

Quiz 4

- In this assignment, we will learn using Markov chain methods to attack classical columnar transposition ciphers automatically.
- The steps to solve it are as follows:
 1. Using the number of vowels to detect ciphertext rectangles (In English approximately 40% of plaintext consists of vowels).
 2. Using plaintext bigrams and trigrams to calculate conditional probabilities for Markov decision processing (MDP).
 3. Using MDP to recover columnar transposition ciphers.

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Transposition Columnar Transposition Diffusion

ECDTM ECAER AUOOL
 EDSAM MERNE
 NASSO DYTNR VBNLC
 RLTIQ
 LAETR IGAW E BAAEI
 HOR

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			Number of vowels	Difference
A	F	L	1	0.2
S	N	S	0	1.2
A	M	O	2	0.8
I	I	I	3	1.8
R	M	E	1	0.2
I	T	E	2	0.8
T	K	M	0	1.2

The sum of the differences is 6.2. It appears that the 3×7 rectangle is more likely.

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Plaintext Reference

WITTH ALICE TOWAR ONORE WITHC HARIT YFORA LHMST
 NFIHM NHHI NTHH IGHIA SGOOG IVEHU STORH ETHEH
 IGHIL EYUHH TAYVE ONTOF IYIHH THURO WORMA RELIT
 OHIND UPTHE NATIO NEMOU NESTO CANEF ORHIM NHOHH
 ALIHA VEHOR NETHH BATHL EANDF OHNIS WIDOW ANDHI
 SORPH ANTCO CALLH HICOM AYACH IYVHA NOCHE RISHA
 JUSTA NDLAS TINGF EACBA NONGO URSUL VESAN DMITH
 ALIHA TIONE GREEC EAMNO UNCED YESTE NGATT HEAGR
 AGREE MENTW ITSTH UVEVE NUTHE CYFRU STRAT THEGR
 EKAN DTURN ISHCO NTING ENTOM HICHA RETOP ARTIC
 IPATE INTHE TRIPA RTTTE HEADQ UARTE RSHHA LLOOM
 PRISE RESPE CTIVE LYGRE EKOFF ICERS NONCO NMISS
 IONED OFFIC ERGAN OMENA ROTUR KISHO PFICE RSNON
 COMMI SEIOW EKOFF ICERS ANOME NTHF RESID ENTAN
 DVICE PRESI GENTO FTHER EPUBL ICOPC YFRUS ACTIN
 GINAG REEME NYMAY REQUE STTHE GREEK ANDTU KISH
 COVER INMENT STVIN CHLAS KORRE DUCTY HIGHE SEAND
 TURKI SHCON TINGE NTHIT ISAGR EEDTH ATTHE SITES
 OFTHE GANTO INMENT SPURT BEGRE EXAND TURKI SHCON
 TINGE NTIFA RTICI PATTI GINTH STRIP ARTIT EHEAD
 QUART ERSTH KIRJU KIDIC ALSTA TURFA CLIT IESAN
 UNDEM PYOW SIBRE SPECT OFCUS TOMBA NUTAX KEANW
 ELLAS OTHER IMGEN ITIES ANCFR IVILE GRESAN DANYO
 THERN ILITA RYAND TECHN ICLAQ UESTI ONSCO NCERN
 INOTH EDGHA NUTAT JORAN OOPER ATION OFTHE HEADQ
 UARTE RSMEN TIONE DABOV ESSAL LSEDE TERMI NEDBY
 ASPEC IALCO NVENT JORNN ICERS ALLO MEINT OFORC
 ENOTI ATERT HANTH EREHA TIOFA LLIAN CE

First count tri-gram plaintext frequency using these messages as training sets

WIT
 ITH
 THM
 HMA
 MAL
 ALI
 ...

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Dan Boneh

Tri-gram plaintext to calculate conditional probability

WORD	Frequency
THE	A like 5 times
THA	B like 2 times
CAR	C
CAN	D

$$\begin{aligned}
 \text{Weight (THE)} &= \\
 &\text{Log Pc(THE/TH)} \\
 &= \log(A / A+B) \\
 &= \log 5/7
 \end{aligned}$$

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WORD	Frequency
THE	A 5
THA	B 2
CAR	C
CAN	D

$$\begin{aligned}
 W(\text{THE}) &= \\
 &\text{Log Pc(THE/TH)} / \text{Random} \\
 &= \log(A / A+B) / (1/26) \\
 &= \log 26 * (5/7)
 \end{aligned}$$

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L	A	S				
A	M	S				
E	M	O				
T	E	D				
R	R	Y				
I	N	T				
G	E	N				
A	N	R				
W	A	V				

We can use Markov chain methods to attack classical columnar transposition ciphers automatically for our assignment last week. That is a supervised learning approaches.

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Then, Write a program to solve these transposition using a supervised learning approach- Markov chain methods

EOEYE GTRNP SECEH
 HETYH SNGND DDDDET
 OCRAE RAEMH
 TECSE USIAR WKDRI
 RNYAR ANUEY ICNTT
 CEIET US

Hint: the first three letters of the plaintext message are **GRE**

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