

# project

2025-11-25

The dataset used in this project corresponds to the supplementary file **MOESM2 (ESM)** from the publication by Fan et al. (2018). It contains the raw GC-TOF-MS metabolomics data for 120 urine samples from healthy adults (60 males and 60 females), enabling independent preprocessing, exploratory analysis, feature selection, and classification.

## Import Library

```
# -----
# Libraries
# -----
# Data import and manipulation
library(readxl)
library(dplyr)
```

```
##
## Attaching package: 'dplyr'
```

```
## The following objects are masked from 'package:stats':
##      filter, lag
```

```
## The following objects are masked from 'package:base':
##      intersect, setdiff, setequal, union
```

```
library(tidyverse)
```

```
## — Attaching core tidyverse packages ————— tidyverse 2.0.0 —
—
## ✓forcats    1.0.1     ✓readr      2.1.6
## ✓ggplot2    4.0.1     ✓stringr    1.6.0
## ✓lubridate  1.9.4     ✓tibble     3.3.0
## ✓purrr     1.2.0     ✓tidyverse  1.3.1
```

```
## — Conflicts ————— tidyverse_conflicts() —  
—  
## * dplyr::filter() masks stats::filter()  
## * dplyr::lag()    masks stats::lag()  
## i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors
```

```
# Visualization  
library(ggplot2)  
library(ellipse)
```

```
##  
## Attaching package: 'ellipse'  
##  
## The following object is masked from 'package:graphics':  
##  
##     pairs
```

```
library(knitr)  
  
# Multivariate analysis  
#library(pls)  
library(mixOmics)
```

```
## Loading required package: MASS
##
## Attaching package: 'MASS'
##
## The following object is masked from 'package:dplyr':
##       select
##
## Loading required package: lattice
##
## Loaded mixOmics 6.30.0
## Thank you for using mixOmics!
## Tutorials: http://mixomics.org
## Bookdown vignette: https://mixomicsteam.github.io/Bookdown
## Questions, issues: Follow the prompts at http://mixomics.org/contact-us
## Cite us: citation('mixOmics')
##
##
## Attaching package: 'mixOmics'
##
## The following object is masked from 'package:purrr':
##       map
```

```
# Machine learning and validation
library(caret)
```

```
##
## Attaching package: 'caret'
##
## The following objects are masked from 'package:mixOmics':
##       nearZeroVar, plsda, splsda
##
## The following object is masked from 'package:purrr':
##       lift
```

```
library(pROC)
```

```
## Type 'citation("pROC")' for a citation.  
##  
## Attaching package: 'pROC'  
##  
## The following objects are masked from 'package:stats':  
##  
##     cov, smooth, var
```

```
# Statistics and utilities  
library(DescTools)
```

```
##  
## Attaching package: 'DescTools'  
##  
## The following objects are masked from 'package:caret':  
##  
##     MAE, RMSE
```

