



CSC380: Principles of Data Science

Predictive Modeling and Classification 1

Credit:

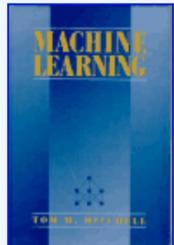
- Jason Pacheco,
- Kwang-Sung Jun,
- Chicheng Zhang
- Xinchen yu

Introduction to Machine Learning

What is machine learning?

- Tom Mitchell established Machine Learning Department at CMU (2006).

Machine Learning, Tom Mitchell, McGraw Hill, 1997. “**through experience**”



Machine Learning is the study of computer algorithms that improve automatically through experience. Applications range from datamining programs that discover general rules in large data sets, to information filtering systems that automatically learn users' interests.

This book provides a single source introduction to the field. It is written for advanced undergraduate and graduate students, and for developers and researchers in the field. No prior background in artificial intelligence or statistics is assumed.

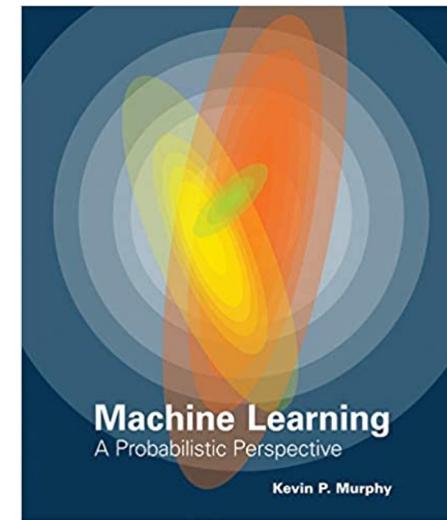
- A bit outdated with recent trends, but still has interesting discussion (and easy to read).
- A subfield of Artificial Intelligence – you want to perform nontrivial, smart tasks. The difference from the traditional AI is “how” you build a computer program to do it.

Textbooks

We will use a more recent textbook for readings

*Takes a **probabilistic approach** to machine learning*

Consistent with the goals of data science in this class



Murphy, K. "Machine Learning: A Probabilistic Perspective." MIT press, 2012
(UA Library)

AI Task 1: Image classification

- Predefined categories: $\mathcal{C} = \{\text{cat, dog, lion, ...}\}$
- Given an image, classify it as one of the categories $c \in \mathcal{C}$ with the highest accuracy.
- Use: sorting/searching images by category.
- Other example: categorize types of stars/events in the Universe (images taken from large surveying telescopes)



AI Task 2: Recommender systems

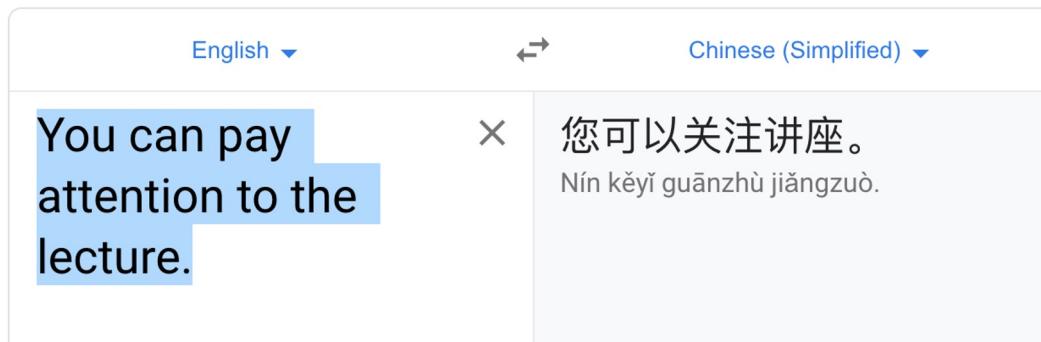
- Predict how user would rate a movie
- Use: For each user, pick an unwatched movie with the high predicted ratings.
- Idea: compute user-user similarity or movie-movie similarity, then compute a weighted average.

	User 1	User 2	User 3
Movie 1	1	2	1
Movie 2	?	3	1
Movie 3	2	5	2
Movie 4	4	?	5
Movie 5	?	4	5

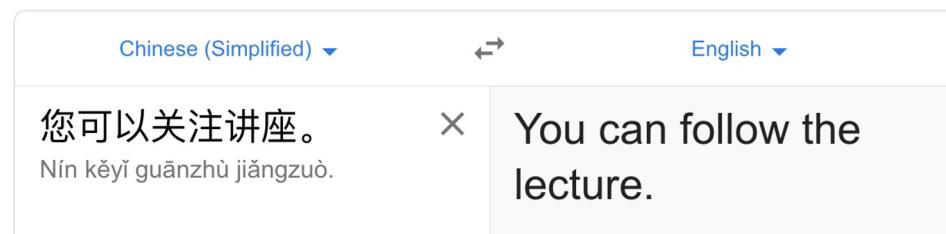
“collaborative
filtering”

AI Task 3: Machine translation

- No need to explain how useful it is.



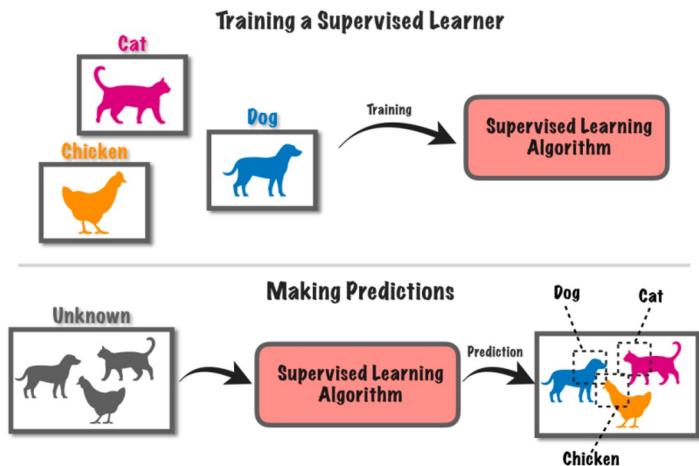
This screenshot shows a machine translation interface. At the top, there are dropdown menus for "English" and "Chinese (Simplified)" with a double-headed arrow between them. Below this, a blue-bordered text box contains the English sentence: "You can pay attention to the lecture." To the right of the text box is a red "X" button. Next to the text is its Chinese translation: "您可以关注讲座。" followed by the Pinyin transcription: "Nín kěyǐ guānzhù jiāngzuò."



