```
In [2]: import numpy as np
import csv
import matplotlib.pyplot as plt
from sklearn.kernel_ridge import KernelRidge
from sklearn.linear_model import Ridge
from scipy import optimize
import pylab as py
from scipy.stats import norm
from sklearn.model_selection import GridSearchCV
from sklearn.svm import SVR
from scipy.stats import norm
import matplotlib.mlab as mlab
from sklearn.model_selection import StratifiedShuffleSplit
from matplotlib.pyplot import plot
import matplotlib
```

```
In [3]: # Rebin function taken from http://scipy-cookbook.readthedocs.io/items/R
        ebinning.html
        def rebin( a, newshape ):
                  'Rebin an array to a new shape.
                assert len(a.shape) == len(newshape)
                slices = [ slice(0,old, float(old)/new) for old,new in zip(a.sha
        pe, newshape) ]
                coordinates = np.mgrid[slices]
                indices = coordinates.astype('i')
                                                   #choose the biggest smaller
        integer index
                return a[tuple(indices)]
         # Add the relative noise
        def add noise(a,rel noise,len data,width data):
            b = np.ones((len_data,width_data+2))
            for i in range(len(a[:,0])):
                b[i,:] = a[i,:]+ np.random.normal(0, rel_noise,len(a[0,:]))
            return b
```

```
In [4]: def ProfPSF(amplitudes, positions, len data, width data, sigmaPSF, rebin=1):
            profdata=np.ones((len_data, width_data))
            profdataout=np.ones((len data, int(width data/rebin)))
            profred=np.ones((rebin,int(width data/rebin)))
            sigPSF=sigmaPSF#125.0e-6 # [m] original range of the profile data i
        s -5...5 mm
             gaussPSF=[]
            gaussPSF = np.exp(-(positions/sigPSF)**2/2)
           # plt.figure(100)
            #plt.plot(gaussPSF)
             for p in positions:
                 gaussPSF.append(np.exp(-(p/sigPSF)**2/2))
            # convolution before rebinning:
            for i in range(len data):
                profdata[i,:]=np.convolve(amplitudes[i,:], gaussPSF, mode="same"
        )
               # plt.figure(99)
                #plt.plot(profdata[i,:])
                profred=(profdata[i,:].reshape(int(width_data/rebin), rebin)) # i
        n case rebinning is needed
                profdataout[i,:] = profred.mean(axis=1)
                profdataout[i,:] = profdataout[i,:]/np.amax(profdataout[i,:])
               # plt.figure(101)
                #plt.plot(profdataout[i,:])
                     print ("Length rebinned",len(profred))
                     print (profred)
        #
        #
                     profmax=np.amax(profred)
        #
                     print (profmax)
                     profdataout[i,:]=float(np.squeeze(profred))
            return profdataout
```

```
In [7]: noise = 0.005
    PSF = 125.0e-6
    pos = np.arange(-5.0e-3,5.0e-3,10.0e-6)
    # This comma separated file is matrix of 375*1002
    file_name = 'input_train.txt'
    sample_num = 375
    profile_length = 1000
    input_data = np.ones((sample_num,profile_length+2)) # 2 accounts for Np
    and sigma_l
    rebinning = 10
    rebinned_data = np.ones((sample_num,int(profile_length/rebinning)+2))
    noisy_rebinned_data = np.ones((sample_num,int(profile_length/rebinning)+2))
```

```
In [9]: # Only profiele data for rebinning
         profile_data = input_data[:,0:1000]
         #plt.figure(5)
         #plt.plot(profile data[10,:])
         # Rebin the data
         # Do the PSF here
         rebinned data = ProfPSF(profile data,pos,sample num,profile length,PSF,r
         ebinning)
         #rebinned data = rebin(profile data,[375,int(profile length/rebinning)])
         # Do the PSF here
         # Add Np and sigma l back
         rebinned data = np.concatenate((rebinned data,input data[:,1000:1002]),1
         # Add noise
         noisy_rebinned_data = add_noise(rebinned_data,noise,sample_num,int(profi
         le_length/rebinning))
         #plt.plot(noisy_rebinned_data[10,0:1000])
         #plt.plot(rebinned_data[10,:])
         #plt.plot(noisy_rebinned_data[10,:])
         #plt.show()
         #print('rebinned data',rebinned_data)
         #print('noisy_rebinned_data',noisy_rebinned_data)
         print('noisy_rebinned_data ',len(noisy_rebinned_data[0]) )
         noisy_rebinned_data 102
In [11]: matrix2=[]
         myfile2= open('output_train.txt','r')
         for line in myfile2.readlines():
             for i in line.split(","):
                 matrix2.append(i)
         Ytrain=np.squeeze(np.asarray(matrix2))
         y0=np.array(Ytrain).astype(np.float)
         print('y0',len(y0))
         y0 375
In [12]: # This comma separated file is matrix of 375*1002
         file name = 'input_val.txt'
         sample num = 128
         input_data50 = np.ones((sample_num,profile_length+2)) # 2 accounts for N
         p and sigma_l
         rebinned data50 = np.ones((sample num,int(profile length/rebinning)+2))
         noisy_rebinned_data50 = np.ones((sample_num,int(profile_length/rebinnin))