# Import dataset

```
raw_df <- read_excel("41598_2018_29592_MOESM2_ESM.xlsx")
```

```
## New names:  
## • ` ` -> `...1`  
## • ` ` -> `...2`  
## • ` ` -> `...3`  
## • ` ` -> `...4`  
## • ` ` -> `...5`  
## • ` ` -> `...6`  
## • ` ` -> `...7`  
## • ` ` -> `...8`  
## • ` ` -> `...9`  
## • ` ` -> `...10`  
## • ` ` -> `...11`  
## • ` ` -> `...12`  
## • ` ` -> `...13`  
## • ` ` -> `...14`
```

```
sex_labels <- unlist(raw_df[3, 17:136])  
sex <- as.factor(sex_labels)  
  
df <- read_excel("41598_2018_29592_MOESM2_ESM.xlsx", skip = 6)
```

```
## New names:
```

```
## • `` -> `...1`  
## • `` -> `...2`  
## • `` -> `...3`  
## • `` -> `...4`  
## • `` -> `...5`  
## • `` -> `...6`  
## • `` -> `...7`  
## • `` -> `...8`  
## • `` -> `...9`  
## • `` -> `...10`  
## • `` -> `...12`  
## • `` -> `...14`  
## • `1 - Male` -> `1 - Male...16`  
## • `1 - Male` -> `1 - Male...17`  
## • `1 - Male` -> `1 - Male...18`  
## • `1 - Male` -> `1 - Male...19`  
## • `1 - Male` -> `1 - Male...20`  
## • `1 - Male` -> `1 - Male...21`  
## • `1 - Male` -> `1 - Male...22`  
## • `1 - Male` -> `1 - Male...23`  
## • `1 - Male` -> `1 - Male...24`  
## • `1 - Male` -> `1 - Male...25`  
## • `1 - Male` -> `1 - Male...26`  
## • `1 - Male` -> `1 - Male...27`  
## • `1 - Male` -> `1 - Male...28`  
## • `1 - Male` -> `1 - Male...29`  
## • `1 - Male` -> `1 - Male...30`  
## • `1 - Male` -> `1 - Male...31`  
## • `1 - Male` -> `1 - Male...32`  
## • `1 - Male` -> `1 - Male...33`  
## • `1 - Male` -> `1 - Male...34`  
## • `1 - Male` -> `1 - Male...35`  
## • `1 - Male` -> `1 - Male...36`  
## • `1 - Male` -> `1 - Male...37`  
## • `1 - Male` -> `1 - Male...38`  
## • `1 - Male` -> `1 - Male...39`  
## • `1 - Male` -> `1 - Male...40`  
## • `1 - Male` -> `1 - Male...41`  
## • `1 - Male` -> `1 - Male...42`  
## • `1 - Male` -> `1 - Male...43`  
## • `1 - Male` -> `1 - Male...44`  
## • `1 - Male` -> `1 - Male...45`  
## • `1 - Male` -> `1 - Male...46`  
## • `1 - Male` -> `1 - Male...47`  
## • `1 - Male` -> `1 - Male...48`  
## • `1 - Male` -> `1 - Male...49`  
## • `1 - Male` -> `1 - Male...50`  
## • `1 - Male` -> `1 - Male...51`  
## • `1 - Male` -> `1 - Male...52`  
## • `1 - Male` -> `1 - Male...53`  
## • `1 - Male` -> `1 - Male...54`
```

```
## • `1 - Male` -> `1 - Male...55`  
## • `1 - Male` -> `1 - Male...56`  
## • `1 - Male` -> `1 - Male...57`  
## • `1 - Male` -> `1 - Male...58`  
## • `1 - Male` -> `1 - Male...59`  
## • `1 - Male` -> `1 - Male...60`  
## • `1 - Male` -> `1 - Male...61`  
## • `1 - Male` -> `1 - Male...62`  
## • `1 - Male` -> `1 - Male...63`  
## • `1 - Male` -> `1 - Male...64`  
## • `1 - Male` -> `1 - Male...65`  
## • `1 - Male` -> `1 - Male...66`  
## • `1 - Male` -> `1 - Male...67`  
## • `1 - Male` -> `1 - Male...68`  
## • `1 - Male` -> `1 - Male...69`  
## • `1 - Male` -> `1 - Male...70`  
## • `1 - Male` -> `1 - Male...71`  
## • `1 - Male` -> `1 - Male...72`  
## • `1 - Male` -> `1 - Male...73`  
## • `1 - Male` -> `1 - Male...74`  
## • `1 - Male` -> `1 - Male...75`  
## • `2 - Female` -> `2 - Female...76`  
## • `2 - Female` -> `2 - Female...77`  
## • `2 - Female` -> `2 - Female...78`  
## • `2 - Female` -> `2 - Female...79`  
## • `2 - Female` -> `2 - Female...80`  
## • `2 - Female` -> `2 - Female...81`  
## • `2 - Female` -> `2 - Female...82`  
## • `2 - Female` -> `2 - Female...83`  
## • `2 - Female` -> `2 - Female...84`  
## • `2 - Female` -> `2 - Female...85`  
## • `2 - Female` -> `2 - Female...86`  
## • `2 - Female` -> `2 - Female...87`  
## • `2 - Female` -> `2 - Female...88`  
## • `2 - Female` -> `2 - Female...89`  
## • `2 - Female` -> `2 - Female...90`  
## • `2 - Female` -> `2 - Female...91`  
## • `2 - Female` -> `2 - Female...92`  
## • `2 - Female` -> `2 - Female...93`  
## • `2 - Female` -> `2 - Female...94`  
## • `2 - Female` -> `2 - Female...95`  
## • `2 - Female` -> `2 - Female...96`  
## • `2 - Female` -> `2 - Female...97`  
## • `2 - Female` -> `2 - Female...98`  
## • `2 - Female` -> `2 - Female...99`  
## • `2 - Female` -> `2 - Female...100`  
## • `2 - Female` -> `2 - Female...101`  
## • `2 - Female` -> `2 - Female...102`  
## • `2 - Female` -> `2 - Female...103`  
## • `2 - Female` -> `2 - Female...104`  
## • `2 - Female` -> `2 - Female...105`
```

```
## • `2 - Female` -> `2 - Female...106`  

## • `2 - Female` -> `2 - Female...107`  

## • `2 - Female` -> `2 - Female...108`  

## • `2 - Female` -> `2 - Female...109`  

## • `2 - Female` -> `2 - Female...110`  

## • `2 - Female` -> `2 - Female...111`  

## • `2 - Female` -> `2 - Female...112`  

## • `2 - Female` -> `2 - Female...113`  

## • `2 - Female` -> `2 - Female...114`  

## • `2 - Female` -> `2 - Female...115`  

## • `2 - Female` -> `2 - Female...116`  

## • `2 - Female` -> `2 - Female...117`  

## • `2 - Female` -> `2 - Female...118`  

## • `2 - Female` -> `2 - Female...119`  

## • `2 - Female` -> `2 - Female...120`  

## • `2 - Female` -> `2 - Female...121`  

## • `2 - Female` -> `2 - Female...122`  

## • `2 - Female` -> `2 - Female...123`  

## • `2 - Female` -> `2 - Female...124`  

## • `2 - Female` -> `2 - Female...125`  

## • `2 - Female` -> `2 - Female...126`  

## • `2 - Female` -> `2 - Female...127`  

## • `2 - Female` -> `2 - Female...128`  

## • `2 - Female` -> `2 - Female...129`  

## • `2 - Female` -> `2 - Female...130`  

## • `2 - Female` -> `2 - Female...131`  

## • `2 - Female` -> `2 - Female...132`  

## • `2 - Female` -> `2 - Female...133`  

## • `2 - Female` -> `2 - Female...134`  

## • `2 - Female` -> `2 - Female...135`  

## • `2 - Female` -> `2 - Female...136`
```

```
glimpse(df)
```

```
## Rows: 415  

## Columns: 136  

## $ ...1 <chr> "index", "1", "2", "3", "4", "5", "6", "7", ...  

## $ ...2 <chr> "Inchikey", "SRBFZHDQGSBBOR-IOVATXLUSA-N", ...  

## $ ...3 <chr> "ret.index", "543267", "590775", "589278", ...  

## $ ...4 <chr> "quant mz", "103", "189", "333", "217", "35...  

## $ ...5 <chr> "BB id", "169", "17400", "3470", "5857", "1...  

## $ ...6 <chr> "PubChem", "135191", "10264", "6602431", "6...  

## $ ...7 <chr> "KEGG", "C00181", "C02341", "C00502", "C003...  

## $ ...8 <chr> "knownORunknown", "known", "known", "known"...  

## $ ...9 <chr> "PLS-DA VIP Score", "1.2817599999999998", "...  

## $ ...10 <chr> "RSD Pooled QC", "0.21743276163921682", "0....  

## $ `Male vs Female` <chr> "p_value", "1.87244428976912E-2", "0.919478...  

## $ ...12 <chr> "p_value_adj", "0.107665546661724", "0.9564...  

## $ `median Male/median Femal` <chr> "FoldChange", "0.69725822693591988", "1.047...
```

```
## $ ...14
## $ treatment
## $ `1 - Male...16` 
## $ `1 - Male...17` 
## $ `1 - Male...18` 
## $ `1 - Male...19` 
## $ `1 - Male...20` 
## $ `1 - Male...21` 
## $ `1 - Male...22` 
## $ `1 - Male...23` 
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## $ `1 - Male...40` 
## $ `1 - Male...41` 
## $ `1 - Male...42` 
## $ `1 - Male...43` 
## $ `1 - Male...44` 
## $ `1 - Male...45` 
## $ `1 - Male...46` 
## $ `1 - Male...47` 
## $ `1 - Male...48` 
## $ `1 - Male...49` 
## $ `1 - Male...50` 
## $ `1 - Male...51` 
## $ `1 - Male...52` 
## $ `1 - Male...53` 
## $ `1 - Male...54` 
## $ `1 - Male...55` 
## $ `1 - Male...56` 
## $ `1 - Male...57` 
## $ `1 - Male...58` 
## $ `1 - Male...59` 
## $ `1 - Male...60` 
## $ `1 - Male...61` 
## $ `1 - Male...62` 
## $ `1 - Male...63` 
## $ `1 - Male...64` 

<chr> "log2FoldChange", "-0.36059945342486499", ...
<chr> "label", "xylose", "xylonic acid isomer", ...
<chr> "M1_001", "19537", "685", "534", "4766", "3...
<chr> "M2_002", "6619", "607", "58", "4525", "28"...
<chr> "M3_003", "20015", "1371", "176", "8679", "...
<chr> "M4_004", "13599", "2057", "1722", "23461", ...
<chr> "M5_005", "21525", "1509", "597", "8231", "...
<chr> "M6_006", "11649", "1187", "691", "5288", "...
<chr> "M7_007", "41682", "1681", "630", "10392", ...
<chr> "M8_008", "31105", "912", "168", "4884", "7...
<chr> "M9_009", "18169", "940", "800", "5900", "4...
<chr> "M10_010", "64254", "4816", "1571", "6805", ...
<chr> "M11_011", "49394", "1426", "556", "7627", ...
<chr> "M12_012", "21989", "1347", "648", "24960", ...
<chr> "M13_013", "21908", "1454", "584", "24409", ...
<chr> "M14_014", "31015", "1399", "437", "12902", ...
<chr> "M15_015", "6137", "437", "172", "4718", "2...
<chr> "M16_016", "64278", "1251", "460", "13487", ...
<chr> "M19_017", "28667", "2713", "361", "24524", ...
<chr> "M25_018", "13701", "1426", "103", "5171", ...
<chr> "M26_019", "85301", "1324", "304", "13610", ...
<chr> "M27_020", "17763", "1290", "195", "5099", ...
<chr> "M28_021", "12335", "1187", "311", "7043", ...
<chr> "M29_022", "11820", "1655", "280", "7592", ...
<chr> "M30_023", "11597", "5584", "137", "4677", ...
<chr> "M31_024", "43870", "1904", "159", "292573", ...
<chr> "M32_025", "99634", "2148", "723", "9605", ...
<chr> "M33_026", "23361", "1853", "791", "2358", ...
<chr> "M34_027", "27391", "1311", "378", "9844", ...
<chr> "M35_028", "19707", "958", "145", "6664", ...
<chr> "M36_029", "19578", "1426", "222", "8813", ...
<chr> "M37_030", "69364", "1661", "423", "11889", ...
<chr> "M38_031", "26924", "2012", "1112", "7238", ...
<chr> "M39C_032", "19304", "1516", "329", "4464", ...
<chr> "M38C_033", "16851", "971", "230", "6012", ...
<chr> "M41_034", "26777", "2083", "330", "6137", ...
<chr> "M42_035", "31988", "2286", "921", "5853", ...
<chr> "M43_036", "22082", "1404", "402", "9731", ...
<chr> "M44_037", "25969", "770", "733", "9075", ...
<chr> "M45_038", "22631", "1501", "146", "6569", ...
<chr> "M46_039", "6895", "1229", "350", "8359", ...
<chr> "M47_040", "7945", "2317", "527", "2445", ...
<chr> "M48_041", "46258", "2201", "432", "12879", ...
<chr> "M49_042", "32313", "1969", "923", "7531", ...
<chr> "M50_043", "33191", "474", "1156", "11364", ...
<chr> "M51_044", "27520", "2273", "578", "7694", ...
<chr> "M52_045", "20968", "455", "367", "9312", ...
<chr> "M53_046", "23805", "1754", "352", "8930", ...
<chr> "M54_047", "29822", "1805", "694", "11447", ...
<chr> "M55_048", "11049", "1927", "546", "5333", ...
<chr> "M56_049", "15787", "1413", "182", "3473", ...
```

```
## $ `1 - Male...65` <chr> "M57_050", "26463", "1791", "342", "11472",...
## $ `1 - Male...66` <chr> "M59_051", "27187", "1697", "1349", "4936",...
## $ `1 - Male...67` <chr> "M60_052", "22953", "327", "319", "1968", "...
## $ `1 - Male...68` <chr> "M61_053", "8921", "1968", "352", "11250", ...
## $ `1 - Male...69` <chr> "M62_054", "23322", "1846", "410", "13670", ...
## $ `1 - Male...70` <chr> "M63_055", "7730", "1585", "647", "2934", "...
## $ `1 - Male...71` <chr> "M64_056", "34764", "1795", "245", "10920",...
## $ `1 - Male...72` <chr> "M65_057", "19825", "1605", "785", "2955", ...
## $ `1 - Male...73` <chr> "M66_058", "26585", "1884", "308", "6479", ...
## $ `1 - Male...74` <chr> "M68_059", "33453", "1406", "283", "8139", ...
## $ `1 - Male...75` <chr> "M69_060", "21094", "1927", "260", "7171", ...
## $ `2 - Female...76` <chr> "F1_061", "207654", "2272", "802", "8907", ...
## $ `2 - Female...77` <chr> "F2_062", "138959", "2283", "304", "6531", ...
## $ `2 - Female...78` <chr> "F3_063", "44637", "1158", "639", "4529", "...
## $ `2 - Female...79` <chr> "F4_064", "47100", "1383", "369", "12162", ...
## $ `2 - Female...80` <chr> "F5_065", "43956", "1041", "255", "7904", "...
## $ `2 - Female...81` <chr> "F6_066", "24287", "1983", "855", "8075", "...
## $ `2 - Female...82` <chr> "F7_067", "44540", "1758", "517", "11145", ...
## $ `2 - Female...83` <chr> "F8_068", "20695", "1267", "272", "12828", ...
## $ `2 - Female...84` <chr> "F9_069", "40152", "1765", "274", "10461", ...
## $ `2 - Female...85` <chr> "F13_070", "23179", "1173", "335", "6387", ...
## $ `2 - Female...86` <chr> "F14_071", "9091", "1238", "283", "8957", ...
## $ `2 - Female...87` <chr> "F15_072", "34901", "1684", "714", "2412", ...
## $ `2 - Female...88` <chr> "F17_073", "16010", "1390", "332", "5117", ...
## $ `2 - Female...89` <chr> "F18_074", "33081", "1279", "465", "18314", ...
## $ `2 - Female...90` <chr> "F19_075", "25998", "1822", "282", "19522", ...
## $ `2 - Female...91` <chr> "F20_076", "41107", "4023", "530", "8338", ...
## $ `2 - Female...92` <chr> "F21_077", "20267", "1631", "728", "1495", ...
## $ `2 - Female...93` <chr> "F22_078", "36248", "1427", "291", "9259", ...
## $ `2 - Female...94` <chr> "F23_079", "28616", "1013", "288", "10373", ...
## $ `2 - Female...95` <chr> "F24_080", "35872", "1025", "399", "4675", ...
## $ `2 - Female...96` <chr> "F25C_081", "10802", "1465", "306", "12318", ...
## $ `2 - Female...97` <chr> "F27C_082", "44126", "1365", "593", "4528", ...
## $ `2 - Female...98` <chr> "F28C_083", "54269", "1962", "566", "5922", ...
## $ `2 - Female...99` <chr> "F29C_084", "357540", "1708", "834", "7701", ...
## $ `2 - Female...100` <chr> "F30_085", "38477", "1575", "328", "7569", ...
## $ `2 - Female...101` <chr> "F31_086", "40909", "2075", "946", "8371", ...
## $ `2 - Female...102` <chr> "F32_087", "74415", "917", "597", "7763", ...
## $ `2 - Female...103` <chr> "F33_088", "43431", "3299", "864", "12328", ...
## $ `2 - Female...104` <chr> "F34_089", "80439", "1264", "359", "7527", ...
## $ `2 - Female...105` <chr> "F35C_090", "34328", "1134", "352", "8894", ...
## $ `2 - Female...106` <chr> "F36C_091", "19135", "2424", "358", "5976", ...
## $ `2 - Female...107` <chr> "F37_092", "24238", "1451", "513", "9855", ...
## $ `2 - Female...108` <chr> "F38_093", "22072", "1775", "566", "9779", ...
## $ `2 - Female...109` <chr> "F39_094", "29264", "2206", "499", "4779", ...
## $ `2 - Female...110` <chr> "F43_095", "47070", "1764", "356", "6239", ...
## $ `2 - Female...111` <chr> "F44_096", "18263", "1723", "284", "7309", ...
## $ `2 - Female...112` <chr> "F45_097", "16612", "1448", "157", "11034", ...
## $ `2 - Female...113` <chr> "F47_098", "155085", "1282", "402", "148486", ...
## $ `2 - Female...114` <chr> "F48_099", "13783", "1178", "238", "6571", ...
## $ `2 - Female...115` <chr> "F49_100", "44815", "1391", "416", "8434", ...
```

```

## $ `2 - Female...116`      <chr> "F50_101", "83091", "888", "964", "10702", ...
## $ `2 - Female...117`      <chr> "F51_102", "18811", "1431", "381", "9231", ...
## $ `2 - Female...118`      <chr> "F52_103", "18699", "1374", "223", "8527", ...
## $ `2 - Female...119`      <chr> "103_104", "17372", "1644", "599", "7258", ...
## $ `2 - Female...120`      <chr> "105_105", "18347", "1422", "406", "6321", ...
## $ `2 - Female...121`      <chr> "108_106", "15163", "1299", "37", "7601", ...
## $ `2 - Female...122`      <chr> "111_107", "42048", "2153", "576", "16220", ...
## $ `2 - Female...123`      <chr> "116_108", "33530", "1209", "496", "2713", ...
## $ `2 - Female...124`      <chr> "120_109", "13645", "2249", "892", "729", ...
## $ `2 - Female...125`      <chr> "121_110", "66094", "4184", "874", "14473", ...
## $ `2 - Female...126`      <chr> "122_111", "13053", "1648", "1135", "6141", ...
## $ `2 - Female...127`      <chr> "123_112", "27924", "1472", "303", "10796", ...
## $ `2 - Female...128`      <chr> "124_113", "28929", "1825", "323", "10386", ...
## $ `2 - Female...129`      <chr> "125_114", "69691", "78", "498", "13457", ...
## $ `2 - Female...130`      <chr> "126_115", "16387", "1434", "285", "3818", ...
## $ `2 - Female...131`      <chr> "127_116", "15305", "2168", "351", "10821", ...
## $ `2 - Female...132`      <chr> "128_117", "13898", "1726", "136", "12544", ...
## $ `2 - Female...133`      <chr> "129_118", "240411", "1941", "627", "7634", ...
## $ `2 - Female...134`      <chr> "130_119", "16822", "1495", "368", "8759", ...
## $ `2 - Female...135`      <chr> "131_120", "17116", "1226", "131", "12496", ...
## $ `2 - Female...136`      <chr> "132_121", "19975", "386", "381", "3202", ...

