# הטכניון – מכון טכנולוגי לישראל NUMERICAL METHODS IN AEROSPACE ENGINEERING

## HOMEWORK ASSIGNMENT x סמסטר אביב תשפ"ה SPRING SEMESTER 2025

GRADE	OUT OF	CHAPTER	
	2	ABSTRACT	
	2	CONTENTS, STYLE &C.	
	4	PHYSICAL PROBLEM	
	4	MATHEMATICAL MODEL	
	26	NUMERICAL METHODS	
	20	INFLUENCE OF NUMERICAL METHODS	
	20	RESULTS	
	2	SUMMARY & CONCLUSIONS	
	20	COMPUTER PROGRAM	
	100	TOTAL	

Almog Dobrescu ID 214254252

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#### Abstract

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## Contents

1	The Physical Problem	1
2	The Mathematical Model 2.1 Boundary Conditions	<b>1</b> 1
3	The Numerical Methods 3.1 Finite Differencing	2 2 2 2
4		3 3 4
5	Results and Discussion	4
6	Summary and Conclusion	5
A	Listing of The Computer Program  A.1 Parameters	<b>6</b> 6 7
$\mathbf{L}_{\mathbf{i}}$	ist of Figures	
	The Channel	1 3 3 4 4
$\mathbf{L}_{\mathbf{i}}$	istings	
	Parameters file	6 6 7

## Nomenclature

 $\Delta x$ step size in the x coordinate  $\Delta y$ step size in the y coordinate viscosity of the fluid  $\mu$ convergence criteria  $\varepsilon$ pressure gradient on the flow in a section ciindex in the x coordinate jindex in the y coordinate iterative index nninumber of indexes in the x direction number of indexes in the y direction nj

## 1 The Physical Problem

An incompressible viscose Newtonian fluid flows in a channel.

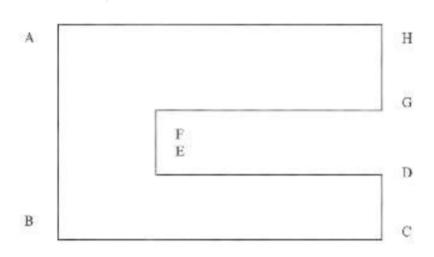


Figure 1: The Channel

Where:

•	AB =	12	[in]	

• 
$$BC = 12[in]$$

• 
$$CD = 2[in]$$

• 
$$DE = 6[in]$$

• 
$$EF = 6[in]$$

• 
$$FG = 6[in]$$

• 
$$GH = 4[in]$$

• 
$$HA = 12[in]$$

The x-axis will be from left to right and the y-axis will be from bottom to top such that the origin is at point B.

### 2 The Mathematical Model

The steady-state velocity of the fluid is given by:

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} = -\frac{c}{\mu} \tag{1}$$

In our case:

- $c = 0.0002 \left[ \frac{lb}{in^3} \right]$
- $\mu = 0.25 \cdot 10^{-5} \left[ \frac{lb \cdot sec}{in^2} \right]$

## 2.1 Boundary Conditions

Since the flow is viscose, the boundary conditions are no penetration and no slip. The flow is at a steady state so the only direction of the flow is normal the sectional area (outside the paper). Hence the velocity at the boundaries is:

$$\phi|_{AB} = \phi|_{BC} = \phi|_{CD} = \phi|_{DE} = \phi|_{EF} = \phi|_{FG} = \phi|_{GH} = \phi|_{HA} = 0$$
 (2)

#### 3 The Numerical Methods

#### 3.1 Finite Differencing

In order to solve the partial differential equation we will use finite differences. For the second derivative in space, we will use central differencing:

$$\frac{\phi_{i-1,j} - 2\phi_{i,j} + \phi_{i+1,j}}{\Delta x^2} + \mathcal{O}\left(\Delta x^2\right) + \frac{\phi_{i,j-1} - 2\phi_{i,j} + \phi_{i,j+1}}{\Delta y^2} + \mathcal{O}\left(\Delta y^2\right) = -\frac{c}{\mu}$$

$$(\phi_{i-1,j} - 2\phi_{i,j} + \phi_{i+1,j}) \Delta y^2 + (\phi_{i,j-1} - 2\phi_{i,j} + \phi_{i,j+1}) \Delta x^2 = -\Delta x^2 \Delta y^2 \frac{c}{\mu} + \mathcal{O}\left(\Delta x^2, \Delta y^2\right)$$

