_row()

```
void mat2D_add_row_to_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

##### Parameters

|                |                      |
|----------------|----------------------|
| <i>src_row</i> | Row index in source. |
|----------------|----------------------|

##### Precondition

`des.cols == src.cols`

##### Parameters

|                |   |
|----------------|---|
| <i>des</i>     | Destination matrix (same number of columns as <i>src</i> ). |
| <i>des_row</i> | Row index in destination.                                   |
| <i>src</i>     | Source matrix.  |
| <i>src_row</i> | Row index in source.  |

Definition at line 1031 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.5 mat2D\_alloc()

```
Mat2D mat2D_alloc (
    size_t rows,
    size_t cols )
```

Allocate a rows-by-cols matrix of double.

##### Parameters

|             |                                 |
|-------------|---------------------------------|
| <i>rows</i> | Number of rows. Must be > 0.    |
| <i>cols</i> | Number of columns. Must be > 0. |

##### Returns

A [Mat2D](#) owning a contiguous buffer of  $\text{rows} * \text{cols}$  elements.

##### Postcondition

The returned matrix has  $\text{stride\_r} == \text{cols}$ .

The returned matrix must be released with [mat2D\\_free\(\)](#).

**Warning**

This function asserts allocation success via MAT2D\_ASSERT.

Definition at line 344 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D::elements](#), [MAT2D\\_ASSERT](#), [MAT2D\\_MALLOC](#), [Mat2D::rows](#), and [Mat2D::stride\\_r](#).

Referenced by [main\(\)](#), [mat2D\\_det\(\)](#), [mat2D\\_invert\(\)](#), [mat2D\\_set\\_DCM\\_zyx\(\)](#), and [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#).

**4.1.3.6 mat2D\_alloc\_uint32()**

```
Mat2D_uint32 mat2D_alloc_uint32 (
    size_t rows,
    size_t cols )
```

Allocate a rows-by-cols matrix of uint32\_t.

**Parameters**

|             |                                 |
|-------------|---------------------------------|
| <i>rows</i> | Number of rows. Must be > 0.    |
| <i>cols</i> | Number of columns. Must be > 0. |

**Returns**

A [Mat2D\\_uint32](#) owning a contiguous buffer of  $\text{rows} * \text{cols}$  elements.

**Postcondition**

The returned matrix has  $\text{stride\_r} == \text{cols}$ .

The returned matrix must be released with [mat2D\\_free\\_uint32\(\)](#).

**Warning**

This function asserts allocation success via MAT2D\_ASSERT.

Definition at line 368 of file [Matrix2D.h](#).

References [Mat2D\\_uint32::cols](#), [Mat2D\\_uint32::elements](#), [MAT2D\\_ASSERT](#), [MAT2D\\_MALLOC](#), [Mat2D\\_uint32::rows](#), and [Mat2D\\_uint32::stride\\_r](#).

**4.1.3.7 mat2D\_calc\_norma()**

```
double mat2D_calc_norma (
    Mat2D m )
```

Compute the Frobenius norm of a matrix,  $\sqrt{\sum(m_{ij})^2}$ .

**Parameters**

|          |         |
|----------|---------|
| <i>m</i> | Matrix. |
|----------|---------|

**Returns**

Frobenius norm.

Definition at line 1068 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

**4.1.3.8 mat2D\_col\_is\_all\_digit()**

```
bool mat2D_col_is_all_digit (
    Mat2D m,
    double digit,
    size_t c )
```

Check if all elements of a column equal a given digit.

**Parameters**

|              |                   |
|--------------|-------------------|
| <i>m</i>     | Matrix.           |
| <i>digit</i> | Value to compare. |
| <i>c</i>     | Column index.     |

**Returns**

true if every element equals digit, false otherwise.

**Warning**

Uses exact floating-point equality.

Definition at line 1128 of file [Matrix2D.h](#).

References [MAT2D\\_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_det\(\)](#).

**4.1.3.9 mat2D\_copy()**

```
void mat2D_copy (
    Mat2D des,
    Mat2D src )
```

Copy all elements from src to des.

**Parameters**

|            |                     |
|------------|---------------------|
| <i>des</i> | Destination matrix. |
| <i>src</i> | Source matrix.      |

**Precondition**

Shapes match.

*des* and *src* have identical shape.

Definition at line 887 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_det\(\)](#), [mat2D\\_invert\(\)](#), and [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#).

**4.1.3.10 mat2D\_copy\_mat\_to\_mat\_at\_window()**

```
void mat2D_copy_mat_to_mat_at_window (
    Mat2D des,
    Mat2D src,
    size_t is,
    size_t js,
    size_t ie,
    size_t je )
```

Copy a rectangular window from *src* into *des*.

**Parameters**

|            |   |
|------------|---|
| <i>des</i> | Destination matrix. Must have size $(ie - is + 1) \times (je - js + 1)$ . |
| <i>src</i> | Source matrix.  |
| <i>is</i>  | Start row index in <i>src</i> (inclusive).                                |
| <i>js</i>  | Start column index in <i>src</i> (inclusive).                             |
| <i>ie</i>  | End row index in <i>src</i> (inclusive).                                  |
| <i>je</i>  | End column index in <i>src</i> (inclusive).                               |

**Precondition**

$0 \leq is \leq ie < src.rows$ ,  $0 \leq js \leq je < src.cols$ .

Definition at line 909 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.11 mat2D\_cross()

```
void mat2D_cross (
    Mat2D dst,
    Mat2D a,
    Mat2D b )
```

3D cross product:  $\text{dst} = \mathbf{a} \times \mathbf{b}$  for  $3 \times 1$  vectors.

##### Parameters

|            |                         |
|------------|-------------------------|
| <i>dst</i> | 3x1 destination vector. |
| <i>a</i>   | 3x1 input vector.       |
| <i>b</i>   | 3x1 input vector.       |

##### Precondition

All matrices have shape  $3 \times 1$ .

Definition at line 572 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.12 mat2D\_det()

```
double mat2D_det (
    Mat2D m )
```

Determinant of a square matrix via Gaussian elimination.

##### Parameters

|          |                |
|----------|----------------|
| <i>m</i> | Square matrix. |
|----------|----------------|

##### Returns

$\det(\mathbf{m})$ .

Copies  $\mathbf{m}$  internally, transforms the copy to upper triangular form, and returns the product of diagonal elements adjusted by the row-swap factor.

##### Warning

The early “all-zero row/column” check uses exact comparisons to 0.

Limited pivoting may cause poor numerical results for some inputs.

Definition at line 1215 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D\\_Minor::cols](#), [mat2D\\_alloc\(\)](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), [mat2D\\_col\\_is\\_all\\_digit\(\)](#), [mat2D\\_copy\(\)](#), [mat2D\\_det\\_2x2\\_mat\\_minor\(\)](#), [mat2D\\_free\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\(\)](#), [mat2D\\_minor\\_det\(\)](#), [mat2D\\_minor\\_free\(\)](#), [mat2D\\_row\\_is\\_all\\_digit\(\)](#), [mat2D\\_upper\\_triangulate\(\)](#), [Mat2D::rows](#), and [Mat2D\\_Minor::rows](#).

Referenced by [mat2D\\_invert\(\)](#).

#### 4.1.3.13 mat2D\_det\_2x2\_mat()

```
double mat2D_det_2x2_mat (
    Mat2D m )
```

Determinant of a 2x2 matrix.

##### Parameters

|          |                       |
|----------|-----------------------|
| <i>m</i> | Matrix (must be 2x2). |
|----------|-----------------------|

##### Returns

$\det(m) = m_{00}*m_{11} - m_{01}*m_{10}$ .

Definition at line 1143 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.14 mat2D\_det\_2x2\_mat\_minor()

```
double mat2D_det_2x2_mat_minor (
    Mat2D_Minor mm )
```

Determinant of a 2x2 minor.

##### Parameters

|           |                      |
|-----------|----------------------|
| <i>mm</i> | Minor (must be 2x2). |
|-----------|----------------------|

##### Returns

$\det(mm)$ .

Definition at line 1582 of file [Matrix2D.h](#).

References [Mat2D\\_Minor::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_MINOR\\_AT](#), and [Mat2D\\_Minor::rows](#).

Referenced by [mat2D\\_det\(\)](#), and [mat2D\\_minor\\_det\(\)](#).

#### 4.1.3.15 mat2D\_dot()

```
void mat2D_dot (
    Mat2D dst,
    Mat2D a,
    Mat2D b )
```

Matrix product:  $\text{dst} = \text{a} * \text{b}$ .

##### Parameters

|            |  |
|------------|--|
| <i>dst</i> | Destination matrix (size $\text{a.rows} \times \text{b.cols}$ ). |
| <i>a</i>   | Left matrix (size $\text{a.rows} \times \text{a.cols}$ ).        |
| <i>b</i>   | Right matrix (size $\text{a.cols} \times \text{b.cols}$ ).       |

##### Precondition

```
a.cols == b.rows
dst.rows == a.rows
dst.cols == b.cols
```

##### Postcondition

*dst* is fully overwritten.

##### Warning

*dst* must not alias *a* or *b* (overlap is not handled).

Definition at line 515 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_set\\_DCM\\_zyx\(\)](#), and [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#).

#### 4.1.3.16 mat2D\_dot\_product()

```
double mat2D_dot_product (
    Mat2D a,
    Mat2D b )
```

Dot product between two vectors.

##### Parameters

|          |   |
|----------|---|
| <i>a</i> | Vector (shape $n \times 1$ or $1 \times n$ ). |
| <i>b</i> | Vector (same shape as <i>a</i> ).             |

**Returns**

The scalar dot product sum.

**Precondition**

```
a.rows == b.rows and a.cols == b.cols
(a.cols == 1 && b.cols == 1) || (a.rows == 1 && b.rows == 1)
```

Definition at line 544 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

**4.1.3.17 mat2D\_fill()**

```
void mat2D_fill (
    Mat2D m,
    double x )
```

Fill all elements of a matrix of doubles with a scalar value.

**Parameters**

|          |                                   |
|----------|-----------------------------------|
| <i>m</i> | Matrix to fill.                   |
| <i>x</i> | Value to assign to every element. |

Definition at line 443 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), and [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#).

**4.1.3.18 mat2D\_fill\_sequence()**