```

# Cleaning and Data Transformation

```

# organize names
# first df line has de colnames
colnames(df) <- as.character(unlist(df[1, ]))
df <- df[-1, , drop = FALSE]

# Convert measurement columns (17:end) to numeric explicitly
measure_cols <- 17:ncol(df)

for (i in measure_cols) {
  df[[i]] <- as.numeric(df[[i]])
}

X <- as.data.frame(df[, measure_cols])

colnames(X) <- paste0("S", seq_len(ncol(X)))
# number of metabolites and samples
if ("Metabolite" %in% colnames(df)) {
  rownames(X) <- df$Metabolite
}

dim(X)

```

```
## [1] 414 120
```

It matches with the article 120 samples (60 males + 60 females)

# Summary statistics

```
summary(X)
```

	S1	S2	S3	S4
## Min.	: 11.0	Min. : 49.0	Min. : 35.0	Min. : 55.0
## 1st Qu.	: 361.8	1st Qu.: 974.8	1st Qu.: 928.5	1st Qu.: 886.2
## Median	: 931.5	Median : 2567.0	Median : 2413.5	Median : 2200.0
## Mean	: 10396.4	Mean : 17884.3	Mean : 15434.6	Mean : 16240.0
## 3rd Qu.	: 2820.5	3rd Qu.: 7546.2	3rd Qu.: 7103.8	3rd Qu.: 6561.8
## Max.	: 1159279.0	Max. : 1312984.0	Max. : 887773.0	Max. : 846476.0
## S5		S6	S7	S8
## Min.	: 57	Min. : 49	Min. : 63	Min. : 36
## 1st Qu.	: 1034	1st Qu.: 1218	1st Qu.: 871	1st Qu.: 1084
## Median	: 2678	Median : 3170	Median : 2626	Median : 2892
## Mean	: 20265	Mean : 17583	Mean : 19948	Mean : 15306
## 3rd Qu.	: 7338	3rd Qu.: 9827	3rd Qu.: 8472	3rd Qu.: 7588
## Max.	: 1331535	Max. : 756697	Max. : 1085291	Max. : 654485
## S9		S10	S11	S12
## Min.	: 45.0	Min. : 51.0	Min. : 42	Min. : 32
## 1st Qu.	: 883.2	1st Qu.: 999.8	1st Qu.: 854	1st Qu.: 836
## Median	: 2420.0	Median : 2603.5	Median : 2386	Median : 2347
## Mean	: 16003.7	Mean : 16155.8	Mean : 15655	Mean : 14944
## 3rd Qu.	: 8532.5	3rd Qu.: 7937.0	3rd Qu.: 7422	3rd Qu.: 7623
## Max.	: 613979.0	Max. : 979339.0	Max. : 662597	Max. : 600872
## S13		S14	S15	S16
## Min.	: 53.0	Min. : 23.0	Min. : 31	Min. : 32
## 1st Qu.	: 898.2	1st Qu.: 425.2	1st Qu.: 652	1st Qu.: 814
## Median	: 2714.5	Median : 1077.5	Median : 1932	Median : 2408
## Mean	: 20509.0	Mean : 12255.6	Mean : 14991	Mean : 15781
## 3rd Qu.	: 8495.5	3rd Qu.: 2973.8	3rd Qu.: 5742	3rd Qu.: 7016
## Max.	: 1223172.0	Max. : 1357588.0	Max. : 664051	Max. : 923306
## S17		S18	S19	S20
## Min.	: 45	Min. : 43.0	Min. : 37.0	Min. : 57
## 1st Qu.	: 802	1st Qu.: 872.5	1st Qu.: 760.8	1st Qu.: 1001
## Median	: 2398	Median : 2497.0	Median : 2002.5	Median : 2714
## Mean	: 22298	Mean : 14868.9	Mean : 16331.1	Mean : 16196
## 3rd Qu.	: 8043	3rd Qu.: 7397.0	3rd Qu.: 5930.2	3rd Qu.: 6979
## Max.	: 1412185	Max. : 615658.0	Max. : 1047043.0	Max. : 718072
## S21		S22	S23	S24
## Min.	: 63.0	Min. : 42	Min. : 19.0	Min. : 35.0
## 1st Qu.	: 829.8	1st Qu.: 1020	1st Qu.: 517.5	1st Qu.: 997.5
## Median	: 2398.0	Median : 2610	Median : 1475.0	Median : 2618.5
## Mean	: 17775.5	Mean : 16756	Mean : 12719.6	Mean : 17888.5

```

## 3rd Qu.: 7253.5   3rd Qu.: 7651   3rd Qu.: 4454.2   3rd Qu.: 7489.2
## Max.    :1026464.0  Max.    :849364  Max.    :704274.0  Max.    :1002880.0
##          S25           S26           S27           S28
## Min.    : 57    Min.    : 57.0    Min.    : 38.0    Min.    : 55.0
## 1st Qu.: 1102   1st Qu.: 843.2   1st Qu.: 769.5   1st Qu.: 995.8
## Median  : 2633   Median : 2615.0   Median : 2272.0   Median : 2581.0
## Mean    : 17566  Mean    : 28104.5  Mean    : 15048.0  Mean    : 15940.6
## 3rd Qu.: 7642   3rd Qu.: 9100.0   3rd Qu.: 7267.2   3rd Qu.: 8733.2
## Max.    :1243970  Max.    :2448882.0  Max.    :590052.0  Max.    :795015.0
##          S29           S30           S31           S32
## Min.    : 30    Min.    : 61    Min.    : 28.0    Min.    : 43
## 1st Qu.: 1006   1st Qu.: 1034   1st Qu.: 835.8   1st Qu.: 634
## Median  : 2598   Median : 3132   Median : 2850.0   Median : 1934
## Mean    : 21812  Mean    : 20275  Mean    : 19758.3  Mean    : 14803
## 3rd Qu.: 8412   3rd Qu.: 8966   3rd Qu.: 8962.2   3rd Qu.: 6673
## Max.    :1474685  Max.    :1033848  Max.    :652214.0  Max.    :611685
##          S33           S34           S35           S36
## Min.    : 57    Min.    : 49.0   Min.    : 69    Min.    : 40
## 1st Qu.: 1094   1st Qu.: 875.5   1st Qu.: 1199   1st Qu.: 1023
## Median  : 3131   Median : 2439.5   Median : 2678   Median : 3118
## Mean    : 18916  Mean    : 20133.2  Mean    : 17923  Mean    : 20058
## 3rd Qu.: 8026   3rd Qu.: 8751.2   3rd Qu.: 8075   3rd Qu.: 9702
## Max.    :988258  Max.    :1156623.0  Max.    :750958  Max.    :903330
##          S37           S38           S39           S40
## Min.    : 56.0   Min.    : 30.0   Min.    : 27    Min.    : 49
## 1st Qu.: 792.8  1st Qu.: 913.2   1st Qu.: 1198   1st Qu.: 1165
## Median  : 2520.0  Median : 2379.5   Median : 2990   Median : 3186
## Mean    : 21491.9  Mean    : 20571.5  Mean    : 18004  Mean    : 16763
## 3rd Qu.: 9072.8  3rd Qu.: 7049.2   3rd Qu.: 8534   3rd Qu.: 9282
## Max.    :1382326.0  Max.    :1343658.0  Max.    :930312  Max.    :622009
##          S41           S42           S43           S44
## Min.    : 67.0   Min.    : 60    Min.    : 58    Min.    : 47.0
## 1st Qu.: 933.2  1st Qu.: 1284   1st Qu.: 1288   1st Qu.: 930.2
## Median  : 2570.5  Median : 3593   Median : 3736   Median : 2621.5
## Mean    : 18537.8  Mean    : 21514  Mean    : 19702  Mean    : 20043.4
## 3rd Qu.: 7634.5  3rd Qu.: 10507  3rd Qu.: 10996  3rd Qu.: 9137.2
## Max.    :958901.0  Max.    :1050715  Max.    :978076  Max.    :1062304.0
##          S45           S46           S47           S48
## Min.    : 45.0   Min.    : 27.0   Min.    : 71    Min.    : 14
## 1st Qu.: 928.5  1st Qu.: 983.2   1st Qu.: 1028   1st Qu.: 367
## Median  : 2550.0  Median : 2764.0   Median : 2775   Median : 1138
## Mean    : 19243.2  Mean    : 18173.2  Mean    : 22158  Mean    : 10432
## 3rd Qu.: 8023.2  3rd Qu.: 8656.0   3rd Qu.: 8392   3rd Qu.: 3546
## Max.    :894751.0  Max.    :814803.0  Max.    :1384220  Max.    :1378594
##          S49           S50           S51           S52
## Min.    : 33    Min.    : 37    Min.    : 11.0   Min.    : 44
## 1st Qu.: 948   1st Qu.: 1020   1st Qu.: 327.8  1st Qu.: 1118
## Median  : 2785  Median : 2486   Median : 996.0  Median : 2982
## Mean    : 19689  Mean    : 16457  Mean    : 9556.1  Mean    : 20580
## 3rd Qu.: 7976  3rd Qu.: 6876   3rd Qu.: 2873.2 3rd Qu.: 8585
## Max.    :928126  Max.    :895948  Max.    :920842.0  Max.    :1012064

