Functional programming, Seminar No. 3

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Intro

On the previous seminar, we

- studied the basic Haskell syntax
- introduced the notion of a weak head normal form to describe the operatonal semantics of Haskell
- analysed the regrettable cicrumstances according to which Haskell doesn't have the Church-Rosser property as a system of typed lambda calculus

Intro

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- studied the basic Haskell syntax
- introduced the notion of a weak head normal form to describe the operatonal semantics of Haskell
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Today we

- investigate the Haskell type system more deeply and overview the advantages of parametric polymorphism
- take a look at bounded polymorphism and discuss type classes

Motivation

Let us recall the example of a higher order function from the previous seminar:

- $_{\scriptscriptstyle 1}$ changeTwiceBy :: $(\mathbf{Int} -> \mathbf{Int}) -> \mathbf{Int} -> \mathbf{Int}$
- changeTwiceBy operation value = operation (operation value)

It is clear that one may implement the function for Boolean values and strings that have the same behaviour as the function above:

- $_{\scriptscriptstyle 1}$ changeTwiceByBool :: (Bool -> Bool) -> Bool -> Bool
- changeTwiceByBool operation value = operation (operation value)
- changeTwiceByString :: (String -> String) -> String -> String
 - changeTwiceByString operation value = operation (operation value)

Motivation

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It is clear that one may implement the function for Boolean values and strings that have the same behaviour as the function above:

- changeTwiceByBool :: (Bool -> Bool) -> Bool -> Bool
- changeTwiceByBool operation value = operation (operation value)
- changeTwiceByString :: (String -> String) -> String -> String
- ${}_{\scriptscriptstyle{5}}\quad \text{changeTwiceByString operation value} = \text{operation (operation value)}$

One needs to have a way to avoid such a boilerplate.

Parametric polymorphism

The key idea of parametric polymorphism that the same function might be called on distinct data types. Here are the initial polymorphic examples:

```
id :: a -> a
    id \times = \times
     const :: a \rightarrow b \rightarrow a
     const a b = a
     fst :: (a, b) \rightarrow a
    fst (a, b) = a
     snd :: (a. b) \rightarrow b
     \mathbf{snd} = "guess what"
11
12
     swap :: (a, b) -> (b, a)
     swap (a, b) = (b, a)
```

The meme time



The functions above in the GHCi session

```
Prelude> id 7
Prelude> id "strina"
"string"
Prelude> const 7 "string"
Prelude> const "string" 7
"string"
Prelude> fst (7, 'k')
Prelude> snd (7, 'k')
'k'
Prelude> fst (swap (7, 'k'))
'k'
```

Higher order functions and parametric polymorpism

```
infixr 9.
(.) :: (b -> c) -> (a -> b) -> a -> c
g = x - f(g x)
    flip :: (a -> b -> c) -> b -> a -> c
   flip f b a = f a b
   fix :: (a -> a) -> a
    fix = error "this is your homework"
10
    curry :: ((a, b) -> c) -> a -> b -> c
    \operatorname{\mathbf{currv}} f \times v = f(x, v)
13
    uncurry :: (a -> b -> c) -> ((a, b) -> c)
    uncurry f p = f (fst p) (snd p)
```

The functions above in the GHCi session. The composition examples

```
incNegate :: Int -> Int
incNegate x = negate (x + 1)

incNegate x = negate $ x + 1

incNegate x = (negate . (+1)) x

incNegate x = negate . (+1) $ x

incNegate x = negate . (+1)
```

The functions above in the GHCi session. curry and uncurry

```
Prelude> uncurry (+) (3,4)
Prelude> curry fst 3 4
Prelude> curry snd 3 4
Prelude> curry id 3 4
(3,4)
Prelude> uncurry const (3,4)
Prelude> uncurry (flip const) (3,4)
```

The functions above in the GHCi session. The flip example

```
show2 :: Int -> Int -> String
show2 x y = show x ++ " and " ++ show y

showSnd, showFst, showFst' :: Int -> String
showSnd = show2 1
showFst = flip show2 2
showFst' = ('show2' 2)
```

The functions above in the GHCi session. The flip example

```
show2 :: Int -> Int -> String
show2 x y = show x ++ " and " ++ show y

showSnd, showFst, showFst' :: Int -> String
showSnd = show2 1
showFst = flip show2 2
showFst' = ('show2' 2)
```

Prelude> showSnd 10
"1 and 10"
Prelude> showFst 10
"10 and 2"
Prelude> showFst' 42
"42 and 2"

Bye-bye boilerplate!

All these functions

```
changeTwiceBy :: (Int -> Int) -> Int -> Int
  changeTwiceBy operation value = operation (operation value)
  changeTwiceByBool :: (Bool -> Bool) -> Bool -> Bool
  changeTwiceByBool operation value = operation (operation value)
  changeTwiceByString :: (String -> String) -> String -> String
  changeTwiceByString operation value = operation (operation value)
might be replaced to the following ones:
  applyTwice :: (a -> a) -> a -> a
  applyTwice f a = f (f a)
  applyTwice' :: (a -> a) -> a -> a
  applyTwice' f a = f \cdot f  a
  applyTwice'' :: (a -> a) -> a -> a
  applyTwice" f = f \cdot f
```

HOF, polymorpism, and lists

HOF, polymorpism, and lists

```
1 map :: (a -> b) -> [a] -> [b]
3 filter :: (a -> Bool) -> [a] -> [a]
4 zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]
6 length :: [a] -> Int
```

We discuss their implementations closely on the next seminar. Here we just take a look at their behaviour.

The functions above in the GHCi session. The composition examples + list functions

```
foo, bar :: [Int] -> Int
foo patak = length $ filter odd $ map (div 2) $ filter even $ map (div 7) patak
bar = length . filter odd . map (div 2) . filter even . map (div 7)
```

The functions above in the GHCi session. The composition examples + list functions

```
stringsTransform :: [String] -> [String]
stringsTransform | = map (\s -> map toUpper s) (filter (\s -> length s == 5) |)

stringsTransform | = map (\s -> map toUpper s) $ filter (\s -> length s == 5) |

stringsTransform | = map (map toUpper) $ filter ((== 5) . length) |

stringsTransform = map (map toUpper) . filter ((== 5) . length)
```

Restricted strictness

Bounded polymorphism and type classes

The Eq type class

The Show type class

The Ord type class

The Num type class

The Enum type class

The Fractional type class

The Bounded type class

Summary