```
void mat2D_fill_sequence (
    Mat2D m,
    double start,
    double step )
```

Fill a matrix with an arithmetic sequence laid out in row-major order.

**Parameters**

|              |   |
|--------------|---|
| <i>m</i>     | Matrix to fill.                         |
| <i>start</i> | First value in the sequence.            |
| <i>step</i>  | Increment between consecutive elements. |

Element at linear index k gets value start + step \* k.

Definition at line 459 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), [mat2D\\_offset2d\(\)](#), and [Mat2D::rows](#).

#### 4.1.3.19 mat2D\_fill\_uint32()

```
void mat2D_fill_uint32 (
    Mat2D_uint32 m,
    uint32_t x )
```

Fill all elements of a matrix of `uint32_t` with a scalar value.

Parameters

|                |                                   |
|----------------|-----------------------------------|
| <code>m</code> | Matrix to fill.                   |
| <code>x</code> | Value to assign to every element. |

Definition at line 472 of file [Matrix2D.h](#).

References [Mat2D\\_uint32::cols](#), [MAT2D\\_AT\\_UINT32](#), and [Mat2D\\_uint32::rows](#).

#### 4.1.3.20 mat2D\_free()

```
void mat2D_free (
    Mat2D m )
```

Free the buffer owned by a [Mat2D](#).

Parameters

|                |  |
|----------------|--|
| <code>m</code> | Matrix whose elements were allocated via <code>MAT2D_MALLOC</code> . |
|----------------|--|

#### Note

This does not modify `m` (it is passed by value).

It is safe to call with `m.elements == NULL`.

Definition at line 388 of file [Matrix2D.h](#).

References [Mat2D::elements](#), and [MAT2D\\_FREE](#).

Referenced by [main\(\)](#), [mat2D\\_det\(\)](#), [mat2D\\_invert\(\)](#), [mat2D\\_set\\_DCM\\_zyx\(\)](#), and [mat2D\\_solve\\_linear\\_sys\\_LUP\\_decomposition\(\)](#).

#### 4.1.3.21 mat2D\_free\_uint32()

```
void mat2D_free_uint32 (
    Mat2D_uint32 m )
```

Free the buffer owned by a [Mat2D\\_uint32](#).

##### Parameters

|          |  |
|----------|--|
| <i>m</i> | Matrix whose elements were allocated via MAT2D_MALLOC. |
|----------|--|

##### Note

This does not modify *m* (it is passed by value).

It is safe to call with *m.elements* == NULL.

Definition at line 401 of file [Matrix2D.h](#).

References [Mat2D\\_uint32::elements](#), and [MAT2D\\_FREE](#).

#### 4.1.3.22 mat2D\_get\_col()

```
void mat2D_get_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Copy a column from *src* into a column of *des*.

##### Parameters

|                |   |
|----------------|---|
| <i>des</i>     | Destination matrix (same row count as <i>src</i> ). |
| <i>des_col</i> | Column index in destination.                        |
| <i>src</i>     | Source matrix.                                      |
| <i>src_col</i> | Column index in source.                             |

##### Precondition

```
des.rows == src.rows
des_col < des.cols and src_col < src.cols
```

Definition at line 932 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.23 mat2D\_get\_row()

```
void mat2D_get_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

Copy a row from src into a row of des.

##### Parameters

|                |   |
|----------------|---|
| <i>des</i>     | Destination matrix (same number of columns as src). |
| <i>des_row</i> | Row index in destination.                           |
| <i>src</i>     | Source matrix.                                      |
| <i>src_row</i> | Row index in source.                                |

##### Precondition

`des.cols == src.cols`

Definition at line 1011 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.24 mat2D\_invert()

```
void mat2D_invert (
    Mat2D des,
    Mat2D src )
```

Invert a square matrix using Gauss-Jordan elimination.

##### Parameters

|            |   |
|------------|---|
| <i>des</i> | Destination matrix (same shape as src). |
| <i>src</i> | Source square matrix.                   |

##### Precondition

`src` is square.

`des` is allocated as the same shape as `src`.

On singular matrices (`det == 0`), prints an error message, writes all zeros into `des`, and returns.

**Warning**

This implementation performs limited pivoting (only when a pivot is “near zero” per `MAT2D_EPS`). It may be unstable for ill-conditioned matrices.

This routine computes `det(src)` first, which performs an additional elimination pass and can amplify numerical issues.

Definition at line 1353 of file [Matrix2D.h](#).

References `Mat2D::cols`, `mat2D_alloc()`, `MAT2D_ASSERT`, `MAT2D_AT`, `mat2D_copy()`, `mat2D_det()`, `mat2D_fill()`, `mat2D_free()`, `MAT2D_IS_ZERO`, `mat2D_mult_row()`, `mat2D_set_identity()`, `mat2D_sub_row_time_factor_to_row()`, `mat2D_swap_rows()`, and `Mat2D::rows`.

Referenced by `mat2D_solve_linear_sys_LUP_decomposition()`.

**4.1.3.25 mat2D\_LUP\_decomposition\_with\_swap()**

```
void mat2D_LUP_decomposition_with_swap (
    Mat2D src,
    Mat2D l,
    Mat2D p,
    Mat2D u )
```

Compute LUP decomposition:  $P \cdot A = L \cdot U$  with L unit diagonal.

**Parameters**

|                  |   |
|------------------|---|
| <code>src</code> | Input matrix A (not modified by this function).                       |
| <code>l</code>   | Output lower-triangular-like matrix (intended to have unit diagonal). |
| <code>p</code>   | Output permutation matrix.  |
| <code>u</code>   | Output upper-triangular-like matrix.                                  |

**Precondition**

`src` is square.

`l`, `p`, `u` are allocated with the same shape as `src`.

**Warning**

Pivoting is limited: a row swap is performed only when the pivot is “near zero” (`MAT2D_IS_ZERO()`).

This routine swaps rows of L during decomposition; for a standard LUP implementation, care is required when swapping partially-built L.

Definition at line 1278 of file [Matrix2D.h](#).

References `Mat2D::cols`, `MAT2D_AT`, `mat2D_copy()`, `mat2D_fill()`, `MAT2D_IS_ZERO`, `mat2D_set_identity()`, `mat2D_sub_row_time_factor_to_row()`, `mat2D_swap_rows()`, and `Mat2D::rows`.

Referenced by `mat2D_solve_linear_sys_LUP_decomposition()`.

#### 4.1.3.26 mat2D\_make\_identity()

```
double mat2D_make_identity (
    Mat2D m )
```

Reduce a matrix to identity using Gauss-Jordan style elimination.

##### Parameters

|          |                           |
|----------|---------------------------|
| <i>m</i> | Matrix modified in-place. |
|----------|---------------------------|

##### Returns

A multiplicative factor that tracks the effect of row swaps and row scalings performed inside this routine (useful when relating the transformation to determinants).

Internally calls [mat2D\\_upper\\_triangulate\(\)](#) and then performs backward elimination and row scaling to reach identity (if the matrix is nonsingular and pivots are usable).

##### Warning

No full pivoting is performed. Ill-conditioned matrices may produce poor results or floating-point exceptions.

Definition at line [754](#) of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), [mat2D\\_mult\\_row\(\)](#), [mat2D\\_sub\\_row\\_time\\_factor\\_to\\_row\(\)](#), [mat2D\\_upper\\_triangulate\(\)](#), and [Mat2D::rows](#).

#### 4.1.3.27 mat2D\_mat\_is\_all\_digit()

```
bool mat2D_mat_is_all_digit (
    Mat2D m,
    double digit )
```

Check if all elements of a matrix equal a given digit.

##### Parameters

|              |                   |
|--------------|-------------------|
| <i>m</i>     | Matrix.           |
| <i>digit</i> | Value to compare. |

##### Returns

true if every element equals digit, false otherwise.

**Warning**

Uses exact floating-point equality.

Definition at line 1088 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

**4.1.3.28 mat2D\_minor\_alloc\_fill\_from\_mat()**

```
Mat2D_Minor mat2D_minor_alloc_fill_from_mat (
    Mat2D ref_mat,
    size_t i,
    size_t j )
```

Allocate a minor view by excluding row *i* and column *j* of *ref\_mat*.

**Parameters**

|                |   |
|----------------|---|
| <i>ref_mat</i> | Reference square matrix.                  |
| <i>i</i>       | Excluded row index in <i>ref_mat</i> .    |
| <i>j</i>       | Excluded column index in <i>ref_mat</i> . |

**Returns**

A [Mat2D\\_Minor](#) that references *ref\_mat*.

**Note**

The returned minor owns *rows\_list* and *cols\_list* and must be released with [mat2D\\_minor\\_free\(\)](#).

The returned minor does not own *ref\_mat.elements*.

Definition at line 1475 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D\\_Minor::cols](#), [Mat2D\\_Minor::cols\\_list](#), [MAT2D\\_ASSERT](#), [MAT2D\\_MALLOC](#), [Mat2D\\_Minor::ref\\_mat](#), [Mat2D::rows](#), [Mat2D\\_Minor::rows](#), [Mat2D\\_Minor::rows\\_list](#), and [Mat2D\\_Minor::stride\\_r](#).

Referenced by [mat2D\\_det\(\)](#).

**4.1.3.29 mat2D\_minor\_alloc\_fill\_from\_mat\_minor()**

```
Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor (
    Mat2D_Minor ref_mm,
    size_t i,
    size_t j )
```

Allocate a nested minor view from an existing minor by excluding row *i* and column *j* of the minor.

**Parameters**

|               |                                     |
|---------------|-------------------------------------|
| <i>ref_mm</i> | Reference minor.                    |
| <i>i</i>      | Excluded row index in the minor.    |
| <i>j</i>      | Excluded column index in the minor. |

**Returns**

A new [Mat2D\\_Minor](#) that references the same underlying matrix.

**Note**

The returned minor owns `rows_list` and `cols_list` and must be released with [mat2D\\_minor\\_free\(\)](#).

The returned minor does not own the underlying reference matrix data.

Definition at line 1517 of file [Matrix2D.h](#).

References [Mat2D\\_Minor::cols](#), [Mat2D\\_Minor::cols\\_list](#), [MAT2D\\_ASSERT](#), [MAT2D\\_MALLOC](#), [Mat2D\\_Minor::ref\\_mat](#), [Mat2D\\_Minor::rows](#), [Mat2D\\_Minor::rows\\_list](#), and [Mat2D\\_Minor::stride\\_r](#).

Referenced by [mat2D\\_minor\\_det\(\)](#).

**4.1.3.30 mat2D\_minor\_det()**

