

Matrix2D

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Chapter 1

Class Index

1.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

| | | |
|------------------------------|--|---|
| Mat2D | Dense row-major matrix of double | 5 |
| Mat2D_Minor | A minor "view" into a reference matrix | 7 |
| Mat2D_uint32 | Dense row-major matrix of uint32_t | 9 |

Chapter 2

File Index

2.1 File List

Here is a list of all files with brief descriptions:

| | | |
|----------------------------|---|--------------------|
| Matrix2D.h | Lightweight 2D matrix helpers (double / uint32_t) | 11 |
| temp.c | | 59 |

Chapter 3

Class Documentation

3.1 Mat2D Struct Reference

Dense row-major matrix of double.

```
#include <Matrix2D.h>
```

Public Attributes

- size_t [rows](#)
- size_t [cols](#)
- size_t [stride_r](#)
- double * [elements](#)

3.1.1 Detailed Description

Dense row-major matrix of double.

- rows Number of rows (height).
- cols Number of columns (width).
- stride_r Number of elements between successive rows in memory. For contiguous storage, stride_r == cols.
- elements Pointer to a contiguous buffer of rows * cols doubles.

Note

This type is a shallow handle; copying [Mat2D](#) copies the pointer, not the underlying data.

Definition at line [117](#) of file [Matrix2D.h](#).

3.1.2 Member Data Documentation

3.1.2.1 cols

```
size_t Mat2D::cols
```

Definition at line 119 of file [Matrix2D.h](#).

Referenced by [mat2D_add\(\)](#), [mat2D_add_col_to_col\(\)](#), [mat2D_add_row_time_factor_to_row\(\)](#), [mat2D_add_row_to_row\(\)](#), [mat2D_alloc\(\)](#), [mat2D_calc_norma\(\)](#), [mat2D_copy\(\)](#), [mat2D_copy_mat_to_mat_at_window\(\)](#), [mat2D_cross\(\)](#), [mat2D_det\(\)](#), [mat2D_det_2x2_mat\(\)](#), [mat2D_dot\(\)](#), [mat2D_dot_product\(\)](#), [mat2D_fill\(\)](#), [mat2D_fill_sequence\(\)](#), [mat2D_get_col\(\)](#), [mat2D_get_row\(\)](#), [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), [mat2D_make_identity\(\)](#), [mat2D_mat_is_all_digit\(\)](#), [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_mult\(\)](#), [mat2D_mult_row\(\)](#), [mat2D_offset2d\(\)](#), [mat2D_print\(\)](#), [mat2D_print_as_col\(\)](#), [mat2D_rand\(\)](#), [mat2D_row_is_all_digit\(\)](#), [mat2D_set_identity\(\)](#), [mat2D_set_rot_mat_x\(\)](#), [mat2D_set_rot_mat_y\(\)](#), [mat2D_set_rot_mat_z\(\)](#), [mat2D_solve_linear_sys_LUP_decomposition\(\)](#), [mat2D_sub\(\)](#), [mat2D_sub_col_to_col\(\)](#), [mat2D_sub_row_time_factor_to_row\(\)](#), [mat2D_sub_row_to_row\(\)](#), [mat2D_swap_rows\(\)](#), [mat2D_transpose\(\)](#), and [mat2D_upper_triangularize\(\)](#).

3.1.2.2 elements

```
double* Mat2D::elements
```

Definition at line 121 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc\(\)](#), [mat2D_free\(\)](#), and [mat2D_print_as_col\(\)](#).

3.1.2.3 rows

```
size_t Mat2D::rows
```

Definition at line 118 of file [Matrix2D.h](#).

Referenced by [mat2D_add\(\)](#), [mat2D_add_col_to_col\(\)](#), [mat2D_add_row_to_row\(\)](#), [mat2D_alloc\(\)](#), [mat2D_calc_norma\(\)](#), [mat2D_col_is_all_digit\(\)](#), [mat2D_copy\(\)](#), [mat2D_copy_mat_to_mat_at_window\(\)](#), [mat2D_cross\(\)](#), [mat2D_det\(\)](#), [mat2D_det_2x2_mat\(\)](#), [mat2D_dot\(\)](#), [mat2D_dot_product\(\)](#), [mat2D_fill\(\)](#), [mat2D_fill_sequence\(\)](#), [mat2D_get_col\(\)](#), [mat2D_get_row\(\)](#), [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), [mat2D_make_identity\(\)](#), [mat2D_mat_is_all_digit\(\)](#), [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_mult\(\)](#), [mat2D_offset2d\(\)](#), [mat2D_print\(\)](#), [mat2D_print_as_col\(\)](#), [mat2D_rand\(\)](#), [mat2D_set_identity\(\)](#), [mat2D_set_rot_mat_x\(\)](#), [mat2D_set_rot_mat_y\(\)](#), [mat2D_set_rot_mat_z\(\)](#), [mat2D_solve_linear_sys_LUP_decomposition\(\)](#), [mat2D_sub\(\)](#), [mat2D_sub_col_to_col\(\)](#), [mat2D_sub_row_to_row\(\)](#), [mat2D_transpose\(\)](#), and [mat2D_upper_triangularize\(\)](#).

3.1.2.4 stride_r

```
size_t Mat2D::stride_r
```

Definition at line 120 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc\(\)](#), and [mat2D_offset2d\(\)](#).

The documentation for this struct was generated from the following file:

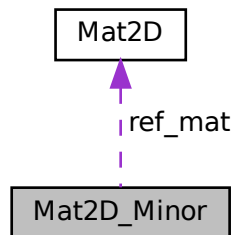
- [Matrix2D.h](#)

3.2 Mat2D_Minor Struct Reference

A minor "view" into a reference matrix.

```
#include <Matrix2D.h>
```

Collaboration diagram for Mat2D_Minor:



Public Attributes

- `size_t` [rows](#)
- `size_t` [cols](#)
- `size_t` [stride_r](#)
- `size_t *` [rows_list](#)
- `size_t *` [cols_list](#)
- [Mat2D](#) [ref_mat](#)

3.2.1 Detailed Description

A minor "view" into a reference matrix.

Represents a minor by excluding one row and one column of a reference matrix. The minor does not own the reference matrix data; instead it stores two index arrays (`rows_list`, `cols_list`) mapping minor coordinates to the reference matrix coordinates.

Memory ownership:

- `rows_list` and `cols_list` are heap-allocated by the minor allocators and must be freed with [mat2D_minor_free\(\)](#).
- `ref_mat.elements` is not owned by the minor and must not be freed by [mat2D_minor_free\(\)](#).

Definition at line [152](#) of file [Matrix2D.h](#).

3.2.2 Member Data Documentation

3.2.2.1 cols

```
size_t Mat2D_Minor::cols
```

Definition at line 154 of file [Matrix2D.h](#).

Referenced by [mat2D_det\(\)](#), [mat2D_det_2x2_mat_minor\(\)](#), [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_minor_alloc_fill_from_mat_m](#), [mat2D_minor_det\(\)](#), and [mat2D_minor_print\(\)](#).

3.2.2.2 cols_list

```
size_t* Mat2D_Minor::cols_list
```

Definition at line 157 of file [Matrix2D.h](#).

Referenced by [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_minor_alloc_fill_from_mat_minor\(\)](#), and [mat2D_minor_free\(\)](#).

3.2.2.3 ref_mat

```
Mat2D Mat2D_Minor::ref_mat
```

Definition at line 158 of file [Matrix2D.h](#).

Referenced by [mat2D_minor_alloc_fill_from_mat\(\)](#), and [mat2D_minor_alloc_fill_from_mat_minor\(\)](#).

3.2.2.4 rows

```
size_t Mat2D_Minor::rows
```

Definition at line 153 of file [Matrix2D.h](#).

Referenced by [mat2D_det\(\)](#), [mat2D_det_2x2_mat_minor\(\)](#), [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_minor_alloc_fill_from_mat_m](#), [mat2D_minor_det\(\)](#), and [mat2D_minor_print\(\)](#).

3.2.2.5 rows_list

```
size_t* Mat2D_Minor::rows_list
```

Definition at line 156 of file [Matrix2D.h](#).

Referenced by [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_minor_alloc_fill_from_mat_minor\(\)](#), and [mat2D_minor_free\(\)](#).

3.2.2.6 stride_r

```
size_t Mat2D_Minor::stride_r
```

Definition at line 155 of file [Matrix2D.h](#).

Referenced by [mat2D_minor_alloc_fill_from_mat\(\)](#), and [mat2D_minor_alloc_fill_from_mat_minor\(\)](#).

The documentation for this struct was generated from the following file:

- [Matrix2D.h](#)

3.3 Mat2D_uint32 Struct Reference

Dense row-major matrix of uint32_t.

```
#include <Matrix2D.h>
```

Public Attributes

- size_t [rows](#)
- size_t [cols](#)
- size_t [stride_r](#)
- uint32_t * [elements](#)

3.3.1 Detailed Description

Dense row-major matrix of uint32_t.

Same layout rules as [Mat2D](#), but with uint32_t elements.

Definition at line 130 of file [Matrix2D.h](#).

3.3.2 Member Data Documentation

3.3.2.1 cols

```
size_t Mat2D_uint32::cols
```

Definition at line 132 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc_uint32\(\)](#), [mat2D_fill_uint32\(\)](#), and [mat2D_offset2d_uint32\(\)](#).

3.3.2.2 elements

```
uint32_t* Mat2D_uint32::elements
```

Definition at line 134 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc_uint32\(\)](#), and [mat2D_free_uint32\(\)](#).

3.3.2.3 rows

```
size_t Mat2D_uint32::rows
```

Definition at line 131 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc_uint32\(\)](#), [mat2D_fill_uint32\(\)](#), and [mat2D_offset2d_uint32\(\)](#).

3.3.2.4 stride_r

```
size_t Mat2D_uint32::stride_r
```

Definition at line 133 of file [Matrix2D.h](#).

Referenced by [mat2D_alloc_uint32\(\)](#), and [mat2D_offset2d_uint32\(\)](#).

The documentation for this struct was generated from the following file:

- [Matrix2D.h](#)

Chapter 4

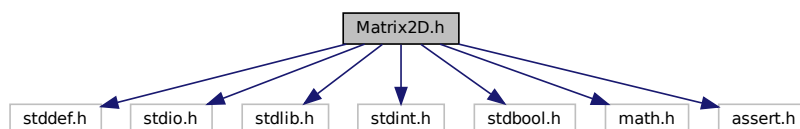
File Documentation

4.1 Matrix2D.h File Reference

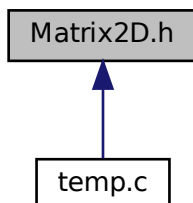
Lightweight 2D matrix helpers (double / uint32_t).

```
#include <stddef.h>
#include <stdio.h>
#include <stdlib.h>
#include <stdint.h>
#include <stdbool.h>
#include <math.h>
#include <assert.h>
```

Include dependency graph for Matrix2D.h:



This graph shows which files directly or indirectly include this file:



Classes

- struct [Mat2D](#)
Dense row-major matrix of double.
- struct [Mat2D_uint32](#)
Dense row-major matrix of uint32_t.
- struct [Mat2D_Minor](#)
A minor "view" into a reference matrix.

Macros

- #define [MAT2D_MALLOC](#) malloc
Allocation function used by this library.
- #define [MAT2D_FREE](#) free
Deallocation function used by this library.
- #define [MAT2D_ASSERT](#) assert
Assertion macro used by this library for parameter validation.
- #define [MAT2D_AT](#)(m, i, j) (m).elements[[mat2D_offset2d](#)((m), (i), (j))]
Access element (i, j) of a [Mat2D](#) (0-based).
- #define [MAT2D_AT_UINT32](#)(m, i, j) (m).elements[[mat2D_offset2d_uint32](#)((m), (i), (j))]
Access element (i, j) of a [Mat2D_uint32](#) (0-based).
- #define [MAT2D_PI](#) 3.14159265358979323846
- #define [MAT2D_EPS](#) 1e-15
- #define [MAT2D_IS_ZERO](#)(x) (fabs(x) < [MAT2D_EPS](#))
Test whether a floating-point value is "near zero".
- #define [MAT2D_MINOR_AT](#)(mm, i, j) [MAT2D_AT](#)((mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j])
Access element (i, j) of a [Mat2D_Minor](#) (0-based).
- #define [MAT2D_PRINT](#)(m) [mat2D_print](#)(m, #m, 0)
Convenience macro to print a matrix with its variable name.
- #define [MAT2D_PRINT_AS_COL](#)(m) [mat2D_print_as_col](#)(m, #m, 0)
Convenience macro to print a matrix as a single column with its name.
- #define [MAT2D_MINOR_PRINT](#)(mm) [mat2D_minor_print](#)(mm, #mm, 0)
Convenience macro to print a minor with its variable name.
- #define [mat2D_normalize](#)(m) [mat2D_mult](#)((m), 1.0 / [mat2D_calc_norma](#)((m)))
Normalize a matrix in-place to unit Frobenius norm.

Functions

- double [mat2D_rand_double](#) (void)
Return a pseudo-random double in the range [0, 1].
- [Mat2D](#) [mat2D_alloc](#) (size_t rows, size_t cols)
Allocate a rows-by-cols matrix of double.
- [Mat2D_uint32](#) [mat2D_alloc_uint32](#) (size_t rows, size_t cols)
Allocate a rows-by-cols matrix of uint32_t.
- void [mat2D_free](#) ([Mat2D](#) m)
Free the buffer owned by a [Mat2D](#).
- void [mat2D_free_uint32](#) ([Mat2D_uint32](#) m)
Free the buffer owned by a [Mat2D_uint32](#).
- size_t [mat2D_offset2d](#) ([Mat2D](#) m, size_t i, size_t j)
Compute the linear offset of element (i, j) in a [Mat2D](#).

