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Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

1 STABILITY

1.1 Second order System

1.1. The Block diagram of a system is illustrated in the figure shown, where $X(s)$ is the input and $Y(s)$ is the output. The transfer function $H(s) = Y(s)/X(s)$

$$H(s) = \frac{Y(s)}{X(s)} \quad (1.1.1)$$

$$H(s) = \frac{s^2 + 1}{s^3 + s^2 + s + 1} \quad (1.1.2)$$

$$H(s) = \frac{s^2 + 1}{s^3 + 2s^2 + s + 1} \quad (1.1.3)$$

$$H(s) = \frac{s^2 + 1}{s^2 + s + 1} \quad (1.1.4)$$

$$H(s) = \frac{s^2 + 1}{2s^2 + 1} \quad (1.1.5)$$

Solution: Here we have two transfer functions s and $\frac{1}{s}$ in parallel with an adder as shown in figure. After solving these two parallel transfer functions by just adding both of them we will get

Now we will convert three input adder into two input adder as shown in figure given below.

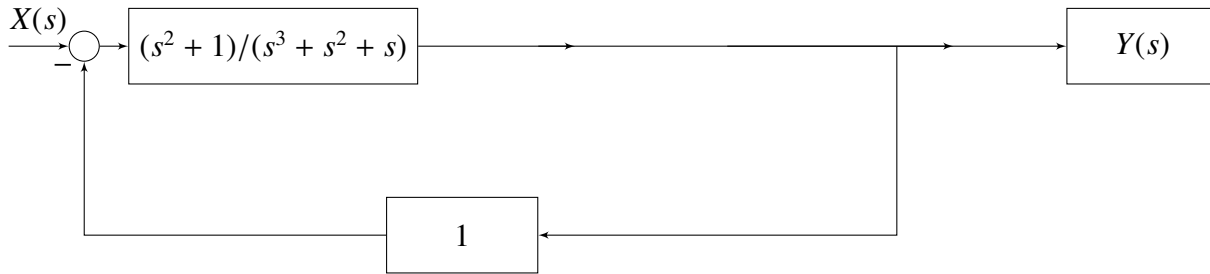
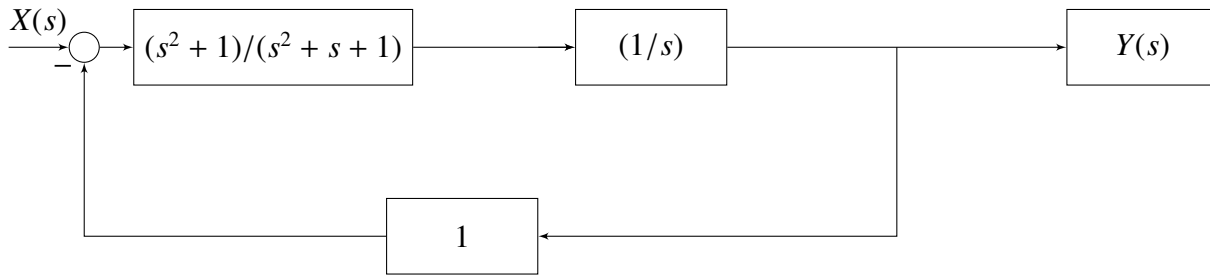
Now we have Negative Unity Feedback System (NUFS) in closed loop transfer function. Let's say we have transfer function $G(s)$ with Negative Unity Feedback System in closed loop then we will solve this by

$$H(s) = \frac{G(s)}{1 + G(s)} \quad (1.1.6)$$

Here we have two transfer functions in series. Now we have one more transfer function with negative unity feedback.

Again we will solve this then we will get

$$X(s) \left(\frac{s^2 + 1}{s^3 + 2s^2 + s + 1} \right) = Y(s) \quad (1.1.7)$$



$$\frac{Y(s)}{X(s)} = \frac{s^2 + 1}{s^3 + 2s^2 + s + 1} \quad (1.1.8)$$

2 ROUTH HURWITZ CRITERION

3 COMPENSATORS

4 NYQUIST PLOT