```

##	S53	S54	S55	S56
##	Min. : 59	Min. : 81	Min. : 53	Min. : 37.0
##	1st Qu.: 1013	1st Qu.: 1026	1st Qu.: 1404	1st Qu.: 920.8
##	Median : 3070	Median : 2434	Median : 3426	Median : 2498.0
##	Mean : 21624	Mean : 19055	Mean : 17594	Mean : 19834.2
##	3rd Qu.: 9218	3rd Qu.: 7902	3rd Qu.: 9361	3rd Qu.: 7251.0
##	Max. : 1159151	Max. : 1158978	Max. : 897174	Max. : 1274193.0
##	S57	S58	S59	S60
##	Min. : 41	Min. : 48	Min. : 55.0	Min. : 32
##	1st Qu.: 1067	1st Qu.: 1032	1st Qu.: 747.8	1st Qu.: 882
##	Median : 2767	Median : 2590	Median : 2419.0	Median : 2614
##	Mean : 19441	Mean : 19249	Mean : 17639.2	Mean : 15477
##	3rd Qu.: 9708	3rd Qu.: 8131	3rd Qu.: 8217.2	3rd Qu.: 7118
##	Max. : 1521963	Max. : 1204027	Max. : 857508.0	Max. : 481398
##	S61	S62	S63	S64
##	Min. : 30.0	Min. : 14	Min. : 44.0	Min. : 45
##	1st Qu.: 756.5	1st Qu.: 550	1st Qu.: 810.5	1st Qu.: 697
##	Median : 2116.5	Median : 1470	Median : 2586.0	Median : 1960
##	Mean : 14449.6	Mean : 10995	Mean : 19064.3	Mean : 16921
##	3rd Qu.: 6930.0	3rd Qu.: 4598	3rd Qu.: 7443.8	3rd Qu.: 5548
##	Max. : 654335.0	Max. : 473352	Max. : 1252073.0	Max. : 1166064
##	S65	S66	S67	S68
##	Min. : 37	Min. : 36	Min. : 43.0	Min. : 47
##	1st Qu.: 1117	1st Qu.: 1033	1st Qu.: 809.8	1st Qu.: 1122
##	Median : 2720	Median : 2960	Median : 2232.0	Median : 3137
##	Mean : 16367	Mean : 20217	Mean : 16391.2	Mean : 16657
##	3rd Qu.: 8012	3rd Qu.: 9554	3rd Qu.: 7177.2	3rd Qu.: 9066
##	Max. : 645905	Max. : 1239046	Max. : 809789.0	Max. : 717275
##	S69	S70	S71	S72
##	Min. : 46.0	Min. : 45	Min. : 73	Min. : 65.0
##	1st Qu.: 893.2	1st Qu.: 947	1st Qu.: 1064	1st Qu.: 709.5
##	Median : 2427.5	Median : 2646	Median : 2829	Median : 1909.0
##	Mean : 15771.6	Mean : 18762	Mean : 24544	Mean : 18327.2
##	3rd Qu.: 6434.0	3rd Qu.: 7962	3rd Qu.: 8758	3rd Qu.: 5963.2
##	Max. : 786634.0	Max. : 1026648	Max. : 1763202	Max. : 1164459.0
##	S73	S74	S75	S76
##	Min. : 89	Min. : 41.0	Min. : 51.0	Min. : 94.0
##	1st Qu.: 1027	1st Qu.: 833.2	1st Qu.: 824.5	1st Qu.: 973.5
##	Median : 2436	Median : 2737.5	Median : 2282.5	Median : 2513.5
##	Mean : 19399	Mean : 18837.0	Mean : 17355.3	Mean : 15380.8
##	3rd Qu.: 7973	3rd Qu.: 8114.0	3rd Qu.: 8586.5	3rd Qu.: 7788.5
##	Max. : 1431153	Max. : 1011305.0	Max. : 817150.0	Max. : 756530.0
##	S77	S78	S79	S80
##	Min. : 55	Min. : 50.0	Min. : 57.0	Min. : 49
##	1st Qu.: 729	1st Qu.: 896.8	1st Qu.: 718.8	1st Qu.: 1025
##	Median : 2194	Median : 2277.5	Median : 1976.0	Median : 3026
##	Mean : 18062	Mean : 14365.5	Mean : 16101.9	Mean : 16095
##	3rd Qu.: 7172	3rd Qu.: 6604.8	3rd Qu.: 6489.0	3rd Qu.: 9898
##	Max. : 1236177	Max. : 727831.0	Max. : 876808.0	Max. : 585919
##	S81	S82	S83	S84
##	Min. : 21.0	Min. : 46	Min. : 37.0	Min. : 54.0

```

## 1st Qu.: 826.5   1st Qu.: 827    1st Qu.: 904.8   1st Qu.: 967.8
## Median : 2425.5 Median : 1850    Median : 2553.0   Median : 2523.5
## Mean   : 16124.8 Mean  : 15839   Mean  : 22022.1  Mean  : 16216.5
## 3rd Qu.: 6523.0 3rd Qu.: 6794    3rd Qu.: 7966.8   3rd Qu.: 7958.8
## Max.   :766114.0 Max.  :803939   Max.  :1093912.0  Max.  :739373.0
##          S85           S86           S87           S88
## Min.   : 55       Min.   : 46.0     Min.   : 76      Min.   : 39
## 1st Qu.: 838      1st Qu.: 828.2   1st Qu.: 1249   1st Qu.: 777
## Median : 2952     Median : 2569.0   Median : 3672   Median : 2065
## Mean   : 23280    Mean  : 18416.6  Mean  : 18228  Mean  : 15579
## 3rd Qu.: 9084     3rd Qu.: 8779.8   3rd Qu.: 11428  3rd Qu.: 5805
## Max.   :1358932    Max.  :1076740.0  Max.  :793472  Max.  :838662
##          S89           S90           S91           S92
## Min.   : 42       Min.   : 38.0     Min.   : 0.0     Min.   : 66.0
## 1st Qu.: 1044     1st Qu.: 678.8    1st Qu.: 701.8   1st Qu.: 989.2
## Median : 2636     Median : 2041.5   Median : 2077.0  Median : 2734.0
## Mean   : 15765    Mean  : 14162.8  Mean  : 16451.8  Mean  : 14734.1
## 3rd Qu.: 7137     3rd Qu.: 5630.2   3rd Qu.: 7192.8  3rd Qu.: 7427.8
## Max.   :709939     Max.  :651143.0  Max.  :1002377.0 Max.  :485330.0
##          S93           S94           S95           S96
## Min.   : 53       Min.   : 0        Min.   : 42.0    Min.   : 45
## 1st Qu.: 860      1st Qu.: 941     1st Qu.: 676.5   1st Qu.: 914
## Median : 2600     Median : 2556    Median : 1890.5  Median : 2553
## Mean   : 17691    Mean  : 16531   Mean  : 17419.6  Mean  : 17090
## 3rd Qu.: 8764     3rd Qu.: 7706    3rd Qu.: 6036.5  3rd Qu.: 8547
## Max.   :858142     Max.  :713027   Max.  :1147218.0 Max.  :838240
##          S97           S98           S99           S100
## Min.   : 23.0     Min.   : 33.0    Min.   : 46      Min.   : 33.0
## 1st Qu.: 475.8    1st Qu.: 842.8   1st Qu.: 796     1st Qu.: 890.2
## Median : 1519.0   Median : 2379.5  Median : 2492    Median : 2497.5
## Mean   : 11912.7  Mean  : 19292.5  Mean  : 17882   Mean  : 17162.3
## 3rd Qu.: 4719.5   3rd Qu.: 6850.2   3rd Qu.: 7372   3rd Qu.: 7196.5
## Max.   :394734.0  Max.  :1195071.0 Max.  :937666  Max.  :1047894.0
##          S101          S102          S103          S104
## Min.   : 41       Min.   : 86.0    Min.   : 51      Min.   : 37.0
## 1st Qu.: 961      1st Qu.: 900.5   1st Qu.: 1150   1st Qu.: 752.5
## Median : 2355     Median : 2503.5  Median : 2639   Median : 2033.5
## Mean   : 14641    Mean  : 21895.1  Mean  : 17280  Mean  : 14209.1
## 3rd Qu.: 6269     3rd Qu.: 7907.5   3rd Qu.: 7093   3rd Qu.: 6888.2
## Max.   :555121     Max.  :1875999.0 Max.  :1476436 Max.  :835449.0
##          S105          S106          S107          S108
## Min.   : 18.0     Min.   : 47.0    Min.   : 34      Min.   : 53
## 1st Qu.: 735.2    1st Qu.: 890.5   1st Qu.: 910     1st Qu.: 981
## Median : 2122.5   Median : 3107.5  Median : 2410   Median : 2956
## Mean   : 14972.5  Mean  : 17048.6  Mean  : 14732  Mean  : 17213
## 3rd Qu.: 7262.2   3rd Qu.: 9262.5  3rd Qu.: 7289   3rd Qu.: 7791
## Max.   :658556.0  Max.  :681033.0  Max.  :608973 Max.  :939649
##          S109          S110          S111          S112
## Min.   : 50       Min.   : 46.0    Min.   : 52      Min.   : 52
## 1st Qu.: 942      1st Qu.: 834.2   1st Qu.: 1023   1st Qu.: 1009
## Median : 2816     Median : 2394.0   Median : 2802   Median : 2761