         q)+2))
```

```
In [13]: with open(file name, 'r') as f:
              reader = csv.reader(f,delimiter=',')
             rownum = 0
             for row in reader:
         #
                  print (row)
                 colnum = 0
                 for col in row:
                      input data50[rownum,colnum] = float(col)
                      colnum = colnum +1
                  rownum = rownum+1
         # Only profiele data for rebinning
         profile_data50 = input_data50[:,0:1000]
         # Rebin the data
         rebinned_data50 = ProfPSF(profile_data50,pos,sample_num,profile_length,P
         SF, rebinning)
         #rebinned data50 = rebin(profile data50,[sample num,int(profile length/r
         ebinning)])
         #function rebin is defined already
         # Add Np and sigma l back
         rebinned_data50 = np.concatenate((rebinned_data50,input_data50[:,1000:10
         02]),1)
         \#noise = 0.0
         # Add noise
         noisy_rebinned_data50 = add_noise(rebinned_data50, noise, sample_num, int(p
         rofile_length/rebinning))
         #plt.plot(rebinned_data50[10,:])
         #plt.plot(noisy_rebinned_data50[10,:])
         #plt.show()
         #print('rebinned data50', rebinned data50)
         #print('noisy_rebinned_data50', noisy_rebinned_data50)
```

```
In [14]: matrix50=[]

myfile50= open('output_val.txt','r')
for line in myfile50.readlines():
    for i in line.split(","):
        matrix50.append(i)

Ytrain50=np.squeeze(np.asarray(matrix50))
y50=np.array(Ytrain50).astype(np.float)
print('y50',len(y50))
#x=noisy_rebinned_data50
#y=y50

#25%validation data
```

y50 128

```
In [15]: # This comma separated file is matrix of 375*1002
         file name = 'input_val.txt'
         sample_num = 128
         input data25 = np.ones((sample num,profile length+2)) # 2 accounts for N
         p and sigma l
         rebinned_data25 = np.ones((sample_num,int(profile_length/rebinning)+2))
         noisy_rebinned_data25 = np.ones((sample_num,int(profile_length/rebinnin
         q)+2))
         with open(file name, 'r') as f:
             reader = csv.reader(f,delimiter=',')
             rownum = 0
             for row in reader:
                  print (row)
                 colnum = 0
                 for col in row:
                      input data25[rownum,colnum] = float(col)
                     colnum = colnum + 1
                 rownum = rownum+1
         # Only profiele data for rebinning
         profile_data25 = input_data25[:,0:1000]
         # Rebin the data
         rebinned_data25 = ProfPSF(profile_data25,pos,sample_num,profile_length,P
         SF, rebinning)
         #rebinned data25 = rebin(profile data25,[128,int(profile length/rebinnin
         g)])
         # Add Np and sigma l back
         rebinned_data25 = np.concatenate((rebinned_data25,input_data25[:,1000:10
         02]),1)
         \#noise = 0.01
         # Add noise
         noisy_rebinned_data25 = add_noise(rebinned_data25,noise,sample_num,int(p
         rofile_length/rebinning))
         #plt.plot(rebinned data50[10,:])
         #plt.plot(noisy rebinned data50[10,:])
         #plt.show()
         #print('rebinned data50', rebinned_data50)
         #print('noisy_rebinned_data50', noisy_rebinned_data50)
```

```
In [17]: matrix25=[]

myfile25= open('output_val.txt','r')
for line in myfile25.readlines():
    for i in line.split(","):
        matrix25.append(i)

Ytrain25=np.squeeze(np.asarray(matrix25))
y25=np.array(Ytrain25).astype(np.float)
print('y25',len(y25))
#x=noisy_rebinned_data25
#y=y25

#1% validation data
```

y25 128

```
In [19]: # This comma separated file is matrix of 375*1002
         file_name = 'input_val.txt'
         sample_num = 128
         input data01 = np.ones((sample num,profile length+2)) # 2 accounts for N
         p and sigma l
         rebinned_data01 = np.ones((sample_num,int(profile_length/rebinning)+2))
         noisy_rebinned_data01 = np.ones((sample_num,int(profile_length/rebinnin
         q)+2))
         with open(file name, 'r') as f:
             reader = csv.reader(f,delimiter=',')
             rownum = 0
             for row in reader:
                  print (row)
                 colnum = 0
                 for col in row:
                      input data01[rownum,colnum] = float(col)
                     colnum = colnum + 1
                 rownum = rownum+1
         # Only profiele data for rebinning
         profile_data01 = input_data01[:,0:1000]
         # Rebin the data
         rebinned_data01 = ProfPSF(profile_data01,pos,sample_num,profile_length,P
         SF, rebinning)
         #rebinned data01 = rebin(profile data01,[sample num,int(profile length/r
         ebinning)])
         # Add Np and sigma l back
         rebinned_data01 = np.concatenate((rebinned_data01,input_data01[:,1000:10
         02]),1)
         \#noise = 0.01
         # Add noise
         noisy_rebinned_data01 = add_noise(rebinned_data01, noise, sample_num, int(p
         rofile_length/rebinning))
