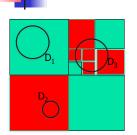


- Assume we are given a red/green picture defined on a $2^h \times 2^h$ grid of
- Each pixel has as a unique color (Green or Red)
- Every node $v \in T$ is associated with a geometric region R(v).
- This is the region that *v* is "in
- •Output a Quadtree T_{ij} representing the shape of S within R(v)).
- If S is fully green in R(v), or S is fully red in R(v) then
- v is a leaf, labeled Green or Red. Return;
- •Otherwise, divide R(v) into 4 equal-sized quadrants, corresponding to nodes v.NW. v.NE. v.SW. v.SE.
- Call ConstructOT recursively for each quadrant





Assume we are given a red/green picture defined a $2^h \times 2^h$ grid. E.g. pixels. Each pixel is either green or red.

(more general and interesting examples soon)

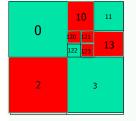
Need to represent the shape "compactly"

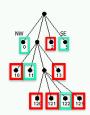
Need a data structure that could answers multiple types of queries. For example:

- 1. For a given point q, is q red or green?
- 2. For a given query disk D, are there any green points in D?
- 3. How many green points are there in D?
- 4. Etc etc

2







Consider a picture stored on an 2h × 2h grid. Each pixel is either red or green.

We can represent the shape "compactly" using a QT.

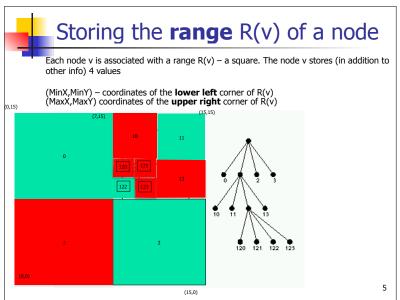
Height – at most h.

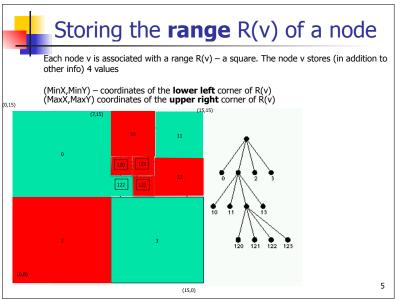
Point location operation – given a point q, is it black or white

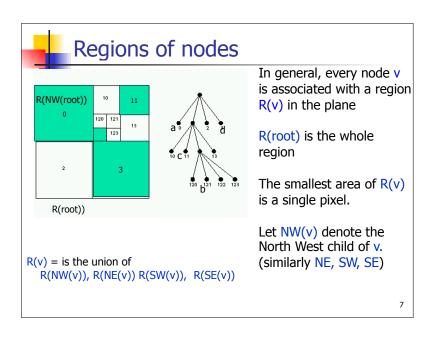
- takes time O(h)
- could it be much smaller ?

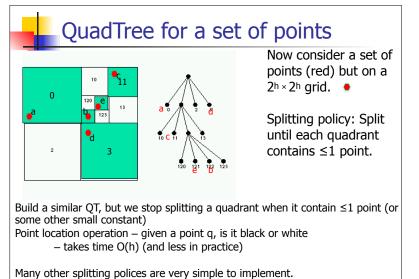
Many other operations are very simple to implement.

4



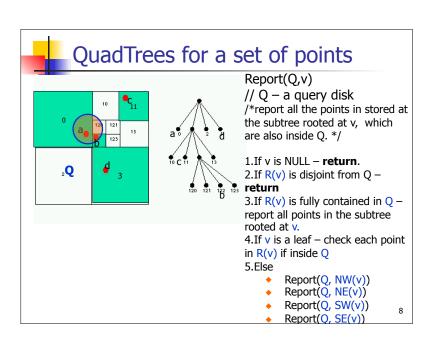


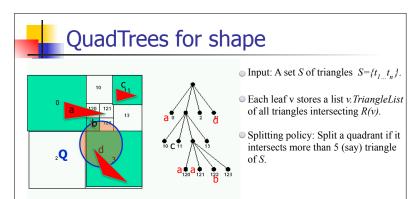




6

(eg. A leaf could contain contains ≤17 points)