```

```

##  Mean    : 16926   Mean    : 17572.9   Mean    : 21115   Mean    : 18704
## 3rd Qu.: 7823    3rd Qu.: 7052.0    3rd Qu.: 8988    3rd Qu.: 8308
## Max.   :533155   Max.   :1037573.0   Max.   :1427015   Max.   :777934
##          S113           S114           S115           S116
##  Min.   : 48       Min.   : 33       Min.   : 82       Min.   : 41
## 1st Qu.: 1098    1st Qu.: 1011    1st Qu.: 1132    1st Qu.: 1107
## Median : 3168    Median : 2760    Median : 2595    Median : 2692
## Mean   : 17953   Mean   : 14737   Mean   : 16030   Mean   : 18147
## 3rd Qu.: 8649    3rd Qu.: 7086    3rd Qu.: 8018    3rd Qu.: 7900
## Max.   :818457   Max.   :655562   Max.   :710631   Max.   :994444
##          S117           S118           S119           S120
##  Min.   : 42.0    Min.   : 45.0    Min.   : 51.0    Min.   : 21.0
## 1st Qu.: 859.8   1st Qu.: 989.5   1st Qu.: 926.2   1st Qu.: 421.5
## Median : 2474.0  Median : 2849.0  Median : 2439.0  Median : 1033.0
## Mean   : 14971.4 Mean   : 19385.2 Mean   : 17778.0 Mean   : 10041.5
## 3rd Qu.: 8341.2  3rd Qu.: 7703.2  3rd Qu.: 9066.8  3rd Qu.: 3205.0
## Max.   :655882.0 Max.   :1265896.0 Max.   :944806.0 Max.   :1565960.0

```

```

# Count total zero values
sum(X == 0, na.rm = TRUE)

```

```

## [1] 2

```

```

# Missing values check
sum(is.na(X))

```

```

## [1] 0

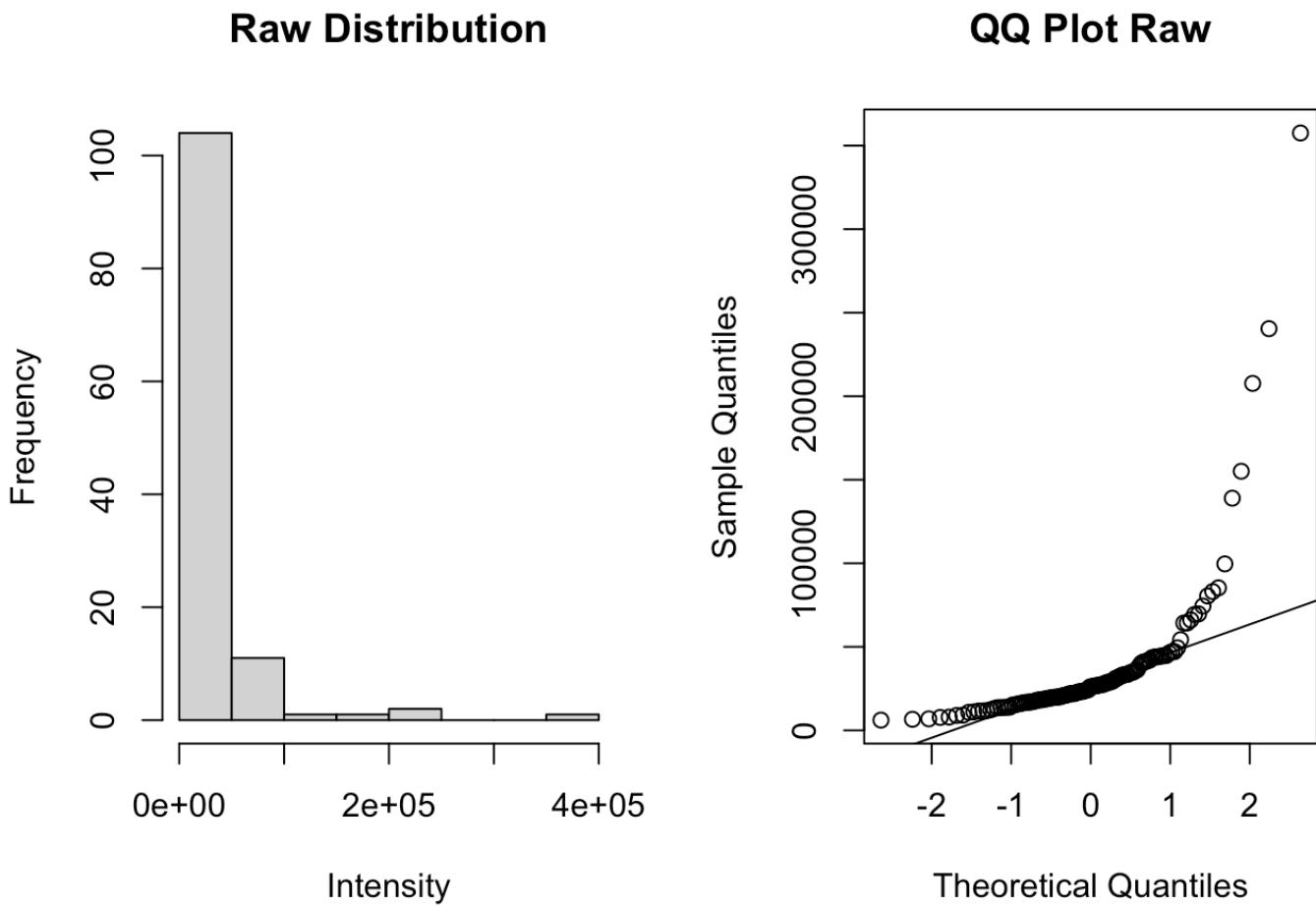
```

## Is it the data Gaussian Distributed?

```

par(mfrow=c(1,2))
hist(as.numeric(X[1,]), main="Raw Distribution", xlab="Intensity")
qqnorm(as.numeric(X[1,]), main="QQ Plot Raw")
qqline(as.numeric(X[1,]))

```



```
par(mfrow=c(1,1))
```

## Histogram inspection

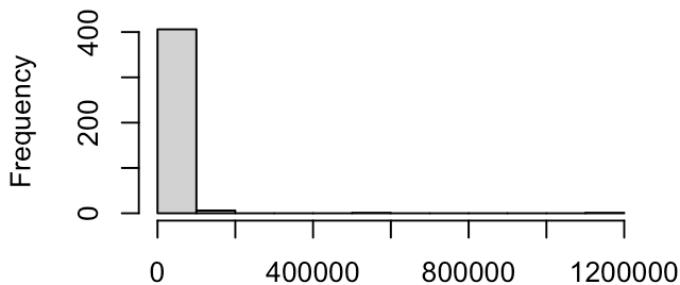
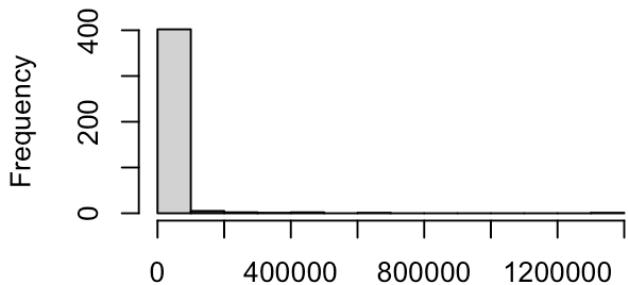
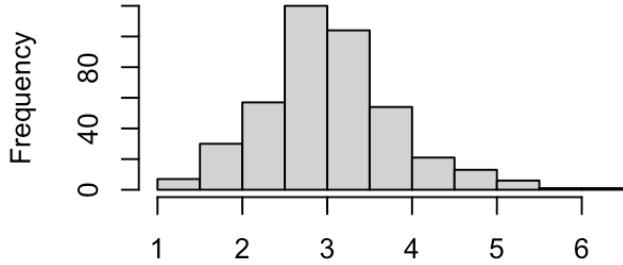
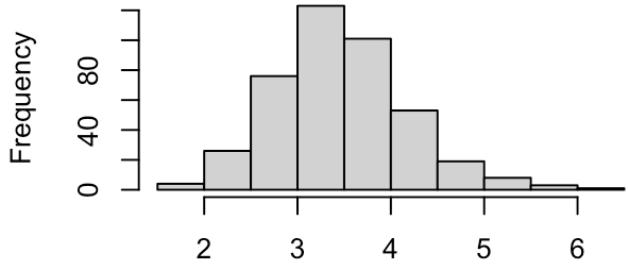
To assess distributional properties, histogram inspection was performed. Raw metabolite intensities showed pronounced right-skewness, supporting the need for a log-transformation to improve normality and stabilize variance prior to multivariate analysis.

```
feat1 <- as.numeric(X[[1]]) #S1
feat2 <- as.numeric(X[[2]]) #S2

par(mfrow = c(2,2))

# Raw intensity distributions
hist(feat1, main = "Raw Intensities - Feature 1", xlab = "", col = "lightgray")
hist(feat2, main = "Raw Intensities - Feature 2", xlab = "", col = "lightgray")

# After log10 transformation
hist(log10(feat1 + 1), main = "Log10 - Feature 1", xlab = "", col = "lightgray")
hist(log10(feat2 + 1), main = "Log10 - Feature 2", xlab = "", col = "lightgray")
```

**Raw Intensities - Feature 1****Raw Intensities - Feature 2****Log10 - Feature 1****Log10 - Feature 2**

```
par(mfrow = c(1,1))
```

The raw intensity histograms show strong right-skewness with extreme values. After log10 transformation, the distributions become more symmetric and less heteroscedastic, supporting the use of log-transformed and autoscaled data for PCA and PLS-DA.

