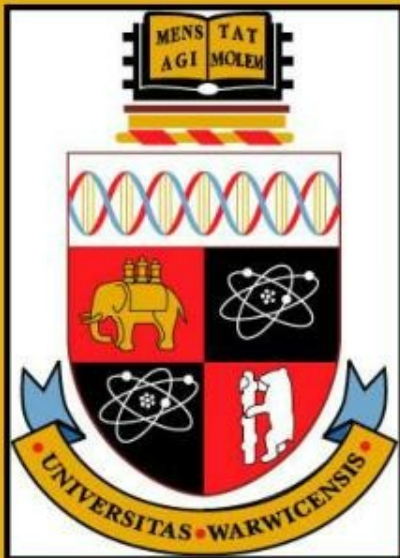


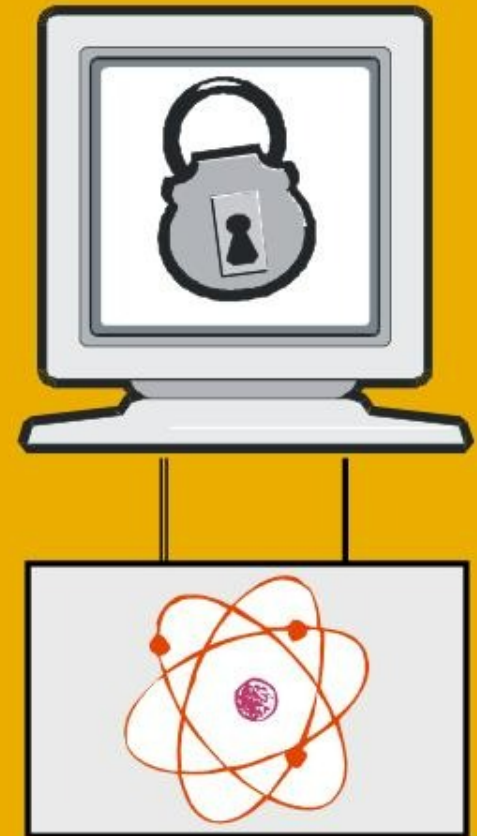
Quantum Cryptography



Nick Papanikolaou

Introduction

- Quantum cryptography is the single **most successful application** of Quantum Computing/Information Theory.
- **For the first time in history**, we can hope to use the forces of nature to implement **perfectly secure** cryptosystems.
- Quantum cryptography **works in practice!**



State of the Art

- Classical Cryptosystems such as RSA relies on the **complexity of factoring integers**.
- Quantum Computers can use **Shor's Algorithm** to efficiently break today's cryptosystems.
- We need a **new kind** of cryptography!

Today's Talk

- Basic Ideas in **Cryptography**
- Ideas from the **Quantum World**
- Quantum Key Distribution (**QKD**)
- **BB84** without eavesdropping
- **BB84** with eavesdropping
- Working **Prototypes**
- Research here at **Warwick**
- **Conclusion**

Basic Ideas in Cryptography

- **Cryptography:** “the coding and decoding of secret messages.” [Merriam-Webster]
- Cryptography < κρυπτός + γραφή.
- The basic idea is **to modify a message so as to make it unintelligible to anyone but the intended recipient.**
- For message (plaintext) M ,
 $e(M, K)$ **encryption -**
ciphertext
 $d[e(M, K), K] = M$ **decryption**

Keys and Key Distribution

- **K** is called the **key**.
- The key is known only to sender and receiver: it is **secret**.
- **Anyone** who knows the key can decrypt the message.
- **Key distribution** is the problem of exchanging the key between sender and receiver.



Perfect Secrecy and the OTP

- There exist **perfect cryptosystems**.
- Example: **One-Time Pad (OTP)**
- The problem of **distributing the keys** in the first place remains.



Enter QKD ...

- QKD: **Quantum Key Distribution**
- Using **quantum effects**, we can distribute keys in perfect secrecy!
- The Result: The Perfect Cryptosystem,

QC = QKD + OTP



Ideas from the Quantum World

■ Measurement

- Observing, or **measuring**, a quantum system will alter its state.
- Example: the **Qubit**

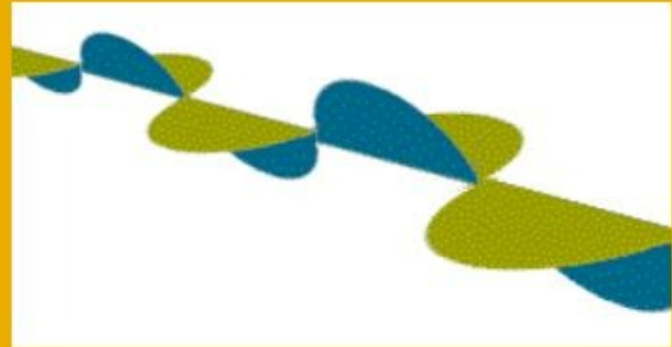
$$|\psi\rangle = a \cdot |0\rangle + b \cdot |1\rangle$$

- When observed, the state of a qubit will **collapse** to either $a=0$ or $b=0$.