         #plt.plot(rebinned data50[10,:])
         #plt.plot(noisy rebinned data50[10,:])
         #plt.show()
         #print('rebinned data50', rebinned data50)
         #print('noisy_rebinned_data50', noisy_rebinned_data50)
```

```
In [21]: matrix01=[]

myfile01= open('output_val.txt','r')
for line in myfile01.readlines():
    for i in line.split(","):
        matrix01.append(i)

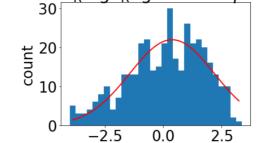
Ytrain01=np.squeeze(np.asarray(matrix01))
y01=np.array(Ytrain01).astype(np.float)
print('y01',len(y01))
#x=noisy_rebinned_data01
#y=y01
```

y01 128

```
In [40]: #kernel ridge regression:
         clf = KernelRidge(alpha=1.0, kernel='linear')
         print(clf.fit)
         print('w',rebinned data)
         clf.fit(noisy_rebinned_data, y0)
         print('KR regression coef length',len(clf.dual coef )) #coefficients of
         prediction function
         print(clf.fit)
         #50% validation data
         y_pred50=clf.predict(noisy_rebinned_data50) #prediction function Ridge R
         earession
         print('y50',len(y50))
         Error K ridge regression50=((y50-y pred50)*100)/(y50)
         #25% validation data
         y_pred25=clf.predict(noisy_rebinned_data25) #prediction function Ridge R
         egression
         print('y25',len(y25))
         Error_K_ridge_regression25=((y25-y_pred25)*100)/(y25)
         #01% validation data
         y pred01=clf.predict(noisy rebinned data01) #prediction function Ridge R
         egression
         print('y01',len(y01))
         Error_K_ridge_regression01=((y01-y_pred01)*100)/(y01)
         matplotlib.rcParams.update({'font.size': 26}) #coefficients of predictio
         n function
         #plt.figure(10)
         #plt.plot(clf.dual_coef_)
         #plt.plot(noisy_rebinned_data[10,:]/5)
         #plt.ylabel('weight')
         #plt.xlabel('coefficients and original profile')
         total error=[]
         total_error=np.concatenate((Error_K_ridge_regression50,Error_K_ridge_reg
         ression25,Error_K_ridge_regression01), axis=0)
         mu = np.mean(total error)
         sigma = np.std(total_error)
         x1 = total_error
         plt.figure(27)
         data = py.hist(x1, bins = 30)
         #Equation for Gaussian
         def f(x, a, b, c):
             return a * py.exp(-(x - b*b)**2.0 / (2 * c**2))
         # Generate data from bins as a set of points
         x = [0.5 * (data[1][i] + data[1][i+1])  for i in range(len(data[1])-1)]
         y = data[0]
         popt, pcov = optimize.curve_fit(f, x, y)
         x_{fit} = py.linspace(x[0], x[-1], 100)
         print('x_fit',x_fit)
         y_fit = f(x_fit, *popt) #generates the fitting-curve
         print('y_fit',y_fit)
         print('constant:a. mean:b. sigma:c'.*popt)
```

```
<bound method KernelRidge.fit of KernelRidge(alpha=1.0, coef0=1, degree=3</pre>
, gamma=None, kernel='linear',
      kernel params=None)>
      2.57263727e-137
                         6.04419396e-129
                                           7.49405765e-121 ...,
    5.78008700e-146
                      8.75000000e-001
                                         9.11764706e-0011
    6.95857486e-156
                      6.25892641e-147
                                         2.97057423e-138 ...,
                                         1.00000000e+000]
    3.41045952e-163
                      8.75000000e-001
    2.66198872e-162
                      3.75270537e-153
                                         2.79210599e-144 ...,
    8.05448032e-170
                      8.75000000e-001
                                         7.35294118e-001]
                                         3.89698597e-128 ...,
 [ 4.23369661e-145
                      1.76818806e-136
    6.02054751e-134
                      7.50000000e-001
                                         7.35294118e-001]
    9.27540622e-141
                      2.81406311e-132
                                         4.50548081e-124 ...,
    3.85714932e-128
                      7.50000000e-001
                                         8.23529412e-001]
                                         2.20465991e-131 ...,
    1.41416988e-148
                      7.68486441e-140
    4.12235581e-133
                      7.50000000e-001
                                         8.23529412e-001]]
KR_regression coef length 375
<bound method KernelRidge.fit of KernelRidge(alpha=1.0, coef0=1, degree=3</pre>
, gamma=None, kernel='linear',
      kernel params=None)>
y50 128
y25 128
y01 128
x_fit [ -3.89237182e+00 -3.82032759e+00 -3.74828336e+00 -3.67623913e+0
  -3.60419490e+00
                   -3.53215067e+00
                                     -3.46010644e+00
                                                       -3.38806221e+00
  -3.31601798e+00
                   -3.24397374e+00
                                     -3.17192951e+00
                                                       -3.09988528e+00
  -3.02784105e+00
                   -2.95579682e+00
                                     -2.88375259e+00
                                                       -2.81170836e+00