- `size_t mat2D_offset2d_uint32 (Mat2D_uint32 m, size_t i, size_t j)`
Compute the linear offset of element (i, j) in a Mat2D_uint32.
- `void mat2D_fill (Mat2D m, double x)`
Fill all elements of a matrix of doubles with a scalar value.
- `void mat2D_fill_sequence (Mat2D m, double start, double step)`
Fill a matrix with an arithmetic sequence laid out in row-major order.
- `void mat2D_fill_uint32 (Mat2D_uint32 m, uint32_t x)`
Fill all elements of a matrix of uint32_t with a scalar value.
- `void mat2D_rand (Mat2D m, double low, double high)`
Fill a matrix with pseudo-random doubles in [low, high].
- `void mat2D_dot (Mat2D dst, Mat2D a, Mat2D b)`
*Matrix product: $dst = a * b$.*
- `double mat2D_dot_product (Mat2D a, Mat2D b)`
Dot product between two vectors.
- `void mat2D_cross (Mat2D dst, Mat2D a, Mat2D b)`
3D cross product: $dst = a \times b$ for 3x1 vectors.
- `void mat2D_add (Mat2D dst, Mat2D a)`
In-place addition: $dst += a$.
- `void mat2D_add_row_time_factor_to_row (Mat2D m, size_t des_r, size_t src_r, double factor)`
*Row operation: $row(des_r) += factor * row(src_r)$.*
- `void mat2D_sub (Mat2D dst, Mat2D a)`
In-place subtraction: $dst -= a$.
- `void mat2D_sub_row_time_factor_to_row (Mat2D m, size_t des_r, size_t src_r, double factor)`
*Row operation: $row(des_r) -= factor * row(src_r)$.*
- `void mat2D_mult (Mat2D m, double factor)`
*In-place scalar multiplication: $m *= factor$.*
- `void mat2D_mult_row (Mat2D m, size_t r, double factor)`
*In-place row scaling: $row(r) *= factor$.*
- `void mat2D_print (Mat2D m, const char *name, size_t padding)`
Print a matrix to stdout with a name and indentation padding.
- `void mat2D_print_as_col (Mat2D m, const char *name, size_t padding)`
Print a matrix as a flattened column vector to stdout.
- `void mat2D_set_identity (Mat2D m)`
Set a square matrix to the identity matrix.
- `double mat2D_make_identity (Mat2D m)`
Reduce a matrix to identity using Gauss-Jordan style elimination.
- `void mat2D_set_rot_mat_x (Mat2D m, float angle_deg)`
Set a 3x3 rotation matrix for rotation about the X-axis.
- `void mat2D_set_rot_mat_y (Mat2D m, float angle_deg)`
Set a 3x3 rotation matrix for rotation about the Y-axis.
- `void mat2D_set_rot_mat_z (Mat2D m, float angle_deg)`
Set a 3x3 rotation matrix for rotation about the Z-axis.
- `void mat2D_set_DCM_zyx (Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg)`
Build a 3x3 direction cosine matrix (DCM) from Z-Y-X Euler angles.
- `void mat2D_copy (Mat2D des, Mat2D src)`
Copy all elements from src to des.
- `void mat2D_copy_mat_to_mat_at_window (Mat2D des, Mat2D src, size_t is, size_t js, size_t ie, size_t je)`
Copy a rectangular window from src into des.
- `void mat2D_get_col (Mat2D des, size_t des_col, Mat2D src, size_t src_col)`
Copy a column from src into a column of des.
- `void mat2D_add_col_to_col (Mat2D des, size_t des_col, Mat2D src, size_t src_col)`

- Add a source column into a destination column.*

 - void `mat2D_sub_col_to_col` (`Mat2D` des, `size_t` des_col, `Mat2D` src, `size_t` src_col)
- Subtract a source column from a destination column.*

 - void `mat2D_swap_rows` (`Mat2D` m, `size_t` r1, `size_t` r2)
- Swap two rows of a matrix in-place.*

 - void `mat2D_get_row` (`Mat2D` des, `size_t` des_row, `Mat2D` src, `size_t` src_row)
- Copy a row from src into a row of des.*

 - void `mat2D_add_row_to_row` (`Mat2D` des, `size_t` des_row, `Mat2D` src, `size_t` src_row)
 - void `mat2D_sub_row_to_row` (`Mat2D` des, `size_t` des_row, `Mat2D` src, `size_t` src_row)
- Subtract a source row from a destination row.*

 - double `mat2D_calc_norma` (`Mat2D` m)
- Compute the Frobenius norm of a matrix, $\sqrt{\sum(m_{ij}^2)}$.*

 - bool `mat2D_mat_is_all_digit` (`Mat2D` m, double digit)
- Check if all elements of a matrix equal a given digit.*

 - bool `mat2D_row_is_all_digit` (`Mat2D` m, double digit, `size_t` r)
- Check if all elements of a row equal a given digit.*

 - bool `mat2D_col_is_all_digit` (`Mat2D` m, double digit, `size_t` c)
- Check if all elements of a column equal a given digit.*

 - double `mat2D_det_2x2_mat` (`Mat2D` m)
- Determinant of a 2x2 matrix.*

 - double `mat2D_upper_triangulate` (`Mat2D` m)
- Forward elimination to transform a matrix to upper triangular form.*

 - double `mat2D_det` (`Mat2D` m)
- Determinant of a square matrix via Gaussian elimination.*

 - void `mat2D_LUP_decomposition_with_swap` (`Mat2D` src, `Mat2D` l, `Mat2D` p, `Mat2D` u)
- Compute LUP decomposition: $P*A = L*U$ with L unit diagonal.*

 - void `mat2D_transpose` (`Mat2D` des, `Mat2D` src)
- Transpose a matrix: $des = src^T$.*

 - void `mat2D_invert` (`Mat2D` des, `Mat2D` src)
- Invert a square matrix using Gauss-Jordan elimination.*

 - void `mat2D_solve_linear_sys_LUP_decomposition` (`Mat2D` A, `Mat2D` x, `Mat2D` B)
- Solve the linear system $Ax = B$ using an LUP-based approach.*

 - `Mat2D_Minor` `mat2D_minor_alloc_fill_from_mat` (`Mat2D` ref_mat, `size_t` i, `size_t` j)
- Allocate a minor view by excluding row i and column j of ref_mat.*

 - `Mat2D_Minor` `mat2D_minor_alloc_fill_from_mat_minor` (`Mat2D_Minor` ref_mm, `size_t` i, `size_t` j)
- Allocate a nested minor view from an existing minor by excluding row i and column j of the minor.*

 - void `mat2D_minor_free` (`Mat2D_Minor` mm)
- Free the index arrays owned by a minor.*

 - void `mat2D_minor_print` (`Mat2D_Minor` mm, const char *name, `size_t` padding)
- Print a minor matrix to stdout with a name and indentation padding.*

 - double `mat2D_det_2x2_mat_minor` (`Mat2D_Minor` mm)
- Determinant of a 2x2 minor.*

 - double `mat2D_minor_det` (`Mat2D_Minor` mm)
- Determinant of a minor via recursive expansion by minors.*

4.1.1 Detailed Description

Lightweight 2D matrix helpers (double / uint32_t).

This single-header module provides small utilities for dense row-major matrices:

- Allocation/free for [Mat2D](#) (double) and [Mat2D_uint32](#)
- Basic arithmetic and row/column operations
- Matrix multiplication, transpose, dot and cross products
- Determinant and inversion (Gaussian / Gauss-Jordan style)
- A simple LUP decomposition helper and a linear system solver
- Rotation matrix helpers (X/Y/Z) and a Z-Y-X DCM builder (as implemented)
- “Minor” views (index lists into a reference matrix) for educational determinant-by-minors computation

Storage model

- Matrices are dense and row-major (C-style).
- Element at row *i* and column *j* (0-based) is: `elements[i * stride_r + j]`
- For matrices created by [mat2D_alloc\(\)](#), `stride_r == cols`.

Usage

- In exactly one translation unit, define `MATRIX2D_IMPLEMENTATION` before including this header to compile the implementation.
- In all other files, include the header without that macro to get declarations only.

Example: `#define MATRIX2D_IMPLEMENTATION #include "matrix2d.h"`

Notes and limitations

- This one-file library is heavily inspired by Tsoding's `nn.h` implementation of matrix creation and operations: <https://github.com/tsoding/nn.h> and the video: <https://youtu.be/L1TbWe8b4V0c?list=PLpM-Dvs8t0VZPZKggcql-MmjaBdZKeDMw>
- All APIs assume the caller provides correctly-sized destination matrices. Shape mismatches are checked with `MAT2D_ASSERT` in many routines.
- This library does not try to be numerically robust:
 - Pivoting is limited (only performed when a pivot is “near zero” per `MAT2D_EPS` in several routines).
 - Ill-conditioned matrices may produce inaccurate determinants/inverses.
- RNG uses `C rand()`; it is not cryptographically secure.

Warning

Numerical stability and correctness

- [mat2D_minor_det\(\)](#) is factorial-time and is intended only for very small matrices (educational use).
- [mat2D_invert\(\)](#) uses Gauss-Jordan elimination and may be unstable for ill-conditioned matrices. Consider a more robust decomposition for production use (full pivoting / QR / SVD).
- Several routines do not guard against aliasing (e.g. `dst == a`). Unless documented otherwise, assume inputs and outputs must not overlap.

Definition in file [Matrix2D.h](#).

4.1.2 Macro Definition Documentation

4.1.2.1 MAT2D_ASSERT

```
#define MAT2D_ASSERT assert
```

Assertion macro used by this library for parameter validation.

Defaults to `assert()`. Override by defining `MAT2D_ASSERT` before including this header to customize validation behavior.

Definition at line 101 of file [Matrix2D.h](#).

4.1.2.2 MAT2D_AT

```
#define MAT2D_AT(  
    m,  
    i,  
    j ) (m).elements[mat2D_offset2d((m), (i), (j))]
```

Access element (i, j) of a [Mat2D](#) (0-based).

Expands to row-major indexing using `stride_r`: `(m).elements[(i) * (m).stride_r + (j)]`

Warning

In the “fast” configuration this macro performs no bounds checking.

Definition at line 179 of file [Matrix2D.h](#).

4.1.2.3 MAT2D_AT_UINT32

```
#define MAT2D_AT_UINT32(  
    m,  
    i,  
    j ) (m).elements[mat2D_offset2d_uint32((m), (i), (j))]
```

Access element (i, j) of a [Mat2D_uint32](#) (0-based).

Warning

In the “fast” configuration this macro performs no bounds checking.

Definition at line 180 of file [Matrix2D.h](#).

4.1.2.4 MAT2D_EPS

```
#define MAT2D_EPS 1e-15
```

Definition at line 191 of file [Matrix2D.h](#).

4.1.2.5 MAT2D_FREE

```
#define MAT2D_FREE free
```

Deallocation function used by this library.

Defaults to free(). Override by defining MAT2D_FREE before including this header to match a custom allocator.

Definition at line 88 of file [Matrix2D.h](#).

4.1.2.6 MAT2D_IS_ZERO

```
#define MAT2D_IS_ZERO(  
    x ) (fabs(x) < MAT2D_EPS)
```

Test whether a floating-point value is “near zero”.

Uses fabs(x) < MAT2D_EPS.

Definition at line 201 of file [Matrix2D.h](#).

4.1.2.7 MAT2D_MALLOC

```
#define MAT2D_MALLOC malloc
```

Allocation function used by this library.

Defaults to malloc(). Override by defining MAT2D_MALLOC before including this header to use a custom allocator.

Definition at line 76 of file [Matrix2D.h](#).

4.1.2.8 MAT2D_MINOR_AT

```
#define MAT2D_MINOR_AT(  
    mm,  
    i,  
    j ) MAT2D_AT((mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j])
```

Access element (i, j) of a [Mat2D_Minor](#) (0-based).

Dereferences into the underlying reference matrix using rows_list/cols_list.

Definition at line 210 of file [Matrix2D.h](#).

4.1.2.9 MAT2D_MINOR_PRINT

```
#define MAT2D_MINOR_PRINT(  
    mm ) mat2D_minor_print(mm, #mm, 0)
```

Convenience macro to print a minor with its variable name.

Definition at line 228 of file [Matrix2D.h](#).

4.1.2.10 mat2D_normalize

```
#define mat2D_normalize(  
    m ) mat2D_mult((m), 1.0 / mat2D_calc_norma((m)))
```

Normalize a matrix in-place to unit Frobenius norm.

Equivalent to: `m *= 1.0 / mat2D_calc_norma(m)`

Warning

If the Frobenius norm is 0, this performs a division by zero.

Definition at line 240 of file [Matrix2D.h](#).

4.1.2.11 MAT2D_PI

```
#define MAT2D_PI 3.14159265358979323846
```

Definition at line 187 of file [Matrix2D.h](#).

4.1.2.12 MAT2D_PRINT

```
#define MAT2D_PRINT(
    m ) mat2D_print(m, #m, 0)
```

Convenience macro to print a matrix with its variable name.

Definition at line 216 of file [Matrix2D.h](#).