## Non linear

```
# Convert to standard data frame to avoid tibble recycling issues
X_nozero <- as.data.frame(X)

for(i in 1:nrow(X_nozero)){
  row_vals <- as.numeric(X_nozero[i, ]) # convert row to numeric vector

  # Safeguard: if the row is all zeros (rare but possible)
  if(all(row_vals == 0)){
    row_vals[row_vals == 0] <- 1 # placeholder before log10
  } else {
    min_val <- min(row_vals[row_vals > 0], na.rm = TRUE)
    row_vals[row_vals == 0] <- min_val / 2
  }

  X_nozero[i, ] <- row_vals # assign back properly
}
```

## PCA

A preliminary variance-based feature filtering step (top 20% most variable metabolites) was evaluated as an unsupervised method for noise reduction and dimensionality control. However, this procedure resulted in the removal of several metabolites previously identified as statistically significant in the univariate analysis, consequently reducing the number of biologically relevant features and weakening the discrimination between sexes in downstream multivariate models. Therefore, variance filtering was not retained in the final workflow to preserve subtle yet meaningful metabolic differences.

The matrix was transposed so that samples correspond to rows and metabolites to columns, which is the correct structure required for multivariate analyses such as PCA and PLS-DA, where each row must represent an independent observation:

- With <- scale(t(X\_log)).

```
# Log10 transformation
X_log <- log10(X_nozero)

# Scaling for PCA (samples as rows)
X_scaled <- scale(t(X_log))

# PCA
pca <- prcomp(X_scaled, center = TRUE, scale. = FALSE)
summary(pca)
```

```
## Importance of components:
##                               PC1      PC2      PC3      PC4      PC5      PC6      PC7
## Standard deviation     8.9816  4.96339  4.88671  4.34067  3.71722  3.65416  3.42666
## Proportion of Variance 0.1948  0.05951  0.05768  0.04551  0.03338  0.03225  0.02836
## Cumulative Proportion   0.1948  0.25436  0.31204  0.35755  0.39093  0.42318  0.45154
##                               PC8      PC9      PC10     PC11     PC12     PC13     PC14
```

```

## Standard deviation      3.05556 2.93806 2.73820 2.66792 2.60252 2.49513 2.43427
## Proportion of Variance 0.02255 0.02085 0.01811 0.01719 0.01636 0.01504 0.01431
## Cumulative Proportion  0.47410 0.49495 0.51306 0.53025 0.54661 0.56165 0.57596
##                               PC15     PC16     PC17     PC18     PC19     PC20     PC21
## Standard deviation      2.38762 2.33392 2.23402 2.21841 2.16754 2.08917 2.07092
## Proportion of Variance 0.01377 0.01316 0.01206 0.01189 0.01135 0.01054 0.01036
## Cumulative Proportion  0.58973 0.60289 0.61494 0.62683 0.63818 0.64872 0.65908
##                               PC22     PC23     PC24     PC25     PC26     PC27     PC28
## Standard deviation      2.00821 1.96491 1.92119 1.9196  1.89262 1.86169 1.82722
## Proportion of Variance 0.00974 0.00933 0.00892 0.0089  0.00865 0.00837 0.00806
## Cumulative Proportion  0.66882 0.67815 0.68706 0.6960  0.70462 0.71299 0.72105
##                               PC29     PC30     PC31     PC32     PC33     PC34     PC35
## Standard deviation      1.8090  1.78058 1.74800 1.70625 1.68245 1.67253 1.64633
## Proportion of Variance 0.0079  0.00766 0.00738 0.00703 0.00684 0.00676 0.00655
## Cumulative Proportion  0.7290  0.73661 0.74399 0.75103 0.75786 0.76462 0.77117
##                               PC36     PC37     PC38     PC39     PC40     PC41     PC42
## Standard deviation      1.62664 1.60528 1.57799 1.54693 1.52758 1.51314 1.50251
## Proportion of Variance 0.00639 0.00622 0.00601 0.00578 0.00564 0.00553 0.00545
## Cumulative Proportion  0.77756 0.78378 0.78980 0.79558 0.80121 0.80675 0.81220
##                               PC43     PC44     PC45     PC46     PC47     PC48     PC49
## Standard deviation      1.47915 1.46136 1.44511 1.42020 1.40728 1.40112 1.38371
## Proportion of Variance 0.00528 0.00516 0.00504 0.00487 0.00478 0.00474 0.00462
## Cumulative Proportion  0.81748 0.82264 0.82769 0.83256 0.83734 0.84208 0.84671
##                               PC50     PC51     PC52     PC53     PC54     PC55     PC56
## Standard deviation      1.3504  1.34801 1.33024 1.32638 1.30937 1.27730 1.26135
## Proportion of Variance 0.0044  0.00439 0.00427 0.00425 0.00414 0.00394 0.00384
## Cumulative Proportion  0.8511  0.85550 0.85978 0.86403 0.86817 0.87211 0.87595
##                               PC57     PC58     PC59     PC60     PC61     PC62     PC63
## Standard deviation      1.24856 1.23645 1.22854 1.22654 1.20842 1.18012 1.16099
## Proportion of Variance 0.00377 0.00369 0.00365 0.00363 0.00353 0.00336 0.00326
## Cumulative Proportion  0.87972 0.88341 0.88705 0.89069 0.89422 0.89758 0.90084
##                               PC64     PC65     PC66     PC67     PC68     PC69     PC70
## Standard deviation      1.15572 1.14283 1.13768 1.11035 1.10403 1.08755 1.07984
## Proportion of Variance 0.00323 0.00315 0.00313 0.00298 0.00294 0.00286 0.00282
## Cumulative Proportion  0.90406 0.90722 0.91034 0.91332 0.91626 0.91912 0.92194
##                               PC71     PC72     PC73     PC74     PC75     PC76     PC77
## Standard deviation      1.07325 1.0564  1.04196 1.0383  1.01892 1.01293 1.01156
## Proportion of Variance 0.00278 0.0027  0.00262 0.0026  0.00251 0.00248 0.00247
## Cumulative Proportion  0.92472 0.9274  0.93004 0.9326  0.93515 0.93763 0.94010
##                               PC78     PC79     PC80     PC81     PC82     PC83     PC84
## Standard deviation      1.00178 0.98745 0.97119 0.96110 0.94572 0.92841 0.92163
## Proportion of Variance 0.00242 0.00236 0.00228 0.00223 0.00216 0.00208 0.00205
## Cumulative Proportion  0.94252 0.94488 0.94716 0.94939 0.95155 0.95363 0.95568
##                               PC85     PC86     PC87     PC88     PC89     PC90     PC91
## Standard deviation      0.90321 0.89679 0.88415 0.87200 0.8639  0.85119 0.83708
## Proportion of Variance 0.00197 0.00194 0.00189 0.00184 0.0018  0.00175 0.00169
## Cumulative Proportion  0.95765 0.95960 0.96148 0.96332 0.9651  0.96687 0.96857
##                               PC92     PC93     PC94     PC95     PC96     PC97     PC98
## Standard deviation      0.83220 0.82397 0.80990 0.79329 0.77982 0.77263 0.76297
## Proportion of Variance 0.00167 0.00164 0.00158 0.00152 0.00147 0.00144 0.00141
## Cumulative Proportion  0.97024 0.97188 0.97346 0.97498 0.97645 0.97789 0.97930

```

```

##          PC99   PC100   PC101   PC102   PC103   PC104   PC105
## Standard deviation 0.75965 0.7335 0.72827 0.70693 0.7059 0.69253 0.68757
## Proportion of Variance 0.00139 0.0013 0.00128 0.00121 0.0012 0.00116 0.00114
## Cumulative Proportion 0.98069 0.9820 0.98328 0.98448 0.9857 0.98684 0.98799
##          PC106   PC107   PC108   PC109   PC110   PC111   PC112
## Standard deviation 0.67829 0.66059 0.65036 0.63401 0.61801 0.60428 0.60118
## Proportion of Variance 0.00111 0.00105 0.00102 0.00097 0.00092 0.00088 0.00087
## Cumulative Proportion 0.98910 0.99015 0.99117 0.99214 0.99307 0.99395 0.99482
##          PC113   PC114   PC115   PC116   PC117   PC118   PC119
## Standard deviation 0.58644 0.58182 0.56989 0.55374 0.54339 0.53442 0.4991
## Proportion of Variance 0.00083 0.00082 0.00078 0.00074 0.00071 0.00069 0.0006
## Cumulative Proportion 0.99565 0.99647 0.99725 0.99800 0.99871 0.99940 1.0000
##          PC120
## Standard deviation 3.989e-15
## Proportion of Variance 0.000e+00
## Cumulative Proportion 1.000e+00

```

- Summary statistics show very different scales and non-normal distributions
- A few zero values detected → replaced with half of minimum value  
→ required for log10 transformation
- Applied log10(x) to reduce skewness and stabilize variance
- Autoscaling (mean-center + unit variance) to make metabolites comparable

```

# Sanity check: do sex labels align with PCA samples?
sex_row <- as.character(raw_df[3, ])
sample_names_raw <- sex_row[sex_row %in% c("Male", "Female")]
sample_cols <- colnames(X)

sex <- factor(sample_names_raw[1:length(sample_cols)])
length(sex)

```

```
## [1] 120
```

```
table(sex)
```

```

## sex
## Female    Male
##      60      60