Photons

■ Physical qubits

- Any **subatomic particle** can be used to represent a qubit, e.g. an electron.
- A **photon** is a convenient choice.
- A photon is an **electromagnetic wave**.



Polarization

- A photon has a property called **polarization**, which is the plane in which the electric field oscillates.
- We can use photons of different polarizations to represent quantum states:

$$\theta = 0^\circ \Rightarrow \text{state } |0\rangle$$

$$\theta' = 90^\circ \Rightarrow \text{state } |1\rangle$$

Polarizers and Bases

- A device called a **polarizer** allows us to place a photon in a particular polarization. A **Pockels Cell** can be used too.
- The polarization **basis** is the mapping we decide to use for a particular state.

Rectilinear:

$$\theta = 0^\circ \Rightarrow \text{state } |0\rangle$$

$$\theta' = 90^\circ \Rightarrow \text{state } |1\rangle$$

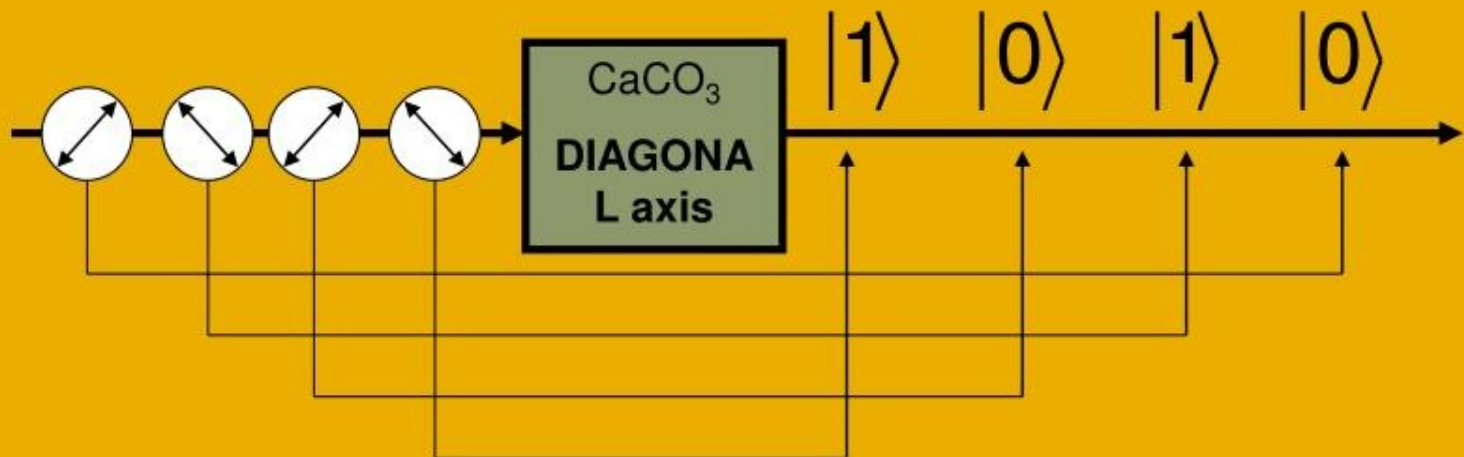
Diagonal:

$$\theta = 45^\circ \Rightarrow \text{state } |0\rangle$$

$$\theta' = 135^\circ \Rightarrow \text{state } |1\rangle$$

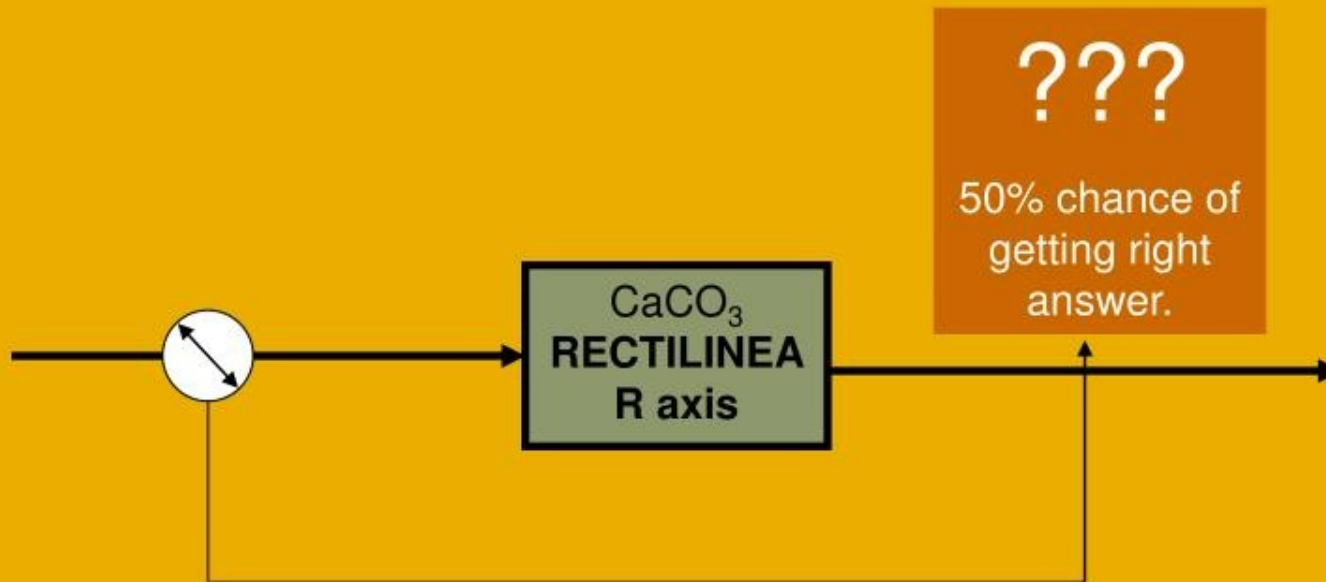
Measuring Photons

- A **calcite crystal** can be used to recover the bits encoded into a stream of photons.



Uncertainty Principle

- What if the crystal has the **wrong orientation**?



Meet Alice and Bob



Alan J. Learner,
Quantum
Cryptographer

We have to prevent **Eve** from **eavesdropping** on communications between **Alice** and **Bob**.



Ev
e

Alice



Bob



Quantum Key Distribution

- **Quantum Key Distribution** exploits the effects discussed in order to **thwart eavesdropping**.
- If an eavesdropper uses the wrong polarization basis to measure the channel, **the result of the measurement will be random**.

QKD Protocols

- A **protocol** is a set of rules governing the exchange of messages over a channel.
- A **security protocol** is a special protocol designed to ensure security properties are met during communications.
- There are three main security protocols for QKD: **BB84**, **B92**, and **Entanglement-Based QKD**.
- We will only discuss **BB84** here.






BB84 ...

- **BB84** was the first security protocol implementing Quantum Key Distribution.
- It uses the idea of **photon polarization**.
- The **key** consists of bits that will be transmitted as photons.
- Each bit is encoded with a **random polarization basis!**

BB84 with no eavesdropping






- **Alice** is going to send **Bob** a key.
- She begins with a **random sequence of bits**.
- Bits are encoded with a **random basis**, and then sent to Bob:



Bit	0	1	0	1	1
Basis	+	×	×	+	×
Photon					

BB84 with no eavesdropping (2)

- **Bob receives the photons** and must decode them using a random basis.

Photon					
Basis?	+	+	x	+	x
Bit?	0	0	0	1	1






- **Some** of his measurements are correct.



BB84 with no eavesdropping (3)

- Alice and Bob talk **on the telephone**:
 - **Alice** chooses a subset of the bits (the **test bits**) and reveals which basis she used to encode them to Bob.
 - **Bob** tells Alice which basis he used to decode **the same** bits.
 - **Where the same basis was used**, Alice tells Bob what bits he ought to have got.

Comparing measurements

Alice's Bit	0	1	0	1	1
Alice's Basis	+	x	x	+	x
Photon					
Bob's Basis	+	+	x	+	x
Bob's Bit	0	0	0	1	1

Test bits








The **test bits** allow Alice and Bob to test **whether the channel is secure**.

The Trick

- As long as no errors and/or eavesdropping have occurred, **the test bits should agree.**
- Alice and Bob have now made sure that **the channel is secure.** The test bits are removed.
- Alice tells Bob **the basis she used for the other bits**, and they both have a common set of bits: the final key!

Getting the Final Key

Alice's Bit	0	1	0	1	1
Alice's Basis	+	x	x	+	x
Photon					
Bob's Basis	+	+	x	+	x
Bob's Bit	0	0	0	1	1

Test bits
discarded

Final Key = 01

In the presence of eavesdropping

- If an eavesdropper **Eve** tries to tap the channel, this will automatically show up in Bob's measurements.
- In those cases where **Alice and Bob** have used the same basis, Bob is likely to obtain an **incorrect measurement**: Eve's measurements are bound to affect the states of the photons.

Working Prototypes

- Quantum cryptography has been tried experimentally over **fibre-optic cables** and, more recently, **open air (23km)**.



Left: The first prototype implementation of quantum cryptography (IBM, 1989)

Research at Warwick

- *RN* and *NP* are working on **Specification and Verification** of Quantum Protocols.
 - **Specifying a system formally** removes ambiguities from descriptions.
 - Verification allows us **to prove that a protocol is indeed secure** and operates correctly under certain input conditions.



Conclusion

- Quantum cryptography is a **major achievement** in security engineering.
- As it gets implemented, it will allow perfectly secure **bank transactions**, secret discussions for **government** officials, and well-guarded **trade secrets** for industry!