4.1.2.13 MAT2D_PRINT_AS_COL

```
#define MAT2D_PRINT_AS_COL(
    m ) mat2D_print_as_col(m, #m, 0)
```

Convenience macro to print a matrix as a single column with its name.

Definition at line 222 of file [Matrix2D.h](#).

4.1.3 Function Documentation

4.1.3.1 mat2D_add()

```
void mat2D_add (
    Mat2D dst,
    Mat2D a )
```

In-place addition: $\text{dst} += \text{a}$.

Parameters

| | |
|------------|---------------------------------------|
| <i>dst</i> | Destination matrix to be incremented. |
| <i>a</i> | Summand of same shape as <i>dst</i> . |

Precondition

dst and *a* have identical shape.

Definition at line 591 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.2 mat2D_add_col_to_col()

```
void mat2D_add_col_to_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Add a source column into a destination column.

Performs: `des[:, des_col] += src[:, src_col]`

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same row count as src). |
| <i>des_col</i> | Column index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_col</i> | Column index in source. |

Definition at line 953 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.3 mat2D_add_row_time_factor_to_row()

```
void mat2D_add_row_time_factor_to_row (
    Mat2D m,
    size_t des_r,
    size_t src_r,
    double factor )
```

Row operation: `row(des_r) += factor * row(src_r)`.

Parameters

| | |
|------------------------|------------------------|
| <i>m</i> | Matrix. |
| <i>des_r</i> | Destination row index. |
| <i>src_r</i> | Source row index. |
| <i>factor</i> | Scalar multiplier. |

Warning

Indices are not bounds-checked in this routine.

Definition at line 611 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D_AT](#).

4.1.3.4 `mat2D_add_row_to_row()`

```
void mat2D_add_row_to_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

Parameters

| | |
|----------------|----------------------|
| <i>src_row</i> | Row index in source. |
|----------------|----------------------|

Precondition

`des.cols == src.cols`

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same number of columns as src). |
| <i>des_row</i> | Row index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_row</i> | Row index in source. |

Definition at line 1031 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.5 `mat2D_alloc()`

```
Mat2D mat2D_alloc (
    size_t rows,
    size_t cols )
```

Allocate a rows-by-cols matrix of double.

Parameters

| | |
|-------------|---------------------------------|
| <i>rows</i> | Number of rows. Must be > 0. |
| <i>cols</i> | Number of columns. Must be > 0. |

Returns

A [Mat2D](#) owning a contiguous buffer of `rows * cols` elements.

Postcondition

The returned matrix has `stride_r == cols`.

The returned matrix must be released with [mat2D_free\(\)](#).

Warning

This function asserts allocation success via MAT2D_ASSERT.

Definition at line 344 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D::elements](#), [MAT2D_ASSERT](#), [MAT2D_MALLOC](#), [Mat2D::rows](#), and [Mat2D::stride_r](#).

Referenced by [main\(\)](#), [mat2D_det\(\)](#), [mat2D_invert\(\)](#), [mat2D_set_DCM_zyx\(\)](#), and [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.6 mat2D_alloc_uint32()

```
Mat2D_uint32 mat2D_alloc_uint32 (
    size_t rows,
    size_t cols )
```

Allocate a rows-by-cols matrix of uint32_t.

Parameters

| | |
|-------------|---------------------------------|
| <i>rows</i> | Number of rows. Must be > 0. |
| <i>cols</i> | Number of columns. Must be > 0. |

Returns

A [Mat2D_uint32](#) owning a contiguous buffer of rows * cols elements.

Postcondition

The returned matrix has stride_r == cols.

The returned matrix must be released with [mat2D_free_uint32\(\)](#).

Warning

This function asserts allocation success via MAT2D_ASSERT.

Definition at line 368 of file [Matrix2D.h](#).

References [Mat2D_uint32::cols](#), [Mat2D_uint32::elements](#), [MAT2D_ASSERT](#), [MAT2D_MALLOC](#), [Mat2D_uint32::rows](#), and [Mat2D_uint32::stride_r](#).

4.1.3.7 mat2D_calc_norma()

```
double mat2D_calc_norma (
    Mat2D m )
```

Compute the Frobenius norm of a matrix, sqrt(sum(m_ij^2)).

Parameters

| | |
|----------|---------|
| <i>m</i> | Matrix. |
|----------|---------|

Returns

Frobenius norm.

Definition at line 1068 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.8 `mat2D_col_is_all_digit()`

```
bool mat2D_col_is_all_digit (
    Mat2D m,
    double digit,
    size_t c )
```

Check if all elements of a column equal a given digit.

Parameters

| | |
|--------------|-------------------|
| <i>m</i> | Matrix. |
| <i>digit</i> | Value to compare. |
| <i>c</i> | Column index. |

Returns

true if every element equals digit, false otherwise.

Warning

Uses exact floating-point equality.

Definition at line 1128 of file [Matrix2D.h](#).

References [MAT2D_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D_det\(\)](#).

4.1.3.9 `mat2D_copy()`

```
void mat2D_copy (
    Mat2D des,
    Mat2D src )
```

Copy all elements from src to des.

Parameters

| | |
|------------|---------------------|
| <i>des</i> | Destination matrix. |
| <i>src</i> | Source matrix. |

Precondition

Shapes match.

des and *src* have identical shape.

Definition at line 887 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D_det\(\)](#), [mat2D_invert\(\)](#), and [mat2D_LUP_decomposition_with_swap\(\)](#).

4.1.3.10 mat2D_copy_mat_to_mat_at_window()

```
void mat2D_copy_mat_to_mat_at_window (
    Mat2D des,
    Mat2D src,
    size_t is,
    size_t js,
    size_t ie,
    size_t je )
```

Copy a rectangular window from *src* into *des*.

Parameters

| | |
|------------|---|
| <i>des</i> | Destination matrix. Must have size (ie - is + 1) x (je - js + 1). |
| <i>src</i> | Source matrix. |
| <i>is</i> | Start row index in <i>src</i> (inclusive). |
| <i>js</i> | Start column index in <i>src</i> (inclusive). |
| <i>ie</i> | End row index in <i>src</i> (inclusive). |
| <i>je</i> | End column index in <i>src</i> (inclusive). |

Precondition

$0 \leq is \leq ie < \text{src.rows}$, $0 \leq js \leq je < \text{src.cols}$.

Definition at line 909 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.11 mat2D_cross()

```
void mat2D_cross (
    Mat2D dst,
    Mat2D a,
    Mat2D b )
```

3D cross product: $\text{dst} = \mathbf{a} \times \mathbf{b}$ for 3x1 vectors.

Parameters

| | |
|------------|-------------------------|
| <i>dst</i> | 3x1 destination vector. |
| <i>a</i> | 3x1 input vector. |
| <i>b</i> | 3x1 input vector. |

Precondition

All matrices have shape 3x1.

Definition at line 572 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.12 mat2D_det()

```
double mat2D_det (
    Mat2D m )
```

Determinant of a square matrix via Gaussian elimination.

Parameters

| | |
|----------|----------------|
| <i>m</i> | Square matrix. |
|----------|----------------|

Returns

$\text{det}(\mathbf{m})$.

Copies *m* internally, transforms the copy to upper triangular form, and returns the product of diagonal elements adjusted by the row-swap factor.

Warning

The early “all-zero row/column” check uses exact comparisons to 0.

Limited pivoting may cause poor numerical results for some inputs.

Definition at line 1215 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D_Minor::cols](#), [mat2D_alloc\(\)](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), [mat2D_col_is_all_digit\(\)](#), [mat2D_copy\(\)](#), [mat2D_det_2x2_mat_minor\(\)](#), [mat2D_free\(\)](#), [mat2D_minor_alloc_fill_from_mat\(\)](#), [mat2D_minor_det\(\)](#), [mat2D_minor_free\(\)](#), [mat2D_row_is_all_digit\(\)](#), [mat2D_upper_triangulate\(\)](#), [Mat2D::rows](#), and [Mat2D_Minor::rows](#).

Referenced by [mat2D_invert\(\)](#).

4.1.3.13 mat2D_det_2x2_mat()

```
double mat2D_det_2x2_mat (
    Mat2D m )
```

Determinant of a 2x2 matrix.

Parameters

| | |
|----------|-----------------------|
| <i>m</i> | Matrix (must be 2x2). |
|----------|-----------------------|

Returns

$\det(m) = m_{00} * m_{11} - m_{01} * m_{10}$.

Definition at line 1143 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.14 mat2D_det_2x2_mat_minor()

```
double mat2D_det_2x2_mat_minor (
    Mat2D\_Minor mm )
```

Determinant of a 2x2 minor.

Parameters

| | |
|-----------|----------------------|
| <i>mm</i> | Minor (must be 2x2). |
|-----------|----------------------|

Returns

$\det(mm)$.

Definition at line 1582 of file [Matrix2D.h](#).

References [Mat2D_Minor::cols](#), [MAT2D_ASSERT](#), [MAT2D_MINOR_AT](#), and [Mat2D_Minor::rows](#).

Referenced by [mat2D_det\(\)](#), and [mat2D_minor_det\(\)](#).

4.1.3.15 mat2D_dot()

```
void mat2D_dot (
    Mat2D dst,
    Mat2D a,
    Mat2D b )
```

Matrix product: $\text{dst} = a * b$.

Parameters

| | |
|------------|--|
| <i>dst</i> | Destination matrix (size a.rows x b.cols). |
| <i>a</i> | Left matrix (size a.rows x a.cols). |
| <i>b</i> | Right matrix (size a.cols x b.cols). |

Precondition

$a.\text{cols} == b.\text{rows}$
 $\text{dst}.\text{rows} == a.\text{rows}$
 $\text{dst}.\text{cols} == b.\text{cols}$

Postcondition

dst is fully overwritten.

Warning

dst must not alias a or b (overlap is not handled).

Definition at line 515 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D_set_DCM_zyx\(\)](#), and [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.16 mat2D_dot_product()

```
double mat2D_dot_product (
    Mat2D a,
    Mat2D b )
```

Dot product between two vectors.

Parameters

| | |
|----------|--------------------------------|
| <i>a</i> | Vector (shape n x 1 or 1 x n). |
| <i>b</i> | Vector (same shape as a). |

Returns

The scalar dot product sum.

Precondition

a.rows == b.rows and a.cols == b.cols
 (a.cols == 1 && b.cols == 1) || (a.rows == 1 && b.rows == 1)

Definition at line 544 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.17 mat2D_fill()

```
void mat2D_fill (
    Mat2D m,
    double x )
```

Fill all elements of a matrix of doubles with a scalar value.

Parameters

| | |
|----------|-----------------------------------|
| <i>m</i> | Matrix to fill. |
| <i>x</i> | Value to assign to every element. |

Definition at line 443 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), and [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.18 mat2D_fill_sequence()

```
void mat2D_fill_sequence (
    Mat2D m,
    double start,
    double step )
```

Fill a matrix with an arithmetic sequence laid out in row-major order.

Parameters

| | |
|--------------|---|
| <i>m</i> | Matrix to fill. |
| <i>start</i> | First value in the sequence. |
| <i>step</i> | Increment between consecutive elements. |

Element at linear index k gets value $\text{start} + \text{step} * k$.

Definition at line 459 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), [mat2D_offset2d\(\)](#), and [Mat2D::rows](#).

4.1.3.19 mat2D_fill_uint32()

```
void mat2D_fill_uint32 (
    Mat2D_uint32 m,
    uint32_t x )
```

Fill all elements of a matrix of `uint32_t` with a scalar value.

Parameters

| | |
|----------|-----------------------------------|
| <i>m</i> | Matrix to fill. |
| <i>x</i> | Value to assign to every element. |

Definition at line 472 of file [Matrix2D.h](#).

References [Mat2D_uint32::cols](#), [MAT2D_AT_UINT32](#), and [Mat2D_uint32::rows](#).

4.1.3.20 mat2D_free()

```
void mat2D_free (
    Mat2D m )
```

Free the buffer owned by a [Mat2D](#).

Parameters

| | |
|----------|--|
| <i>m</i> | Matrix whose elements were allocated via <code>MAT2D_MALLOC</code> . |
|----------|--|

Note

This does not modify `m` (it is passed by value).

It is safe to call with `m.elements == NULL`.

Definition at line 388 of file [Matrix2D.h](#).

References [Mat2D::elements](#), and [MAT2D_FREE](#).

Referenced by [main\(\)](#), [mat2D_det\(\)](#), [mat2D_invert\(\)](#), [mat2D_set_DCM_zyx\(\)](#), and [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.21 mat2D_free_uint32()

```
void mat2D_free_uint32 (
    Mat2D_uint32 m )
```

Free the buffer owned by a [Mat2D_uint32](#).

Parameters

| | |
|----------|--|
| <i>m</i> | Matrix whose elements were allocated via MAT2D_MALLOC. |
|----------|--|

Note

This does not modify *m* (it is passed by value).

It is safe to call with *m.elements* == NULL.

Definition at line 401 of file [Matrix2D.h](#).

References [Mat2D_uint32::elements](#), and [MAT2D_FREE](#).

4.1.3.22 mat2D_get_col()

```
void mat2D_get_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Copy a column from *src* into a column of *des*.

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same row count as <i>src</i>). |
| <i>des_col</i> | Column index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_col</i> | Column index in source. |

Precondition

des.rows == *src.rows*

des_col < *des.cols* and *src_col* < *src.cols*

Definition at line 932 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.23 mat2D_get_row()

```
void mat2D_get_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

Copy a row from src into a row of des.