  -2.73966413e+00
                   -2.66761990e+00
                                     -2.59557567e+00
                                                       -2.52353144e+00
  -2.45148721e+00
                   -2.37944298e+00
                                     -2.30739875e+00
                                                       -2.23535452e+00
                                                       -1.94717760e+00
  -2.16331029e+00
                   -2.09126606e+00
                                     -2.01922183e+00
  -1.87513337e+00
                   -1.80308914e+00
                                     -1.73104491e+00
                                                       -1.65900068e+00
  -1.58695645e+00
                   -1.51491221e+00
                                     -1.44286798e+00
                                                       -1.37082375e+00
  -1.29877952e+00
                   -1.22673529e+00
                                     -1.15469106e+00
                                                       -1.08264683e+00
  -1.01060260e+00
                   -9.38558371e-01
                                     -8.66514141e-01
                                                       -7.94469910e-01
  -7.22425680e-01
                   -6.50381450e-01
                                     -5.78337219e-01
                                                       -5.06292989e-01
  -4.34248758e-01
                   -3.62204528e-01
                                     -2.90160297e-01
                                                       -2.18116067e-01
  -1.46071837e-01
                   -7.40276062e-02
                                     -1.98337577e-03
                                                        7.00608547e-02
   1.42105085e-01
                    2.14149315e-01
                                      2.86193546e-01
                                                        3.58237776e-01
                                      5.74370468e-01
   4.30282007e-01
                    5.02326237e-01
                                                        6.46414698e-01
                                      8.62547389e-01
                                                        9.34591620e-01
   7.18458928e-01
                    7.90503159e-01
   1.00663585e+00
                    1.07868008e+00
                                      1.15072431e+00
                                                        1.22276854e+00
   1.29481277e+00
                    1.36685700e+00
                                      1.43890123e+00
                                                        1.51094546e+00
   1.58298969e+00
                    1.65503392e+00
                                      1.72707815e+00
                                                        1.79912238e+00
   1.87116662e+00
                    1.94321085e+00
                                      2.01525508e+00
                                                        2.08729931e+00
   2.15934354e+00
                    2.23138777e+00
                                      2.30343200e+00
                                                        2.37547623e+00
   2.44752046e+00
                    2.51956469e+00
                                      2.59160892e+00
                                                        2.66365315e+00
   2.73569738e+00
                    2.80774161e+00
                                      2.87978584e+00
                                                        2.95183007e+00
   3.02387430e+00
                    3.09591853e+00
                                      3.16796276e+00
                                                        3.24000699e+001
                      1.49177477
y_fit [ 1.35915875
                                    1.63473648
                                                1.78856068
                                                              1.95375917
   2.13083492
                2.32027792
                              2.52256077
                                           2.73813396
                                                         2.96742105
   3.2108135
                3.46866545
                              3.74128829
                                           4.0289452
                                                         4.33184565
   4.65013983
                4.98391328
                              5.33318155
                                           5.69788508
                                                         6.07788432
   6.47295518
                6.88278488
                              7.30696822
                                           7.74500437
                                                         8.19629426
   8.66013861
                9.13573662
                              9.62218548
                                          10.11848062
                                                        10.62351683
  11.13609027
               11.65490134
