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Program assignment3 report

1. Simple depict about merge sort:

At first, we have an original array with several numbers. Then we divide the original array into two new arrays (I called these two array as left and right in my code.). Continue this step of “dividing” with recursion until it reaches the end which means the size of the last new array is 1. After this, we start the merge with comparing number in each array until its size go back to the size of the original array.

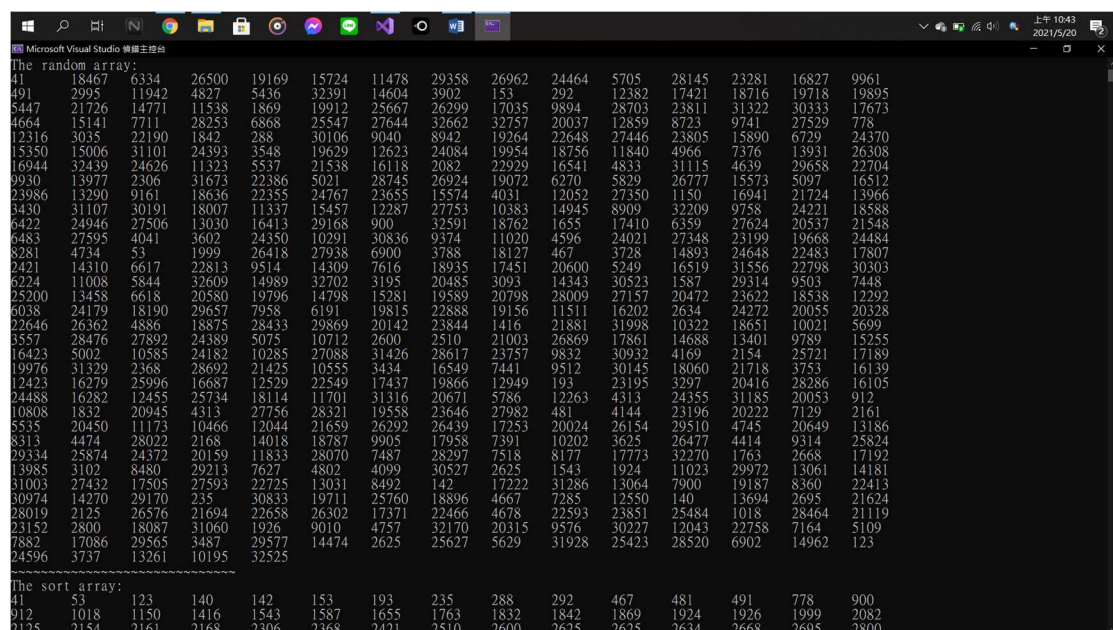
2. Explain its complexity and the reason:

At first step, we use the loop “for” to divide the original array into two arrays (the first one goes to left array, the second one goes to right array, the third one goes to left array, the forth one goes to right array.....). For n numbers, the complexity is ‘n’. And if we want to divide this array 1/2 by 1/2 until the number of its size reaches 1. Its complexity is $\log(n)$. So, in the “divide” step its complexity is equal $n\log(n)$.

In the next step, we also use the loop “for” to compare the numbers in each array, and the complexity is n. Because there are n numbers, and we are merge it two by two. So its complexity is $\log(n)$. In this step, the complexity is $n\log(n)$.

In total, the complexity is $n\log(n)+n\log(n)=2n\log(n)$. In the big O, the complexity will equal $n\log(n)$.

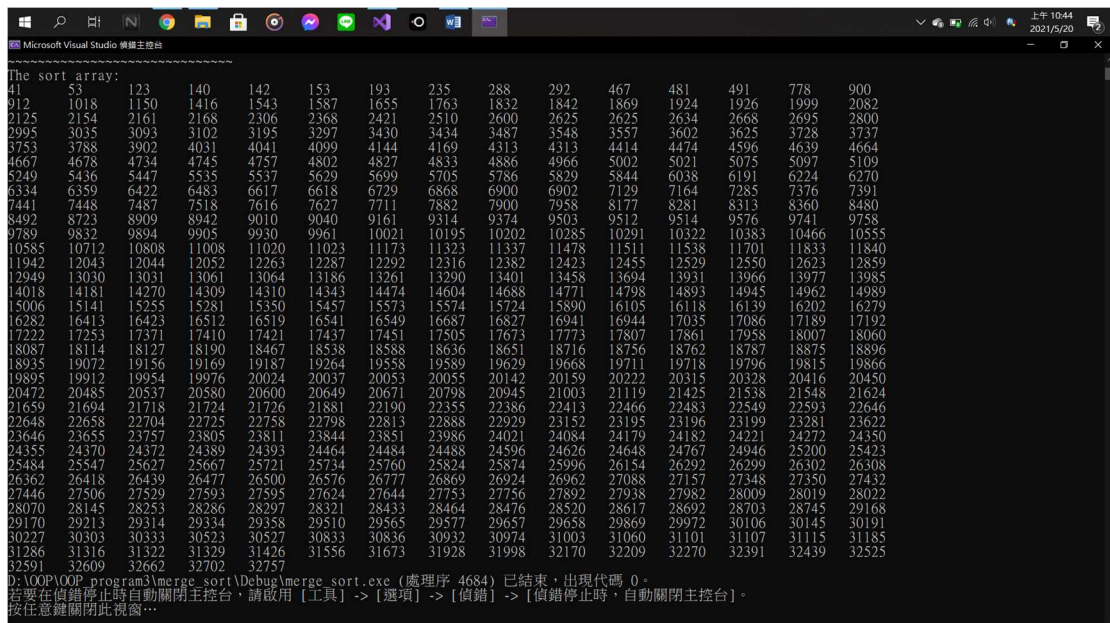
3. Result-before: 500 random numbers for each line is 15 numbers