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same number of columns as src). |
| <i>des_row</i> | Row index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_row</i> | Row index in source. |

Precondition

`des.cols == src.cols`

Definition at line 1011 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.24 mat2D_invert()

```
void mat2D_invert (
    Mat2D des,
    Mat2D src )
```

Invert a square matrix using Gauss-Jordan elimination.

Parameters

| | |
|------------|---|
| <i>des</i> | Destination matrix (same shape as src). |
| <i>src</i> | Source square matrix. |

Precondition

`src` is square.

`des` is allocated as the same shape as `src`.

On singular matrices (`det == 0`), prints an error message, writes all zeros into `des`, and returns.

Warning

This implementation performs limited pivoting (only when a pivot is “near zero” per `MAT2D_EPS`). It may be unstable for ill-conditioned matrices.

This routine computes `det(src)` first, which performs an additional elimination pass and can amplify numerical issues.

Definition at line 1353 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [mat2D_alloc\(\)](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), [mat2D_copy\(\)](#), [mat2D_det\(\)](#), [mat2D_fill\(\)](#), [mat2D_free\(\)](#), [MAT2D_IS_ZERO](#), [mat2D_mult_row\(\)](#), [mat2D_set_identity\(\)](#), [mat2D_sub_row_time_factor_to_row\(\)](#), [mat2D_swap_rows\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.25 mat2D_LUP_decomposition_with_swap()

```
void mat2D_LUP_decomposition_with_swap (
    Mat2D src,
    Mat2D l,
    Mat2D p,
    Mat2D u )
```

Compute LUP decomposition: $P \cdot A = L \cdot U$ with L unit diagonal.

Parameters

| | |
|------------|---|
| <i>src</i> | Input matrix A (not modified by this function). |
| <i>l</i> | Output lower-triangular-like matrix (intended to have unit diagonal). |
| <i>p</i> | Output permutation matrix. |
| <i>u</i> | Output upper-triangular-like matrix. |

Precondition

`src` is square.

`l`, `p`, `u` are allocated with the same shape as `src`.

Warning

Pivoting is limited: a row swap is performed only when the pivot is “near zero” ([MAT2D_IS_ZERO\(\)](#)).

This routine swaps rows of L during decomposition; for a standard LUP implementation, care is required when swapping partially-built L.

Definition at line 1278 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), [mat2D_copy\(\)](#), [mat2D_fill\(\)](#), [MAT2D_IS_ZERO](#), [mat2D_set_identity\(\)](#), [mat2D_sub_row_time_factor_to_row\(\)](#), [mat2D_swap_rows\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D_solve_linear_sys_LUP_decomposition\(\)](#).

4.1.3.26 mat2D_make_identity()

```
double mat2D_make_identity (
    Mat2D m )
```

Reduce a matrix to identity using Gauss-Jordan style elimination.

Parameters

| | |
|----------|---------------------------|
| <i>m</i> | Matrix modified in-place. |
|----------|---------------------------|

Returns

A multiplicative factor that tracks the effect of row swaps and row scalings performed inside this routine (useful when relating the transformation to determinants).

Internally calls [mat2D_upper_triangulate\(\)](#) and then performs backward elimination and row scaling to reach identity (if the matrix is nonsingular and pivots are usable).

Warning

No full pivoting is performed. Ill-conditioned matrices may produce poor results or floating-point exceptions.

Definition at line [754](#) of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), [mat2D_mult_row\(\)](#), [mat2D_sub_row_time_factor_to_row\(\)](#), [mat2D_upper_triangulate\(\)](#), and [Mat2D::rows](#).

4.1.3.27 mat2D_mat_is_all_digit()

```
bool mat2D_mat_is_all_digit (
    Mat2D m,
    double digit )
```

Check if all elements of a matrix equal a given digit.

Parameters

| | |
|--------------|-------------------|
| <i>m</i> | Matrix. |
| <i>digit</i> | Value to compare. |

Returns

true if every element equals digit, false otherwise.

Warning

Uses exact floating-point equality.

Definition at line 1088 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.28 mat2D_minor_alloc_fill_from_mat()

```
Mat2D_Minor mat2D_minor_alloc_fill_from_mat (
    Mat2D ref_mat,
    size_t i,
    size_t j )
```

Allocate a minor view by excluding row *i* and column *j* of *ref_mat*.

Parameters

| | |
|----------------|---|
| <i>ref_mat</i> | Reference square matrix. |
| <i>i</i> | Excluded row index in <i>ref_mat</i> . |
| <i>j</i> | Excluded column index in <i>ref_mat</i> . |

Returns

A [Mat2D_Minor](#) that references *ref_mat*.

Note

The returned minor owns *rows_list* and *cols_list* and must be released with [mat2D_minor_free\(\)](#).

The returned minor does not own *ref_mat.elements*.

Definition at line 1475 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D_Minor::cols](#), [Mat2D_Minor::cols_list](#), [MAT2D_ASSERT](#), [MAT2D_MALLOC](#), [Mat2D_Minor::ref_mat](#), [Mat2D::rows](#), [Mat2D_Minor::rows](#), [Mat2D_Minor::rows_list](#), and [Mat2D_Minor::stride_r](#).

Referenced by [mat2D_det\(\)](#).

4.1.3.29 mat2D_minor_alloc_fill_from_mat_minor()

```
Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor (
    Mat2D_Minor ref_mm,
    size_t i,
    size_t j )
```

Allocate a nested minor view from an existing minor by excluding row *i* and column *j* of the minor.

Parameters

| | |
|---------------|-------------------------------------|
| <i>ref_mm</i> | Reference minor. |
| <i>i</i> | Excluded row index in the minor. |
| <i>j</i> | Excluded column index in the minor. |

Returns

A new [Mat2D_Minor](#) that references the same underlying matrix.

Note

The returned minor owns `rows_list` and `cols_list` and must be released with [mat2D_minor_free\(\)](#).

The returned minor does not own the underlying reference matrix data.

Definition at line 1517 of file [Matrix2D.h](#).

References [Mat2D_Minor::cols](#), [Mat2D_Minor::cols_list](#), [MAT2D_ASSERT](#), [MAT2D_MALLOC](#), [Mat2D_Minor::ref_mat](#), [Mat2D_Minor::rows](#), [Mat2D_Minor::rows_list](#), and [Mat2D_Minor::stride_r](#).

Referenced by [mat2D_minor_det\(\)](#).

4.1.3.30 mat2D_minor_det()

```
double mat2D_minor_det (
    Mat2D\_Minor mm )
```

Determinant of a minor via recursive expansion by minors.

Parameters

| | |
|-----------|---------------|
| <i>mm</i> | Square minor. |
|-----------|---------------|

Returns

`det(mm)`.

Warning

Exponential complexity (factorial). Intended for educational or very small matrices only.

Definition at line 1595 of file [Matrix2D.h](#).

References [Mat2D_Minor::cols](#), [MAT2D_ASSERT](#), [mat2D_det_2x2_mat_minor\(\)](#), [mat2D_minor_alloc_fill_from_mat_minor\(\)](#), [MAT2D_MINOR_AT](#), [mat2D_minor_free\(\)](#), and [Mat2D_Minor::rows](#).

Referenced by [mat2D_det\(\)](#).

4.1.3.31 `mat2D_minor_free()`

```
void mat2D_minor_free (
    Mat2D_Minor mm )
```

Free the index arrays owned by a minor.

Parameters

| | |
|-----------|----------------|
| <i>mm</i> | Minor to free. |
|-----------|----------------|

Note

After this call, `mm.rows_list` and `mm.cols_list` are invalid.

Definition at line 1552 of file [Matrix2D.h](#).

References [Mat2D_Minor::cols_list](#), [MAT2D_FREE](#), and [Mat2D_Minor::rows_list](#).

Referenced by [mat2D_det\(\)](#), and [mat2D_minor_det\(\)](#).

4.1.3.32 `mat2D_minor_print()`

```
void mat2D_minor_print (
    Mat2D_Minor mm,
    const char * name,
    size_t padding )
```

Print a minor matrix to stdout with a name and indentation padding.

Parameters

| | |
|----------------|-------------------------|
| <i>mm</i> | Minor to print. |
| <i>name</i> | Label to print. |
| <i>padding</i> | Left padding in spaces. |

Definition at line 1564 of file [Matrix2D.h](#).

References [Mat2D_Minor::cols](#), [MAT2D_MINOR_AT](#), and [Mat2D_Minor::rows](#).

4.1.3.33 `mat2D_mult()`

```
void mat2D_mult (
    Mat2D m,
    double factor )
```

In-place scalar multiplication: `m *= factor`.

Parameters

| | |
|---------------|--------------------|
| <i>m</i> | Matrix. |
| <i>factor</i> | Scalar multiplier. |

Definition at line 657 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.34 mat2D_mult_row()

```
void mat2D_mult_row (
    Mat2D m,
    size_t r,
    double factor )
```

In-place row scaling: row(r) *= factor.

Parameters

| | |
|---------------|--------------------|
| <i>m</i> | Matrix. |
| <i>r</i> | Row index. |
| <i>factor</i> | Scalar multiplier. |

Warning

Indices are not bounds-checked in this routine.

Definition at line 674 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D_AT](#).

Referenced by [mat2D_invert\(\)](#), and [mat2D_make_identity\(\)](#).

4.1.3.35 mat2D_offset2d()

```
size_t mat2D_offset2d (
    Mat2D m,
    size_t i,
    size_t j )
```

Compute the linear offset of element (i, j) in a [Mat2D](#).

Parameters

| | |
|----------|-------------------------|
| <i>m</i> | Matrix. |
| <i>i</i> | Row index (0-based). |
| <i>j</i> | Column index (0-based). |

Returns

The linear offset $i * \text{stride_r} + j$.

Precondition

$0 \leq i < \text{m.rows}$ and $0 \leq j < \text{m.cols}$ (checked by `MAT2D_ASSERT`).

Definition at line 416 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [Mat2D::rows](#), and [Mat2D::stride_r](#).

Referenced by [mat2D_fill_sequence\(\)](#).

4.1.3.36 mat2D_offset2d_uint32()

```
size_t mat2D_offset2d_uint32 (
    Mat2D_uint32 m,
    size_t i,
    size_t j )
```

Compute the linear offset of element (i, j) in a [Mat2D_uint32](#).

Parameters

| | |
|----------|-------------------------|
| <i>m</i> | Matrix. |
| <i>i</i> | Row index (0-based). |
| <i>j</i> | Column index (0-based). |

Returns

The linear offset $i * \text{stride_r} + j$.

Precondition

$0 \leq i < \text{m.rows}$ and $0 \leq j < \text{m.cols}$ (checked by `MAT2D_ASSERT`).

Definition at line 432 of file [Matrix2D.h](#).

References [Mat2D_uint32::cols](#), [MAT2D_ASSERT](#), [Mat2D_uint32::rows](#), and [Mat2D_uint32::stride_r](#).

4.1.3.37 mat2D_print()

```
void mat2D_print (
    Mat2D m,
    const char * name,
    size_t padding )
```

Print a matrix to stdout with a name and indentation padding.

Parameters

| | |
|----------------|-------------------------|
| <i>m</i> | Matrix to print. |
| <i>name</i> | Label to print. |
| <i>padding</i> | Left padding in spaces. |

Definition at line 687 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.38 mat2D_print_as_col()

```
void mat2D_print_as_col (
    Mat2D m,
    const char * name,
    size_t padding )
```

Print a matrix as a flattened column vector to stdout.

Parameters

| | |
|----------------|---|
| <i>m</i> | Matrix to print (flattened in row-major). |
| <i>name</i> | Label to print. |
| <i>padding</i> | Left padding in spaces. |

Definition at line 706 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [Mat2D::elements](#), and [Mat2D::rows](#).

4.1.3.39 mat2D_rand()

```
void mat2D_rand (
    Mat2D m,
    double low,
    double high )
```

Fill a matrix with pseudo-random doubles in [low, high].

Parameters

| | |
|-------------|--------------------------|
| <i>m</i> | Matrix to fill. |
| <i>low</i> | Lower bound (inclusive). |
| <i>high</i> | Upper bound (inclusive). |

Precondition

$\text{high} > \text{low}$ (not checked here; caller responsibility).

Note

Uses [mat2D_rand_double\(\)](#) ([rand\(\)](#)).

Definition at line [491](#) of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), [mat2D_rand_double\(\)](#), and [Mat2D::rows](#).

Referenced by [main\(\)](#).

4.1.3.40 mat2D_rand_double()

```
double mat2D_rand_double (
    void )
```

Return a pseudo-random double in the range [0, 1].

Uses [rand\(\)](#) / [RAND_MAX](#) from the C standard library.

Note

This RNG is not cryptographically secure and may have weak statistical properties depending on the platform.

Definition at line [327](#) of file [Matrix2D.h](#).

Referenced by [mat2D_rand\(\)](#).

4.1.3.41 mat2D_row_is_all_digit()

```
bool mat2D_row_is_all_digit (
    Mat2D m,
    double digit,
    size_t r )
```

Check if all elements of a row equal a given digit.

Parameters

| | |
|--------------|-------------------|
| <i>m</i> | Matrix. |
| <i>digit</i> | Value to compare. |
| <i>r</i> | Row index. |

Returns

true if every element equals digit, false otherwise.

Warning

Uses exact floating-point equality.

Definition at line 1109 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D_AT](#).

Referenced by [mat2D_det\(\)](#).