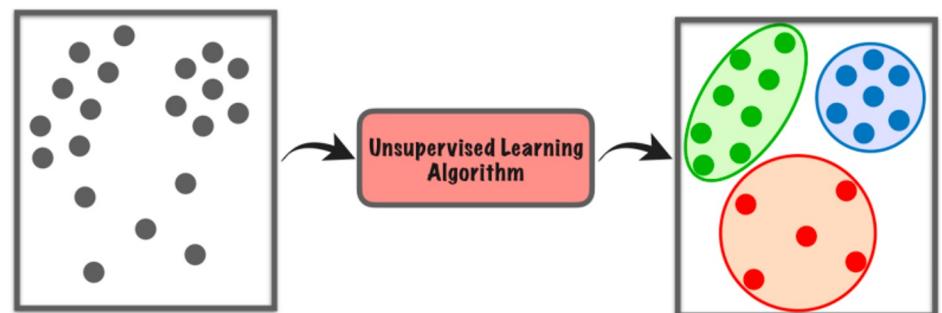
This screenshot shows a machine translation interface with the roles swapped. The top row has "Chinese (Simplified)" on the left and "English" on the right. Below this, a blue-bordered text box contains the Chinese sentence: "您可以关注讲座。" followed by the Pinyin transcription: "Nín kěyǐ guānzhù jiāngzuò." To the right of the text is a red "X" button. Next to the text is its English translation: "You can follow the lecture."

Supervised vs Unsupervised Learning

- **Supervised Learning** - Training data consist of inputs and outputs
 - Classification, regression, translation, ...



- **Unsupervised Learning** – Training data only contain inputs
 - Clustering, dimensionality reduction, segmentation, k-nearest neighbors ...



Supervised learning

example = data point
labeled = categorized

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- Train data: dataset comprised of labeled examples: a pair of (input, label)

airplane	
automobile	
bird	
cat	
deer	
dog	
frog	
horse	
ship	
truck	



supervised
learning
algorithm

training



function
("classifier")

testing

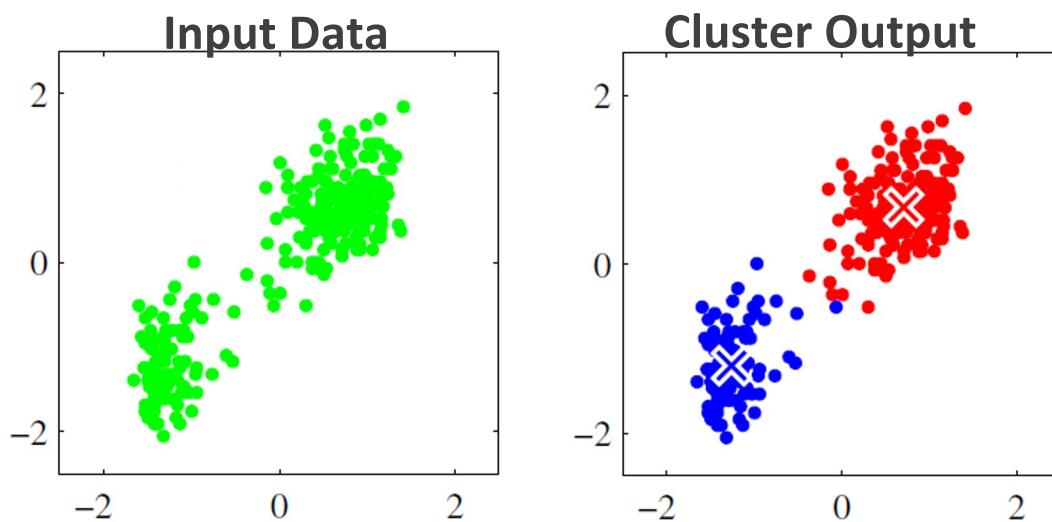


cat!



Unsupervised learning: Clustering

Identify groups (clusters) of similar data



Useful for interpreting large datasets

Clusters are assigned arbitrary labels (e.g. 1, 2, ..., K).
=> afterwards, you may look at the data and name **each group**.
(no need to name each sample)

Common clustering algorithms: K-means, Expectation Maximization (EM)

Decision Trees

Majority Vote Classifier

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The most basic classifier you can think of.

How to train:

- Given: A (train) dataset with m data points $\{(x^{(i)}, y^{(i)})\}_{i=1}^m$ with C classes.
- Compute the most common class c^* in the dataset.

$$c^* = \arg \max_{c \in \{1, \dots, C\}} \sum_{i=1}^m \mathbf{I}\{y^{(i)} = c\}$$

- Output a classifier $f(x) = c^*$.

Stupid enough classifier! Always try to beat this classifier.