$$-2\phi_{i,j} \left(\Delta y^2 + \Delta x^2\right) + (\phi_{i-1,j} + \phi_{i+1,j}) \Delta y^2 + (\phi_{i,j-1} + \phi_{i,j+1}) \Delta x^2 = -\Delta x^2 \Delta y^2 \frac{c}{\mu}$$

$$2\phi_{i,j} \left(\Delta y^2 + \Delta x^2\right) = (\phi_{i-1,j} + \phi_{i+1,j}) \Delta y^2 + (\phi_{i,j-1} + \phi_{i,j+1}) \Delta x^2 + \Delta x^2 \Delta y^2 \frac{c}{\mu}$$

$$2\phi_{i,j} = (\phi_{i-1,j} + \phi_{i+1,j}) \frac{\Delta y^2}{\Delta y^2 + \Delta x^2} + (\phi_{i,j-1} + \phi_{i,j+1}) \frac{\Delta x^2}{\Delta y^2 + \Delta x^2} + \frac{\Delta x^2 \Delta y^2}{\Delta y^2 + \Delta x^2} \frac{c}{\mu}$$

$$\phi_{i,j} = \frac{1}{2} \left( (\phi_{i-1,j} + \phi_{i+1,j}) \frac{\Delta y^2}{\Delta y^2 + \Delta x^2} + (\phi_{i,j-1} + \phi_{i,j+1}) \frac{\Delta x^2}{\Delta y^2 + \Delta x^2} + \frac{\Delta x^2 \Delta y^2}{\Delta y^2 + \Delta x^2} \frac{c}{\mu} \right)$$
(3)

Where:

• 
$$\Delta x = \frac{x_{max} - x_{min}}{ni}$$

• ni and nj will be chosen such that the walls will be at the middle of an element.

To solve the system of equations we will use the Gauss-Seidel method:

$$\phi_{i,j}^{n+1} = \frac{1}{2} \left( \left( \phi_{i-1,j}^{n+1} + \phi_{i+1,j}^{n} \right) \frac{\Delta y^{2}}{\Delta y^{2} + \Delta x^{2}} + \left( \phi_{i,j-1}^{n+1} + \phi_{i,j+1}^{n} \right) \frac{\Delta x^{2}}{\Delta y^{2} + \Delta x^{2}} + \frac{\Delta x^{2} \Delta y^{2}}{\Delta y^{2} + \Delta x^{2}} \frac{c}{\mu} \right) + \mathcal{O}\left( \Delta x^{2}, \Delta y^{2} \right)$$

$$(4)$$

#### 3.2 Boundary Conditions

The computational mesh is a grid so we will set all the cell outside the channel and on the walls to be zero. Therefore:

$$\phi|_{i_{AB}} = \phi|_{i_{CD}} = \phi|_{i_{GH}} = \phi|_{i_{EF}, j_{EF}} = 0$$

$$\phi|_{j_{BC}} = \phi|_{i_{DE}, j_{DE}} = \phi|_{i_{EG}, j_{EG}} = \phi|_{j_{AH}} = 0$$
(5)

#### 3.3 Convergence Criteria

In order determined if the iterative method for solving the system of equation has converged, we will check if the temperature vector at a specific time has changed from step n to step n+1 in the following way:

$$\left| T_{i,j}^{n+1} - T_{i,j}^n \right| < \varepsilon \tag{6}$$

## 4 Influence of The Numerical Methods

#### 4.1 Influence of Number of Elements ni, nj

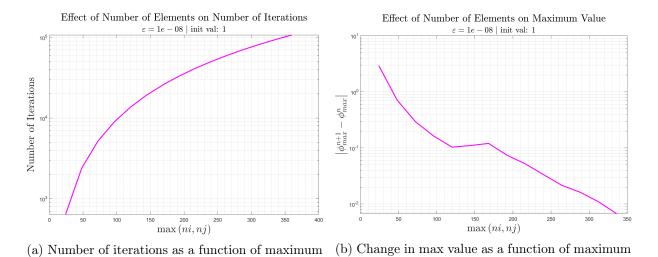


Figure 2: Influence of the number of elements ni nj

of ni and nj

We can see that as the number of grid points increases, the number of iterations increases and the error decreases. Since there is no clear optimal number of grid points we will choose a number that will have a sufficiently small error but not too much of iterations. Hence the chosen number of grid points will be 120.