                             12.17855849
                                          12.705583
                                                        13.23441457
  13.76341796
               14.2908904
                             14.81506989
                                          15.33414434
                                                        15.84626139
  16.34953895
               16.84207633
                             17.32196588
                                          17.78730501
                                                        18.23620863
               19.07733168
                             19.46598162
                                          19.83108216
  18.66682165
                                                        20.17102394
  20.48428936
               20.76946384
                             21.02524646
                                          21.25045979
                                                        21.444059
  21.60513985
               21.73294579
                             21.82687381
                                          21.88647925
                                                        21.91147927
  21.90175507
               21.85735288
                             21.77848354
                                          21.66552086
                                                        21.51899869
  21.33960665
               21.12818481
                             20.88571707
                                          20.61332355
                                                        20.312252
  19.98386826
               19.62964594
                             19.25115545
                                          18.8500524
                                                        18.42806557
  17.98698457
               17.52864727
                             17.05492711
                                          16.56772051
                                                        16.0689344
                                                                     15.560
474
  15.044231
               14.52207215
                             13.99582854
                                          13.46728537
                                                        12.93817254
                             11.36370951
                                                        10.3397184
  12.410156
               11.88482986
                                          10.84822549
```

Histogram of Kernel_Ridge_Regression : μ = 0.099, σ = 1.616

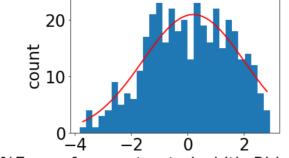


%Error of reconstructed width_Ridge_ridge

```
In [42]: #ridge regression:
         clf = Ridge(alpha=1.0)
         print(clf.fit)
         print('w', rebinned data)
         clf.fit(noisy_rebinned_data, y0)
         print('Ridge regression coef length',len(clf.coef )) #coefficients of pr
         ediction function
         print(clf.fit)
         #50% validation data
         y_pred50=clf.predict(noisy_rebinned_data50) #prediction function Ridge R
         earession
         print('y50',len(y50))
         Error K ridge regression50=((y50-y pred50)*100)/(y50)
         #25% validation data
         y_pred25=clf.predict(noisy_rebinned_data25) #prediction function Ridge R
         egression
         print('y25',len(y25))
         Error_K_ridge_regression25=((y25-y_pred25)*100)/(y25)
         #01% validation data
         y_pred01=clf.predict(noisy_rebinned_data01) #prediction function Ridge R
         egression
         print('y01',len(y01))
         Error_K_ridge_regression01=((y01-y_pred01)*100)/(y01)
         matplotlib.rcParams.update({'font.size': 26}) #coefficients of predictio
         n function
         #plt.figure(10)
         #plt.plot(clf.dual_coef_)
         #plt.plot(noisy_rebinned_data[10,:]/5)
         #plt.ylabel('weight')
         #plt.xlabel('coefficients and original profile')
         total error=[]
         total_error=np.concatenate((Error_K_ridge_regression50,Error_K_ridge_reg
         ression25,Error_K_ridge_regression01), axis=0)
         mu = np.mean(total error)
         sigma = np.std(total_error)
         x1 = total_error
         plt.figure(27)
         data = py.hist(x1, bins = 30)
         #Equation for Gaussian
         def f(x, a, b, c):
             return a * py.exp(-(x - b*b)**2.0 / (2 * c**2))
         # Generate data from bins as a set of points
         x = [0.5 * (data[1][i] + data[1][i+1]) for i in range(len(data[1])-1)]
         y = data[0]
         popt, pcov = optimize.curve_fit(f, x, y)
         x_{fit} = py.linspace(x[0], x[-1], 100)
         print('x_fit',x_fit)
         y_fit = f(x_fit, *popt) #generates the fitting-curve
         print('y_fit',y_fit)
         print('constant:a. mean:b. sigma:c'.*popt)
```

```
<bound method Ridge.fit of Ridge(alpha=1.0, copy X=True, fit intercept=Tr</pre>
ue, max iter=None,
   normalize=False, random state=None, solver='auto', tol=0.001)>
w = 2.57263727e - 137 = 6.04419396e - 129 = 7.49405765e - 121 \dots
    5.78008700e-146
                       8.75000000e-001