```
double mat2D_minor_det (
    Mat2D_Minor mm )
```

Determinant of a minor via recursive expansion by minors.

**Parameters**

|           |               |
|-----------|---------------|
| <i>mm</i> | Square minor. |
|-----------|---------------|

**Returns**

$\det(\text{mm})$ .

**Warning**

Exponential complexity (factorial). Intended for educational or very small matrices only.

Definition at line 1595 of file [Matrix2D.h](#).

References [Mat2D\\_Minor::cols](#), [MAT2D\\_ASSERT](#), [mat2D\\_det\\_2x2\\_mat\\_minor\(\)](#), [mat2D\\_minor\\_alloc\\_fill\\_from\\_mat\\_minor\(\)](#), [MAT2D\\_MINOR\\_AT](#), [mat2D\\_minor\\_free\(\)](#), and [Mat2D\\_Minor::rows](#).

Referenced by [mat2D\\_det\(\)](#).

#### 4.1.3.31 mat2D\_minor\_free()

```
void mat2D_minor_free (
    Mat2D_Minor mm )
```

Free the index arrays owned by a minor.

##### Parameters

|           |                |
|-----------|----------------|
| <i>mm</i> | Minor to free. |
|-----------|----------------|

##### Note

After this call, *mm.rows\_list* and *mm.cols\_list* are invalid.

Definition at line 1552 of file [Matrix2D.h](#).

References [Mat2D\\_Minor::cols\\_list](#), [MAT2D\\_FREE](#), and [Mat2D\\_Minor::rows\\_list](#).

Referenced by [mat2D\\_det\(\)](#), and [mat2D\\_minor\\_det\(\)](#).

#### 4.1.3.32 mat2D\_minor\_print()

```
void mat2D_minor_print (
    Mat2D_Minor mm,
    const char * name,
    size_t padding )
```

Print a minor matrix to stdout with a name and indentation padding.

##### Parameters

|                |                         |
|----------------|-------------------------|
| <i>mm</i>      | Minor to print.         |
| <i>name</i>    | Label to print.         |
| <i>padding</i> | Left padding in spaces. |

Definition at line 1564 of file [Matrix2D.h](#).

References [Mat2D\\_Minor::cols](#), [MAT2D\\_MINOR\\_AT](#), and [Mat2D\\_Minor::rows](#).

#### 4.1.3.33 mat2D\_mult()

```
void mat2D_mult (
    Mat2D m,
    double factor )
```

In-place scalar multiplication: *m \*= factor*.

**Parameters**

|               |                    |
|---------------|--------------------|
| <i>m</i>      | Matrix.            |
| <i>factor</i> | Scalar multiplier. |

Definition at line 657 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

**4.1.3.34 mat2D\_mult\_row()**

```
void mat2D_mult_row (
    Mat2D m,
    size_t r,
    double factor )
```

In-place row scaling:  $\text{row}(r) *= \text{factor}$ .

**Parameters**

|               |                    |
|---------------|--------------------|
| <i>m</i>      | Matrix.            |
| <i>r</i>      | Row index.         |
| <i>factor</i> | Scalar multiplier. |

**Warning**

Indices are not bounds-checked in this routine.

Definition at line 674 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D\\_AT](#).

Referenced by [mat2D\\_invert\(\)](#), and [mat2D\\_make\\_identity\(\)](#).

**4.1.3.35 mat2D\_offset2d()**

```
size_t mat2D_offset2d (
    Mat2D m,
    size_t i,
    size_t j )
```

Compute the linear offset of element (i, j) in a [Mat2D](#).

**Parameters**

|          |                         |
|----------|-------------------------|
| <i>m</i> | Matrix.                 |
| <i>i</i> | Row index (0-based).    |
| <i>j</i> | Column index (0-based). |

**Returns**

The linear offset  $i * \text{stride\_r} + j$ .

**Precondition**

$0 \leq i < m.\text{rows}$  and  $0 \leq j < m.\text{cols}$  (checked by MAT2D\_ASSERT).

Definition at line 416 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [Mat2D::rows](#), and [Mat2D::stride\\_r](#).

Referenced by [mat2D\\_fill\\_sequence\(\)](#).

**4.1.3.36 mat2D\_offset2d\_uint32()**

```
size_t mat2D_offset2d_uint32 (
    Mat2D_uint32 m,
    size_t i,
    size_t j )
```

Compute the linear offset of element  $(i, j)$  in a [Mat2D\\_uint32](#).

**Parameters**

|          |                         |
|----------|-------------------------|
| <i>m</i> | Matrix.                 |
| <i>i</i> | Row index (0-based).    |
| <i>j</i> | Column index (0-based). |

**Returns**

The linear offset  $i * \text{stride\_r} + j$ .

**Precondition**

$0 \leq i < m.\text{rows}$  and  $0 \leq j < m.\text{cols}$  (checked by MAT2D\_ASSERT).

Definition at line 432 of file [Matrix2D.h](#).

References [Mat2D\\_uint32::cols](#), [MAT2D\\_ASSERT](#), [Mat2D\\_uint32::rows](#), and [Mat2D\\_uint32::stride\\_r](#).

**4.1.3.37 mat2D\_print()**

```
void mat2D_print (
    Mat2D m,
    const char * name,
    size_t padding )
```

Print a matrix to stdout with a name and indentation padding.

**Parameters**

|                |                         |
|----------------|-------------------------|
| <i>m</i>       | Matrix to print.        |
| <i>name</i>    | Label to print.         |
| <i>padding</i> | Left padding in spaces. |

Definition at line 687 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

**4.1.3.38 mat2D\_print\_as\_col()**

```
void mat2D_print_as_col (
    Mat2D m,
    const char * name,
    size_t padding )
```

Print a matrix as a flattened column vector to stdout.

**Parameters**

|                |   |
|----------------|---|
| <i>m</i>       | Matrix to print (flattened in row-major). |
| <i>name</i>    | Label to print.                           |
| <i>padding</i> | Left padding in spaces.                   |

Definition at line 706 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D::elements](#), and [Mat2D::rows](#).

**4.1.3.39 mat2D\_rand()**

```
void mat2D_rand (
    Mat2D m,
    double low,
    double high )
```

Fill a matrix with pseudo-random doubles in [low, high].

**Parameters**

|             |                          |
|-------------|--------------------------|
| <i>m</i>    | Matrix to fill.          |
| <i>low</i>  | Lower bound (inclusive). |
| <i>high</i> | Upper bound (inclusive). |

**Precondition**

`high > low` (not checked here; caller responsibility).

**Note**

Uses `mat2D_rand_double()` (`rand()`).

Definition at line 491 of file [Matrix2D.h](#).

References `Mat2D::cols`, `MAT2D_AT`, `mat2D_rand_double()`, and `Mat2D::rows`.

Referenced by `main()`.

**4.1.3.40 mat2D\_rand\_double()**

```
double mat2D_rand_double (
    void )
```

Return a pseudo-random double in the range [0, 1].

Uses `rand()` / `RAND_MAX` from the C standard library.

**Note**

This RNG is not cryptographically secure and may have weak statistical properties depending on the platform.

Definition at line 327 of file [Matrix2D.h](#).

Referenced by `mat2D_rand()`.

**4.1.3.41 mat2D\_row\_is\_all\_digit()**

```
bool mat2D_row_is_all_digit (
    Mat2D m,
    double digit,
    size_t r )
```

Check if all elements of a row equal a given digit.

**Parameters**

|                    |                   |
|--------------------|-------------------|
| <code>m</code>     | Matrix.           |
| <code>digit</code> | Value to compare. |
| <code>r</code>     | Row index.        |

**Returns**

true if every element equals digit, false otherwise.

**Warning**

Uses exact floating-point equality.

Definition at line 1109 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D\\_AT](#).

Referenced by [mat2D\\_det\(\)](#).

**4.1.3.42 mat2D\_set\_DCM\_zyx()**

```
void mat2D_set_DCM_zyx (
    Mat2D DCM,
    float yaw_deg,
    float pitch_deg,
    float roll_deg )
```

Build a 3x3 direction cosine matrix (DCM) from Z-Y-X Euler angles.

**Parameters**

|                  |                              |
|------------------|------------------------------|
| <i>DCM</i>       | 3x3 destination matrix.      |
| <i>yaw_deg</i>   | Rotation about Z in degrees. |
| <i>pitch_deg</i> | Rotation about Y in degrees. |
| <i>roll_deg</i>  | Rotation about X in degrees. |

Computes  $DCM = R_x(\text{roll}) * R_y(\text{pitch}) * R_z(\text{yaw})$ .

**Note**

This routine allocates temporary 3x3 matrices internally.

Definition at line 860 of file [Matrix2D.h](#).

References [mat2D\\_alloc\(\)](#), [mat2D\\_dot\(\)](#), [mat2D\\_free\(\)](#), [mat2D\\_set\\_rot\\_mat\\_x\(\)](#), [mat2D\\_set\\_rot\\_mat\\_y\(\)](#), and [mat2D\\_set\\_rot\\_mat\\_z\(\)](#).

**4.1.3.43 mat2D\_set\_identity()**

```
void mat2D_set_identity (
    Mat2D m )
```

Set a square matrix to the identity matrix.

**Parameters**

|          |                          |
|----------|--------------------------|
| <i>m</i> | Matrix (must be square). |
|----------|--------------------------|

**Precondition**

*m.rows == m.cols* (checked by MAT2D\_ASSERT).

Definition at line 722 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), [mat2D\\_set\\_rot\\_mat\\_x\(\)](#), [mat2D\\_set\\_rot\\_mat\\_y\(\)](#), and [mat2D\\_set\\_rot\\_mat\\_z\(\)](#).

**4.1.3.44 mat2D\_set\_rot\_mat\_x()**

```
void mat2D_set_rot_mat_x (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the X-axis.

**Parameters**

|                  |                         |
|------------------|-------------------------|
| <i>m</i>         | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees.       |

The matrix written is: [ 1, 0 , 0 ] [ 0, cos(a), sin(a) ] [ 0,-sin(a), cos(a) ]

Definition at line 789 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), [MAT2D\\_PI](#), [mat2D\\_set\\_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_set\\_DCM\\_zyx\(\)](#).

