

Fig. 1.1

## CONTENTS

**Abstract**—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

## 1 STABILITY

## 1.1 Second order System

1.1. The Block diagram of a system is illustrated in the figure shown, where  $X(s)$  is the input and  $Y(s)$  is the output. The transfer function  $H(s) = Y(s)/X(s)$

$$H(s) = \frac{Y(s)}{X(s)} \quad (1.1.1)$$

Options -

$$(A) - H(s) = \frac{s^2 + 1}{s^3 + s^2 + s + 1} \quad (1.1.2)$$

$$(B) - H(s) = \frac{s^2 + 1}{s^3 + 2s^2 + s + 1} \quad (1.1.3)$$

$$(C) - H(s) = \frac{s^2 + 1}{s^2 + s + 1} \quad (1.1.4)$$

$$(D) - H(s) = \frac{s^2 + 1}{2s^2 + 1} \quad (1.1.5)$$

**Solution:** Mason's Gain Formula-

$$T = \frac{Y(s)}{X(s)} \quad (1.1.6)$$

$$T = \frac{\sum_{i=1}^N P_i \Delta_i}{\Delta} \quad (1.1.7)$$

Now, Signal flow graph of given above block diagram is

$P_i$  is the  $i$ th forward path.

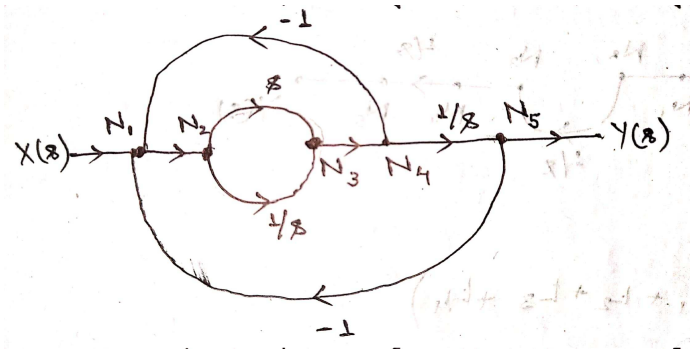


Fig. 1.1: signal flow graph

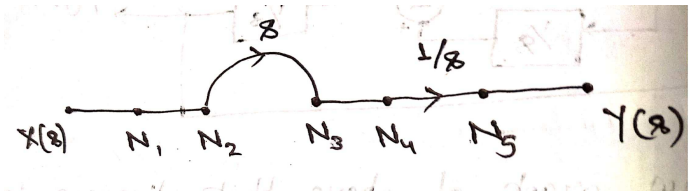


Fig. 1.1: P1

Here,

$$P_1 = \frac{s}{s} = 1 \quad (1.1.8)$$

$$P_2 = (1/s)(1/s) = 1/s^2 \quad (1.1.9)$$

$$\Delta = 1 - (L_1 + L_2 + L_3 + L_4)$$

$$L_1 = (-1)(s) = -s \quad (1.1.10)$$

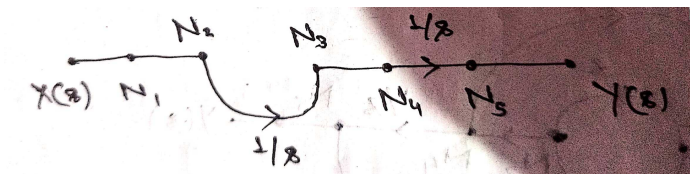


Fig. 1.1: P2

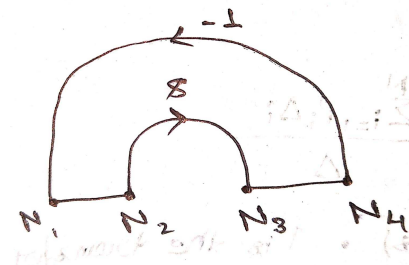


Fig. 1.1: L1

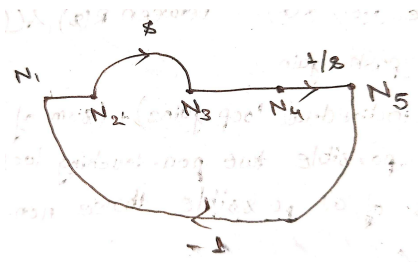


Fig. 1.1: L2

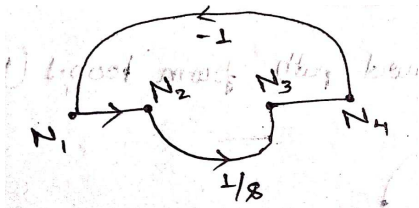


Fig. 1.1: L3

$$L_2 = \frac{s}{-s} = -1 \quad (1.1.11)$$

$$L_3 = \left(\frac{1}{s}\right) * (-1) = \frac{-1}{s} \quad (1.1.12)$$

$$L_4 = \left(\frac{1}{s}\right) * \left(\frac{1}{s}\right) 8(-1) = \frac{-1}{s^2} \quad (1.1.13)$$

$$\Delta = 1 - (-s - 1 - \frac{1}{s} - \frac{1}{s^2}) \quad \Delta = \frac{s^3 + 2s^2 + s + 1}{s^2}$$

$$\Delta_1 = 1$$

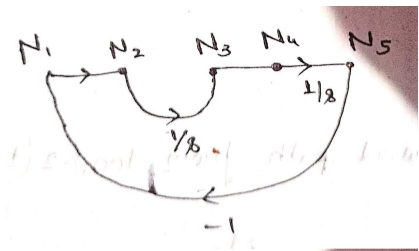


Fig. 1.1: L4



Fig. 1.1: Delta1



Fig. 1.1: Delta2

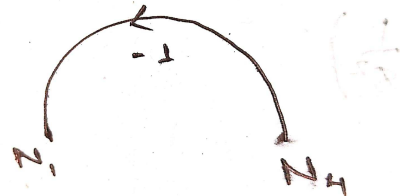


Fig. 1.1: Delta3

$\Delta_2 = 1$   
 $\Delta_3 = 1$   
 $\Delta_4 = 1$   
 Here,

$$T = \frac{\sum_{i=1}^N (P_i)(\Delta_i)}{\Delta} \quad (1.1.14)$$

$$T = \frac{P_1\Delta_1 + P_2\Delta_2 + P_3\Delta_3 + P_4\Delta_4}{\Delta} \quad (1.1.15)$$

$$T = \frac{1 * 1 + \left(\frac{1}{s^2}\right) * 1 + 0 * 1 + 0 * 1}{\frac{s^3 + 2s^2 + s + 1}{s^2}} \quad (1.1.16)$$

$$H(s) = \frac{s^2 + 1}{s^3 + 2s^2 + s + 1} \quad (1.1.17)$$

## 2 ROUTH HURWITZ CRITERION

### 3 COMPENSATORS

### 4 NYQUIST PLOT



Fig. 1.1: Delta4