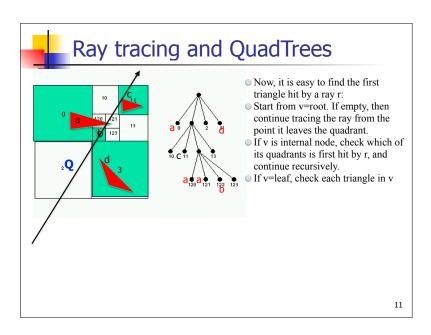


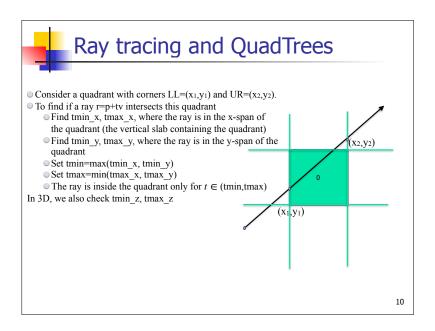


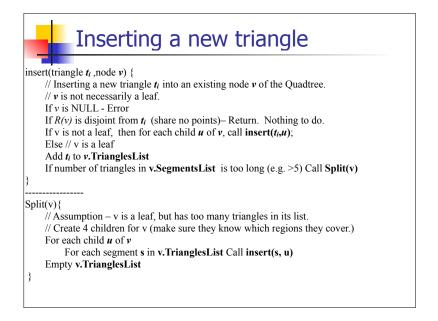
Note – a triangle might be stored in multiple leaves. Some leaves might store no triangles.

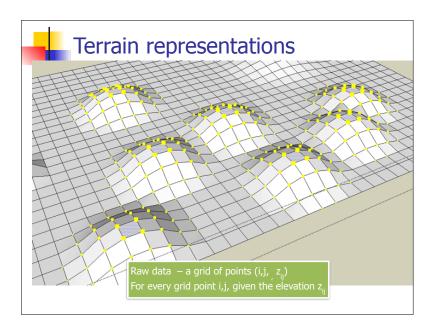
Finding all triangles inside a query region Q. We essentially use the function Report(Q,v) from the previous slide (with minor modifications)

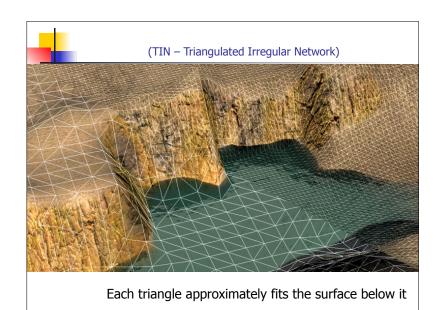
9

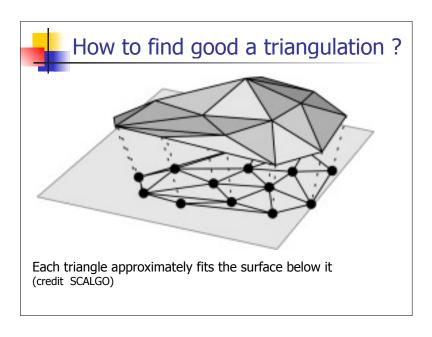


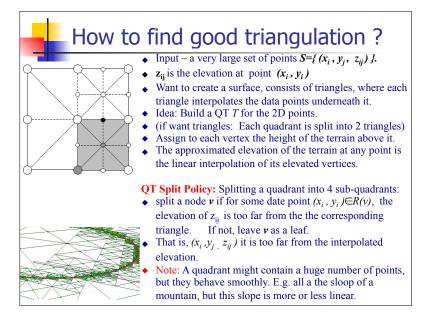








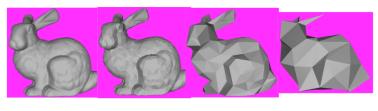






Level Of Details

- Idea the same object is stored several times, but with a different level of details
- Coarser representations for distant objects
- Decision which level to use is accepted `on the fly' (eg in graphics applications, if we are far away from a terrain, we could tolerate usually large error)



69,451 polys

2,502 polys

251 polys

76 polys

R-trees Input: A set S of shapes (segments in this example) Prepare a tree that could assists finding the segments intersecting a query region, answering ray tracing etc We compute for each segment its bounding box (rectangle). These are the leaves of T Match pairs of bounding boxes. For example 1-2, 3-4, 5-6, 7-8. For each such pair, compute their bounding boxes. Each node in level 2 is such a box. Match these bounding boxes. These are the nodes of level 3. Repeat until we are left with one bounding box. In general for every node v, BB(v) = BB(BB(v.right) \igcup BB(v.left)) Once a query region 0 is given we determine whether it intersect BB(v.left) Once a query region 0 is given we determine whether it intersect BB(v.left) S +6+7+8