**4.1.3.45 mat2D\_set\_rot\_mat\_y()**

```
void mat2D_set_rot_mat_y (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the Y-axis.

**Parameters**

|                  |                         |
|------------------|-------------------------|
| <i>m</i>         | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees.       |

The matrix written is: [ cos(a), 0,-sin(a) ] [ 0 , 1, 0 ] [ sin(a), 0, cos(a) ]

Definition at line 813 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), [MAT2D\\_PI](#), [mat2D\\_set\\_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_set\\_DCM\\_zyx\(\)](#).

#### 4.1.3.46 mat2D\_set\_rot\_mat\_z()

```
void mat2D_set_rot_mat_z (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the Z-axis.

**Parameters**

|                  |                         |
|------------------|-------------------------|
| <i>m</i>         | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees.       |

The matrix written is: [ cos(a), sin(a), 0 ] [-sin(a), cos(a), 0 ] [ 0 , 0 , 1 ]

Definition at line 837 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), [MAT2D\\_PI](#), [mat2D\\_set\\_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D\\_set\\_DCM\\_zyx\(\)](#).

#### 4.1.3.47 mat2D\_solve\_linear\_sys\_LUP\_decomposition()

```
void mat2D_solve_linear_sys_LUP_decomposition (
    Mat2D A,
    Mat2D x,
    Mat2D B )
```

Solve the linear system  $A x = B$  using an LUP-based approach.

**Parameters**

|          |  |
|----------|--|
| <i>A</i> | Coefficient matrix (N x N).                  |
| <i>x</i> | Solution vector (N x 1). Written on success. |
| <i>B</i> | Right-hand side vector (N x 1).              |

This routine computes an LUP decomposition and then forms explicit inverses of L and U ( $\text{inv}(L)$ ,  $\text{inv}(U)$ ) to compute:  $x = \text{inv}(U) * \text{inv}(L) * (P * B)$

### Warning

Explicitly inverting L and U is typically less stable and slower than forward/back substitution. Prefer substitution for production-quality solvers.

Definition at line 1429 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [mat2D\\_alloc\(\)](#), [MAT2D\\_ASSERT](#), [mat2D\\_dot\(\)](#), [mat2D\\_fill\(\)](#), [mat2D\\_free\(\)](#), [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), and [Mat2D::rows](#).

### 4.1.3.48 mat2D\_sub()

```
void mat2D_sub (
    Mat2D dst,
    Mat2D a )
```

In-place subtraction:  $\text{dst} -= \text{a}$ .

#### Parameters

|            |  |
|------------|--|
| <i>dst</i> | Destination matrix to be decremented.    |
| <i>a</i>   | Subtrahend of same shape as <i>dst</i> . |

#### Precondition

*dst* and *a* have identical shape.

Definition at line 625 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

### 4.1.3.49 mat2D\_sub\_col\_to\_col()

```
void mat2D_sub_col_to_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Subtract a source column from a destination column.

Performs:  $\text{des}[:, \text{des\_col}] -= \text{src}[:, \text{src\_col}]$

#### Parameters

|                |   |
|----------------|---|
| <i>des</i>     | Destination matrix (same row count as <i>src</i> ). |
| <i>des_col</i> | Column index in destination.                        |
| <i>src</i>     | Source matrix.                                      |
| <i>src_col</i> | Column index in source.                             |

Definition at line 974 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.50 mat2D\_sub\_row\_time\_factor\_to\_row()

```
void mat2D_sub_row_time_factor_to_row (
    Mat2D m,
    size_t des_r,
    size_t src_r,
    double factor )
```

Row operation:  $\text{row}(\text{des\_r}) -= \text{factor} * \text{row}(\text{src\_r})$ .

##### Parameters

|                        |                        |
|------------------------|------------------------|
| <i>m</i>               | Matrix.                |
| <i>des<sub>r</sub></i> | Destination row index. |
| <i>src<sub>r</sub></i> | Source row index.      |
| <i>factor</i>          | Scalar multiplier.     |

##### Warning

Indices are not bounds-checked in this routine.

Definition at line 645 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D\\_AT](#).

Referenced by [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), [mat2D\\_make\\_identity\(\)](#), and [mat2D\\_upper\\_triangulate\(\)](#).

#### 4.1.3.51 mat2D\_sub\_row\_to\_row()

```
void mat2D_sub_row_to_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

Subtract a source row from a destination row.

Performs:  $\text{des}[\text{des\_row}, :] -= \text{src}[\text{src\_row}, :]$

##### Parameters

|                          |   |
|--------------------------|---|
| <i>des</i>               | Destination matrix (same number of columns as <i>src</i> ). |
| <i>des<sub>row</sub></i> | Row index in destination.                                   |
| <i>src</i>               | Source matrix.  |
| <i>src<sub>row</sub></i> | Row index in source.  |

Definition at line 1052 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.52 mat2D\_swap\_rows()

```
void mat2D_swap_rows (
    Mat2D m,
    size_t r1,
    size_t r2 )
```

Swap two rows of a matrix in-place.

##### Parameters

|           |                   |
|-----------|-------------------|
| <i>m</i>  | Matrix.           |
| <i>r1</i> | First row index.  |
| <i>r2</i> | Second row index. |

##### Warning

Row indices are not bounds-checked in this routine.

Definition at line 993 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D\\_AT](#).

Referenced by [mat2D\\_invert\(\)](#), [mat2D\\_LUP\\_decomposition\\_with\\_swap\(\)](#), and [mat2D\\_upper\\_triangulate\(\)](#).

#### 4.1.3.53 mat2D\_transpose()

```
void mat2D_transpose (
    Mat2D des,
    Mat2D src )
```

Transpose a matrix:  $\text{des} = \text{src}^T$ .

##### Parameters

|            |   |
|------------|---|
| <i>des</i> | Destination matrix (shape $\text{src}.cols \times \text{src}.rows$ ). |
| <i>src</i> | Source matrix.  |

##### Warning

If *des* aliases *src*, results are undefined (no in-place transpose).

Definition at line 1322 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_ASSERT](#), [MAT2D\\_AT](#), and [Mat2D::rows](#).

#### 4.1.3.54 mat2D\_upper\_triangulate()

```
double mat2D_upper_triangulate (
    Mat2D m )
```

Forward elimination to transform a matrix to upper triangular form.

##### Parameters

|                |                              |
|----------------|------------------------------|
| <code>m</code> | Matrix transformed in-place. |
|----------------|------------------------------|

##### Returns

Product of row scaling factors (currently 1 in this implementation).

##### Note

Used as part of determinant computation via triangularization.

##### Warning

Not robust for linearly dependent rows or tiny pivots.

##### Returns

A factor tracking the effect of row swaps on the determinant. Currently this is  $\pm 1$  depending on the number of row swaps performed.

This routine performs Gaussian elimination using row operations of the form:  $\text{row}_j = \text{row}_j - (\text{m}[j,i] / \text{m}[i,i]) * \text{row}_i$  which do not change the determinant. Row swaps flip the determinant sign and are tracked by the returned factor.

##### Warning

Pivoting is limited: a row swap is attempted only when the pivot is “near zero” per [MAT2D\\_IS\\_ZERO\(\)](#). No full pivoting is used.

Definition at line 1168 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D\\_AT](#), [MAT2D\\_IS\\_ZERO](#), [mat2D\\_sub\\_row\\_time\\_factor\\_to\\_row\(\)](#), [mat2D\\_swap\\_rows\(\)](#), and [Mat2D::rows](#).

Referenced by [main\(\)](#), [mat2D\\_det\(\)](#), and [mat2D\\_make\\_identity\(\)](#).

## 4.2 Matrix2D.h

```

00001
00057 #ifndef MATRIX2D_H_
00058 #define MATRIX2D_H_
00059
00060 #include <stddef.h>
00061 #include <stdio.h>
00062 #include <stdlib.h>
00063 #include <stdint.h>
00064 #include <stdbool.h>
00065 #include <math.h>
00066
00075 #ifndef MAT2D_MALLOC
00076 #define MAT2D_MALLOC malloc
00077 #endif //MAT2D_MALLOC
00078
00087 #ifndef MAT2D_FREE
00088 #define MAT2D_FREE free
00089 #endif //MAT2D_FREE
00090
00099 #ifndef MAT2D_ASSERT
00100 #include <assert.h>
00101 #define MAT2D_ASSERT assert
00102 #endif //MAT2D_ASSERT
00103
00117 typedef struct {
00118     size_t rows;
00119     size_t cols;
00120     size_t stride_r; /* elements to traverse to reach the next row */
00121     double *elements;
00122 } Mat2D;
00123
00130 typedef struct {
00131     size_t rows;
00132     size_t cols;
00133     size_t stride_r; /* elements to traverse to reach the next row */
00134     uint32_t *elements;
00135 } Mat2D_uint32;
00136
00152 typedef struct {
00153     size_t rows;
00154     size_t cols;
00155     size_t stride_r; /* logical stride for the minor shape (not used for access) */
00156     size_t *rows_list;
00157     size_t *cols_list;
00158     Mat2D ref_mat;
00159 } Mat2D_Minor;
00160
00178 #if 1
00179 #define MAT2D_AT(m, i, j) (m).elements[mat2D_offset2d((m), (i), (j))]
00180 #define MAT2D_AT_UINT32(m, i, j) (m).elements[mat2D_offset2d_uint32((m), (i), (j))]
00181 #else /* use this macro for better performance but no assertion */
00182 #define MAT2D_AT(m, i, j) (m).elements[(i) * (m).stride_r + (j)]
00183 #define MAT2D_AT_UINT32(m, i, j) (m).elements[(i) * (m).stride_r + (j)]
00184 #endif
00185
00186 #ifndef MAT2D_PI
00187     #define MAT2D_PI 3.14159265358979323846
00188 #endif
00189
00190 #ifndef MAT2D_EPS
00191     #define MAT2D_EPS 1e-15
00192 #endif
00193
00201 #define MAT2D_IS_ZERO(x) (fabs(x) < MAT2D_EPS)
00202
00210 #define MAT2D_MINOR_AT(mm, i, j) MAT2D_AT((mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j])
00211
00216 #define MAT2D_PRINT(m) mat2D_print(m, #m, 0)
00217
00222 #define MAT2D_PRINT_AS_COL(m) mat2D_print_as_col(m, #m, 0)
00223
00228 #define MAT2D_MINOR_PRINT(mm) mat2D_minor_print(mm, #mm, 0)
00229
00240 #define mat2D_normalize(m) mat2D_mult((m), 1.0 / mat2D_calc_norma((m)))
00241
00242 double mat2D_rand_double(void);
00243
00244 Mat2D mat2D_alloc(size_t rows, size_t cols);
00245 Mat2D_uint32 mat2D_alloc_uint32(size_t rows, size_t cols);
00246 void mat2D_free(Mat2D m);
00247 void mat2D_free_uint32(Mat2D_uint32 m);
00248 size_t mat2D_offset2d(Mat2D m, size_t i, size_t j);
00249 size_t mat2D_offset2d_uint32(Mat2D_uint32 m, size_t i, size_t j);
00250
00251 void mat2D_fill(Mat2D m, double x);