#### 4.2 Influence of Convergence Criteria $\varepsilon$

of ni and nj

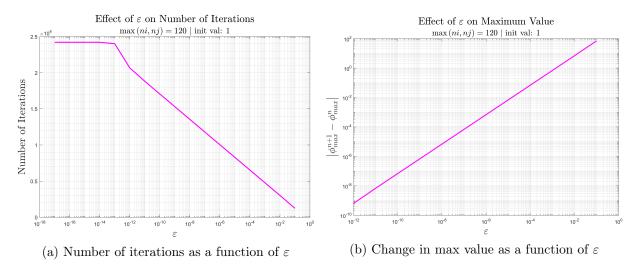
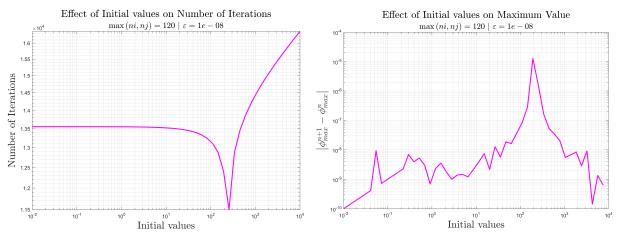


Figure 3: Influence of the convergence criteria  $\varepsilon$ 

Figure 3 shows that as the convergence criteria decreases, the number of iterations increases up to a certain point. This point is probably the accuracy limitation of floating double point. Moreover, the error decreases exponentially with the decrease of the convergence criteria. We can declare that  $\varepsilon = 1 \cdot 10^{-8}$  is a good value for the convergence criteria.



#### 4.3 Influence of Initial Conditions



- (a) Number of iterations as a function of initial value
- (b) Change in max value as a function of initial value

Figure 4: Influence of the initial value

We can see from Fig.4 that when the initial value is close the maximal value of the flow, the number of iterations decreases but the error increases. Furthermore, for all initial values below 10, the number of iterations stays constant and the error has close to no change. So all initial values smaller than 10 are good and we will choose the initial value to be 1.

#### 5 Results and Discussion

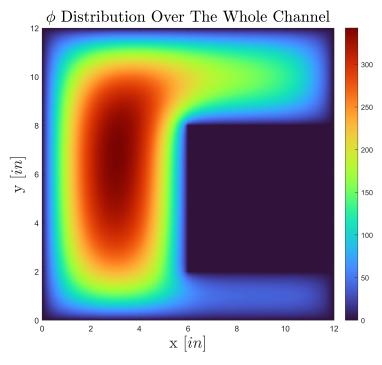


Figure 5:  $\phi$  distribution over the whole field

We can see that as expected, the highest value of  $\phi$  in the flow field is at the widest section of the channel. Moreover, this figure helps us to make sure that the no-slip and no-penetration conditions are enforced.



6 Summary and Conclusion

## A Listing of The Computer Program

#### A.1 Parameters

```
1  x_min = 0;
2  x_max = 12;
3  y_min = 0;
4  y_max = 12;
5  c = 0.0002;
6  mu = 0.25e-5;
7  factor = 4;
8  init_val = 1;
9  epsilon = 1e-5;
```

Listing 1: Parameters file

```
AB = 12; BC = 12; CD = 2; DE = 6;
 2
    EF = 6; FG = 6; GH = 4; HA = 12;
 3
 4
   ni = lcm(BC, BC—DE) * factor;
   nj = lcm(lcm(CD, AB), lcm(CD+EF, AB)) * factor;
 5
 6
   delta_x = (x_max - x_min) / (ni);
    delta_y = (y_max - y_min) / (nj);
    x_{\text{vec}} = x_{\text{min}} + (0:ni)*delta_x;
 8
9
   y_vec = y_min + (0:nj)*delta_y;
11
   i_AB = 0;
12
   j_AB = 0:(AB / delta_y);
13
14
    i_BC = 0:(BC / delta_x);
15
    j_BC = 0;
16
17
    i_CD = BC / delta_x;
18
    j_CD = 0:(CD / delta_y);
19
20
   i_DE = ((BC - DE) / delta_x):(BC / delta_x);
21
    j_DE = CD / delta_y;
23
    i_EF = (BC - DE) / delta_x;
24
    j_EF = (CD / delta_y):((CD + EF) / delta_y);
25
26
   i_FG = ((BC - DE) / delta_x):(BC / delta_x);
27
    j_FG = (CD + EF) / delta_y;
28
29
    i_GH = BC / delta_x;
30
    j_GH = ((CD + EF) / delta_y):((CD + EF + GH) / delta_y);
31
32
    i_HA = i_BC;
33
    j_HA = (AB / delta_y);
34
    for j = j_AB+1
36
        x_{mat}(j, :) = x_{vec};
    for i = i_BC+1
38
39
        y_{mat}(:, i) = y_{vec};
40
    end
```