Often, state-of-the-art ML algorithms perform barely better than the majority vote classifier..
⇒ happens when there is no association between features and labels in the dataset

Train set accuracy

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- Suppose the ML algorithm has trained a function f using the dataset $D = \{(x^{(i)}, y^{(i)})\}_{i=1}^m$ where $x^{(i)}$ is input and $y^{(i)}$ is label.
- Train set accuracy:

$$\widehat{acc}(f) := \frac{1}{m} \sum_{i=1}^m \mathbf{I}\{f(x^{(i)}) = y^{(i)}\}$$

This is 1 if f returns the correct label on $x^{\{(i)\}}$

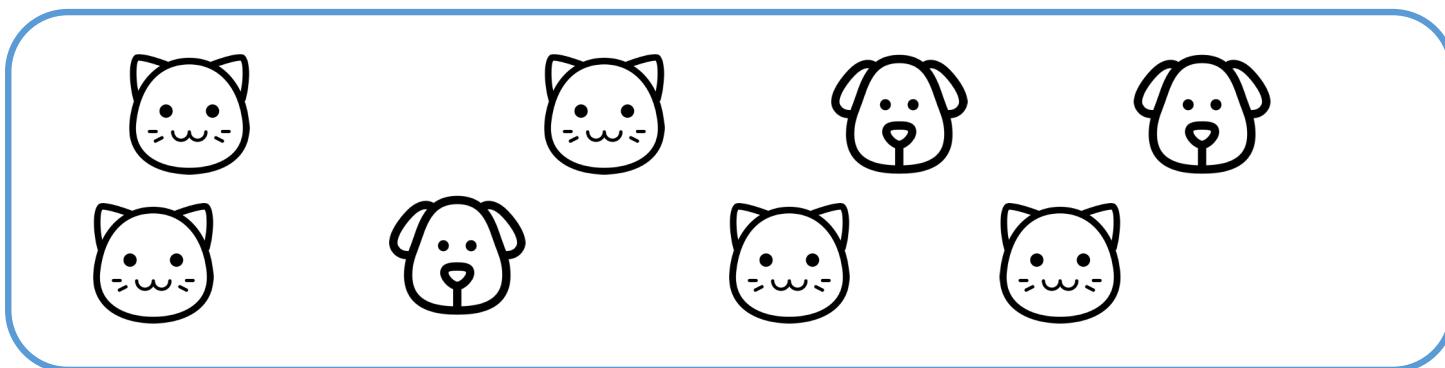
- Q: We have 100 data points (images) with 5 cats, 80 dogs, and 15 lions. What is the train set accuracy of the majority vote classifier?

quiz candidate

For each of 100 data points, the predicted label is dog: 80/100=.80

Train set accuracy

If the model is majority vote classifier..



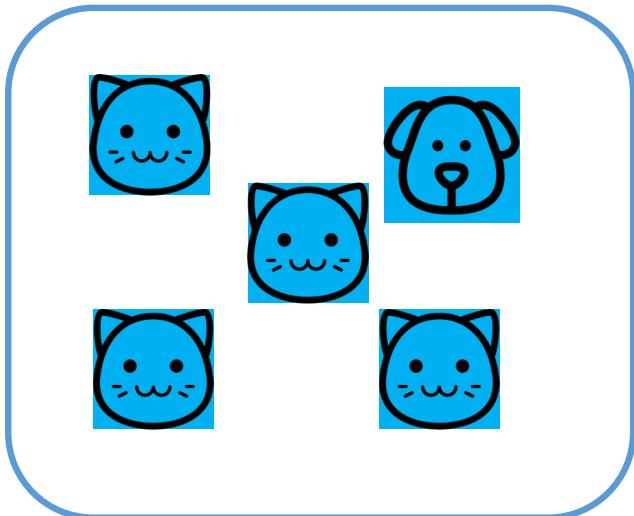
Majority vote: cat

Q: what is the accuracy?

$$\frac{5}{8}$$

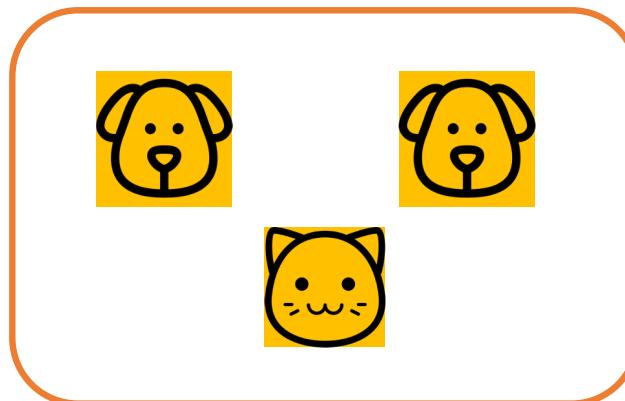
Train set accuracy

Given query, first find the DataSet containing it, and then use majority



Majority vote: cat

Suppose the model is a little bit smarter than majority vote classifier..



Majority vote: dog

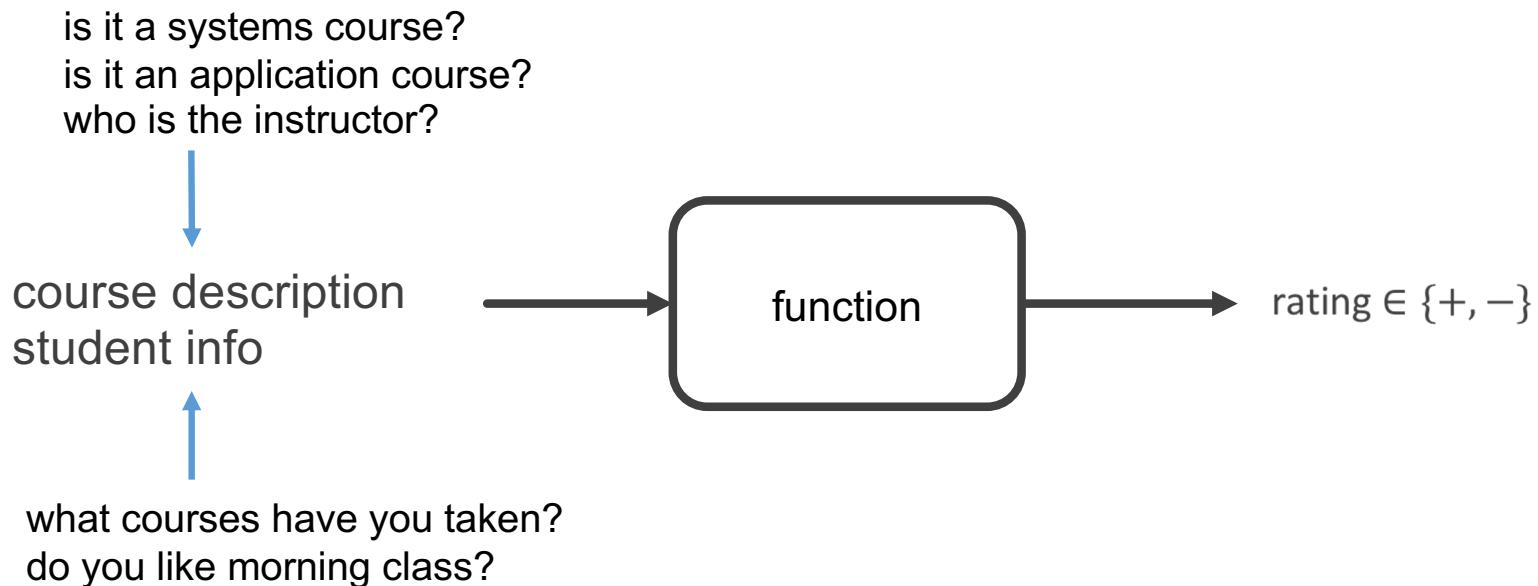
Q: what is the accuracy?