4.1.3.42 mat2D_set_DCM_zyx()

```
void mat2D_set_DCM_zyx (
    Mat2D DCM,
    float yaw_deg,
    float pitch_deg,
    float roll_deg )
```

Build a 3x3 direction cosine matrix (DCM) from Z-Y-X Euler angles.

Parameters

| | |
|------------------|------------------------------|
| <i>DCM</i> | 3x3 destination matrix. |
| <i>yaw_deg</i> | Rotation about Z in degrees. |
| <i>pitch_deg</i> | Rotation about Y in degrees. |
| <i>roll_deg</i> | Rotation about X in degrees. |

Computes $DCM = R_x(roll) * R_y(pitch) * R_z(yaw)$.

Note

This routine allocates temporary 3x3 matrices internally.

Definition at line 860 of file [Matrix2D.h](#).

References [mat2D_alloc\(\)](#), [mat2D_dot\(\)](#), [mat2D_free\(\)](#), [mat2D_set_rot_mat_x\(\)](#), [mat2D_set_rot_mat_y\(\)](#), and [mat2D_set_rot_mat_z\(\)](#).

4.1.3.43 mat2D_set_identity()

```
void mat2D_set_identity (
    Mat2D m )
```

Set a square matrix to the identity matrix.

Parameters

| | |
|----------|--------------------------|
| <i>m</i> | Matrix (must be square). |
|----------|--------------------------|

Precondition

`m.rows == m.cols` (checked by `MAT2D_ASSERT`).

Definition at line 722 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

Referenced by [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), [mat2D_set_rot_mat_x\(\)](#), [mat2D_set_rot_mat_y\(\)](#), and [mat2D_set_rot_mat_z\(\)](#).

4.1.3.44 mat2D_set_rot_mat_x()

```
void mat2D_set_rot_mat_x (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the X-axis.

Parameters

| | |
|------------------|-------------------------|
| <i>m</i> | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees. |

The matrix written is: $\begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos(a) & \sin(a) \\ 0 & -\sin(a) & \cos(a) \end{bmatrix}$

Definition at line 789 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), [MAT2D_PI](#), [mat2D_set_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D_set_DCM_zyx\(\)](#).

4.1.3.45 mat2D_set_rot_mat_y()

```
void mat2D_set_rot_mat_y (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the Y-axis.

Parameters

| | |
|------------------|-------------------------|
| <i>m</i> | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees. |

The matrix written is: $\begin{bmatrix} \cos(a) & 0 & -\sin(a) \\ 0 & 1 & 0 \\ \sin(a) & 0 & \cos(a) \end{bmatrix}$

Definition at line 813 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), [MAT2D_PI](#), [mat2D_set_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D_set_DCM_zyx\(\)](#).

4.1.3.46 mat2D_set_rot_mat_z()

```
void mat2D_set_rot_mat_z (
    Mat2D m,
    float angle_deg )
```

Set a 3x3 rotation matrix for rotation about the Z-axis.

Parameters

| | |
|------------------|-------------------------|
| <i>m</i> | 3x3 destination matrix. |
| <i>angle_deg</i> | Angle in degrees. |

The matrix written is: $\begin{bmatrix} \cos(a) & \sin(a) & 0 \\ -\sin(a) & \cos(a) & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Definition at line 837 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), [MAT2D_PI](#), [mat2D_set_identity\(\)](#), and [Mat2D::rows](#).

Referenced by [mat2D_set_DCM_zyx\(\)](#).

4.1.3.47 mat2D_solve_linear_sys_LUP_decomposition()

```
void mat2D_solve_linear_sys_LUP_decomposition (
    Mat2D A,
    Mat2D x,
    Mat2D B )
```

Solve the linear system $Ax = B$ using an LUP-based approach.

Parameters

| | |
|----------|--|
| <i>A</i> | Coefficient matrix (N x N). |
| <i>x</i> | Solution vector (N x 1). Written on success. |
| <i>B</i> | Right-hand side vector (N x 1). |

This routine computes an LUP decomposition and then forms explicit inverses of L and U ($\text{inv}(L)$, $\text{inv}(U)$) to compute: $x = \text{inv}(U) * \text{inv}(L) * (P * B)$

Warning

Explicitly inverting L and U is typically less stable and slower than forward/back substitution. Prefer substitution for production-quality solvers.

Definition at line 1429 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [mat2D_alloc\(\)](#), [MAT2D_ASSERT](#), [mat2D_dot\(\)](#), [mat2D_fill\(\)](#), [mat2D_free\(\)](#), [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), and [Mat2D::rows](#).

4.1.3.48 mat2D_sub()

```
void mat2D_sub (
    Mat2D dst,
    Mat2D a )
```

In-place subtraction: `dst -= a`.

Parameters

| | |
|------------|--|
| <i>dst</i> | Destination matrix to be decremented. |
| <i>a</i> | Subtrahend of same shape as <i>dst</i> . |

Precondition

dst and *a* have identical shape.

Definition at line 625 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.49 mat2D_sub_col_to_col()

```
void mat2D_sub_col_to_col (
    Mat2D des,
    size_t des_col,
    Mat2D src,
    size_t src_col )
```

Subtract a source column from a destination column.

Performs: `des[:, des_col] -= src[:, src_col]`

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same row count as <i>src</i>). |
| <i>des_col</i> | Column index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_col</i> | Column index in source. |

Definition at line 974 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.50 mat2D_sub_row_time_factor_to_row()

```
void mat2D_sub_row_time_factor_to_row (
    Mat2D m,
    size_t des_r,
    size_t src_r,
    double factor )
```

Row operation: $\text{row}(\text{des_r}) -= \text{factor} * \text{row}(\text{src_r})$.

Parameters

| | |
|-------------------------------------|------------------------|
| <i>m</i> | Matrix. |
| <i>des_↔</i> <i>_r</i> | Destination row index. |
| <i>src_↔</i> <i>_r</i> | Source row index. |
| <i>factor</i> | Scalar multiplier. |

Warning

Indices are not bounds-checked in this routine.

Definition at line 645 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D_AT](#).

Referenced by [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), [mat2D_make_identity\(\)](#), and [mat2D_upper_triangulate\(\)](#).

4.1.3.51 mat2D_sub_row_to_row()

```
void mat2D_sub_row_to_row (
    Mat2D des,
    size_t des_row,
    Mat2D src,
    size_t src_row )
```

Subtract a source row from a destination row.

Performs: $\text{des}[\text{des_row}, :] -= \text{src}[\text{src_row}, :]$

Parameters

| | |
|----------------|---|
| <i>des</i> | Destination matrix (same number of columns as src). |
| <i>des_row</i> | Row index in destination. |
| <i>src</i> | Source matrix. |
| <i>src_row</i> | Row index in source. |

Definition at line 1052 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.52 mat2D_swap_rows()

```
void mat2D_swap_rows (
    Mat2D m,
    size_t r1,
    size_t r2 )
```

Swap two rows of a matrix in-place.

Parameters

| | |
|-----------|-------------------|
| <i>m</i> | Matrix. |
| <i>r1</i> | First row index. |
| <i>r2</i> | Second row index. |

Warning

Row indices are not bounds-checked in this routine.

Definition at line 993 of file [Matrix2D.h](#).

References [Mat2D::cols](#), and [MAT2D_AT](#).

Referenced by [mat2D_invert\(\)](#), [mat2D_LUP_decomposition_with_swap\(\)](#), and [mat2D_upper_triangulate\(\)](#).

4.1.3.53 mat2D_transpose()

```
void mat2D_transpose (
    Mat2D des,
    Mat2D src )
```

Transpose a matrix: $des = src^T$.

Parameters

| | |
|------------|--|
| <i>des</i> | Destination matrix (shape <code>src.cols</code> x <code>src.rows</code>). |
| <i>src</i> | Source matrix. |

Warning

If `des` aliases `src`, results are undefined (no in-place transpose).

Definition at line 1322 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_ASSERT](#), [MAT2D_AT](#), and [Mat2D::rows](#).

4.1.3.54 mat2D_upper_triangulate()

```
double mat2D_upper_triangulate (
    Mat2D m )
```

Forward elimination to transform a matrix to upper triangular form.

Parameters

| | |
|----------|------------------------------|
| <i>m</i> | Matrix transformed in-place. |
|----------|------------------------------|

Returns

Product of row scaling factors (currently 1 in this implementation).

Note

Used as part of determinant computation via triangularization.

Warning

Not robust for linearly dependent rows or tiny pivots.

Returns

A factor tracking the effect of row swaps on the determinant. Currently this is ± 1 depending on the number of row swaps performed.

This routine performs Gaussian elimination using row operations of the form: $\text{row}_j = \text{row}_j - (m[j,i] / m[i,i]) * \text{row}_i$ which do not change the determinant. Row swaps flip the determinant sign and are tracked by the returned factor.

Warning

Pivoting is limited: a row swap is attempted only when the pivot is “near zero” per [MAT2D_IS_ZERO\(\)](#). No full pivoting is used.

Definition at line 1168 of file [Matrix2D.h](#).

References [Mat2D::cols](#), [MAT2D_AT](#), [MAT2D_IS_ZERO](#), [mat2D_sub_row_time_factor_to_row\(\)](#), [mat2D_swap_rows\(\)](#), and [Mat2D::rows](#).

Referenced by [main\(\)](#), [mat2D_det\(\)](#), and [mat2D_make_identity\(\)](#).

4.2 Matrix2D.h

```

00001
00057 #ifndef MATRIX2D_H_
00058 #define MATRIX2D_H_
00059
00060 #include <stddef.h>
00061 #include <stdio.h>
00062 #include <stdlib.h>
00063 #include <stdint.h>
00064 #include <stdbool.h>
00065 #include <math.h>
00066
00075 #ifndef MAT2D_MALLOC
00076 #define MAT2D_MALLOC malloc
00077 #endif //MAT2D_MALLOC
00078
00087 #ifndef MAT2D_FREE
00088 #define MAT2D_FREE free
00089 #endif //MAT2D_FREE
00090
00099 #ifndef MAT2D_ASSERT
00100 #include <assert.h>
00101 #define MAT2D_ASSERT assert
00102 #endif //MAT2D_ASSERT
00103
00117 typedef struct {
00118     size_t rows;
00119     size_t cols;
00120     size_t stride_r; /* elements to traverse to reach the next row */
00121     double *elements;
00122 } Mat2D;
00123
00130 typedef struct {
00131     size_t rows;
00132     size_t cols;
00133     size_t stride_r; /* elements to traverse to reach the next row */
00134     uint32_t *elements;
00135 } Mat2D_uint32;
00136
00152 typedef struct {
00153     size_t rows;
00154     size_t cols;
00155     size_t stride_r; /* logical stride for the minor shape (not used for access) */
00156     size_t *rows_list;
00157     size_t *cols_list;
00158     Mat2D ref_mat;
00159 } Mat2D_Minor;
00160
00178 #if 1
00179 #define MAT2D_AT(m, i, j) (m).elements[mat2D_offset2d((m), (i), (j))]
00180 #define MAT2D_AT_UINT32(m, i, j) (m).elements[mat2D_offset2d_uint32((m), (i), (j))]
00181 #else /* use this macro for better performance but no assertion */
00182 #define MAT2D_AT(m, i, j) (m).elements[(i) * (m).stride_r + (j)]
00183 #define MAT2D_AT_UINT32(m, i, j) (m).elements[(i) * (m).stride_r + (j)]
00184 #endif
00185
00186 #ifndef MAT2D_PI
00187 #define MAT2D_PI 3.14159265358979323846
00188 #endif
00189
00190 #ifndef MAT2D_EPS
00191 #define MAT2D_EPS 1e-15
00192 #endif
00193
00201 #define MAT2D_IS_ZERO(x) (fabs(x) < MAT2D_EPS)
00202
00210 #define MAT2D_MINOR_AT(mm, i, j) MAT2D_AT((mm).ref_mat, (mm).rows_list[i], (mm).cols_list[j])
00211
00216 #define MAT2D_PRINT(m) mat2D_print(m, #m, 0)
00217
00222 #define MAT2D_PRINT_AS_COL(m) mat2D_print_as_col(m, #m, 0)
00223
00228 #define MAT2D_MINOR_PRINT(mm) mat2D_minor_print(mm, #mm, 0)
00229
00240 #define mat2D_normalize(m) mat2D_mult((m), 1.0 / mat2D_calc_norma((m)))
00241
00242 double          mat2D_rand_double(void);
00243
00244 Mat2D            mat2D_alloc(size_t rows, size_t cols);
00245 Mat2D_uint32     mat2D_alloc_uint32(size_t rows, size_t cols);
00246 void             mat2D_free(Mat2D m);
00247 void             mat2D_free_uint32(Mat2D_uint32 m);
00248 size_t           mat2D_offset2d(Mat2D m, size_t i, size_t j);
00249 size_t           mat2D_offset2d_uint32(Mat2D_uint32 m, size_t i, size_t j);
00250
00251 void             mat2D_fill(Mat2D m, double x);