                                           9.11764706e-0011
    6.95857486e-156
                       6.25892641e-147
                                           2.97057423e-138 ...,
                       8.75000000e-001
                                           1.00000000e+000]
    3.41045952e-163
    2.66198872e-162
                       3.75270537e-153
                                           2.79210599e-144 ...,
    8.05448032e-170
                        8.75000000e-001
                                           7.35294118e-001]
                                           3.89698597e-128 ...,
 [ 4.23369661e-145
                        1.76818806e-136
    6.02054751e-134
                        7.50000000e-001
                                           7.35294118e-001]
    9.27540622e-141
                        2.81406311e-132
                                           4.50548081e-124 ...,
    3.85714932e-128
                        7.50000000e-001
                                           8.23529412e-001]
                                           2.20465991e-131 ...,
    1.41416988e-148
                        7.68486441e-140
    4.12235581e-133
                        7.50000000e-001
                                           8.23529412e-001]]
Ridge_regression coef length 102
<bound method Ridge.fit of Ridge(alpha=1.0, copy_X=True, fit_intercept=Tr</pre>
ue, max_iter=None,
   normalize=False, random state=None, solver='auto', tol=0.001)>
y50 128
y25 128
y01 128
x_fit [-3.72356675 -3.65739444 -3.59122213 -3.52504982 -3.45887751 -3.392
 -3.32653289 -3.26036058 -3.19418826 -3.12801595 -3.06184364 -2.99567133
 -2.92949902 -2.86332671 -2.7971544 -2.73098208 -2.66480977 -2.59863746
 -2.53246515 -2.46629284 -2.40012053 -2.33394822 -2.2677759 -2.20160359 -2.13543128 -2.06925897 -2.00308666 -1.93691435 -1.87074204 -1.80456973
 -1.73839741 -1.6722251 -1.60605279 -1.53988048 -1.47370817 -1.40753586
 -1.34136355 -1.27519123 -1.20901892 -1.14284661 -1.0766743 -1.01050199
 -0.94432968 -0.87815737 -0.81198505 -0.74581274 -0.67964043 -0.61346812
 -0.54729581 \ -0.4811235 \ -0.41495119 \ -0.34877888 \ -0.28260656 \ -0.21643425
 -0.15026194 -0.08408963 -0.01791732 0.04825499 0.1144273 0.18059962 0.24677193 0.31294424 0.37911655 0.44528886 0.51146117 0.57763348 0.6438058 0.70997811 0.77615042 0.84232273 0.90849504 0.97466735
  1.04083966 1.10701197 1.17318429 1.2393566
                                                      1.30552891 1.37170122
  1.43787353 1.50404584 1.57021815 1.63639047 1.70256278 1.76873509
  1.8349074
               1.90107971 1.96725202 2.03342433 2.09959664 2.16576896
  2.23194127 2.29811358 2.36428589 2.4304582
                                                      2.49663051 2.56280282
  2.62897514 2.69514745 2.76131976 2.82749207]
y_fit [ 1.97028116
                                                    2.48624061
                       2.13197158 2.30384396
                                                                  2.67948727
                               3.3272696
                                                            3.81830909
   2.88388995
                 3.09973178
                                             3.56673065
   4.08216255
                 4.35840869
                              4.64712179
                                            4.94832941
                                                            5.26200912
   5.5880854
                 5.92642672
                             6.27684274
                                             6.63908185
                                                            7.01282889
   7.39770327
                 7.79325735
                              8.19897521 8.61427187
                                                            9.03849288
                9.91074377 10.35712052 10.80911798 11.26574533
12.18862203 12.65259533 13.11665427 13.57953723
14.49653148 14.94793971 15.3927784 15.82964379
   9.4709144
  11.72595024
                12.18862203
                14.49653148
  14.03994201
                              17.07828231 17.46916289 17.84507779
                16.67380537
  16.25712377
  18.20468808 18.54669302
                              18.86983796 19.17292189 19.45480493
  19.7144154
                19.95075665
                              20.16291339 20.35005761 20.51145397
  20.6464646
                20.75455328
                              20.83528904 20.88834898 20.91352041
  20.91070234 20.87990606
20.48107158 20.31443848
                              20.82125516 20.73498461
20.12219783 19.90510403
                                                          20.62143928
                                                          19.66400312
                              18.80637336
  19.39982723 19.11358866
                                            18.4793341
                                                           18.13368329
  17.77068549 17.39164973
                              16.99792172 16.5908759
                                                           16.17190755