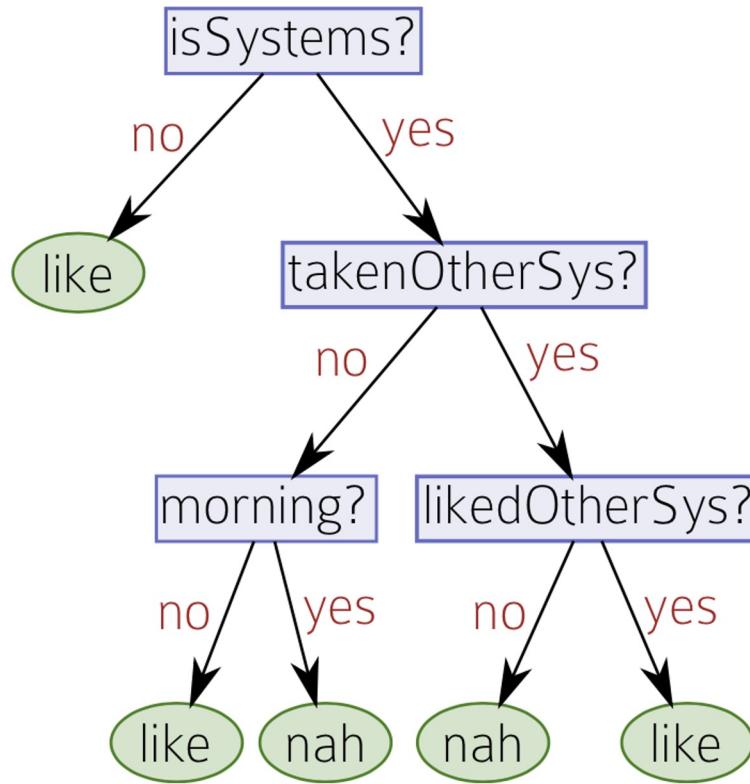
$$\frac{6}{8} = \frac{5}{8} \cdot \frac{4}{5} + \frac{3}{8} \cdot \frac{2}{3} = \frac{3}{4}$$

Example: course recommendation

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- Data: given a student, know the preferences and a set of courses already took
- Task: predict if the student like the course or not





Wouldn't it be nice to construct such a tree automatically by a computer algorithm?

Wouldn't it be nice if it accurately predicts?

You can, if you have data!

HasTakenPrereqs (=: Prereq)

HasTakenACourseFromTheSameLecturer (=: Lecturer)

HasLabs

consider
it to be
'like'

Rating	Easy?			Morning?	
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
0	n	n	n	n	y
0	y	n	n	y	y
0	n	y	n	y	n
0	y	y	y	y	y

consider
it to be
'dislike'

-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

For example, this table is data D;

Each row is a course you have rated;

$x^{(i)}$ is a sequence of 5 yes/no for the i-th course;

$y^{(i)}$ is the sign of rating for the i-th course.

Define the data $D = \{(x^{(i)}, y^{(i)})\}_{i=1}^m$

$$\in \{y, n\}^d \quad \in \{+, -\}$$

Each dimension of $x^{(i)}$ is called a **feature**.
 $x^{(i)}$ is called a **feature vector**.

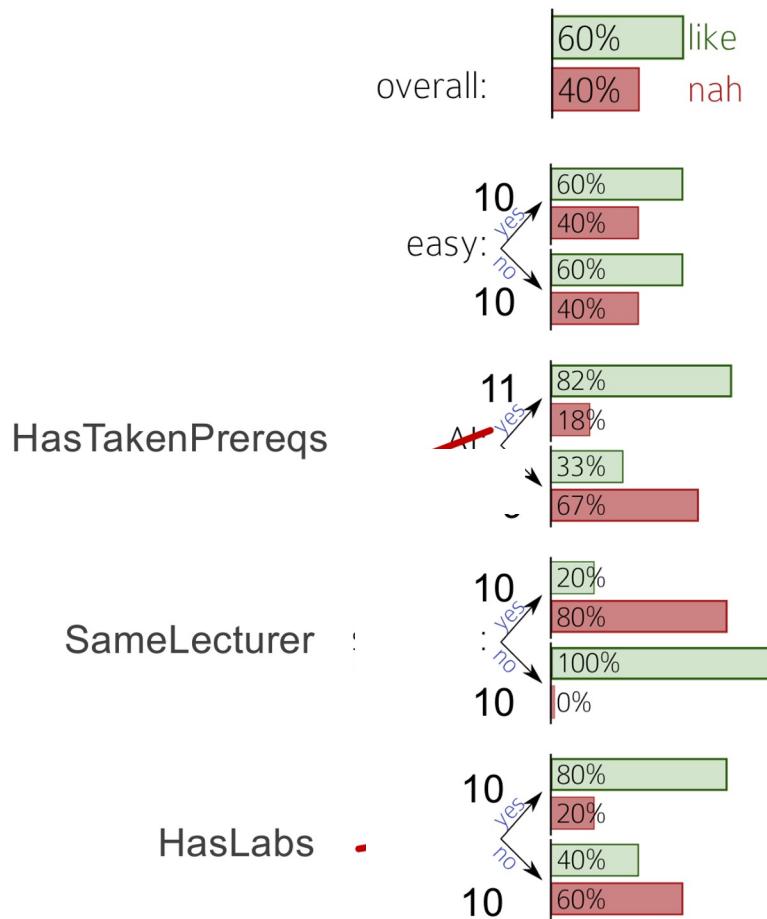
- Main principle: Find a tree that has a high train set accuracy