```

```

00252 void          mat2D_fill_sequence(Mat2D m, double start, double step);
00253 void          mat2D_fill_uint32(Mat2D_uint32 m, uint32_t x);
00254 void          mat2D_rand(Mat2D m, double low, double high);
00255
00256 void          mat2D_dot(Mat2D dst, Mat2D a, Mat2D b);
00257 double        mat2D_dot_product(Mat2D a, Mat2D b);
00258 void          mat2D_cross(Mat2D dst, Mat2D a, Mat2D b);
00259
00260 void          mat2D_add(Mat2D dst, Mat2D a);
00261 void          mat2D_add_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor);
00262
00263 void          mat2D_sub(Mat2D dst, Mat2D a);
00264 void          mat2D_sub_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor);
00265
00266 void          mat2D_mult(Mat2D m, double factor);
00267 void          mat2D_mult_row(Mat2D m, size_t r, double factor);
00268
00269 void          mat2D_print(Mat2D m, const char *name, size_t padding);
00270 void          mat2D_print_as_col(Mat2D m, const char *name, size_t padding);
00271
00272 void          mat2D_set_identity(Mat2D m);
00273 double        mat2D_make_identity(Mat2D m);
00274 void          mat2D_set_rot_mat_x(Mat2D m, float angle_deg);
00275 void          mat2D_set_rot_mat_y(Mat2D m, float angle_deg);
00276 void          mat2D_set_rot_mat_z(Mat2D m, float angle_deg);
00277 void          mat2D_set_DCM_zyx(Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg);
00278
00279 void          mat2D_copy(Mat2D des, Mat2D src);
00280 void          mat2D_copy_mat_to_mat_at_window(Mat2D des, Mat2D src, size_t is, size_t js, size_t ie,
    size_t je);
00281
00282 void          mat2D_get_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00283 void          mat2D_add_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00284 void          mat2D_sub_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col);
00285
00286 void          mat2D_swap_rows(Mat2D m, size_t r1, size_t r2);
00287 void          mat2D_get_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00288 void          mat2D_add_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00289 void          mat2D_sub_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row);
00290
00291 double        mat2D_calc_norma(Mat2D m);
00292
00293 bool          mat2D_mat_is_all_digit(Mat2D m, double digit);
00294 bool          mat2D_row_is_all_digit(Mat2D m, double digit, size_t r);
00295 bool          mat2D_col_is_all_digit(Mat2D m, double digit, size_t c);
00296
00297 double        mat2D_det_2x2_mat(Mat2D m);
00298 double        mat2D_upper_triangularize(Mat2D m);
00299 double        mat2D_det(Mat2D m);
00300 void          mat2D_LUP_decomposition_with_swap(Mat2D src, Mat2D l, Mat2D p, Mat2D u);
00301 void          mat2D_transpose(Mat2D des, Mat2D src);
00302 void          mat2D_invert(Mat2D des, Mat2D src);
00303 void          mat2D_solve_linear_sys_LUP_decomposition(Mat2D A, Mat2D x, Mat2D B);
00304
00305 Mat2D_Minor   mat2D_minor_alloc_fill_from_mat(Mat2D ref_mat, size_t i, size_t j);
00306 Mat2D_Minor   mat2D_minor_alloc_fill_from_mat_minor(Mat2D_Minor ref_mm, size_t i, size_t j);
00307 void          mat2D_minor_free(Mat2D_Minor mm);
00308 void          mat2D_minor_print(Mat2D_Minor mm, const char *name, size_t padding);
00309 double        mat2D_det_2x2_mat_minor(Mat2D_Minor mm);
00310 double        mat2D_minor_det(Mat2D_Minor mm);
00311
00312 #endif // MATRIX2D_H_
00313
00314 #ifndef MATRIX2D_IMPLEMENTATION
00315 #undef MATRIX2D_IMPLEMENTATION
00316
00317
00327 double mat2D_rand_double(void)
00328 {
00329     return (double) rand() / (double) RAND_MAX;
00330 }
00331
00344 Mat2D mat2D_alloc(size_t rows, size_t cols)
00345 {
00346     Mat2D m;
00347     m.rows = rows;
00348     m.cols = cols;
00349     m.stride_r = cols;
00350     m.elements = (double*)MAT2D_MALLOC(sizeof(double)*rows*cols);
00351     MAT2D_ASSERT(m.elements != NULL);
00352
00353     return m;
00354 }
00355
00368 Mat2D_uint32 mat2D_alloc_uint32(size_t rows, size_t cols)
00369 {
00370     Mat2D_uint32 m;

```

```

00371     m.rows = rows;
00372     m.cols = cols;
00373     m.stride_r = cols;
00374     m.elements = (uint32_t*)MAT2D_MALLOC(sizeof(uint32_t)*rows*cols);
00375     MAT2D_ASSERT(m.elements != NULL);
00376
00377     return m;
00378 }
00379
00388 void mat2D_free(Mat2D m)
00389 {
00390     MAT2D_FREE(m.elements);
00391 }
00392
00401 void mat2D_free_uint32(Mat2D_uint32 m)
00402 {
00403     MAT2D_FREE(m.elements);
00404 }
00405
00416 size_t mat2D_offset2d(Mat2D m, size_t i, size_t j)
00417 {
00418     MAT2D_ASSERT(i < m.rows && j < m.cols);
00419     return i * m.stride_r + j;
00420 }
00421
00432 size_t mat2D_offset2d_uint32(Mat2D_uint32 m, size_t i, size_t j)
00433 {
00434     MAT2D_ASSERT(i < m.rows && j < m.cols);
00435     return i * m.stride_r + j;
00436 }
00437
00443 void mat2D_fill(Mat2D m, double x)
00444 {
00445     for (size_t i = 0; i < m.rows; ++i) {
00446         for (size_t j = 0; j < m.cols; ++j) {
00447             MAT2D_AT(m, i, j) = x;
00448         }
00449     }
00450 }
00451
00459 void mat2D_fill_sequence(Mat2D m, double start, double step) {
00460     for (size_t i = 0; i < m.rows; i++) {
00461         for (size_t j = 0; j < m.cols; j++) {
00462             MAT2D_AT(m, i, j) = start + step * mat2D_offset2d(m, i, j);
00463         }
00464     }
00465 }
00466
00472 void mat2D_fill_uint32(Mat2D_uint32 m, uint32_t x)
00473 {
00474     for (size_t i = 0; i < m.rows; ++i) {
00475         for (size_t j = 0; j < m.cols; ++j) {
00476             MAT2D_AT_UINT32(m, i, j) = x;
00477         }
00478     }
00479 }
00480
00491 void mat2D_rand(Mat2D m, double low, double high)
00492 {
00493     for (size_t i = 0; i < m.rows; ++i) {
00494         for (size_t j = 0; j < m.cols; ++j) {
00495             MAT2D_AT(m, i, j) = mat2D_rand_double()*(high - low) + low;
00496         }
00497     }
00498 }
00499
00515 void mat2D_dot(Mat2D dst, Mat2D a, Mat2D b)
00516 {
00517     MAT2D_ASSERT(a.cols == b.rows);
00518     MAT2D_ASSERT(a.rows == dst.rows);
00519     MAT2D_ASSERT(b.cols == dst.cols);
00520
00521     size_t i, j, k;
00522
00523     for (i = 0; i < dst.rows; i++) {
00524         for (j = 0; j < dst.cols; j++) {
00525             MAT2D_AT(dst, i, j) = 0;
00526             for (k = 0; k < a.cols; k++) {
00527                 MAT2D_AT(dst, i, j) += MAT2D_AT(a, i, k)*MAT2D_AT(b, k, j);
00528             }
00529         }
00530     }
00531
00532 }
00533
00544 double mat2D_dot_product(Mat2D a, Mat2D b)
00545 {

```



```

00546     MAT2D_ASSERT(a.rows == b.rows);
00547     MAT2D_ASSERT(a.cols == b.cols);
00548     MAT2D_ASSERT((1 == a.cols && 1 == b.cols) || (1 == a.rows && 1 == b.rows));
00549
00550     double dot_product = 0;
00551
00552     if (1 == a.cols) {
00553         for (size_t i = 0; i < a.rows; i++) {
00554             dot_product += MAT2D_AT(a, i, 0) * MAT2D_AT(b, i, 0);
00555         }
00556     } else {
00557         for (size_t j = 0; j < a.cols; j++) {
00558             dot_product += MAT2D_AT(a, 0, j) * MAT2D_AT(b, 0, j);
00559         }
00560     }
00561
00562     return dot_product;
00563 }
00564
00572 void mat2D_cross(Mat2D dst, Mat2D a, Mat2D b)
00573 {
00574     MAT2D_ASSERT(3 == dst.rows && 1 == dst.cols);
00575     MAT2D_ASSERT(3 == a.rows && 1 == a.cols);
00576     MAT2D_ASSERT(3 == b.rows && 1 == b.cols);
00577
00578     MAT2D_AT(dst, 0, 0) = MAT2D_AT(a, 1, 0) * MAT2D_AT(b, 2, 0) - MAT2D_AT(a, 2, 0) * MAT2D_AT(b, 1,
00579 0);
00579     MAT2D_AT(dst, 1, 0) = MAT2D_AT(a, 2, 0) * MAT2D_AT(b, 0, 0) - MAT2D_AT(a, 0, 0) * MAT2D_AT(b, 2,
00580 0);
00580     MAT2D_AT(dst, 2, 0) = MAT2D_AT(a, 0, 0) * MAT2D_AT(b, 1, 0) - MAT2D_AT(a, 1, 0) * MAT2D_AT(b, 0,
00581 0);
00581 }
00582
00591 void mat2D_add(Mat2D dst, Mat2D a)
00592 {
00593     MAT2D_ASSERT(dst.rows == a.rows);
00594     MAT2D_ASSERT(dst.cols == a.cols);
00595     for (size_t i = 0; i < dst.rows; ++i) {
00596         for (size_t j = 0; j < dst.cols; ++j) {
00597             MAT2D_AT(dst, i, j) += MAT2D_AT(a, i, j);
00598         }
00599     }
00600 }
00601
00611 void mat2D_add_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor)
00612 {
00613     for (size_t j = 0; j < m.cols; ++j) {
00614         MAT2D_AT(m, des_r, j) += factor * MAT2D_AT(m, src_r, j);
00615     }
00616 }
00617
00625 void mat2D_sub(Mat2D dst, Mat2D a)
00626 {
00627     MAT2D_ASSERT(dst.rows == a.rows);
00628     MAT2D_ASSERT(dst.cols == a.cols);
00629     for (size_t i = 0; i < dst.rows; ++i) {
00630         for (size_t j = 0; j < dst.cols; ++j) {
00631             MAT2D_AT(dst, i, j) -= MAT2D_AT(a, i, j);
00632         }
00633     }
00634 }
00635
00645 void mat2D_sub_row_time_factor_to_row(Mat2D m, size_t des_r, size_t src_r, double factor)
00646 {
00647     for (size_t j = 0; j < m.cols; ++j) {
00648         MAT2D_AT(m, des_r, j) -= factor * MAT2D_AT(m, src_r, j);
00649     }
00650 }
00651
00657 void mat2D_mult(Mat2D m, double factor)
00658 {
00659     for (size_t i = 0; i < m.rows; ++i) {
00660         for (size_t j = 0; j < m.cols; ++j) {
00661             MAT2D_AT(m, i, j) *= factor;
00662         }
00663     }
00664 }
00665
00674 void mat2D_mult_row(Mat2D m, size_t r, double factor)
00675 {
00676     for (size_t j = 0; j < m.cols; ++j) {
00677         MAT2D_AT(m, r, j) *= factor;
00678     }
00679 }
00680
00687 void mat2D_print(Mat2D m, const char *name, size_t padding)
00688 {

```

```

00689     printf("%s%s = [\n", (int) padding, "", name);
00690     for (size_t i = 0; i < m.rows; ++i) {
00691         printf("%s", "", (int) padding, "");
00692         for (size_t j = 0; j < m.cols; ++j) {
00693             printf("%9.6f ", MAT2D_AT(m, i, j));
00694         }
00695         printf("\n");
00696     }
00697     printf("%s]\n", (int) padding, "");
00698 }
00699
00706 void mat2D_print_as_col(Mat2D m, const char *name, size_t padding)
00707 {
00708     printf("%s%s = [\n", (int) padding, "", name);
00709     for (size_t i = 0; i < m.rows*m.cols; ++i) {
00710         printf("%s", "", (int) padding, "");
00711         printf("%f\n", m.elements[i]);
00712     }
00713     printf("%s]\n", (int) padding, "");
00714 }
00715
00722 void mat2D_set_identity(Mat2D m)
00723 {
00724     MAT2D_ASSERT(m.cols == m.rows);
00725     for (size_t i = 0; i < m.rows; ++i) {
00726         for (size_t j = 0; j < m.cols; ++j) {
00727             MAT2D_AT(m, i, j) = i == j ? 1 : 0;
00728             // if (i == j) {
00729             //     MAT2D_AT(m, i, j) = 1;
00730             // }
00731             // else {
00732             //     MAT2D_AT(m, i, j) = 0;
00733             // }
00734         }
00735     }
00736 }
00737
00754 double mat2D_make_identity(Mat2D m)
00755 {
00756     /* make identity matrix using Gauss elimination */
00757     /* preforming Gauss elimination: https://en.wikipedia.org/wiki/Gaussian_elimination */
00758     /* returns the factor multiplying the determinant */
00759
00760     double factor_to_return = mat2D_upper_triangulate(m);
00761
00762     double factor = 1 / MAT2D_AT(m, m.rows-1, m.cols-1);
00763     mat2D_mult_row(m, m.rows-1, factor);
00764     factor_to_return *= factor;
00765     for (size_t c = m.cols-1; c > 0; c--) {
00766         double factor = 1 / MAT2D_AT(m, c, c);
00767         mat2D_mult_row(m, c, factor);
00768         for (int r = c-1; r >= 0; r--) {
00769             mat2D_sub_row_time_factor_to_row(m, r, c, MAT2D_AT(m, r, c));
00770         }
00771     }
00772
00773     return factor_to_return;
00774 }
00775
00776
00789 void mat2D_set_rot_mat_x(Mat2D m, float angle_deg)
00790 {
00791     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);
00792
00793     float angle_rad = angle_deg * MAT2D_PI / 180;
00794     mat2D_set_identity(m);
00795     MAT2D_AT(m, 1, 1) = cos(angle_rad);
00796     MAT2D_AT(m, 1, 2) = sin(angle_rad);
00797     MAT2D_AT(m, 2, 1) = -sin(angle_rad);
00798     MAT2D_AT(m, 2, 2) = cos(angle_rad);
00799 }
00800
00813 void mat2D_set_rot_mat_y(Mat2D m, float angle_deg)
00814 {
00815     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);
00816
00817     float angle_rad = angle_deg * MAT2D_PI / 180;
00818     mat2D_set_identity(m);
00819     MAT2D_AT(m, 0, 0) = cos(angle_rad);
00820     MAT2D_AT(m, 0, 2) = -sin(angle_rad);
00821     MAT2D_AT(m, 2, 0) = sin(angle_rad);
00822     MAT2D_AT(m, 2, 2) = cos(angle_rad);
00823 }
00824
00837 void mat2D_set_rot_mat_z(Mat2D m, float angle_deg)
00838 {
00839     MAT2D_ASSERT(3 == m.cols && 3 == m.rows);