                              14.85756802 14.40500599 13.94753965
  15.74242491 15.30384139
                                                         11.63309008
  13.48652965 13.02330656
                              12.55916485 12.09535734
  9.8216645
                                                            9.38325911
   8.95242659
                8.52994582
                              8.11652672
                                             7.71280973
                                                            7.3193659 1
constant:a, mean:b, sigma:c 20.9157538149 -0.455001681828 1.80831114614
```

Histogram of RidgeRegression: $\mu = 0.044$, $\sigma = 1.476$

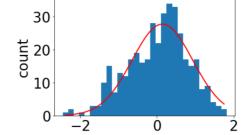


%Error of reconstructed width_Ridge_ridge

```
In [48]: #Using SVM for regression (SVR) :
         clf = SVR(C=10, cache size=200, coef0=0.0, degree=3, epsilon=0.01, gamma
         =0.01, \
                 kernel='rbf', max iter=-1, shrinking=True, tol=0.001, verbose=Fa
         lse)
         #print('SVR_regression_coefficients',clf.dual coef )
         print(clf.fit)
         print('w', rebinned data)
         clf.fit(noisy_rebinned_data, y0)
         print('KR regression coef length',len(clf.dual coef )) #coefficients of
         prediction function
         print(clf.fit)
         #50% validation data
         y_pred50=clf.predict(noisy_rebinned_data50) #prediction function Ridge R
         egression
         print('y50',len(y50))
         Error_K_ridge_regression50=((y50-y_pred50)*100)/(y50)
         #25% validation data
         y_pred25=clf.predict(noisy_rebinned_data25) #prediction function Ridge R
         egression
         print('y25',len(y25))
         Error_K_ridge_regression25=((y25-y_pred25)*100)/(y25)
         #01% validation data
         y_pred01=clf.predict(noisy_rebinned_data01) #prediction function Ridge R
         egression
         print('y01',len(y01))
         Error_K_ridge_regression01=((y01-y_pred01)*100)/(y01)
         matplotlib.rcParams.update({'font.size': 26}) #coefficients of predictio
         n function
         #plt.figure(10)
         #plt.plot(clf.dual_coef_)
         #plt.plot(noisy_rebinned_data[10,:]/5)
         #plt.ylabel('weight')
         #plt.xlabel('coefficients and original profile')
         total_error=[]
         total_error=np.concatenate((Error_K_ridge_regression50,Error_K_ridge_reg
         ression25,Error_K_ridge_regression01), axis=0)
         mu = np.mean(total error)
         sigma = np.std(total_error)
         x1 = total_error
         plt.figure(27)
         data = py.hist(x1, bins = 30)
         #Equation for Gaussian
         def f(x, a, b, c):
             return a * py.exp(-(x - b*b)**2.0 / (2 * c**2))
         # Generate data from bins as a set of points
         x = [0.5 * (data[1][i] + data[1][i+1]) for i in range(len(data[1])-1)]
         y = data[0]
         popt, pcov = optimize.curve_fit(f, x, y)
         x fit = pv.linspace(x[0]. x[-1]. 100)
```

```
<bound method BaseLibSVM.fit of SVR(C=10, cache size=200, coef0=0.0, degr</pre>
ee=3, epsilon=0.01, gamma=0.01,
  kernel='rbf', max iter=-1, shrinking=True, tol=0.001, verbose=False)>
w [[ 2.57263727e-137
                       6.04419396e-129 7.49405765e-121 ...,
    5.78008700e-146
                    8.75000000e-001
                                       9.11764706e-0011
   6.95857486e-156
                     6.25892641e-147
                                       2.97057423e-138 ...,
                     8.75000000e-001
                                       1.00000000e+000]
    3.41045952e-163
    2.66198872e-162
                     3.75270537e-153
                                       2.79210599e-144 ...,
    8.05448032e-170
                     8.75000000e-001
                                       7.35294118e-001]
                                       3.89698597e-128 ...,
 [ 4.23369661e-145
                     1.76818806e-136
    6.02054751e-134
                     7.50000000e-001
                                       7.35294118e-001]
   9.27540622e-141
                     2.81406311e-132
                                       4.50548081e-124 ...,
    3.85714932e-128
                     7.50000000e-001
                                       8.23529412e-001]
                                       2.20465991e-131 ...,
   1.41416988e-148
                     7.68486441e-140
    4.12235581e-133
                     7.50000000e-001
                                       8.23529412e-001]]
KR_regression coef length 1
<bound method BaseLibSVM.fit of SVR(C=10, cache_size=200, coef0=0.0, degr</pre>
ee=3, epsilon=0.01, gamma=0.01,
  kernel='rbf', max iter=-1, shrinking=True, tol=0.001, verbose=False)>
y50 128
y25 128
y01 128
x_fit [-2.38881189 -2.34698372 -2.30515555 -2.26332737 -2.2214992 -2.179
 -2.13784286 -2.09601469 -2.05418652 -2.01235835 -1.97053018 -1.92870201
 -1.38493579 -1.34310762 -1.30127945 -1.25945128 -1.21762311 -1.17579493
 -1.13396676 -1.09213859 -1.05031042 -1.00848225 -0.96665408 -0.92482591