Listing 2: Extra parameters file

#### A.2 Main Code

```
clc; clear; close all;
 2
 3
   % flow_field_init = init_flow_field(ni, nj, i_AB, j_AB, i_BC, j_BC, i_CD, j_CD, i_DE,
        j_EF, i_GH, j_GH, i_HA, j_HA);
   % figure
 4
   % contourf(x_mat, y_mat, flow_field_init, 100, "LineStyle","none")
 6
   % colormap('turbo')
 7
   % colorbar()
   % axis equal
 9
   parameters
   factor = 5;
   % init_val = 0.1;
12
13
14 \mid \text{result} = \text{solve\_Gauss\_Seidel}(x\_\text{min}, x\_\text{max}, y\_\text{min}, y\_\text{max}, c, mu, factor, init\_val, epsilon)
15
16
   fig1 = figure('Name','1','Position',[0, 250, 900, 600]);
   contourf(result.x_mat, result.y_mat, result.flow_field, 200, "LineStyle", "none")
17
18 | colormap('turbo')
19 | colorbar()
20 axis equal
21 | title('$\phi$ Distribution Over The Hole Channel','FontSize',20,'Interpreter','latex')
22 | xlabel('x $[in]$', 'FontSize', 20, 'Interpreter', 'latex')
   ylabel('y $[in]$','FontSize',20,'Interpreter','latex')
   % exportgraphics(fig1, 'images/phi ditribution.png','Resolution',400);
24
25
26
27
   28
29 parameters
30 \mid factors = 1:1:15;
   results = {};
32
   lg = \{\};
   for factor_index = 1:length(factors)
34
        factor = factors(factor_index);
        results{end+1} = solve_Gauss_Seidel(x_min, x_max, y_min, y_max, c, mu, factor,
            init_val, epsilon);
36
   end
38
   fig2 = figure('Name','2','Position',[0, 250, 900, 600]);
39
   size = 20;
   colors = cool(length(factors));
40
41
   max_ni_nj_vec = [];
42
   n_{\text{vec}} = [];
43
   for factor_index = 1:length(factors)
44
        max_ni_nj_vec(factor_index) = max(results{factor_index}.ni, results{factor_index}.nj)
45
        n_vec(factor_index) = results{factor_index}.n;
46
   end
47
   semilogy(max_ni_nj_vec, n_vec, 'LineStyle','-','LineWidth',2,'Color',colors(end,:))
48
49
50 | title('Effect of Number of Elements on Number of Iterations', 'FontSize', size,'
        Interpreter', 'latex')
```