```

```

00252 void mat2D_fill_sequence(Mat2D m, double start, double step);
00253 void mat2D_fill_uint32(Mat2D uint32 m, uint32_t x);
00254 void mat2D_rand(Mat2D m, double low, double high);
00255
00256 void mat2D_dot(Mat2D dst, Mat2D a, Mat2D b);
00257 double mat2D_dot_product(Mat2D a, Mat2D b);
00258 void mat2D_cross(Mat2D dst, Mat2D a, Mat2D b);
00259
00260 void mat2D_add(Mat2D dst, Mat2D a);
00261 void mat2D_add_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor);
00262
00263 void mat2D_sub(Mat2D dst, Mat2D a);
00264 void mat2D_sub_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor);
00265
00266 void mat2D_mult(Mat2D m, double factor);
00267 void mat2D_mult_row(Mat2D m, size_t r, double factor);
00268
00269 void mat2D_print(Mat2D m, const char *name, size_t padding);
00270 void mat2D_print_as_col(Mat2D m, const char *name, size_t padding);
00271
00272 void mat2D_set_identity(Mat2D m);
00273 double mat2D_make_identity(Mat2D m);
00274 void mat2D_set_rot_mat_x(Mat2D m, float angle_deg);
00275 void mat2D_set_rot_mat_y(Mat2D m, float angle_deg);
00276 void mat2D_set_rot_mat_z(Mat2D m, float angle_deg);
00277 void mat2D_set_DCM_zyx(Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg);
00278
00279 void mat2D_copy(Mat2D des, Mat2D src);
00280 void mat2D_copy_mat_to_mat_at_window(Mat2D des, Mat2D src, size_t is, size_t js, size_t ie,
00281     size_t je);
00282
00283 void mat2D_get_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00284 void mat2D_add_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00285 void mat2D_sub_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00286
00287 void mat2D_swap_rows(Mat2D m, size_t r1, size_t r2);
00288 void mat2D_get_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00289 void mat2D_add_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00290 void mat2D_sub_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00291
00292 void mat2D_calc_norma(Mat2D m);
00293
00294 bool mat2D_mat_is_all_digit(Mat2D m, double digit);
00295 bool mat2D_row_is_all_digit(Mat2D m, double digit, size_t r);
00296 bool mat2D_col_is_all_digit(Mat2D m, double digit, size_t c);
00297
00298 double mat2D_det_2x2_mat(Mat2D m);
00299 double mat2D_upper_triangulate(Mat2D m);
00300 void mat2D_LUP_decomposition_with_swap(Mat2D src, Mat2D l, Mat2D p, Mat2D u);
00301 void mat2D_transpose(Mat2D des, Mat2D src);
00302 void mat2D_invert(Mat2D des, Mat2D src);
00303 void mat2D_solve_linear_sys_LUP_decomposition(Mat2D A, Mat2D x, Mat2D B);
00304
00305 Mat2D_Minor mat2D_minor_alloc_fill_from_mat(Mat2D ref_mat, size_t i, size_t j);
00306 Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor(Mat2D_Minor ref_mm, size_t i, size_t j);
00307 void mat2D_minor_free(Mat2D_Minor mm);
00308 void mat2D_minor_print(Mat2D_Minor mm, const char *name, size_t padding);
00309 double mat2D_det_2x2_mat_minor(Mat2D_Minor mm);
00310 double mat2D_minor_det(Mat2D_Minor mm);
00311
00312 #endif // MATRIX2D_H_
00313
00314 #ifdef MATRIX2D_IMPLEMENTATION
00315 #undef MATRIX2D_IMPLEMENTATION
00316
00317
00318 double mat2D_rand_double(void)
00319 {
00320     return (double) rand() / (double) RAND_MAX;
00321 }
00322
00323 Mat2D mat2D_alloc(size_t rows, size_t cols)
00324 {
00325     Mat2D m;
00326     m.rows = rows;
00327     m.cols = cols;
00328     m.stride_r = cols;
00329     m.elements = (double*)MAT2D_MALLOC(sizeof(double)*rows*cols);
00330     MAT2D_ASSERT(m.elements != NULL);
00331
00332     return m;
00333 }
00334
00335 Mat2D_uint32 mat2D_alloc_uint32(size_t rows, size_t cols)
00336 {
00337     Mat2D_uint32 m;
00338
00339 }
```

```

00371     m.rows = rows;
00372     m.cols = cols;
00373     m.stride_r = cols;
00374     m.elements = (uint32_t*)MAT2D_MALLOC(sizeof(uint32_t)*rows*cols);
00375     MAT2D_ASSERT(m.elements != NULL);
00376
00377     return m;
00378 }
00379
00380 void mat2D_free(Mat2D m)
00381 {
00382     MAT2D_FREE(m.elements);
00383 }
00384
00385 void mat2D_free_uint32(Mat2D_uint32 m)
00386 {
00387     MAT2D_FREE(m.elements);
00388 }
00389
00390 size_t mat2D_offset2d(Mat2D m, size_t i, size_t j)
00391 {
00392     MAT2D_ASSERT(i < m.rows && j < m.cols);
00393     return i * m.stride_r + j;
00394 }
00395
00396 size_t mat2D_offset2d_uint32(Mat2D_uint32 m, size_t i, size_t j)
00397 {
00398     MAT2D_ASSERT(i < m.rows && j < m.cols);
00399     return i * m.stride_r + j;
00400 }
00401
00402 void mat2D_fill(Mat2D m, double x)
00403 {
00404     for (size_t i = 0; i < m.rows; ++i) {
00405         for (size_t j = 0; j < m.cols; ++j) {
00406             MAT2D_AT(m, i, j) = x;
00407         }
00408     }
00409 }
00410
00411 void mat2D_fill_sequence(Mat2D m, double start, double step) {
00412     for (size_t i = 0; i < m.rows; i++) {
00413         for (size_t j = 0; j < m.cols; j++) {
00414             MAT2D_AT(m, i, j) = start + step * mat2D_offset2d(m, i, j);
00415         }
00416     }
00417 }
00418
00419 void mat2D_fill_uint32(Mat2D_uint32 m, uint32_t x)
00420 {
00421     for (size_t i = 0; i < m.rows; ++i) {
00422         for (size_t j = 0; j < m.cols; ++j) {
00423             MAT2D_AT_UINT32(m, i, j) = x;
00424         }
00425     }
00426 }
00427
00428 void mat2D_rand(Mat2D m, double low, double high)
00429 {
00430     for (size_t i = 0; i < m.rows; ++i) {
00431         for (size_t j = 0; j < m.cols; ++j) {
00432             MAT2D_AT(m, i, j) = mat2D_rand_double()*(high - low) + low;
00433         }
00434     }
00435 }
00436
00437 void mat2D_dot(Mat2D dst, Mat2D a, Mat2D b)
00438 {
00439     MAT2D_ASSERT(a.cols == b.rows);
00440     MAT2D_ASSERT(a.rows == dst.rows);
00441     MAT2D_ASSERT(b.cols == dst.cols);
00442
00443     size_t i, j, k;
00444
00445     for (i = 0; i < dst.rows; i++) {
00446         for (j = 0; j < dst.cols; j++) {
00447             MAT2D_AT(dst, i, j) = 0;
00448             for (k = 0; k < a.cols; k++) {
00449                 MAT2D_AT(dst, i, j) += MAT2D_AT(a, i, k)*MAT2D_AT(b, k, j);
00450             }
00451         }
00452     }
00453 }
00454
00455 double mat2D_dot_product(Mat2D a, Mat2D b)
00456 {

