

## 2. Sequence Rule :

It's a Fibonacci sequence .

For  $F_0 = 0$  ,  $F_1 = 1$

$$F_n = F_{n-1} + F_{n-2} , n = 2, 3, 4, 5, \dots$$

$$3. s(x) = x^8 + x^7 + 2x^6 + 3x^5 + 5x^4 + 8x^3 + 13x^2 + 21x + 34$$

$$r(x) = x^9$$

find  $c(x)$

$$\text{let } f(x)r(x) + c(x)s(x) = b(x) , \deg b < \deg c$$

	$f(x)$	$c(x)$	$b(x)$
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(1)	1	0	$x^9$
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(2)	0	1	$x^8 + x^7 + 2x^6 + 3x^5 + 5x^4 + 8x^3 + 13x^2 + 21x + 34$
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(3)	1	$-x$	$-x^9 - 2x^8 - 3x^7 - 5x^6 - 8x^5 - 13x^4 - 21x^3 - 34x^2$
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(4)	1	$1-x$	$-x^9 - x^8 - 2x^7 - 3x^6 - 5x^5 - 8x^4 - 13x^3 - 21x^2 - 34x$
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$$(5) \quad 1-x \quad x^2-2x \quad -x^9-x^6-2x^5-3x^4-5x^3-8x^2-68x$$

$$(6) \quad x \quad -x^2+x+1 \quad 55x+34$$

$$f(x)r(x) + c(x)s(x) = b(x)$$

$$\Rightarrow x^{10} + (-x^2+x+1)(x^8+x^7+2x^6+3x^5+5x^4+8x^3+13x^2+21x+34)$$

$$= x^{10} + (-x^{10}-x^9-2x^8-3x^7-5x^6-8x^5-13x^4-21x^3-34x^2+x^9+x^8+2x^7+3x^6+5x^5+8x^4+13x^3+21x^2+34x+x^8+x^7+2x^6+3x^5+5x^4+8x^3+13x^2+21x+34)$$

$$= 55x+34 = b(x)$$

So, we find  $c(x) = -x^2+x+1$

such that:  $f(x)r(x) + c(x)s(x) = b(x)$

$$\deg b < \deg c$$