$$\widehat{acc}(f) = \frac{1}{m} \sum_{i=1}^m \mathbf{I}\{f(x^{(i)}) = y^{(i)}\}$$

- This is essentially the main principle governing pretty much all the machine learning algorithms!
 - “[Empirical risk minimization](#)” principle
(empirical risk := 1 – train_accuracy)

How to construct a tree: choosing root

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Rating	Easy?			Morning?	
	Prereqs	Lecturer	HasLabs		
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
o	n	n	n	n	y
o	y	n	n	y	y
o	n	y	n	y	n
o	y	y	y	y	y
-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

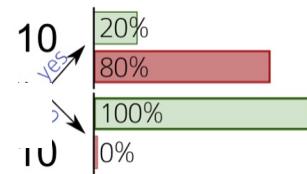
How to construct a tree



Rating	Easy?	Prereqs	Lecturer	HasLabs	Morning?
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
0	n	n	n	n	y
0	y	n	n	y	y
0	n	y	n	y	n
0	y	y	y	y	y
-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

How to construct a tree

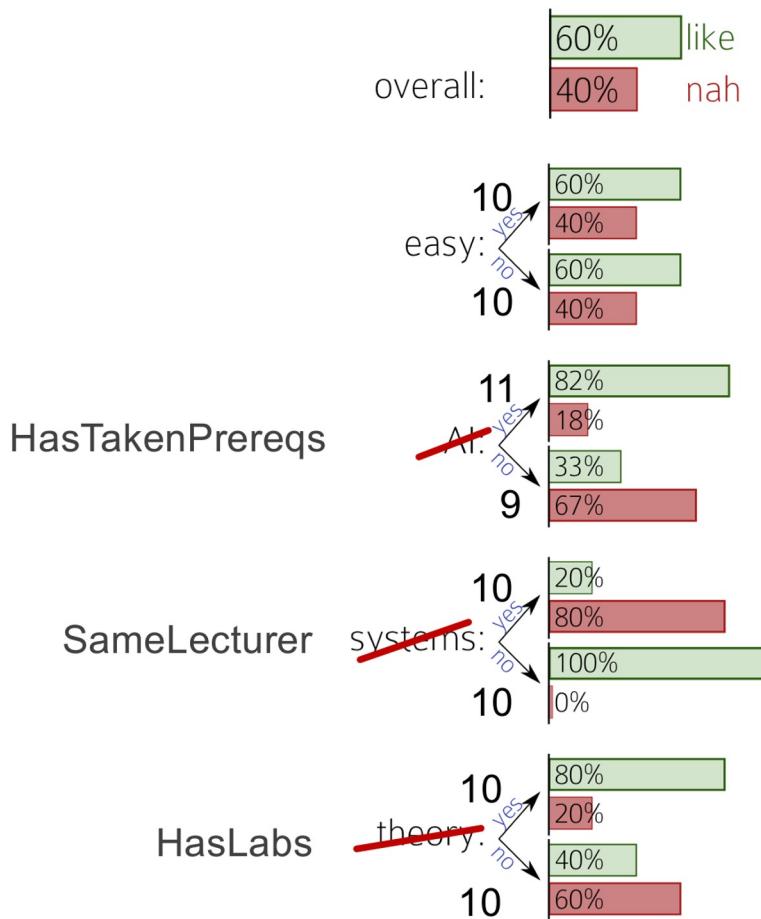
SameLecturer



Rating	Easy?			Morning?	
	Prereqs	Lecturer	HasLabs		
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
0	n	n	n	n	y
0	y	n	n	y	y
0	n	y	n	y	n
0	y	y	y	y	y
-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

How to construct a tree: choosing root

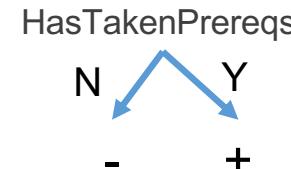
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Baseline: majority vote classifier

Q: What is the train set accuracy? $12/20 = 0.60$

Suppose we place the node **HasTakenPrereqs** at the root.
Set the prediction at each leaf node as the majority vote.



What is the train set accuracy now?

$$\frac{9}{20} \cdot \frac{6}{9} + \frac{11}{20} \cdot \frac{9}{11} = \frac{15}{20} = 0.75 \quad \text{improved!}$$

How to construct a tree

What is the train set accuracy now?

$$\frac{9}{20} \cdot \frac{6}{9} + \frac{11}{20} \cdot \frac{9}{11} = \frac{15}{20} = 0.75$$

Accuracy for two groups:

- Prereqs = yes (11): 9/11
- Prereqs = no (9): 6/9

For the 11 people prereqs = y, use the majority vote label **like** (9 like, 2 dislike).