 -0.88299774 \ -0.84116957 \ -0.7993414 \ -0.75751323 \ -0.71568506 \ -0.67385689
 -0.63202871 -0.59020054 -0.54837237 -0.5065442 -0.46471603 -0.42288786
 -0.38105969 \ -0.33923152 \ -0.29740335 \ -0.25557518 \ -0.21374701 \ -0.17191884
 -0.13009067 \ -0.08826249 \ -0.04643432 \ -0.00460615 \ \ 0.03722202 \ \ 0.07905019
  0.12087836
             0.16270653 0.2045347
                                     0.24636287 0.28819104 0.33001921
             0.41367555 0.45550372 0.4973319
  0.37184738
                                                 0.53916007
                                                             0.58098824
  0.62281641 \quad 0.66464458 \quad 0.70647275 \quad 0.74830092 \quad 0.79012909 \quad 0.83195726
  0.87378543 0.9156136
                         0.95744177 0.99926994 1.04109812
                                                             1.08292629
  1.12475446 1.16658263 1.2084108
                                     1.25023897 1.29206714
                                                             1.33389531
  1.37572348 1.41755165 1.45937982 1.50120799
                                                 1.54303616 1.58486434
  1.62669251
             1.66852068 1.71034885 1.75217702]
y_fit [ 0.16581229
                     0.19610332
                                               0.2720067
                                  0.23128062
                                                            0.31901127
                                         0.58691112
                                                      0.67878005
   0.37309421
               0.43512802
                            0.50605959
                                         1.18090957
   0.78283795
               0.90032795
                            1.03256085
                                                      1.34680181
   1.5317109
               1.73714462
                           1.964632
                                         2.21570794
                                                      2.49189579
   2.79468782
               3.12552366
                            3.4857669
                                         3.87668002
                                                      4.29939782
   4.75489982
                                         6.32497722
               5.24398178
                            5.7672269
                                                      6.91730549
   7.54398835
               8.20448121
                            8.89789555
                                         9.62297914
                                                     10.37809993
                           12.80144917
  11.16123404
              11.96995848
                                        13.65248446
                                                     14.51945478
                           17.17443812 18.06198204
  15.39837844
              16.28492384
                                                     18.94237095
  19.81022148
                           21.48609577 22.28284756
              20.66000336
                                                     23.04464032
                                                     26.14310092
  23.76595343
              24.44143002
                           25.06594285 25.63465877
  26.58720723 26.96338449
                           27.26855667 27.50020687
                                                     27.65641179
                           27.66252541 27.51033944
  27.73586839
              27.73791197
                                                     27.28262382
  26.98126972
              26.60876357
                           26.1681529
                                        25.66300482
                                                     25.09735796
                           23.08372436
  24.47566877
              23.80275312
                                        22.32392888
                                                     21.52888032
  20.70419357
              19.85551966
                           18.98848253
                                        18.10861867
                                                     17.22132054
  16.33178446 15.4449637
                           14.56552715 13.6978241
                                                     12.84585529
                                         9.66205298
  12.01325037
              11.20325173
                           10.41870456
                                                      8.93534177
   8.24022339
               7.57796971
                            6.94948797
                                         6.35534034
                                                      5.7957665
   5.27070866
               4.77983829
                            4.32258418
                                         3.89816106
                                                      3.50559839]
constant:a, mean:b, sigma:c 27.7466100434 -0.378014516514 0.791157420439
```

Histogram of SupportVectorRegression: $\mu = 0.030$, $\sigma = 0.779$



%Error of reconstructed width_Ridge_ridge