

## BSP tree

Given a set of triangles  $S=\{t_1...t_n\}$  in 3D, a BSP T, for S is an tree where 1. Each leaf stores a triangle  $t_i$ 

- 1. Each internal (non-leaf) node  $\ v$  stores a plane  $\ h_v$  and pointers to two children  $\ v$  .  $right, \ v$  . left
- 3. All triangles in the subtree v , left are fully **below**  $h_v$ , and all triangles in v , right are fully on or above  $h_v$



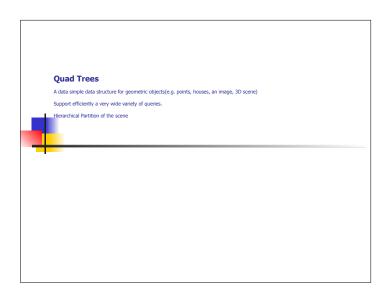
See further example on the board.

Sometimes we need to split triangles to construct the BSP

If a (perfect) BSP exist, then for any location of a viewer, we can use the painter algorithm.

Numerous other applications in graphics. (e.g. combine with imposers/billboards)

If the number of triangles above and below  $h_{\rm v}$  are roughly the same, then the height is  $O(\log n)$ 





Assume we are given a red/green picture defined a  $2^h \times 2^h$  grid. E.g. pixels. Each pixel is either **green** or **red**.

(more general and interesting examples – soon)

Need to represent the shape "compactly"

Need a data structure that could answers multiple types of queries. For example:

- 1. For a given point q, is q red or green?
- 2. For a given query disk D, are there any green points in D?
- 3. How many green points are there in D?
- 4.Etc etc

## QuadTrees NW 0 10 11 13 NW 2 SE

- Assume we are given a red/green picture defined on a 2h × 2h grid of pixels.
- Each pixel has as a unique color (Green or Red)
- Every node  $v \in T$  is associated
- with a geometric region R(v).
  This is the region that v is "in charge of".

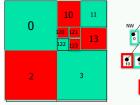
## Alg ConstructQT for a shape S.

**•input** – a node  $v \in T$ , and a shape S.

•Output – a Quadtree  $T_v$  representing the shape of S within R(v)).

- If S is fully green in R(v), or S is fully red in R(v) then
- v is a leaf, labeled Green or Red. Return;
- •Otherwise, divide R(v) into 4 equal-sized quadrants, corresponding to nodes v.NW, v.NE, v.SW, v.SE.
- Call ConstructQT recursively for each quadrant.

## QuadTrees





Consider a picture stored on an  $2^h \times 2^h$  grid. Each pixel is either red or green.

We can represent the shape "compactly" using a QT.

Height – at most h.

Point location operation – given a point q, is it black or white

- takes time O(h)
- could it be much smaller ?

Many other operations are very simple to implement.

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