Generative Models

Problem Introduction:

The Longest Increasing Subsequence (LIS) problem is to find the length of the longest subsequence of a given sequence such that all elements of the subsequence are sorted in increasing order.

Method used: (Dynamic Programming)

To accomplish this task, we define an array d [0...n−1], where d[i] is the length of the longest increasing subsequence that ends in the element at index i. We will compute this array gradually. So let the current index be i. i.e. we want to compute the value d[i] and all previous values d[0] ...,d[i−1] are already known. Then there are two options:

- d[i]=1: the required subsequence consists of only the element a[i].

- d[i]>1: then in the required subsequence is another number before the number a[i].

If the second option is true, then we append the element a[j] to a third array which will hold our wanted LIS.

This method is a little complex, although it takes time equal to n^2 but its main problem is in consuming much memory.

```cpp
vector<int> longestSubSeq(vector<int> const& a) {

    int n = a.size();
    vector<vector<int>> lis;
    for(size_t i=0; i<n; i++) {
        lis.push_back({});
    }
    vector<int> d(n, 1);
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < i; j++) {
            if (a[i] > a[j] && d[i] < d[j]+1) {
                d[i] = d[j] + 1;
                lis[i].push_back(a[j]);
            }
        }
    }
    auto pos = distance(d.begin(), std::max_element(d.begin(), d.end()));
    lis[pos].push_back(a[pos]);
    return lis[pos];
}
```

```
The Original Subsequence is: 7 3 8 4 2 6
Length of Longest Increasing Subsequence is: 3
The Longest Increasing Subsequence is: 3 4 6
```