```

```

00546     MAT2D_ASSERT(a.rows == b.rows);
00547     MAT2D_ASSERT(a.cols == b.cols);
00548     MAT2D_ASSERT((l == a.cols && l == b.cols) || (l == a.rows && l == b.rows));
00549
00550     double dot_product = 0;
00551
00552     if (l == a.cols) {
00553         for (size_t i = 0; i < a.rows; i++) {
00554             dot_product += MAT2D_AT(a, i, 0) * MAT2D_AT(b, i, 0);
00555         }
00556     } else {
00557         for (size_t j = 0; j < a.cols; j++) {
00558             dot_product += MAT2D_AT(a, 0, j) * MAT2D_AT(b, 0, j);
00559         }
00560     }
00561
00562     return dot_product;
00563 }
00564
00572 void mat2D_cross(Mat2D dst, Mat2D a, Mat2D b)
00573 {
00574     MAT2D_ASSERT(3 == dst.rows && 1 == dst.cols);
00575     MAT2D_ASSERT(3 == a.rows && 1 == a.cols);
00576     MAT2D_ASSERT(3 == b.rows && 1 == b.cols);
00577
00578     MAT2D_AT(dst, 0, 0) = MAT2D_AT(a, 1, 0) * MAT2D_AT(b, 2, 0) - MAT2D_AT(a, 2, 0) * MAT2D_AT(b, 1, 0);
00579     MAT2D_AT(dst, 1, 0) = MAT2D_AT(a, 2, 0) * MAT2D_AT(b, 0, 0) - MAT2D_AT(a, 0, 0) * MAT2D_AT(b, 2, 0);
00580     MAT2D_AT(dst, 2, 0) = MAT2D_AT(a, 0, 0) * MAT2D_AT(b, 1, 0) - MAT2D_AT(a, 1, 0) * MAT2D_AT(b, 0, 0);
00581 }
00582
00591 void mat2D_add(Mat2D dst, Mat2D a)
00592 {
00593     MAT2D_ASSERT(dst.rows == a.rows);
00594     MAT2D_ASSERT(dst.cols == a.cols);
00595     for (size_t i = 0; i < dst.rows; ++i) {
00596         for (size_t j = 0; j < dst.cols; ++j) {
00597             MAT2D_AT(dst, i, j) += MAT2D_AT(a, i, j);
00598         }
00599     }
00600 }
00601
00611 void mat2D_add_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor)
00612 {
00613     for (size_t j = 0; j < m.cols; ++j) {
00614         MAT2D_AT(m, des_r, j) += factor * MAT2D_AT(m, src_r, j);
00615     }
00616 }
00617
00625 void mat2D_sub(Mat2D dst, Mat2D a)
00626 {
00627     MAT2D_ASSERT(dst.rows == a.rows);
00628     MAT2D_ASSERT(dst.cols == a.cols);
00629     for (size_t i = 0; i < dst.rows; ++i) {
00630         for (size_t j = 0; j < dst.cols; ++j) {
00631             MAT2D_AT(dst, i, j) -= MAT2D_AT(a, i, j);
00632         }
00633     }
00634 }
00635
00645 void mat2D_sub_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor)
00646 {
00647     for (size_t j = 0; j < m.cols; ++j) {
00648         MAT2D_AT(m, des_r, j) -= factor * MAT2D_AT(m, src_r, j);
00649     }
00650 }
00651
00657 void mat2D_mult(Mat2D m, double factor)
00658 {
00659     for (size_t i = 0; i < m.rows; ++i) {
00660         for (size_t j = 0; j < m.cols; ++j) {
00661             MAT2D_AT(m, i, j) *= factor;
00662         }
00663     }
00664 }
00665
00674 void mat2D_mult_row(Mat2D m, size_t r, double factor)
00675 {
00676     for (size_t j = 0; j < m.cols; ++j) {
00677         MAT2D_AT(m, r, j) *= factor;
00678     }
00679 }
00680
00687 void mat2D_print(Mat2D m, const char *name, size_t padding)
00688 {

```

```

00689     printf("%*s%s = [\n", (int) padding, "", name);
00690     for (size_t i = 0; i < m.rows; ++i) {
00691         printf("%*s    ", (int) padding, "");
00692         for (size_t j = 0; j < m.cols; ++j) {
00693             printf("%9.6f ", MAT2D_AT(m, i, j));
00694         }
00695         printf("\n");
00696     }
00697     printf("%*s]\n", (int) padding, "");
00698 }
00699
00706 void mat2D_print_as_col(Mat2D m, const char *name, size_t padding)
00707 {
00708     printf("%*s%s = [\n", (int) padding, "", name);
00709     for (size_t i = 0; i < m.rows*m.cols; ++i) {
00710         printf("%*s    ", (int) padding, "");
00711         printf("%f\n", m.elements[i]);
00712     }
00713     printf("%*s]\n", (int) padding, "");
00714 }
00715
00722 void mat2D_set_identity(Mat2D m)
00723 {
00724     MAT2D_ASSERT(m.cols == m.rows);
00725     for (size_t i = 0; i < m.rows; ++i) {
00726         for (size_t j = 0; j < m.cols; ++j) {
00727             MAT2D_AT(m, i, j) = i == j ? 1 : 0;
00728             // if (i == j) {
00729             //     MAT2D_AT(m, i, j) = 1;
00730             // }
00731             // else {
00732             //     MAT2D_AT(m, i, j) = 0;
00733             // }
00734         }
00735     }
00736 }
00737
00754 double mat2D_make_identity(Mat2D m)
00755 {
00756     /* make identity matrix using Gauss elimination */
00757     /* preforming Gauss elimination: https://en.wikipedia.org/wiki/Gaussian_elimination */
00758     /* returns the factor multiplying the determinant */
00759
00760     double factor_to_return = mat2D_upper_triangulate(m);
00761
00762     double factor = 1 / MAT2D_AT(m, m.rows-1, m.cols-1);
00763     mat2D_mult_row(m, m.rows-1, factor);
00764     factor_to_return *= factor;
00765     for (size_t c = m.cols-1; c > 0; c--) {
00766         double factor = 1 / MAT2D_AT(m, c, c);
00767         mat2D_mult_row(m, c, factor);
00768         for (int r = c-1; r >= 0; r--) {
00769             mat2D_sub_row_time_factor_to_row(m, r, c, MAT2D_AT(m, r, c));
00770         }
00771     }
00772
00773
00774     return factor_to_return;
00775 }
00776
00789 void mat2D_set_rot_mat_x(Mat2D m, float angle_deg)
00790 {
00791     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);
00792
00793     float angle_rad = angle_deg * MAT2D_PI / 180;
00794     mat2D_set_identity(m);
00795     MAT2D_AT(m, 1, 1) = cos(angle_rad);
00796     MAT2D_AT(m, 1, 2) = sin(angle_rad);
00797     MAT2D_AT(m, 2, 1) = -sin(angle_rad);
00798     MAT2D_AT(m, 2, 2) = cos(angle_rad);
00799 }
00800
00813 void mat2D_set_rot_mat_y(Mat2D m, float angle_deg)
00814 {
00815     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);
00816
00817     float angle_rad = angle_deg * MAT2D_PI / 180;
00818     mat2D_set_identity(m);
00819     MAT2D_AT(m, 0, 0) = cos(angle_rad);
00820     MAT2D_AT(m, 0, 2) = -sin(angle_rad);
00821     MAT2D_AT(m, 2, 0) = sin(angle_rad);
00822     MAT2D_AT(m, 2, 2) = cos(angle_rad);
00823 }
00824
00837 void mat2D_set_rot_mat_z(Mat2D m, float angle_deg)
00838 {
00839     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);

```

```

00840
00841     float angle_rad = angle_deg * MAT2D_PI / 180;
00842     mat2D_set_identity(m);
00843     MAT2D_AT(m, 0, 0) = cos(angle_rad);
00844     MAT2D_AT(m, 0, 1) = sin(angle_rad);
00845     MAT2D_AT(m, 1, 0) = -sin(angle_rad);
00846     MAT2D_AT(m, 1, 1) = cos(angle_rad);
00847 }
00848
00849 void mat2D_set_DCM_zyx(Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg)
00850 {
00851     Mat2D RotZ = mat2D_alloc(3,3);
00852     mat2D_set_rot_mat_z(RotZ, yaw_deg);
00853     Mat2D RotY = mat2D_alloc(3,3);
00854     mat2D_set_rot_mat_y(RotY, pitch_deg);
00855     Mat2D RotX = mat2D_alloc(3,3);
00856     mat2D_set_rot_mat_x(RotX, roll_deg);
00857     Mat2D temp = mat2D_alloc(3,3);
00858
00859     mat2D_dot(temp, RotY, RotZ);
00860     mat2D_dot(DCM, RotX, temp); /* I have a DCM */
00861
00862     mat2D_free(RotZ);
00863     mat2D_free(RotY);
00864     mat2D_free(RotX);
00865     mat2D_free(temp);
00866 }
00867
00868 void mat2D_copy(Mat2D des, Mat2D src)
00869 {
00870     MAT2D_ASSERT(des.cols == src.cols);
00871     MAT2D_ASSERT(des.rows == src.rows);
00872
00873     for (size_t i = 0; i < des.rows; ++i) {
00874         for (size_t j = 0; j < des.cols; ++j) {
00875             MAT2D_AT(des, i, j) = MAT2D_AT(src, i, j);
00876         }
00877     }
00878
00879 void mat2D_copy_mat_to_mat_at_window(Mat2D des, Mat2D src, size_t is, size_t js, size_t ie, size_t je)
00880 {
00881     MAT2D_ASSERT(je >= js && ie >= is);
00882     MAT2D_ASSERT(je-js+1 == des.cols);
00883     MAT2D_ASSERT(ie-is+1 == des.rows);
00884
00885     for (size_t index = 0; index < des.rows; ++index) {
00886         for (size_t jndex = 0; jndex < des.cols; ++jndex) {
00887             MAT2D_AT(des, index, jndex) = MAT2D_AT(src, is+index, js+jndex);
00888         }
00889     }
00890 }
00891
00892 void mat2D_get_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00893 {
00894     MAT2D_ASSERT(src_col < src.cols);
00895     MAT2D_ASSERT(des.rows == src.rows);
00896     MAT2D_ASSERT(des_col < des.cols);
00897
00898     for (size_t i = 0; i < des.rows; i++) {
00899         MAT2D_AT(des, i, des_col) = MAT2D_AT(src, i, src_col);
00900     }
00901 }
00902
00903 void mat2D_add_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00904 {
00905     MAT2D_ASSERT(src_col < src.cols);
00906     MAT2D_ASSERT(des.rows == src.rows);
00907     MAT2D_ASSERT(des_col < des.cols);
00908
00909     for (size_t i = 0; i < des.rows; i++) {
00910         MAT2D_AT(des, i, des_col) += MAT2D_AT(src, i, src_col);
00911     }
00912 }
00913
00914 void mat2D_sub_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00915 {
00916     MAT2D_ASSERT(src_col < src.cols);
00917     MAT2D_ASSERT(des.rows == src.rows);
00918     MAT2D_ASSERT(des_col < des.cols);
00919
00920     for (size_t i = 0; i < des.rows; i++) {
00921         MAT2D_AT(des, i, des_col) -= MAT2D_AT(src, i, src_col);
00922     }
00923 }
00924
00925 void mat2D_swap_rows(Mat2D m, size_t r1, size_t r2)