Predicted label for 11 people is **like**, 9 people are correctly predicted.

consider it to be 'like'

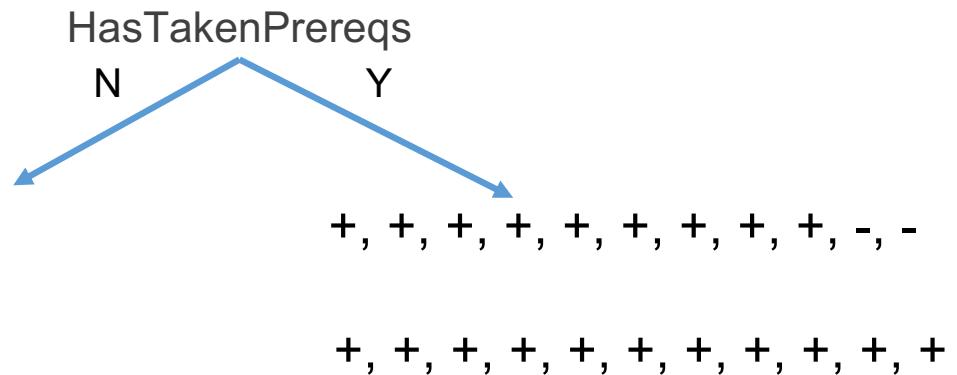
consider it to be 'dislike'

Rating	Easy?	Prereqs	Lecturer	HasLabs	Morning?
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
0	n	n	n	n	y
0	y	n	n	y	y
0	n	y	n	y	n
0	y	y	y	y	y
-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

True label: +, +, +, -, -, -, -, -, -

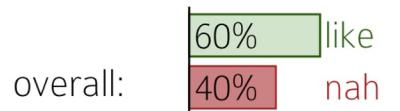
Predicted label: -, -, -, -, -, -, -, -, -

Accuracy: $\frac{9}{20} \cdot \frac{6}{9} + \frac{11}{20} \cdot \frac{9}{11} = \frac{15}{20} = 0.75$

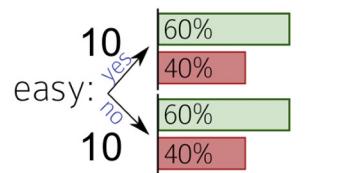


How to construct a tree

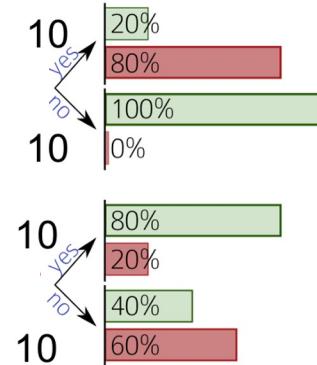
HasTakenPrereqs



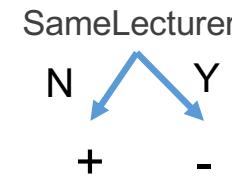
SameLecturer



HasLabs



Suppose placing the node SameLecturer at the root.



What is the train set accuracy now?

$$\frac{10}{20} \cdot \frac{10}{10} + \frac{10}{20} \cdot \frac{8}{10} = \frac{18}{20} = 0.9 \quad \text{even better!}$$

What would you do to build a depth-1 tree?

try out each feature and choose the one that leads to the largest accuracy!

How to construct a tree

What is the train set accuracy now?

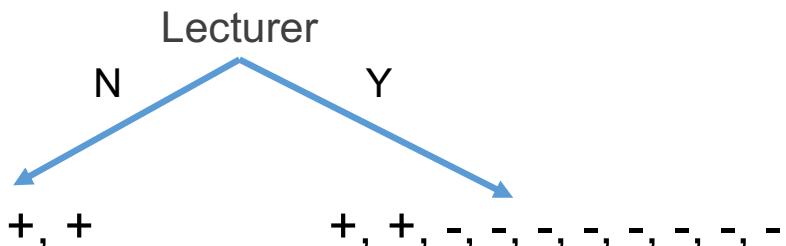
$$\boxed{\frac{10}{20}} \quad \frac{10}{10} + \frac{10}{20} \cdot \frac{8}{10} = \frac{18}{20} = 0.9$$

consider
it to be
'like'

Rating	Easy'	Prereqs	Lecturer	HasLabs	Morning?
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y	y	n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
o	n	n	n	n	y
o	y	n	n	y	y
o	n	y	n	y	n
o	y	y	y	y	y
<hr/>					
-1	y	y	y	n	y
-1	n	n	y	y	n
-1	n	n	y	n	y
-1	y	n	y	n	y
-2	n	n	y	y	n
-2	n	y	y	n	y
-2	y	n	y	n	n
-2	y	n	y	n	y

consider
it to be
'dislike'

How to construct a tree



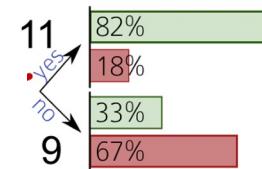
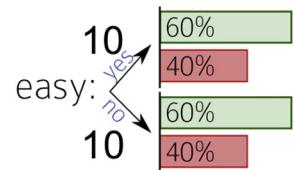
True label: +, +, +, +, +, +, +, +, +, +, +, +, +, +, -

Predicted label: +, +, +, +, +, +, +, +, +, +, -,-,-,-,-,-,-,-,-,-,-,-,-

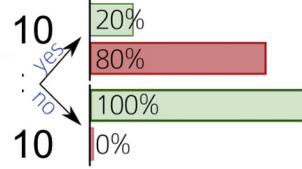
$$\text{Accuracy: } \frac{10}{20} \cdot \frac{10}{10} + \frac{10}{20} \cdot \frac{8}{10} = \frac{18}{20} = 0.9$$

How to construct a tree

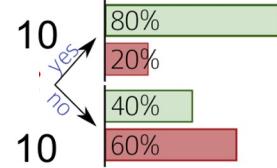
HasTakenPrereqs



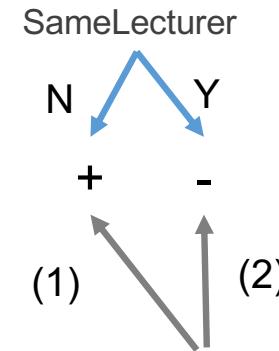
SameLecturer



HasLabs



What about depth 2?



