1

Assignment 1: Matrix Theory

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Abstract—This assignment solves a problem to find the slope of a line.

Download all python codes from

https://github.com/Alok0895/Assignment1/blob/ master/Assignment1.py

and latex-tikz codes from

https://github.com/Alok0895/Assignment1/blob/ master/Assignment1.tex

1 Problem

The perpendicular from the origin to the line $\begin{pmatrix} -m & 1 \end{pmatrix} \mathbf{x} = c$ meets it at the point $\mathbf{P} = \begin{pmatrix} -1 \\ 2 \end{pmatrix}$. find the value of m and c.

2 Solution

According to the question, the given line can be expressed as:-

$$L_1 \implies \begin{pmatrix} -m & 1 \end{pmatrix} \mathbf{x} = c$$

Direction vector of line L_2 perpendicular to L_1 should be $\binom{1}{m}$ such that the equation of line should be:-

$$L_2 \implies \begin{pmatrix} 1 & m \end{pmatrix}^T (\mathbf{x} - \begin{pmatrix} -1 & 2 \end{pmatrix}) = 0$$

Therefore L_2 can be expressed as:-

$$\implies (1 \quad m)(\mathbf{x} - \begin{pmatrix} -1\\2 \end{pmatrix}) = 0$$

since it passes through (0,0) therefore:-

$$\begin{pmatrix} m & 1 \end{pmatrix} \begin{pmatrix} 0 \\ 0 \end{pmatrix} - \begin{pmatrix} 1 & m \end{pmatrix} \begin{pmatrix} -1 \\ 2 \end{pmatrix} = 0 \tag{2.0.1}$$

$$\implies (-1 + 2m) = 0 \tag{2.0.2}$$

$$\implies m = \frac{1}{2} \tag{2.0.3}$$

$$\implies m = 0.5 \tag{2.0.4}$$

Hence, the value of m and c are obtained as 0.5 and 2.5 respectively.

$$(-0.5 1)(x) = c (2.0.5)$$

$$\implies (-0.5 1)\begin{pmatrix} -1\\2 \end{pmatrix} = c$$

$$\implies c = 2.5 (2.0.6)$$

Hence, the value of m and c are obtained as 0.5 and 2.5 respectively.

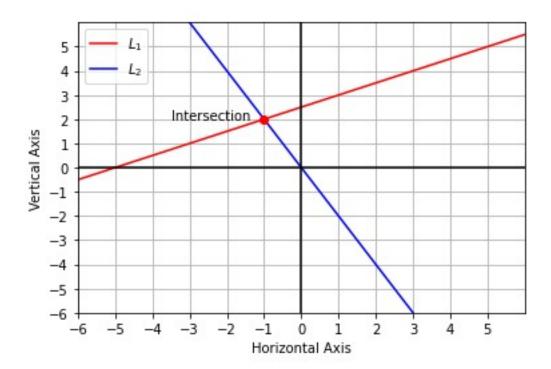


Fig. 0: Perpendicular Lines crossing