```

```

00994 {
00995     for (size_t j = 0; j < m.cols; j++) {
00996         double temp = MAT2D_AT(m, r1, j);
00997         MAT2D_AT(m, r1, j) = MAT2D_AT(m, r2, j);
00998         MAT2D_AT(m, r2, j) = temp;
00999     }
01000 }
01001
01011 void mat2D_get_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01012 {
01013     MAT2D_ASSERT(src_row < src.rows);
01014     MAT2D_ASSERT(des.cols == src.cols);
01015     MAT2D_ASSERT(des_row < des.rows);
01016
01017     for (size_t j = 0; j < des.cols; j++) {
01018         MAT2D_AT(des, des_row, j) = MAT2D_AT(src, src_row, j);
01019     }
01020 }
01021
01031 void mat2D_add_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01032 {
01033     MAT2D_ASSERT(src_row < src.rows);
01034     MAT2D_ASSERT(des.cols == src.cols);
01035     MAT2D_ASSERT(des_row < des.rows);
01036
01037     for (size_t j = 0; j < des.cols; j++) {
01038         MAT2D_AT(des, des_row, j) += MAT2D_AT(src, src_row, j);
01039     }
01040 }
01041
01052 void mat2D_sub_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01053 {
01054     MAT2D_ASSERT(src_row < src.rows);
01055     MAT2D_ASSERT(des.cols == src.cols);
01056     MAT2D_ASSERT(des_row < des.rows);
01057
01058     for (size_t j = 0; j < des.cols; j++) {
01059         MAT2D_AT(des, des_row, j) -= MAT2D_AT(src, src_row, j);
01060     }
01061 }
01062
01068 double mat2D_calc_norma(Mat2D m)
01069 {
01070     double sum = 0;
01071
01072     for (size_t i = 0; i < m.rows; ++i) {
01073         for (size_t j = 0; j < m.cols; ++j) {
01074             sum += MAT2D_AT(m, i, j) * MAT2D_AT(m, i, j);
01075         }
01076     }
01077     return sqrt(sum);
01078 }
01079
01088 bool mat2D_mat_is_all_digit(Mat2D m, double digit)
01089 {
01090     for (size_t i = 0; i < m.rows; ++i) {
01091         for (size_t j = 0; j < m.cols; ++j) {
01092             if (MAT2D_AT(m, i, j) != digit) {
01093                 return false;
01094             }
01095         }
01096     }
01097     return true;
01098 }
01099
01109 bool mat2D_row_is_all_digit(Mat2D m, double digit, size_t r)
01110 {
01111     for (size_t j = 0; j < m.cols; ++j) {
01112         if (MAT2D_AT(m, r, j) != digit) {
01113             return false;
01114         }
01115     }
01116     return true;
01117 }
01118
01128 bool mat2D_col_is_all_digit(Mat2D m, double digit, size_t c)
01129 {
01130     for (size_t i = 0; i < m.rows; ++i) {
01131         if (MAT2D_AT(m, i, c) != digit) {
01132             return false;
01133         }
01134     }
01135     return true;
01136 }
01137
01143 double mat2D_det_2x2_mat(Mat2D m)
01144 {

```

```

01145     MAT2D_ASSERT(2 == m.cols && 2 == m.rows && "Not a 2x2 matrix");
01146     return MAT2D_AT(m, 0, 0) * MAT2D_AT(m, 1, 1) - MAT2D_AT(m, 0, 1) * MAT2D_AT(m, 1, 0);
01147 }
01148
01149 double mat2D_upper_triangulate(Mat2D m)
01150 {
01151     /* preforming Gauss elimination: https://en.wikipedia.org/wiki/Gaussian_elimination */
01152     /* returns the factor multiplying the determinant */
01153
01154     double factor_to_return = 1;
01155
01156     size_t size = (size_t)fmin(m.rows, m.cols);
01157     for (size_t i = 0; i < size; i++) {
01158         if (MAT2D_IS_ZERO(MAT2D_AT(m, i, i))) { /* swapping only if it is zero */
01159             /* finding biggest first number (absolute value) */
01160             size_t biggest_r = i;
01161             for (size_t index = i; index < m.rows; index++) {
01162                 if (fabs(MAT2D_AT(m, index, i)) > fabs(MAT2D_AT(m, biggest_r, i))) {
01163                     biggest_r = index;
01164                 }
01165             }
01166             if (i != biggest_r) {
01167                 mat2D_swap_rows(m, i, biggest_r);
01168                 factor_to_return *= -1;
01169             }
01170         }
01171         for (size_t j = i+1; j < m.rows; j++) {
01172             double factor = 1 / MAT2D_AT(m, i, i);
01173             if (!isfinite(factor)) {
01174                 printf("%s:%d:\n%s:[Error] unable to transfrom into uperr triangular matrix.\n"
01175                     "Probably some of the rows are not independent.\n", __FILE__, __LINE__, __func__);
01176             }
01177             double mat_value = MAT2D_AT(m, j, i);
01178             mat2D_sub_row_time_factor_to_row(m, j, i, mat_value * factor);
01179         }
01180     }
01181     return factor_to_return;
01182 }
01183
01184
01185 double mat2D_det(Mat2D m)
01186 {
01187     MAT2D_ASSERT(m.cols == m.rows && "should be a square matrix");
01188
01189     /* checking if there is a row or column with all zeros */
01190     /* checking rows */
01191     for (size_t i = 0; i < m.rows; i++) {
01192         if (mat2D_row_is_all_digit(m, 0, i)) {
01193             return 0;
01194         }
01195     }
01196     /* checking cols */
01197     for (size_t j = 0; j < m.rows; j++) {
01198         if (mat2D_col_is_all_digit(m, 0, j)) {
01199             return 0;
01200         }
01201     }
01202
01203     #if 0/* This is an implementation of naive determinant calculation using minors. This is too slow
01204 */
01205     double det = 0;
01206     /* TODO: finding beast row or col? */
01207     for (size_t i = 0, j = 0; i < m.rows; i++) { /* first column */
01208         if (MAT2D_AT(m, i, j) < 1e-10) continue;
01209         Mat2D_Minor sub_mm = mat2D_minor_alloc_fill_from_mat(m, i, j);
01210         int factor = (i+j)%2 ? -1 : 1;
01211         if (sub_mm.cols != 2) {
01212             MAT2D_ASSERT(sub_mm.cols == sub_mm.rows && "should be a square matrix");
01213             det += MAT2D_AT(m, i, j) * (factor) * mat2D_minor_det(sub_mm);
01214         } else if (sub_mm.cols == 2 && sub_mm.rows == 2) {
01215             det += MAT2D_AT(m, i, j) * (factor) * mat2D_det_2x2_mat_minor(sub_mm);
01216         }
01217         mat2D_minor_free(sub_mm);
01218     }
01219     #endif
01220
01221     Mat2D temp_m = mat2D_alloc(m.rows, m.cols);
01222     mat2D_copy(temp_m, m);
01223     double factor = mat2D_upper_triangulate(temp_m);
01224     double diag_mul = 1;
01225     for (size_t i = 0; i < temp_m.rows; i++) {
01226         diag_mul *= MAT2D_AT(temp_m, i, i);
01227     }
01228     mat2D_free(temp_m);
01229
01230     return diag_mul / factor;
01231 }
01232
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01259
01260 }
01261

```

```

01278 void mat2D_LUP_decomposition_with_swap(Mat2D src, Mat2D l, Mat2D p, Mat2D u)
01279 {
01280     /* performing LU decomposition Following the Wikipedia page:
01281      https://en.wikipedia.org/wiki/LU_decomposition */
01282     mat2D_copy(u, src);
01283     mat2D_set_identity(p);
01284     mat2D_fill(l, 0);
01285
01286     for (size_t i = 0; i < (size_t)fmin(u.rows-1, u.cols); i++) {
01287         if (MAT2D_IS_ZERO(MAT2D_AT(u, i, i))) { /* swapping only if it is zero */
01288             /* finding biggest first number (absolute value) */
01289             size_t biggest_r = i;
01290             for (size_t index = i; index < u.rows; index++) {
01291                 if (fabs(MAT2D_AT(u, index, i)) > fabs(MAT2D_AT(u, biggest_r, i))) {
01292                     biggest_r = index;
01293                 }
01294             }
01295             if (i != biggest_r) {
01296                 mat2D_swap_rows(u, i, biggest_r);
01297                 mat2D_swap_rows(p, i, biggest_r);
01298                 mat2D_swap_rows(l, i, biggest_r);
01299             }
01300         }
01301         for (size_t j = i+1; j < u.cols; j++) {
01302             double factor = 1 / MAT2D_AT(u, i, i);
01303             if (!isfinite(factor)) {
01304                 printf("%s:%d:\n%s:\n[Error] unable to transfrom into uper triangular matrix. Probably
01305 some of the rows are not independent.\n", __FILE__, __LINE__, __func__);
01306                 double mat_value = MAT2D_AT(u, j, i);
01307                 mat2D_sub_row_time_factor_to_row(u, j, i, mat_value * factor);
01308                 MAT2D_AT(l, j, i) = mat_value * factor;
01309             }
01310             MAT2D_AT(l, i, i) = 1;
01311         }
01312         MAT2D_AT(l, l.rows-1, l.cols-1) = 1;
01313     }
01314
01322 void mat2D_transpose(Mat2D des, Mat2D src)
01323 {
01324     MAT2D_ASSERT(des.cols == src.rows);
01325     MAT2D_ASSERT(des.rows == src.cols);
01326
01327     for (size_t index = 0; index < des.rows; ++index) {
01328         for (size_t jndex = 0; jndex < des.cols; ++jndex) {
01329             MAT2D_AT(des, index, jndex) = MAT2D_AT(src, jndex, index);
01330         }
01331     }
01332 }
01333
01353 void mat2D_invert(Mat2D des, Mat2D src)
01354 {
01355     MAT2D_ASSERT(src.cols == src.rows && "should be an NxN matrix");
01356     MAT2D_ASSERT(des.cols == src.cols && des.rows == des.cols);
01357
01358     Mat2D m = mat2D_alloc(src.rows, src.cols);
01359     mat2D_copy(m, src);
01360
01361     mat2D_set_identity(des);
01362
01363     if (!(mat2D_det(m))) {
01364         mat2D_fill(des, 0);
01365         printf("%s:%d:\n%s:\n[Error] Can't invert the matrix. Determinant is zero! Set the inverse
01366 matrix to all zeros\n", __FILE__, __LINE__, __func__);
01367         mat2D_free(m);
01368         return;
01369     }
01370
01371     size_t size = (size_t)fmin(m.rows, m.cols);
01372     for (size_t i = 0; i < size; i++) {
01373         if (MAT2D_IS_ZERO(MAT2D_AT(m, i, i))) { /* swapping only if it is zero */
01374             /* finding biggest first number (absolute value) */
01375             size_t biggest_r = i;
01376             for (size_t index = i; index < m.rows; index++) {
01377                 if (fabs(MAT2D_AT(m, index, i)) > fabs(MAT2D_AT(m, biggest_r, i))) {
01378                     biggest_r = index;
01379                 }
01380             }
01381             if (i != biggest_r) {
01382                 mat2D_swap_rows(m, i, biggest_r);
01383                 mat2D_swap_rows(des, i, biggest_r);
01384                 printf("%s:%d:\n%s:\n[INFO] swapping row %zu with row %zu.\n", __FILE__, __LINE__,
01385 __func__, i, biggest_r);
01386             } else {
01387                 MAT2D_ASSERT(0 && "can't inverse");
01388             }
01389     }
}