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```
51
    subtitle(sprintf('$\\varepsilon=%g$ $|$ init val: %g', results{end}.epsilon, results{end
        }.init_val), 'FontSize',size-4,'Interpreter','latex')
52
    ylabel('Number of Iterations', 'FontSize', size,'Interpreter','latex')
53 | xlabel('$\max{\left(ni,nj\right)}$', 'FontSize', size,'Interpreter','latex')
54 grid on
55 grid minor
56
   box on
57
    % exportgraphics(fig2, 'images/ni nj - n.png', 'Resolution', 400);
58
59 | fig3 = figure('Name','3','Position',[200, 250, 900, 600]);
60 | size = 20;
61 | colors = cool(length(factors));
62 \mid \mathsf{max\_vec} = [];
63
    for factor_index = 1:length(factors)-1
64
        max_vec(factor_index) = calc_diff(results{factor_index}, results{factor_index+1});
65
    end
66
67
    semilogy(max_ni_nj_vec(1:end-1), max_vec, 'LineStyle','-','LineWidth',2,'Color',colors(
        end,:))
68
    title('Effect of Number of Elements on Maximum Value', 'FontSize', size, 'Interpreter','
69
    subtitle(sprintf('$\\varepsilon=%g$ $|$ init val: %g', results{end}.epsilon, results{end}
        }.init_val), 'FontSize',size-4,'Interpreter','latex')
    ylabel('\$\left|\phi_{max}^{n+1}-\phi_{max}^{n}\right|\$', 'FontSize', size,'Interpreter','
71
    xlabel('$\max{\left(ni,nj\right)}$', 'FontSize', size,'Interpreter','latex')
 72
73
    grid on
 74
    grid minor
 75
    box on
 76
    % exportgraphics(fig3, 'images/ni nj - max diff.png', 'Resolution', 400);
    % exportgraphics(fig2, 'images/ni nj - n.png','Resolution',400); exportgraphics(fig3, '
 77
        images/ni nj - max diff.png', 'Resolution', 400);
 78
80
    81
82
    parameters
83
    epsilons = logspace(-1, -17, 17);
84 |% epsilons = logspace(0, -5, 6);
85 \mid results = \{\};
86
    lg = {};
87
    for epsilons_index = 1:length(epsilons)
88
        epsilon = epsilons(epsilons_index);
89
        results{end+1} = solve_Gauss_Seidel(x_min, x_max, y_min, y_max, c, mu, factor,
            init_val, epsilon);
90
    end
92
    fig4 = figure('Name','4','Position',[400, 250, 900, 600]);
93 | size = 20;
94 | colors = cool(length(epsilons));
95 \mid max_ni_nj_vec = [];
96
    n_{vec} = [];
    for epsilons_index = 1:length(epsilons)
98
        n_vec(epsilons_index) = results{epsilons_index}.n;
99
    end
100
101 | semilogx(epsilons, n_vec, 'LineStyle','—','LineWidth',2,'Color',colors(end,:))
```

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```
102
    title('Effect of $\phi$ on Number of Iterations', 'FontSize', size,'Interpreter','latex')
104
    subtitle(sprintf('$\\max{\\left(ni,nj\\right)}=%d$ $|$ init val: %g', max(results{end}.ni
         , results{end}.nj), results{end}.init_val), 'FontSize',size—4,'Interpreter','latex')
    ylabel('Number of Iterations', 'FontSize', size,'Interpreter','latex')
105
106
    xlabel('$\varepsilon$', 'FontSize', size,'Interpreter','latex')
107
    arid on
108
    grid minor
109
    box on
110
    % exportgraphics(fig4, 'images/epsilon — n.png','Resolution',400);
111
112 | fig5 = figure('Name','5','Position',[600, 250, 900, 600]);
113 | size = 20;
114
    colors = cool(length(epsilons));
115
    max_vec = [];
116
    for epsilons_index = 1:length(epsilons)—1
117
         max_vec(epsilons_index) = calc_diff(results{epsilons_index}, results{epsilons_index
            +1});
118
    end
119
120
    loglog(epsilons(1:end-1), max_vec, 'LineStyle','-','LineWidth',2,'Color',colors(end,:))
121
122
    title('Effect of $\phi$ on Maximum Value', 'FontSize', size,'Interpreter','latex')
123
    subtitle(sprintf('$\\max{\\left(ni,nj\\right)}=%d$ $|$ init val: %g', max(results{end}.ni
         , results{end}.nj), results{end}.init_val), 'FontSize',size-4,'Interpreter','latex')
124
    ylabel('$\left|\phi_{max}^{n+1}-\phi_{max}^{n}\right|$', 'FontSize', size,'Interpreter','
    xlabel('$\varepsilon$', 'FontSize', size,'Interpreter','latex')
126
    grid on
127
    grid minor
128
    box on
129
    % exportgraphics(fig5, 'images/epsilon — max diff.png','Resolution',400);
    % exportgraphics(fig5, 'images/epsilon — max diff.png','Resolution',400); exportgraphics(
         fig4, 'images/epsilon - n.png', 'Resolution',400);
132
133
    % effect of init val =====
134
    parameters
136
    init_vals = logspace(-2,4,50);
137
    results = {};
    lg = {};
139
    for init_vals_index = 1:length(init_vals)
140
         init_val = init_vals(init_vals_index);
141
         results{end+1} = solve_Gauss_Seidel(x_min, x_max, y_min, y_max, c, mu, factor,
             init_val, epsilon);
142
    end
143
144
    fig6 = figure('Name','6','Position',[0, 150, 900, 600]);
145 | size = 20;
146 | colors = cool(length(init_vals));
147
   |\max_{ni_nj_vec} = [];
148
    n_{vec} = [];
149
    for init_vals_index = 1:length(init_vals)
150
         n_vec(init_vals_index) = results{init_vals_index}.n;
151
    end
152
153 |loglog(init_vals, n_vec, 'LineStyle','-','LineWidth',2,'Color',colors(end,:))
```