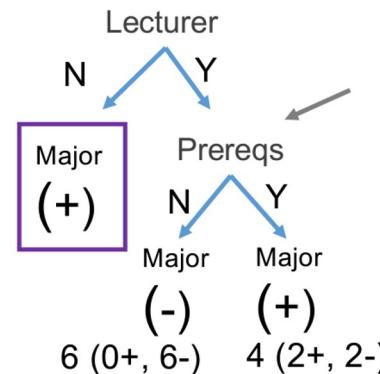
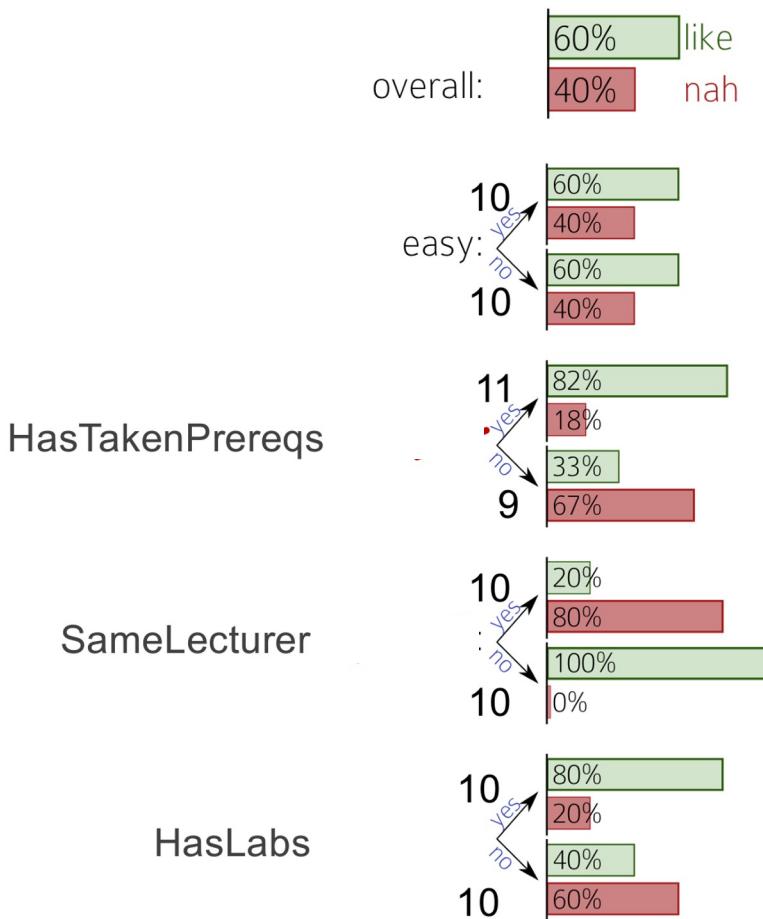
Which nodes to put at each leaf node?

Focus on (2). Try placing HasTakenPrereqs

All the data on (1) has same label "like", no need to do further splitting.

How to construct a tree

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Q: How many training data points fall here? 10

10

Q: How many training data points arrive at these two leaves? How many for each label?

Q: what prediction should we use for each leaf?

Q: What is the train set accuracy, conditioning on SameLecturer=Y? 6 6 4 3 8

$$\frac{6}{10} \cdot \frac{6}{6} + \frac{4}{10} \cdot \frac{2}{4} = \frac{8}{10}$$

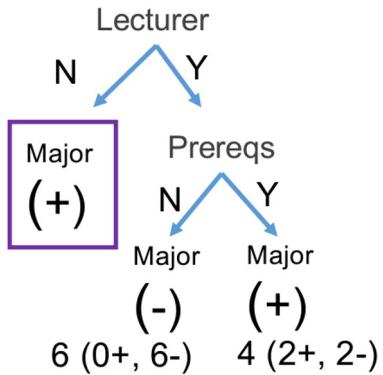
Try all the other nodes and pick the one with the largest acc.!

Then, repeat the same for `SameLecturer=N` branch!

=> but this has 1 local train set acc. So leave it be!

Move onto expanding nodes at depth 2!

How to construct a tree



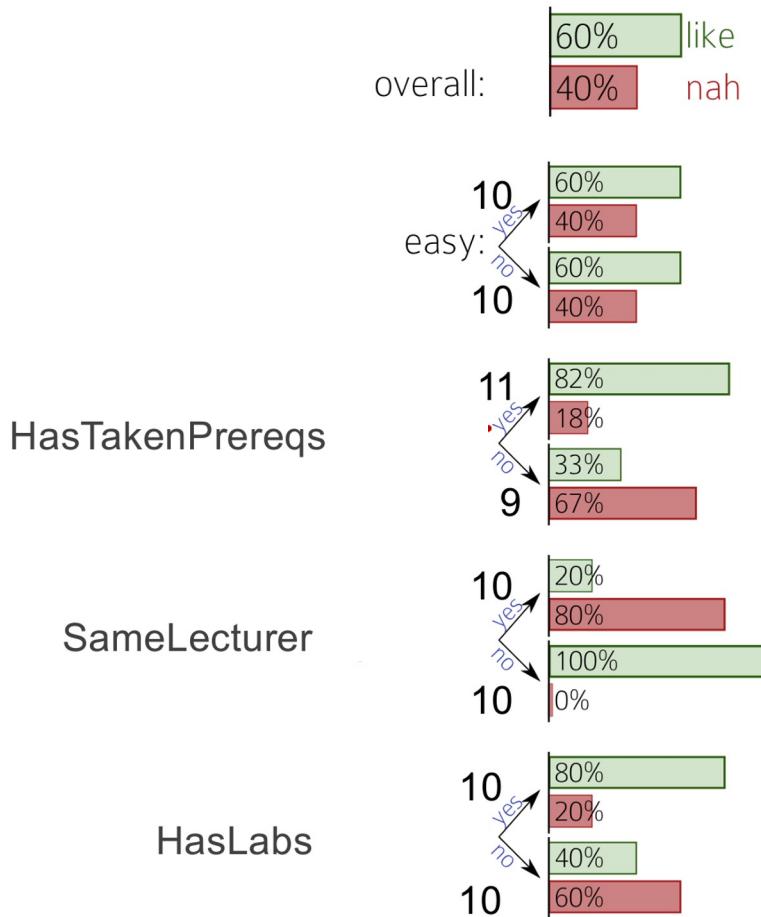
Q: What is the train set accuracy, conditioning on SameLecturer=Y?