```

```

01387         }
01388         for (size_t j = i+1; j < size; j++) {
01389             double factor = 1 / MAT2D_AT(m, i, i);
01390             double mat_value = MAT2D_AT(m, j, i);
01391             mat2D_sub_row_time_factor_to_row(m, j, i, mat_value * factor);
01392             mat2D_sub_row_time_factor_to_row(des, j, i, mat_value * factor);
01393         }
01394     }
01395     double factor = 1 / MAT2D_AT(m, m.rows-1, m.cols-1);
01396     mat2D_mult_row(m, m.rows-1, factor);
01397     mat2D_mult_row(des, des.rows-1, factor);
01398     for (size_t c = m.cols-1; c > 0; c--) {
01399         double factor = 1 / MAT2D_AT(m, c, c);
01400         mat2D_mult_row(m, c, factor);
01401         mat2D_mult_row(des, c, factor);
01402         for (int r = c-1; r >= 0; r--) {
01403             double mat_value = MAT2D_AT(m, r, c);
01404             mat2D_sub_row_time_factor_to_row(m, r, c, mat_value);
01405             mat2D_sub_row_time_factor_to_row(des, r, c, mat_value);
01406         }
01407     }
01408 }
01409 mat2D_free(m);
01410 }
01411 }
01429 void mat2D_solve_linear_sys_LUP_decomposition(Mat2D A, Mat2D x, Mat2D B)
01430 {
01431     MAT2D_ASSERT(A.cols == x.rows);
01432     MAT2D_ASSERT(1 == x.cols);
01433     MAT2D_ASSERT(A.rows == B.rows);
01434     MAT2D_ASSERT(1 == B.cols);
01435
01436     Mat2D y = mat2D_alloc(x.rows, x.cols);
01437     Mat2D l = mat2D_alloc(A.rows, A.cols);
01438     Mat2D p = mat2D_alloc(A.rows, A.cols);
01439     Mat2D u = mat2D_alloc(A.rows, A.cols);
01440     Mat2D inv_l = mat2D_alloc(l.rows, l.cols);
01441     Mat2D inv_u = mat2D_alloc(u.rows, u.cols);
01442
01443     mat2D_LUP_decomposition_with_swap(A, l, p, u);
01444
01445     mat2D_invert(inv_l, l);
01446     mat2D_invert(inv_u, u);
01447
01448     mat2D_fill(x, 0); /* x here is only a temp mat*/
01449     mat2D_fill(y, 0);
01450     mat2D_dot(x, p, B);
01451     mat2D_dot(y, inv_l, x);
01452
01453     mat2D_fill(x, 0);
01454     mat2D_dot(x, inv_u, y);
01455
01456     mat2D_free(y);
01457     mat2D_free(l);
01458     mat2D_free(p);
01459     mat2D_free(u);
01460     mat2D_free(inv_l);
01461     mat2D_free(inv_u);
01462 }
01463
01475 Mat2D_Minor mat2D_minor_alloc_fill_from_mat(Mat2D ref_mat, size_t i, size_t j)
01476 {
01477     MAT2D_ASSERT(ref_mat.cols == ref_mat.rows && "minor is defined only for square matrix");
01478
01479     Mat2D_Minor mm;
01480     mm.cols = ref_mat.cols-1;
01481     mm.rows = ref_mat.rows-1;
01482     mm.stride_r = ref_mat.cols-1;
01483     mm.cols_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mat.cols-1));
01484     mm.rows_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mat.rows-1));
01485     mm.ref_mat = ref_mat;
01486
01487     MAT2D_ASSERT(mm.cols_list != NULL && mm.rows_list != NULL);
01488
01489     for (size_t index = 0, temp_index = 0; index < ref_mat.rows; index++) {
01490         if (index != i) {
01491             mm.rows_list[temp_index] = index;
01492             temp_index++;
01493         }
01494     }
01495     for (size_t jndex = 0, temp_jndex = 0; jndex < ref_mat.cols; jndex++) {
01496         if (jndex != j) {
01497             mm.cols_list[temp_jndex] = jndex;
01498             temp_jndex++;
01499         }
01500     }

```

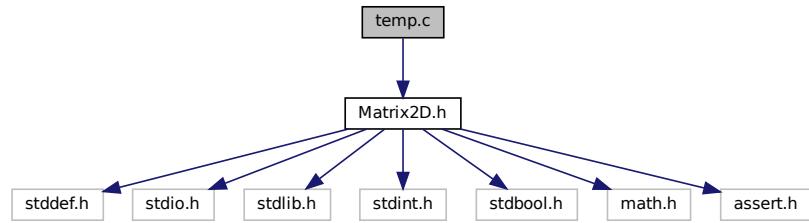
```

01501
01502     return mm;
01503 }
01504
01517 Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor(Mat2D_Minor ref_mm, size_t i, size_t j)
01518 {
01519     MAT2D_ASSERT(ref_mm.cols == ref_mm.rows && "minor is defined only for square matrix");
01520
01521     Mat2D_Minor mm;
01522     mm.cols = ref_mm.cols-1;
01523     mm.rows = ref_mm.rows-1;
01524     mm.stride_r = ref_mm.cols-1;
01525     mm.cols_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mm.cols-1));
01526     mm.rows_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mm.rows-1));
01527     mm.ref_mat = ref_mm.ref_mat;
01528
01529     MAT2D_ASSERT(mm.cols_list != NULL && mm.rows_list != NULL);
01530
01531     for (size_t index = 0, temp_index = 0; index < ref_mm.rows; index++) {
01532         if (index != i) {
01533             mm.rows_list[temp_index] = ref_mm.rows_list[index];
01534             temp_index++;
01535         }
01536     }
01537     for (size_t jndex = 0, temp_jndex = 0; jndex < ref_mm.cols; jndex++) {
01538         if (jndex != j) {
01539             mm.cols_list[temp_jndex] = ref_mm.cols_list[jndex];
01540             temp_jndex++;
01541         }
01542     }
01543
01544     return mm;
01545 }
01546
01552 void mat2D_minor_free(Mat2D_Minor mm)
01553 {
01554     MAT2D_FREE(mm.cols_list);
01555     MAT2D_FREE(mm.rows_list);
01556 }
01557
01564 void mat2D_minor_print(Mat2D_Minor mm, const char *name, size_t padding)
01565 {
01566     printf("%*s%*s = [\n", (int) padding, "", name);
01567     for (size_t i = 0; i < mm.rows; ++i) {
01568         printf("%*s    ", (int) padding, "");
01569         for (size_t j = 0; j < mm.cols; ++j) {
01570             printf("%*f ", MAT2D_MINOR_AT(mm, i, j));
01571         }
01572         printf("\n");
01573     }
01574     printf("%*s]\n", (int) padding, "");
01575 }
01576
01582 double mat2D_det_2x2_mat_minor(Mat2D_Minor mm)
01583 {
01584     MAT2D_ASSERT(2 == mm.cols && 2 == mm.rows && "Not a 2x2 matrix");
01585     return MAT2D_MINOR_AT(mm, 0, 0) * MAT2D_MINOR_AT(mm, 1, 1) - MAT2D_MINOR_AT(mm, 0, 1) *
01586     MAT2D_MINOR_AT(mm, 1, 0);
01587 }
01588
01595 double mat2D_minor_det(Mat2D_Minor mm)
01596 {
01597     MAT2D_ASSERT(mm.cols == mm.rows && "should be a square matrix");
01598
01599     double det = 0;
01600     /* TODO: finding beast row or col? */
01601     for (size_t i = 0, j = 0; i < mm.rows; i++) { /* first column */
01602         if (fabs(MAT2D_MINOR_AT(mm, i, j)) < 1e-10) continue;
01603         Mat2D_Minor sub_mm = mat2D_minor_alloc_fill_from_mat_minor(mm, i, j);
01604         int factor = (i+j)%2 ? -1 : 1;
01605         if (sub_mm.cols != 2) {
01606             MAT2D_ASSERT(sub_mm.cols == sub_mm.rows && "should be a square matrix");
01607             det += MAT2D_MINOR_AT(mm, i, j) * (factor) * mat2D_minor_det(sub_mm);
01608         } else if (sub_mm.cols == 2 && sub_mm.rows == 2) {
01609             det += MAT2D_MINOR_AT(mm, i, j) * (factor) * mat2D_det_2x2_mat_minor(sub_mm);
01610         }
01611         mat2D_minor_free(sub_mm);
01612     }
01613     return det;
01614 }
01615
01616 #endif // MATRIX2D_IMPLEMENTATION

```

## 4.3 temp.c File Reference

```
#include "Matrix2D.h"
Include dependency graph for temp.c:
```



### Macros

- `#define MATRIX2D_IMPLEMENTATION`

### Functions

- `int main (void)`

#### 4.3.1 Macro Definition Documentation

##### 4.3.1.1 MATRIX2D\_IMPLEMENTATION

```
#define MATRIX2D_IMPLEMENTATION
```

Definition at line 1 of file [temp.c](#).

#### 4.3.2 Function Documentation

##### 4.3.2.1 main()

```
int main (
    void )
```

Definition at line 4 of file [temp.c](#).

References [mat2D\\_alloc\(\)](#), [mat2D\\_free\(\)](#), [MAT2D\\_PRINT](#), [mat2D\\_rand\(\)](#), and [mat2D\\_upper\\_triangulate\(\)](#).

## 4.4 temp.c

```
00001 #define MATRIX2D_IMPLEMENTATION
00002 #include "Matrix2D.h"
00003
00004 int main(void)
00005 {
00006     Mat2D m = mat2D_alloc(5, 4);
00007
00008     mat2D_rand(m, 0, 1);
00009
00010     MAT2D_PRINT(m);
00011
00012     mat2D_upper_triangulate(m);
00013
00014     MAT2D_PRINT(m);
00015
00016
00017     mat2D_free(m);
00018
00019     return 0;
00020 }
```

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