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```
154
    title('Effect of Initial values on Number of Iterations', 'FontSize', size, 'Interpreter',
155
    subtitle(sprintf('\$\max{\left(ni,nj\right)}=\%d\$ \$|\$ \$\varepsilon=\%g\$', max(results\{max(max(mi,nj))\}=\%d\$)\}
156
        end}.ni, results{end}.nj), results{end}.epsilon), 'FontSize',size-4,'Interpreter','
        latex')
157
    ylabel('Number of Iterations', 'FontSize', size,'Interpreter','latex')
158
    xlabel('Initial values', 'FontSize', size,'Interpreter','latex')
    grid on
159
160
    grid minor
    box on
162
    % exportgraphics(fig6, 'images/init val - n.png', 'Resolution', 400);
    fig7 = figure('Name','7','Position',[200, 150, 900, 600]);
164
    size = 20;
    colors = cool(length(init_vals));
166
    max_vec = [];
168
    for init_vals_index = 1:length(init_vals)-1
169
         max_vec(init_vals_index) = calc_diff(results{init_vals_index}, results{
            init_vals_index+1});
170
    end
171
172
    loglog(init_vals(1:end-1), max_vec, 'LineStyle','-','LineWidth',2,'Color',colors(end,:))
173
174
    title('Effect of Initial values on Maximum Value', 'FontSize', size, 'Interpreter', 'latex'
175
    subtitle(sprintf('$\\max{\\left(ni,nj\\right)}=%d$ $|$ $\\varepsilon=%g$', max(results{
        end}.ni, results{end}.nj), results{end}.epsilon), 'FontSize',size—4,'Interpreter','
    ylabel('$\left|\phi_{max}^{n+1}-\phi_{max}^{n}\right|$', 'FontSize', size,'Interpreter','
         latex')
    xlabel('Initial values', 'FontSize', size,'Interpreter','latex')
177
178
    grid on
179
    grid minor
180
    box on
181
    % exportgraphics(fig7, 'images/init val — max diff.png','Resolution',400);
    \$ exportgraphics(fig7, 'images/init val - max diff.png','Resolution',400); exportgraphics
182
        (fig6, 'images/init val - n.png', 'Resolution', 400);
183
184
185
186
187
188
    189
190
     function flow_field = set_BC(flow_field, i_AB, j_AB, i_BC, j_BC, i_CD, j_CD, i_DE, j_EF,
        i_GH, j_GH, i_HA, j_HA)
         for i = i_AB+1
192
            for j = j_AB+1
                 flow_field(j, i) = 0;
194
            end
195
        end
196
         for i = i_BC+1
            for j = j_BC+1
                flow_field(j, i) = 0;
199
            end
200
        end
201
         for i = i_CD+1
```

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```
202
             for j = j_CD+1
203
                  flow_field(j, i) = 0;
204
             end
205
         end
206
         for i = i_DE+1
207
             for j = j_EF+1
208
                 flow_field(j, i) = 0;
209
             end
         end
211
         for i = i_GH+1
212
             for j = j_GH+1
213
                 flow_field(j, i) = 0;
214
             end
215
         end
216
         for i = i_HA+1
217
             for j = j_{HA+1}
218
                 flow_field(j, i) = 0;
219
             end
220
         end
221
    end
222
223
     function flow_field = init_flow_field(ni, nj, init_val, i_AB, j_AB, i_BC, j_BC, i_CD,
         j_CD, i_DE, j_EF, i_GH, j_GH, i_HA, j_HA)
224
         flow_field = ones(nj+1,ni+1) * init_val;
         flow_field = set_BC(flow_field, i_AB, j_AB, i_BC, j_BC, i_CD, j_CD, i_DE, j_EF, i_GH,
              j_GH, i_HA, j_HA);
     end
227
228
     function converged = check_convergence(flow_field_next, flow_field_current, epsilon,j_AB,
229
         converged = true;
         for i = i_BC+1
230
231
             for j = j_AB+1
232
                 if abs(flow_field_next(j, i) - flow_field_current(j, i)) > epsilon
233
                      converged = false;
234
                      return
235
                 end
236
             end
237
         end
238
     end
239
240
     function result = solve_Gauss_Seidel(x_min, x_max, y_min, y_max, c, mu, factor, init_val,
          epsilon)
241
         calc_extra_param
242
         flow_field_current = init_flow_field(ni, nj, init_val, i_AB, j_AB, i_BC, j_BC, i_CD,
             j_CD, i_DE, j_EF, i_GH, j_GH, i_HA, j_HA);
243
         flow_field_next = flow_field_current;
         for n = 1:1e6
245
             if \sim mod(n, 100)
246
                 fprintf('factor: %d | epsilon: %g | init val: %g | n: %d\n', factor, epsilon,
                       init_val, n)
247
             end
248
             for i = i_BC(2:end-1)+1
249
                 for j = j_AB(2:end-1)+1
                     % flow_field_next(j, i) = 0.5 * ((flow_field_next(j, i-1) + 
                          flow_field_current(j, i+1)) * delta_y^2 / (delta_y^2+delta_x^2) + (
                          flow_field_next(j-1, i) + flow_field_current(j+1, i)) * delta_x^2 / (
                          delta_y^2+delta_x^2) + delta_x^2*delta_y^2 / (delta_y^2+delta_x^2) *
```