```

```

00840
00841     float angle_rad = angle_deg * MAT2D_PI / 180;
00842     mat2D_set_identity(m);
00843     MAT2D_AT(m, 0, 0) = cos(angle_rad);
00844     MAT2D_AT(m, 0, 1) = sin(angle_rad);
00845     MAT2D_AT(m, 1, 0) = -sin(angle_rad);
00846     MAT2D_AT(m, 1, 1) = cos(angle_rad);
00847 }
00848
00860 void mat2D_set_DCM_zyx(Mat2D DCM, float yaw_deg, float pitch_deg, float roll_deg)
00861 {
00862     Mat2D RotZ = mat2D_alloc(3,3);
00863     mat2D_set_rot_mat_z(RotZ, yaw_deg);
00864     Mat2D RotY = mat2D_alloc(3,3);
00865     mat2D_set_rot_mat_y(RotY, pitch_deg);
00866     Mat2D RotX = mat2D_alloc(3,3);
00867     mat2D_set_rot_mat_x(RotX, roll_deg);
00868     Mat2D temp = mat2D_alloc(3,3);
00869
00870     mat2D_dot(temp, RotY, RotZ);
00871     mat2D_dot(DCM, RotX, temp); /* I have a DCM */
00872
00873     mat2D_free(RotZ);
00874     mat2D_free(RotY);
00875     mat2D_free(RotX);
00876     mat2D_free(temp);
00877 }
00878
00887 void mat2D_copy(Mat2D des, Mat2D src)
00888 {
00889     MAT2D_ASSERT(des.cols == src.cols);
00890     MAT2D_ASSERT(des.rows == src.rows);
00891
00892     for (size_t i = 0; i < des.rows; ++i) {
00893         for (size_t j = 0; j < des.cols; ++j) {
00894             MAT2D_AT(des, i, j) = MAT2D_AT(src, i, j);
00895         }
00896     }
00897 }
00898
00909 void mat2D_copy_mat_to_mat_at_window(Mat2D des, Mat2D src, size_t is, size_t js, size_t ie, size_t je)
00910 {
00911     MAT2D_ASSERT(je >= js && ie >= is);
00912     MAT2D_ASSERT(je-js+1 == des.cols);
00913     MAT2D_ASSERT(ie-is+1 == des.rows);
00914
00915     for (size_t index = 0; index < des.rows; ++index) {
00916         for (size_t jindex = 0; jindex < des.cols; ++jindex) {
00917             MAT2D_AT(des, index, jindex) = MAT2D_AT(src, is+index, js+jindex);
00918         }
00919     }
00920 }
00921
00932 void mat2D_get_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00933 {
00934     MAT2D_ASSERT(src_col < src.cols);
00935     MAT2D_ASSERT(des.rows == src.rows);
00936     MAT2D_ASSERT(des_col < des.cols);
00937
00938     for (size_t i = 0; i < des.rows; ++i) {
00939         MAT2D_AT(des, i, des_col) = MAT2D_AT(src, i, src_col);
00940     }
00941 }
00942
00953 void mat2D_add_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00954 {
00955     MAT2D_ASSERT(src_col < src.cols);
00956     MAT2D_ASSERT(des.rows == src.rows);
00957     MAT2D_ASSERT(des_col < des.cols);
00958
00959     for (size_t i = 0; i < des.rows; ++i) {
00960         MAT2D_AT(des, i, des_col) += MAT2D_AT(src, i, src_col);
00961     }
00962 }
00963
00974 void mat2D_sub_col_to_col(Mat2D des, size_t des_col, Mat2D src, size_t src_col)
00975 {
00976     MAT2D_ASSERT(src_col < src.cols);
00977     MAT2D_ASSERT(des.rows == src.rows);
00978     MAT2D_ASSERT(des_col < des.cols);
00979
00980     for (size_t i = 0; i < des.rows; ++i) {
00981         MAT2D_AT(des, i, des_col) -= MAT2D_AT(src, i, src_col);
00982     }
00983 }
00984
00993 void mat2D_swap_rows(Mat2D m, size_t r1, size_t r2)

```

```

00994 {
00995     for (size_t j = 0; j < m.cols; j++) {
00996         double temp = MAT2D_AT(m, r1, j);
00997         MAT2D_AT(m, r1, j) = MAT2D_AT(m, r2, j);
00998         MAT2D_AT(m, r2, j) = temp;
00999     }
01000 }
01001
01011 void mat2D_get_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01012 {
01013     MAT2D_ASSERT(src_row < src.rows);
01014     MAT2D_ASSERT(des.cols == src.cols);
01015     MAT2D_ASSERT(des_row < des.rows);
01016
01017     for (size_t j = 0; j < des.cols; j++) {
01018         MAT2D_AT(des, des_row, j) = MAT2D_AT(src, src_row, j);
01019     }
01020 }
01021
01031 void mat2D_add_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01032 {
01033     MAT2D_ASSERT(src_row < src.rows);
01034     MAT2D_ASSERT(des.cols == src.cols);
01035     MAT2D_ASSERT(des_row < des.rows);
01036
01037     for (size_t j = 0; j < des.cols; j++) {
01038         MAT2D_AT(des, des_row, j) += MAT2D_AT(src, src_row, j);
01039     }
01040 }
01041
01052 void mat2D_sub_row_to_row(Mat2D des, size_t des_row, Mat2D src, size_t src_row)
01053 {
01054     MAT2D_ASSERT(src_row < src.rows);
01055     MAT2D_ASSERT(des.cols == src.cols);
01056     MAT2D_ASSERT(des_row < des.rows);
01057
01058     for (size_t j = 0; j < des.cols; j++) {
01059         MAT2D_AT(des, des_row, j) -= MAT2D_AT(src, src_row, j);
01060     }
01061 }
01062
01068 double mat2D_calc_norma(Mat2D m)
01069 {
01070     double sum = 0;
01071
01072     for (size_t i = 0; i < m.rows; ++i) {
01073         for (size_t j = 0; j < m.cols; ++j) {
01074             sum += MAT2D_AT(m, i, j) * MAT2D_AT(m, i, j);
01075         }
01076     }
01077     return sqrt(sum);
01078 }
01079
01088 bool mat2D_mat_is_all_digit(Mat2D m, double digit)
01089 {
01090     for (size_t i = 0; i < m.rows; ++i) {
01091         for (size_t j = 0; j < m.cols; ++j) {
01092             if (MAT2D_AT(m, i, j) != digit) {
01093                 return false;
01094             }
01095         }
01096     }
01097     return true;
01098 }
01099
01109 bool mat2D_row_is_all_digit(Mat2D m, double digit, size_t r)
01110 {
01111     for (size_t j = 0; j < m.cols; ++j) {
01112         if (MAT2D_AT(m, r, j) != digit) {
01113             return false;
01114         }
01115     }
01116     return true;
01117 }
01118
01128 bool mat2D_col_is_all_digit(Mat2D m, double digit, size_t c)
01129 {
01130     for (size_t i = 0; i < m.rows; ++i) {
01131         if (MAT2D_AT(m, i, c) != digit) {
01132             return false;
01133         }
01134     }
01135     return true;
01136 }
01137
01143 double mat2D_det_2x2_mat(Mat2D m)
01144 {

```

```

01145     MAT2D_ASSERT(2 == m.cols && 2 == m.rows && "Not a 2x2 matrix");
01146     return MAT2D_AT(m, 0, 0) * MAT2D_AT(m, 1, 1) - MAT2D_AT(m, 0, 1) * MAT2D_AT(m, 1, 0);
01147 }
01148
01168 double mat2D_upper_triangularize(Mat2D m)
01169 {
01170     /* preforming Gauss elimination: https://en.wikipedia.org/wiki/Gaussian_elimination */
01171     /* returns the factor multiplying the determinant */
01172
01173     double factor_to_return = 1;
01174
01175     size_t size = (size_t)fmin(m.rows, m.cols);
01176     for (size_t i = 0; i < size; i++) {
01177         if (MAT2D_IS_ZERO(MAT2D_AT(m, i, i))) { /* swapping only if it is zero */
01178             /* finding biggest first number (absolute value) */
01179             size_t biggest_r = i;
01180             for (size_t index = i; index < m.rows; index++) {
01181                 if (fabs(MAT2D_AT(m, index, i)) > fabs(MAT2D_AT(m, biggest_r, i))) {
01182                     biggest_r = index;
01183                 }
01184             }
01185             if (i != biggest_r) {
01186                 mat2D_swap_rows(m, i, biggest_r);
01187                 factor_to_return *= -1;
01188             }
01189         }
01190         for (size_t j = i+1; j < m.rows; j++) {
01191             double factor = 1 / MAT2D_AT(m, i, i);
01192             if (!isfinite(factor)) {
01193                 printf("%s:%d:\n%s:\n[Error] unable to transform into upper triangular matrix.
01194                 Probably some of the rows are not independent.\n", __FILE__, __LINE__, __func__);
01195             }
01196             double mat_value = MAT2D_AT(m, j, i);
01197             mat2D_sub_row_time_factor_to_row(m, j, i, mat_value * factor);
01198         }
01199     }
01200     return factor_to_return;
01201 }
01215 double mat2D_det(Mat2D m)
01216 {
01217     MAT2D_ASSERT(m.cols == m.rows && "should be a square matrix");
01218
01219     /* checking if there is a row or column with all zeros */
01220     /* checking rows */
01221     for (size_t i = 0; i < m.rows; i++) {
01222         if (mat2D_row_is_all_digit(m, 0, i)) {
01223             return 0;
01224         }
01225     }
01226     /* checking cols */
01227     for (size_t j = 0; j < m.rows; j++) {
01228         if (mat2D_col_is_all_digit(m, 0, j)) {
01229             return 0;
01230         }
01231     }
01232
01233     #if 0/* This is an implementation of naive determinant calculation using minors. This is too slow
01234     */
01235     double det = 0;
01236     /* TODO: finding best row or col? */
01237     for (size_t i = 0, j = 0; i < m.rows; i++) { /* first column */
01238         if (MAT2D_AT(m, i, j) < 1e-10) continue;
01239         Mat2D_Minor sub_mm = mat2D_minor_alloc_fill_from_mat(m, i, j);
01240         int factor = (i+j)%2 ? -1 : 1;
01241         if (sub_mm.cols != 2) {
01242             MAT2D_ASSERT(sub_mm.cols == sub_mm.rows && "should be a square matrix");
01243             det += MAT2D_AT(m, i, j) * (factor) * mat2D_minor_det(sub_mm);
01244         } else if (sub_mm.cols == 2 && sub_mm.rows == 2) {
01245             det += MAT2D_AT(m, i, j) * (factor) * mat2D_det_2x2_mat_minor(sub_mm);
01246         }
01247         mat2D_minor_free(sub_mm);
01248     }
01249     #endif
01250     Mat2D temp_m = mat2D_alloc(m.rows, m.cols);
01251     mat2D_copy(temp_m, m);
01252     double factor = mat2D_upper_triangularize(temp_m);
01253     double diag_mul = 1;
01254     for (size_t i = 0; i < temp_m.rows; i++) {
01255         diag_mul *= MAT2D_AT(temp_m, i, i);
01256     }
01257     mat2D_free(temp_m);
01258     return diag_mul / factor;
01259 }
01260 }
01261