```

```
all(!is.na(sex))
```

```
## [1] TRUE
```

```
identical(length(sex), nrow(pca$x))

## [1] TRUE

pca_scores <- as.data.frame(pca$x[, 1:2])

center <- colMeans(pca_scores)
cov_mat <- cov(pca_scores)

distances <- mahalanobis(pca_scores, center, cov_mat)

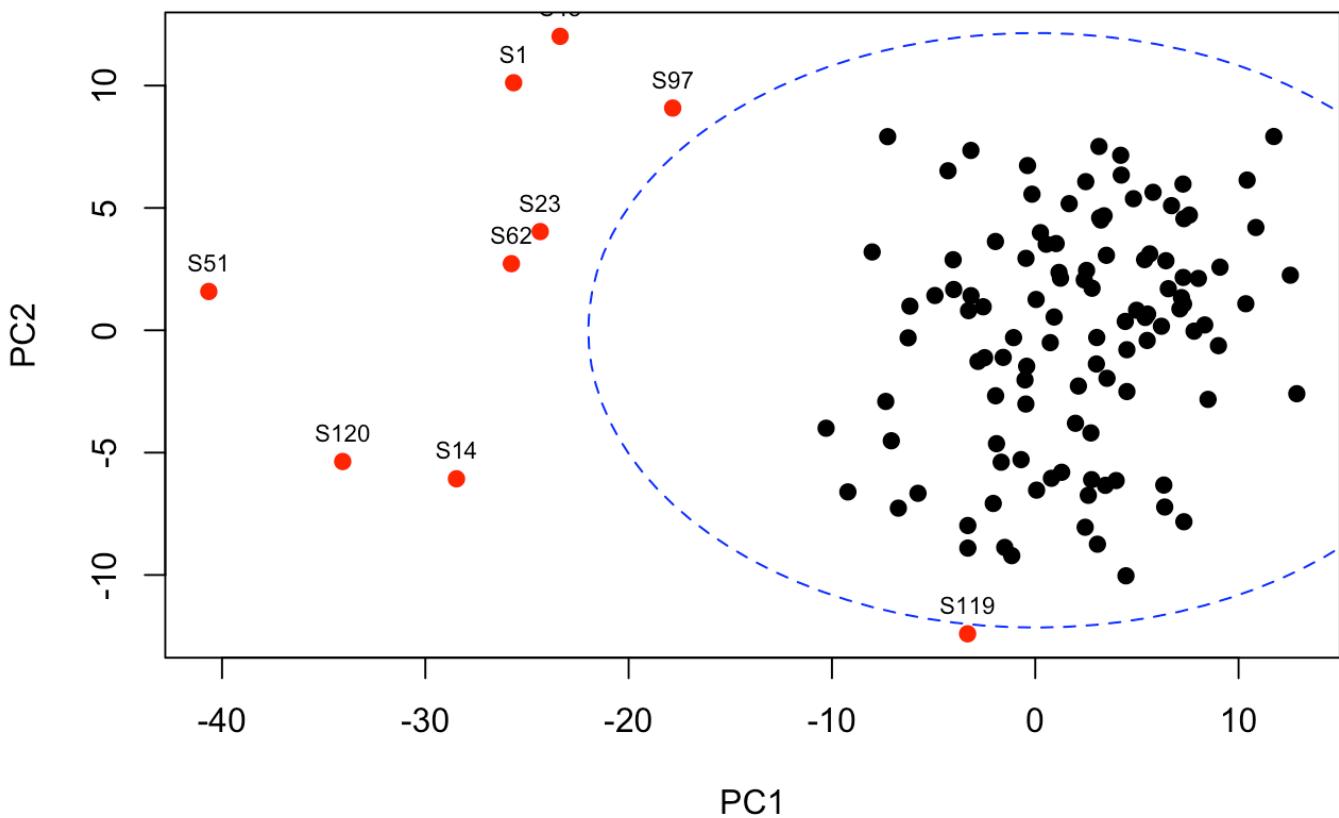
# Cutoff (chi with p=0.95 and 2 df)
cutoff <- qchisq(0.95, df = 2)

# plot with condidese matrix
plot(pca$x[,1], pca$x[,2],
      pch = 19,
      col = ifelse(distances > cutoff, "red", "black"), # Outliers a vermelho
      xlab = "PC1", ylab = "PC2",
      main = "PCA Outlier Detection (95% CI)")

lines(ellipse(cov_mat, centre = center, level = 0.95), col="blue", lty=2)

text(pca$x[,1], pca$x[,2],
     labels = ifelse(distances > cutoff, rownames(pca$x), ""),
     pos = 3, cex = 0.7)
```

## PCA Outlier Detection (95% CI)



```
# Identify outliers
outliers <- which(distances > cutoff)
print(paste("Outliers detected:", length(outliers)))
```

```
## [1] "Outliers detected: 9"
```

We detected 9 outliers, but they weren't removed because:

Outliers reflect **real biological variability** within the healthy population.

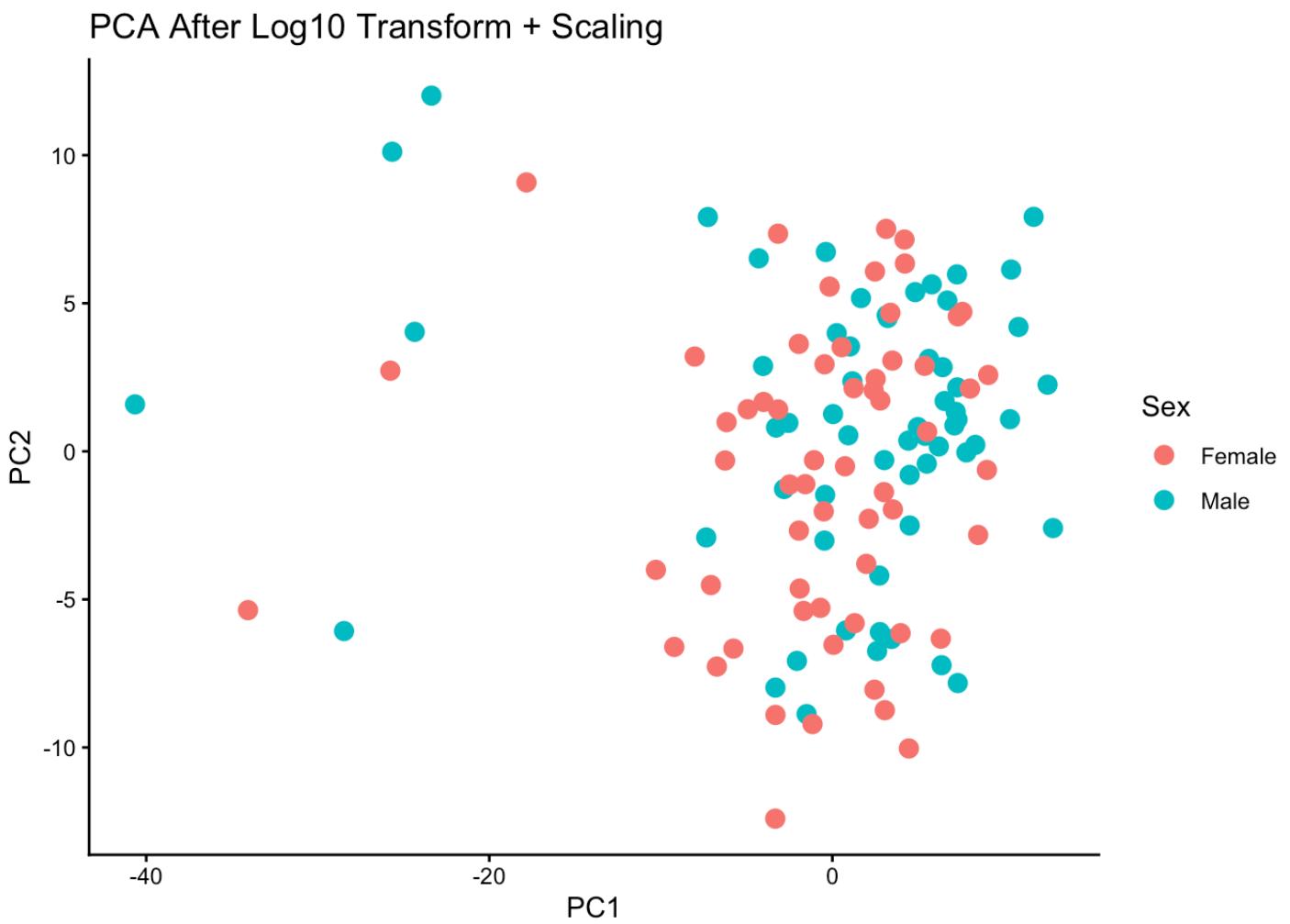
Removing them could introduce **bias**, especially if outliers are unevenly distributed between sexes.

Furthermore, the original study **did not exclude any samples** all **120 subjects** were analyzed in full.

## PCA after log transformation

```
score_df <- data.frame(
  PC1 = pca$x[,1],
  PC2 = pca$x[,2],
  Sex = sex
)

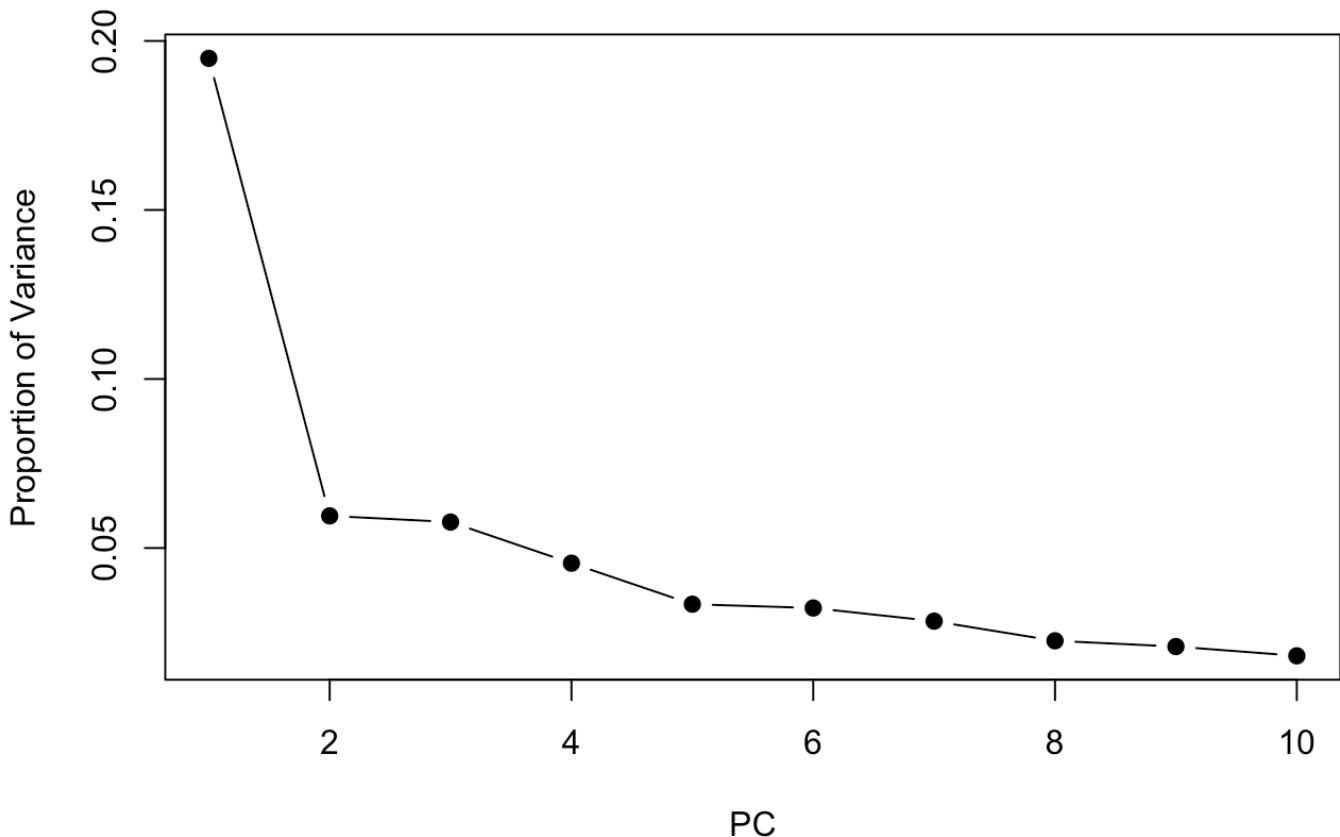
ggplot(score_df, aes(PC1, PC2, color = Sex)) +
  geom_point(size = 3) +
  theme_classic() +
  ggtitle("PCA After Log10 Transform + Scaling")
```



```
# Scree plot (PCA Variance Explained)
variance <- pca$sdev^2 / sum(pca$sdev^2)

plot(variance[1:10], type="b", pch=19,
      xlab="PC", ylab="Proportion of Variance",
      main="Scree Plot - PCA")
```