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The random array:
41 18467 6334 26500 19169 15724 11478 29358 26962 24464 5705 28145 23281 16827 9961
491 2995 11942 4827 5436 32391 14604 3902 153 292 12382 17421 18716 19718 19895
5447 21726 14771 11538 1869 19912 25667 26299 17035 9894 28703 23811 31322 30333 17673
4664 15141 7711 28253 6868 25547 27644 32662 32757 20037 12859 8723 9741 27529 778
12316 3035 22190 1842 288 30106 9040 8942 19264 22648 27446 23805 15890 6729 24370
15350 15006 31101 24393 3548 19629 12623 24084 19954 18756 11840 4966 7376 13931 26308
16944 32439 24626 11323 5537 21538 16118 2082 22929 16541 4833 31115 4639 29658 22704
9930 13977 2306 31673 22386 5021 28745 26924 19072 6270 5829 26777 15573 5097 16512
23986 13290 9161 18636 22355 24767 23655 15574 4031 12052 27350 1150 16941 21724 13966
5430 31107 30191 18007 11337 15457 12287 27753 10383 14945 8909 32209 9758 24221 18588
6422 24946 27506 13030 16413 29168 900 32591 18762 1655 17410 6359 27624 20537 21548
6483 27595 4041 3602 24350 10291 30836 9374 11020 4596 24021 27348 23199 19668 24484
8281 4734 53 1999 26418 27938 6900 3788 18127 467 3728 14893 24648 22483 17807
2421 14310 6617 22813 9514 14309 7616 18935 17451 20600 5249 16519 31556 22798 30303
6224 11008 5844 32609 14989 32702 3195 20485 3093 14343 30523 1587 29314 9503 7448
25200 13458 6618 20580 19796 14798 15281 19589 20798 28009 27157 20472 23622 18538 12292
6038 24179 18190 29657 7958 6191 19815 22888 19156 11511 16202 2634 24272 20055 20328
22646 26362 4886 18875 28433 29869 20142 23844 1416 21881 31998 10322 18651 10021 5699
3557 28476 27892 24389 5075 10712 2600 2510 21003 26869 17861 14688 13401 9789 15255
16423 5002 10585 24182 10285 27088 31426 28617 23757 9832 30932 4169 2154 25721 17189
19976 31829 2368 28692 21425 10555 3434 16549 7441 9512 30145 18060 21718 3753 16139
12423 16279 25996 16687 12529 22549 17437 19866 12949 193 23195 3297 20416 28286 16105
24488 16282 12455 25734 18114 11701 31316 20671 5786 12263 4313 24355 31185 20053 912
10808 1832 20945 4313 27756 28321 19558 23646 27982 481 4144 23196 20222 7129 2161
5535 20450 11173 10466 12044 21659 26292 26439 17253 20024 26154 29510 4745 20649 13186
8313 4474 28022 2168 14018 18787 9905 17958 7391 10202 3625 26477 4414 9314 25824
29334 25874 24372 20159 11833 28070 7487 28297 7518 8177 17773 32270 1763 2668 17192
13985 3102 8480 29213 7627 4802 4099 30527 2625 1543 1924 11023 29972 13061 14181
31003 27432 17505 27593 22725 13031 8492 142 17222 31286 13064 7900 19187 8360 22413
30974 14270 29170 235 30833 19711 25760 18896 4667 7285 12550 140 13694 2695 21624
28019 2125 26576 21694 22658 26302 17271 22466 4678 22593 23831 25484 1018 28464 21119
23152 2800 18087 31060 1926 9010 4757 32170 20315 9576 30227 12043 22758 7164 5109
7882 17086 29565 3487 29577 14474 2625 25627 5629 31928 25423 28520 6902 14962 123
24596 3737 13261 10195 32525

The sort array:
41 53 123 140 142 153 193 235 288 292 467 481 491 778 900
912 1018 1150 1416 1543 1587 1655 1763 1832 1842 1869 1924 1926 1999 2082
2125 2154 2161 2168 2306 2368 2421 2510 2600 2625 2625 2634 2668 2695 2800
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Result-after: 500 random numbers after merge sorted for each line is 15 numbers:



The screenshot shows the Visual Studio IDE with a C# program. The console output displays a sorted array of 500 random numbers, arranged in 33 rows of 15 numbers each. The numbers are sorted in ascending order. At the bottom of the console, there is a status bar indicating that the program has finished execution.

```
The sort array:
41      53      123      140      142      153      193      235      288      292      467      481      491      778      900
912      1018      1150      1416      1543      1587      1655      1763      1832      1842      1869      1924      1926      1999      2082
2125      2154      2161      2168      2306      2368      2421      2510      2600      2625      2625      2634      2668      2695      2800
2995      3035      3093      3102      3195      3297      3430      3434      3487      3548      3557      3602      3625      3728      3737
3753      3788      3902      4031      4041      4099      4144      4169      4313      4313      4414      4474      4596      4639      4664
4667      4678      4734      4745      4757      4802      4827      4833      4886      4966      5002      5021      5075      5097      5109
5249      5436      5447      5535      5537      5629      5699      5705      5786      5829      5844      6038      6191      6224      6270
6334      6359      6422      6483      6617      6618      6729      6868      6900      6902      7129      7164      7285      7376      7391
7441      7448      7487      7518      7616      7627      7711      7882      7900      7958      8177      8281      8313      8360      8480
8492      8723      8909      8942      9010      9040      9161      9314      9374      9503      9512      9514      9576      9741      9758
9789      9832      9894      9905      9930      9961      10021      10195      10202      10285      10291      10322      10383      10466      10555
10585      10712      10808      11008      11020      11023      11173      11323      11337      11478      11511      11538      11701      11833      11840
11942      12043      12044      12052      12263      12287      12292      12316      12382      12423      12455      12529      12550      12623      12859
12949      13030      13031      13061      13064      13186      13261      13290      13401      13458      13694      13931      13966      13977      13985
14018      14181      14270      14309      14343      14474      14604      14688      14771      14798      14893      14945      14962      14989
15006      15141      15255      15281      15350      15457      15573      15574      15724      15890      16105      16118      16139      16202      16279
16282      16413      16423      16512      16519      16541      16549      16687      16827      16941      16944      17035      17086      17189      17192
17222      17253      17371      17410      17421      17437      17451      17505      17673      17773      17807      17861      17958      18007      18060
18087      18114      18127      18190      18467      18538      18588      18636      18651      18716      18756      18762      18787      18875      18896
18935      19072      19156      19169      19187      19264      19558      19589      19629      19668      19711      19718      19796      19815      19866
19895      19912      19954      19976      20024      20037      20053      20055      20142      20159      20222      20315      20328      20416      20450
20472      20485      20537      20580      20600      20649      20671      20798      20945      21003      21119      21425      21538      21548      21624
21659      21694      21718      21724      21726      21881      22190      22355      22386      22413      22466      22483      22549      22593      22646
22648      22658      22704      22725      22758      22798      22813      22888      22929      23152      23195      23196      23199      23281      23622
23646      23655      23757      23805      23811      23844      23851      23986      24021      24084      24179      24182      24221      24272      24350
24355      24370      24372      24389      24464      24484      24488      24596      24626      24648      24767      24946      25200      25423
25484      25547      25627      25667      25721      25734      25760      25824      25874      25996      26154      26292      26299      26302      26308
26362      26418      26439      26477      26500      26576      26777      26869      26924      26962      27088      27157      27348      27350      27432
27446      27506      27529      27593      27595      27624      27644      27753      27756      27892      27938      27982      28009      28019      28022
28070      28145      28253      28286      28297      28321      28433      28464      28476      28520      28617      28692      28703      28745      29168
29170      29213      29314      29334      29358      29510      29565      29577      29657      29658      29869      29972      30106      30145      30191
30227      30303      30333      30523      30527      30833      30836      30932      30974      31003      31060      31101      31107      31115      31185
31286      31316      31322      31329      31426      31556      31673      31928      31998      32170      32209      32270      32391      32439      32525
32591      32609      32662      32702      32757
```

4. How to code in practical?

For the main function, I set an array for 500 numbers in the beginning. And use a “while” loop to push 500 random numbers into the array.

Then, call the function **print_the_arr()** to print the array.

Next, call the function **merge_arr()** to do the main task.

In this function, we will judge that if the size of the input array is 1. If it is true, return and end the function. Otherwise, create two arrays named ‘left’ and ‘right’. Then using a “for” loop to divide the original array into these two arrays.

And continue to call **merge_arr()** with using the property of recursion.

After finishing the step of “divide”, which means the original array has been divided into n arrays with one integer in it, call the function **merge()**.

In this function, we will have 3 arrays, one is the original array, another is the left array, the other is right array. The original array is the array which is divided into the left array and the right array. Then compare the numbers in the left array and the right array, respectively. For which number is smaller than another, push this number back to the original array. Continuing this step until we compare all the “left” and “right” arrays, and pushing all the integer back to the original array.

In the end, call the function **print_the_arr()** to print the sorted array in the main function.