~**%**~

```
c / mu);
                     flow_field_next(j, i) = 0.5 * ((flow_field_current(j, i-1) + i))
                          flow_field_current(j, i+1)) * delta_y^2 / (delta_y^2+delta_x^2) + (
                          flow_field_current(j-1, i) + flow_field_current(j+1, i)) * delta_x^2
                          / (delta_y^2+delta_x^2) + delta_x^2*delta_y^2 / (delta_y^2+delta_x^2)
                           * c / mu);
252
                 end
253
             end
             flow_field_next = set_BC(flow_field_next, i_AB, j_AB, i_BC, j_BC, i_CD, j_CD,
                 i_DE, j_EF, i_GH, j_GH, i_HA, j_HA);
             if check_convergence(flow_field_next, flow_field_current, epsilon,j_AB, i_BC)
255
256
                 break
257
             end
258
             flow_field_current = flow_field_next;
259
260
         result.n
                            = n;
261
         result.x_min
                           = x_{min};
262
         result.x_max
                            = x_max;
263
         result.y_min
                            = y_min;
264
         result.y_max
                            = y_{max};
265
         result.c
                            = c;
266
         result.mu
                           = mu:
267
         result.factor
                           = factor;
268
         result.epsilon
                           = epsilon;
         result.x_mat
                           = x_mat;
270
         result.y_mat
                           = y_mat;
271
         result.delta_x
                           = delta_x;
272
         result.delta_y
                           = delta_y;
273
         result.ni
                           = ni;
274
         result.nj
                           = nj;
275
         result.i_BC
                           = i_BC;
276
                           = j_AB;
         result.j_AB
277
         result.init_val
                           = init_val;
278
         result.flow_field = flow_field_next;
279
    end
280
281
     % function rms = RMS(result1, result2)
282
    % % This functions calcutlates the RMS value for 1 compared to 2
283
    %
           flow_field2_at_coord_of_1 = [];
284
    %
           for i = result1.i_BC+1
285
    %
               for j = result1.j_AB+1
286
                   flow_field2_at_coord_of_1(j, i) = interp2(result2.x_mat, result2.y_mat,
         result2.flow_field, result1.x_min + i*result1.delta_x, result1.y_min + j*result1.
         delta_y);
287
     %
               end
288
     %
289
     %
           flow_field2_at_coord_of_1(isnan(flow_field2_at_coord_of_1)) = 0;
           flow_field1 = result1.flow_field;
290
     %
291
           rms = sqrt(sum(sum((flow_field1—flow_field2_at_coord_of_1).^2)) / (length(
         flow_field1(:,1)) * length(flow_field1(1,:))));
292
    % end
293
294
     function diff = calc_diff(result1, result2)
295
         max1 = max(max(result1.flow_field));
296
         max2 = max(max(result2.flow_field));
297
         diff = abs(max1-max2);
298
    end
```

≎X≎

Listing 3: The main file