```

```

01278 void mat2D_LUP_decomposition_with_swap(Mat2D src, Mat2D l, Mat2D p, Mat2D u)
01279 {
01280     /* performing LU decomposition Following the Wikipedia page:
01281     https://en.wikipedia.org/wiki/LU_decomposition */
01282     mat2D_copy(u, src);
01283     mat2D_set_identity(p);
01284     mat2D_fill(l, 0);
01285
01286     for (size_t i = 0; i < (size_t)fmin(u.rows-1, u.cols); i++) {
01287         if (MAT2D_IS_ZERO(MAT2D_AT(u, i, i))) { /* swapping only if it is zero */
01288             /* finding biggest first number (absolute value) */
01289             size_t biggest_r = i;
01290             for (size_t index = i; index < u.rows; index++) {
01291                 if (fabs(MAT2D_AT(u, index, i)) > fabs(MAT2D_AT(u, biggest_r, i))) {
01292                     biggest_r = index;
01293                 }
01294             }
01295             if (i != biggest_r) {
01296                 mat2D_swap_rows(u, i, biggest_r);
01297                 mat2D_swap_rows(p, i, biggest_r);
01298                 mat2D_swap_rows(l, i, biggest_r);
01299             }
01300             for (size_t j = i+1; j < u.cols; j++) {
01301                 double factor = 1 / MAT2D_AT(u, i, i);
01302                 if (!isfinite(factor)) {
01303                     printf("%s:%d:\n%s:\n[Error] unable to transform into upper triangular matrix. Probably
01304 some of the rows are not independent.\n", __FILE__, __LINE__, __func__);
01305                 }
01306                 double mat_value = MAT2D_AT(u, j, i);
01307                 mat2D_sub_row_time_factor_to_row(u, j, i, mat_value * factor);
01308                 MAT2D_AT(l, j, i) = mat_value * factor;
01309             }
01310             MAT2D_AT(l, i, i) = 1;
01311         }
01312         MAT2D_AT(l, l.rows-1, l.cols-1) = 1;
01313     }
01314 }
01322 void mat2D_transpose(Mat2D des, Mat2D src)
01323 {
01324     MAT2D_ASSERT(des.cols == src.rows);
01325     MAT2D_ASSERT(des.rows == src.cols);
01326
01327     for (size_t index = 0; index < des.rows; ++index) {
01328         for (size_t jindex = 0; jindex < des.cols; ++jindex) {
01329             MAT2D_AT(des, index, jindex) = MAT2D_AT(src, jindex, index);
01330         }
01331     }
01332 }
01333
01353 void mat2D_invert(Mat2D des, Mat2D src)
01354 {
01355     MAT2D_ASSERT(src.cols == src.rows && "should be an NxN matrix");
01356     MAT2D_ASSERT(des.cols == src.cols && des.rows == des.cols);
01357
01358     Mat2D m = mat2D_alloc(src.rows, src.cols);
01359     mat2D_copy(m, src);
01360
01361     mat2D_set_identity(des);
01362
01363     if (!mat2D_det(m)) {
01364         mat2D_fill(des, 0);
01365         printf("%s:%d:\n%s:\n[Error] Can't invert the matrix. Determinant is zero! Set the inverse
01366 matrix to all zeros\n", __FILE__, __LINE__, __func__);
01367         mat2D_free(m);
01368         return;
01369     }
01370
01371     size_t size = (size_t)fmin(m.rows, m.cols);
01372     for (size_t i = 0; i < size; i++) {
01373         if (MAT2D_IS_ZERO(MAT2D_AT(m, i, i))) { /* swapping only if it is zero */
01374             /* finding biggest first number (absolute value) */
01375             size_t biggest_r = i;
01376             for (size_t index = i; index < m.rows; index++) {
01377                 if (fabs(MAT2D_AT(m, index, i)) > fabs(MAT2D_AT(m, biggest_r, i))) {
01378                     biggest_r = index;
01379                 }
01380             }
01381             if (i != biggest_r) {
01382                 mat2D_swap_rows(m, i, biggest_r);
01383                 mat2D_swap_rows(des, i, biggest_r);
01384                 printf("%s:%d:\n%s:\n[INFO] swapping row %zu with row %zu.\n", __FILE__, __LINE__,
01385 __func__, i, biggest_r);
01386             } else {
01387                 MAT2D_ASSERT(0 && "can't inverse");
01388             }
01389         }
01390     }

```

```

01387     }
01388     for (size_t j = i+1; j < size; j++) {
01389         double factor = 1 / MAT2D_AT(m, i, i);
01390         double mat_value = MAT2D_AT(m, j, i);
01391         mat2D_sub_row_time_factor_to_row(m, j, i, mat_value * factor);
01392
01393         mat2D_sub_row_time_factor_to_row(des, j, i, mat_value * factor);
01394     }
01395 }
01396 double factor = 1 / MAT2D_AT(m, m.rows-1, m.cols-1);
01397 mat2D_mult_row(m, m.rows-1, factor);
01398 mat2D_mult_row(des, des.rows-1, factor);
01399 for (size_t c = m.cols-1; c > 0; c--) {
01400     double factor = 1 / MAT2D_AT(m, c, c);
01401     mat2D_mult_row(m, c, factor);
01402     mat2D_mult_row(des, c, factor);
01403     for (int r = c-1; r >= 0; r--) {
01404         double mat_value = MAT2D_AT(m, r, c);
01405         mat2D_sub_row_time_factor_to_row(m, r, c, mat_value);
01406         mat2D_sub_row_time_factor_to_row(des, r, c, mat_value);
01407     }
01408 }
01409
01410 mat2D_free(m);
01411 }
01412
01429 void mat2D_solve_linear_sys_LUP_decomposition(Mat2D A, Mat2D x, Mat2D B)
01430 {
01431     MAT2D_ASSERT(A.cols == x.rows);
01432     MAT2D_ASSERT(1 == x.cols);
01433     MAT2D_ASSERT(A.rows == B.rows);
01434     MAT2D_ASSERT(1 == B.cols);
01435
01436     Mat2D y = mat2D_alloc(x.rows, x.cols);
01437     Mat2D l = mat2D_alloc(A.rows, A.cols);
01438     Mat2D p = mat2D_alloc(A.rows, A.cols);
01439     Mat2D u = mat2D_alloc(A.rows, A.cols);
01440     Mat2D inv_l = mat2D_alloc(l.rows, l.cols);
01441     Mat2D inv_u = mat2D_alloc(u.rows, u.cols);
01442
01443     mat2D_LUP_decomposition_with_swap(A, l, p, u);
01444
01445     mat2D_invert(inv_l, l);
01446     mat2D_invert(inv_u, u);
01447
01448     mat2D_fill(x, 0); /* x here is only a temp mat*/
01449     mat2D_fill(y, 0);
01450     mat2D_dot(x, p, B);
01451     mat2D_dot(y, inv_l, x);
01452
01453     mat2D_fill(x, 0);
01454     mat2D_dot(x, inv_u, y);
01455
01456     mat2D_free(y);
01457     mat2D_free(l);
01458     mat2D_free(p);
01459     mat2D_free(u);
01460     mat2D_free(inv_l);
01461     mat2D_free(inv_u);
01462 }
01463
01475 Mat2D_Minor mat2D_minor_alloc_fill_from_mat(Mat2D ref_mat, size_t i, size_t j)
01476 {
01477     MAT2D_ASSERT(ref_mat.cols == ref_mat.rows && "minor is defined only for square matrix");
01478
01479     Mat2D_Minor mm;
01480     mm.cols = ref_mat.cols-1;
01481     mm.rows = ref_mat.rows-1;
01482     mm.stride_r = ref_mat.cols-1;
01483     mm.cols_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mat.cols-1));
01484     mm.rows_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mat.rows-1));
01485     mm.ref_mat = ref_mat;
01486
01487     MAT2D_ASSERT(mm.cols_list != NULL && mm.rows_list != NULL);
01488
01489     for (size_t index = 0, temp_index = 0; index < ref_mat.rows; index++) {
01490         if (index != i) {
01491             mm.rows_list[temp_index] = index;
01492             temp_index++;
01493         }
01494     }
01495     for (size_t jindex = 0, temp_jindex = 0; jindex < ref_mat.cols; jindex++) {
01496         if (jindex != j) {
01497             mm.cols_list[temp_jindex] = jindex;
01498             temp_jindex++;
01499         }
01500     }

```

```

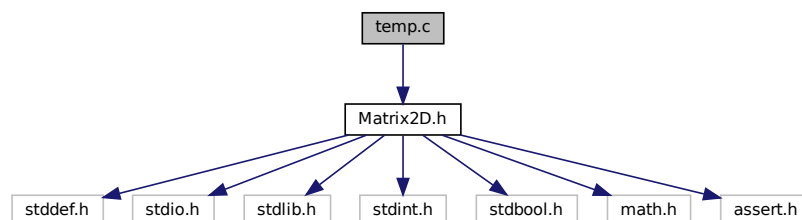
01501
01502     return mm;
01503 }
01504
01517 Mat2D_Minor mat2D_minor_alloc_fill_from_mat_minor(Mat2D_Minor ref_mm, size_t i, size_t j)
01518 {
01519     MAT2D_ASSERT(ref_mm.cols == ref_mm.rows && "minor is defined only for square matrix");
01520
01521     Mat2D_Minor mm;
01522     mm.cols = ref_mm.cols-1;
01523     mm.rows = ref_mm.rows-1;
01524     mm.stride_r = ref_mm.cols-1;
01525     mm.cols_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mm.cols-1));
01526     mm.rows_list = (size_t*)MAT2D_MALLOC(sizeof(size_t)*(ref_mm.rows-1));
01527     mm.ref_mat = ref_mm.ref_mat;
01528
01529     MAT2D_ASSERT(mm.cols_list != NULL && mm.rows_list != NULL);
01530
01531     for (size_t index = 0, temp_index = 0; index < ref_mm.rows; index++) {
01532         if (index != i) {
01533             mm.rows_list[temp_index] = ref_mm.rows_list[index];
01534             temp_index++;
01535         }
01536     }
01537     for (size_t jindex = 0, temp_jindex = 0; jindex < ref_mm.cols; jindex++) {
01538         if (jindex != j) {
01539             mm.cols_list[temp_jindex] = ref_mm.cols_list[jindex];
01540             temp_jindex++;
01541         }
01542     }
01543
01544     return mm;
01545 }
01546
01552 void mat2D_minor_free(Mat2D_Minor mm)
01553 {
01554     MAT2D_FREE(mm.cols_list);
01555     MAT2D_FREE(mm.rows_list);
01556 }
01557
01564 void mat2D_minor_print(Mat2D_Minor mm, const char *name, size_t padding)
01565 {
01566     printf("%s%s = [\n", (int) padding, "", name);
01567     for (size_t i = 0; i < mm.rows; ++i) {
01568         printf("%s", (int) padding, "");
01569         for (size_t j = 0; j < mm.cols; ++j) {
01570             printf("%f ", MAT2D_MINOR_AT(mm, i, j));
01571         }
01572         printf("\n");
01573     }
01574     printf("%s]\n", (int) padding, "");
01575 }
01576
01582 double mat2D_det_2x2_mat_minor(Mat2D_Minor mm)
01583 {
01584     MAT2D_ASSERT(2 == mm.cols && 2 == mm.rows && "Not a 2x2 matrix");
01585     return MAT2D_MINOR_AT(mm, 0, 0) * MAT2D_MINOR_AT(mm, 1, 1) - MAT2D_MINOR_AT(mm, 0, 1) *
        MAT2D_MINOR_AT(mm, 1, 0);
01586 }
01587
01595 double mat2D_minor_det(Mat2D_Minor mm)
01596 {
01597     MAT2D_ASSERT(mm.cols == mm.rows && "should be a square matrix");
01598
01599     double det = 0;
01600     /* TODO: finding beast row or col? */
01601     for (size_t i = 0, j = 0; i < mm.rows; i++) { /* first column */
01602         if (fabs(MAT2D_MINOR_AT(mm, i, j)) < 1e-10) continue;
01603         Mat2D_Minor sub_mm = mat2D_minor_alloc_fill_from_mat_minor(mm, i, j);
01604         int factor = (i+j)%2 ? -1 : 1;
01605         if (sub_mm.cols != 2) {
01606             MAT2D_ASSERT(sub_mm.cols == sub_mm.rows && "should be a square matrix");
01607             det += MAT2D_MINOR_AT(mm, i, j) * (factor) * mat2D_minor_det(sub_mm);
01608         } else if (sub_mm.cols == 2 && sub_mm.rows == 2) {
01609             det += MAT2D_MINOR_AT(mm, i, j) * (factor) * mat2D_det_2x2_mat_minor(sub_mm);
01610         }
01611         mat2D_minor_free(sub_mm);
01612     }
01613     return det;
01614 }
01615
01616 #endif // MATRIX2D_IMPLEMENTATION

```


4.3 temp.c File Reference

```
#include "Matrix2D.h"
```

Include dependency graph for temp.c:



Macros

- `#define` [MATRIX2D_IMPLEMENTATION](#)

Functions

- `int` [main](#) (void)

4.3.1 Macro Definition Documentation

4.3.1.1 MATRIX2D_IMPLEMENTATION

```
#define MATRIX2D_IMPLEMENTATION
```

Definition at line 1 of file [temp.c](#).

4.3.2 Function Documentation

4.3.2.1 main()

```
int main (  
    void )
```

Definition at line 4 of file [temp.c](#).

References [mat2D_alloc\(\)](#), [mat2D_free\(\)](#), [MAT2D_PRINT](#), [mat2D_rand\(\)](#), and [mat2D_upper_triangulate\(\)](#).

4.4 temp.c

```
00001 #define MATRIX2D_IMPLEMENTATION
00002 #include "Matrix2D.h"
00003
00004 int main(void)
00005 {
00006     Mat2D m = mat2D_alloc(5, 4);
00007
00008     mat2D_rand(m, 0, 1);
00009
00010     MAT2D_PRINT(m);
00011
00012     mat2D_upper_triangulate(m);
00013
00014     MAT2D_PRINT(m);
00015
00016     mat2D_free(m);
00017
00018     return 0;
00019 }
00020 }
```

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