$$\frac{6}{10} \cdot \frac{6}{6} + \frac{4}{10} \cdot \frac{2}{4} = \frac{8}{10}$$

Rating	Easy?	Morning?			
		Prereqs	Lecturer	HasLabs	
+2	y	y	n	y	n
+2	y	y	n	y	n
+2	n	y	n	n	n
+2	n	n	n	y	n
+2	n	y y		n	y
+1	y	y	n	n	n
+1	y	y	n	y	n
+1	n	y	n	y	n
0	n	n	n	n	y
0	y	n	n	y	y
0	n	y	n	y	n
0	y	y y		y	y
-1	y	y y		n	y
-1	n	n y		y	n
-1	n	n y		n	y
-1	y	n y		n	y
-2	n	n y		y	n
-2	n	y y		n	y
-2	y	n y		n	n
-2	y	n y		n	y

How to construct a tree

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Overall idea:

1. Set the root node as a leaf node.
2. Grab a leaf node for which its 'local' train accuracy is not 1.
3. Find a feature that maximizes the 'local' train accuracy and replace the leaf node with a node with that feature; add leaf nodes and set their predictions by majority vote.
4. If local accuracy is 1, no need to split the leaf node.
5. Repeat 2-3.

Algorithm 1 DECISIONTREETRAIN(*data*, *remaining features*)

```

1: guess  $\leftarrow$  most frequent answer in data           // default answer for this data
2: if the labels in data are unambiguous then          <= i.e., all data points have the same label
3:   return LEAF(guess)                                // base case: no need to split further
4: else if remaining features is empty then
5:   return LEAF(guess)                                // base case: cannot split further
6: else                                                 // we need to query more features
7:   for all f  $\in$  remaining features do           <= there is no point in adding a feature that
8:     NO  $\leftarrow$  the subset of data on which f=no
9:     YES  $\leftarrow$  the subset of data on which f=yes
10:    score[f]  $\leftarrow$  ( # of majority vote answers in NO
11:      + # of majority vote answers in YES ) /           <= answer = label
12:      size(data)
13:   end for
14:   f  $\leftarrow$  the feature with maximal score(f)
15:   NO  $\leftarrow$  the subset of data on which f=no
16:   YES  $\leftarrow$  the subset of data on which f=yes
17:   left  $\leftarrow$  DECISIONTREETRAIN(NO, remaining features \ {f})
18:   right  $\leftarrow$  DECISIONTREETRAIN(YES, remaining features \ {f})
19:   return NODE(f, left, right)
end if

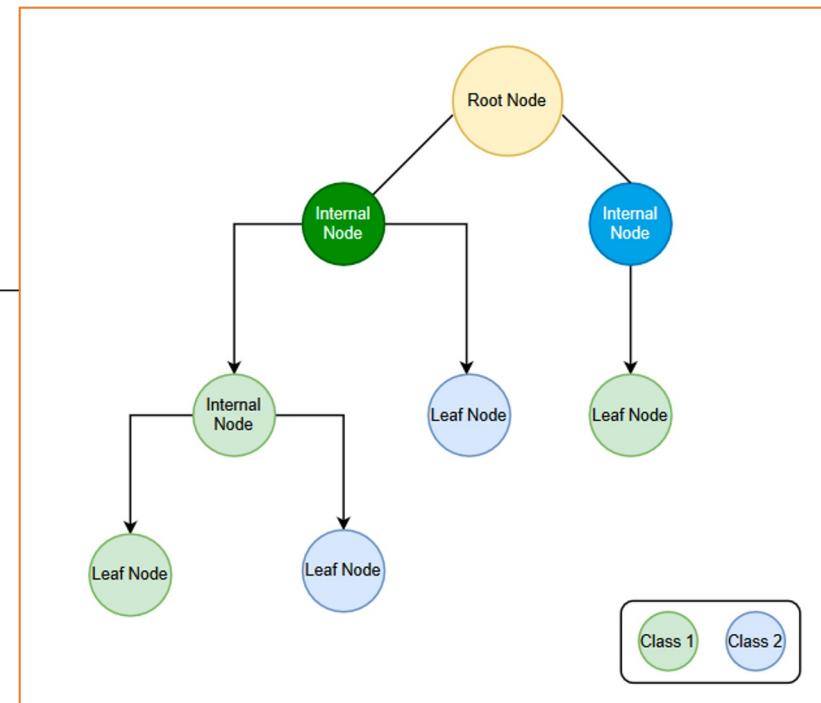
```

Algorithm 2 DECISIONTREETEST(*tree, test point*)

```

1: if tree is of the form LEAF(guess) then
2:   return guess
3: else if tree is of the form NODE(f, left, right) then
4:   if f = no in test point then
5:     return DECISIONTREETEST(left, test point)
6:   else
7:     return DECISIONTREETEST(right, test point)
8:   end if
9: end if

```



Example: spam filtering I

- ▶ Spam dataset
- ▶ 4601 email messages, about 39% are spam
- ▶ Classify message by spam and not-spam
- ▶ 57 features
 - ▶ 48 are of the form “percentage of email words that is (WORD)”
 - ▶ 6 are of the form “percentage of email characters is (CHAR)”
 - ▶ 3 other features (e.g., “longest sequence of all-caps”)
- ▶ Final tree after pruning has 17 leaves, 9.3% test error rate