### Scree Plot - PCA



- Score plot shows a trend of separation between Male and Female
- Some possible outliers appear (next step: detection)
- Scree Plot indicates PC1+PC2 explain ~20–30% variance → normal for metabolomics

## Split Test/Training

We split the data into training and test sets (70/30) and perform univariate t-tests on the training set only. FDR correction is applied to identify metabolites significantly different between sexes.

```

set.seed(123)

train_index <- createDataPartition(sex, p = 0.7, list = FALSE)

X_train <- X_scaled[train_index, ]
X_test <- X_scaled[-train_index, ]

X_train <- as.data.frame(X_train)
X_test <- as.data.frame(X_test)

y_train <- sex[train_index]
y_test <- sex[-train_index]

pvals <- apply(X_train, 2, function(x) t.test(x ~ y_train)$p.value)
pvals_fdr <- p.adjust(pvals, method = "fdr")

head(sort(pvals_fdr))

```

```

##          V22        V399        V10        V84        V51        V113
## 0.001753165 0.002134547 0.044318477 0.044318477 0.044551591 0.044551591

```

Several metabolites show significant sex differences (FDR < 0.05). These will be considered as candidates for biomarker selection in the supervised modeling step.

## Initials PLS-DA

An initial PLS-DA model with 10 components was trained on the training set to evaluate whether the metabolomic profiles discriminate between sexes.

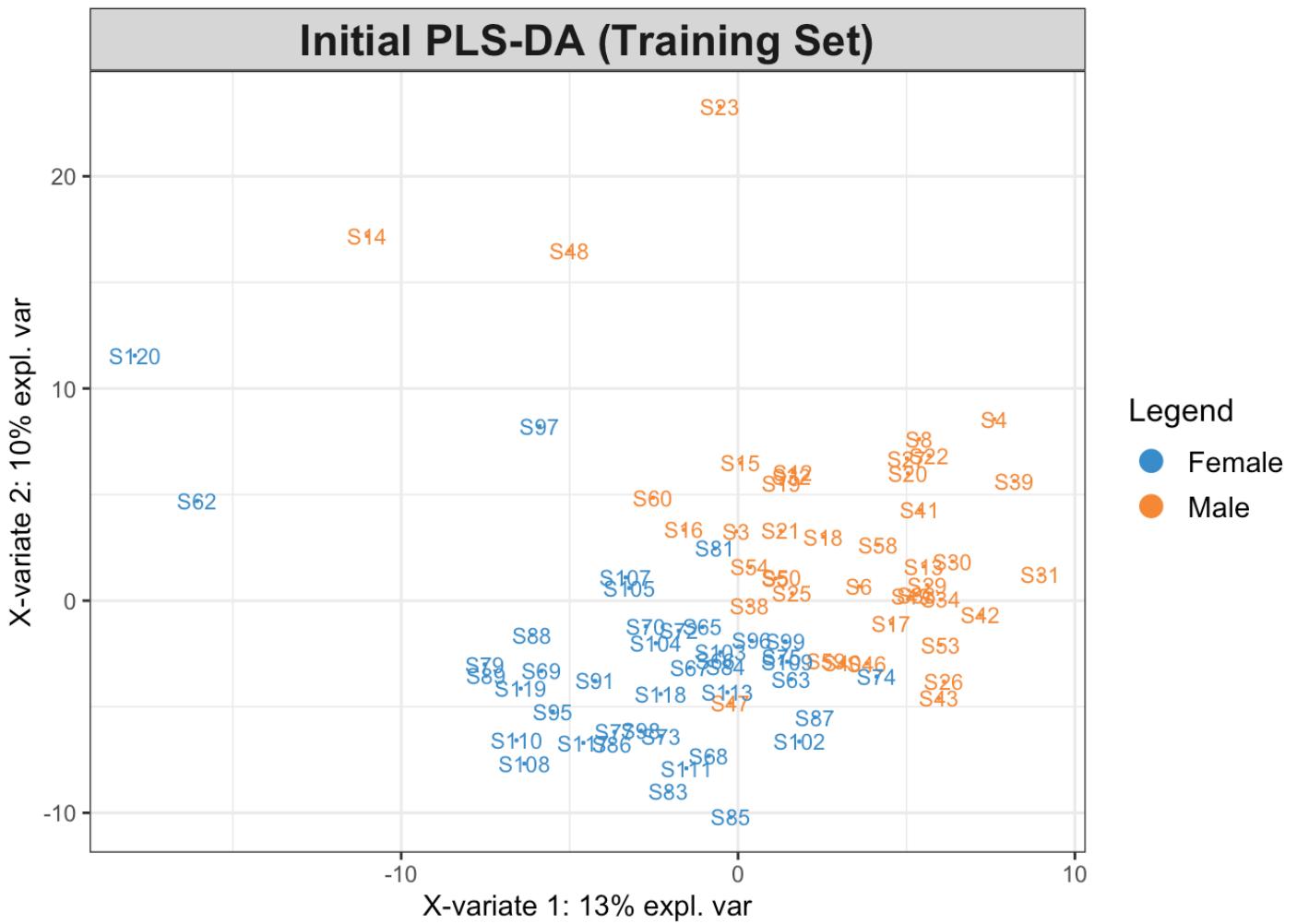
```

#Initial PLS-DA model

pls_initial <- mixOmics::plsda(X_train, y_train, ncomp = 10)

mixOmics::plotIndiv(pls_initial, comp = c(1,2),
                     group = y_train, legend = TRUE,
                     title = "Initial PLS-DA (Training Set)")

```



The PLS-DA score plot shows a clear separation between males and females along the first two latent variables, indicating strong sex-related differences in urinary metabolomic profiles.

## Internal Validation: 5-Fold CV + AUCROC

A 5-fold cross-validation was used on the training set to determine the optimal number of latent variables (LVs) for the PLS-DA model, using AUC as the performance metric.

```
set.seed(123)

folds <- createFolds(y_train, k = 5, returnTrain = TRUE)
auc_results <- data.frame(LV = integer(), AUC = numeric())

for (lv in 1:5) {
  auc_fold <- c()

  for (f in folds) {
    model <- mixOmics::plsda(X_train[f,], y_train[f], ncomp = lv)
    pred <- predict(model, X_train[-f,])$predict[,1,lv]
    roc_obj <- roc(y_train[-f], pred)
    auc_fold <- c(auc_fold, auc(roc_obj))
  }

  auc_results <- rbind(auc_results,
                        data.frame(LV = lv,
                                   AUC = mean(auc_fold)))
}
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
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## Setting direction: controls > cases
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## Setting levels: control = Female, case = Male
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## Setting levels: control = Female, case = Male
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## Setting direction: controls > cases
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## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases
```

```
## Setting levels: control = Female, case = Male
```

```
## Setting direction: controls > cases  
  
## Setting levels: control = Female, case = Male  
  
## Setting direction: controls > cases  
  
auc_results  
  
## LV      AUC  
## 1  1 0.7246914  
## 2  2 0.7500772  
## 3  3 0.8280478  
## 4  4 0.8102623  
## 5  5 0.8032793
```

LV = 3 showed the highest mean AUC, and was therefore selected as the optimal number of components for the final PLS-DA model.

## Univariate Analysis on Training set (Male vs Female)

Univariate Welch t-tests were applied to each metabolite in the training set, followed by FDR correction. Mean differences (Male – Female) were calculated to determine the direction of change.

```
# Compute raw p-values using Welch t-test for each metabolite
pvals <- apply(X_train, 2, function(x) t.test(x ~ y_train)$p.value)

# FDR correction (Benjamini-Hochberg)
pvals_fdr <- p.adjust(pvals, method = "fdr")

fc <- apply(X_train, 2, function(x) mean(x[y_train == "Male"]) -
            mean(x[y_train == "Female"]))

uni_results <- data.frame(
  Metabolite = colnames(X_train),
  p_value = pvals,
  p_FDR = pvals_fdr,
  mean_diff = fc
)

uni_results <- uni_results[order(uni_results$p_FDR), ]
significant <- uni_results[uni_results$p_FDR < 0.05, ]
significant
```

	Metabolite	p_value	p_FDR	mean_diff
##	V22	4.234697e-06	0.001753165	-0.9561637
##	V399	1.031182e-05	0.002134547	-0.9196217
##	V10	4.281978e-04	0.044318477	0.7449845
##	V84	3.253387e-04	0.044318477	-0.7615165
##	V51	6.958870e-04	0.044551591	-0.7565657
##	V113	6.825835e-04	0.044551591	0.7638415
##	V291	7.532878e-04	0.044551591	-0.6712124
##	V57	8.641712e-04	0.044720859	-0.6346747
##	V250	1.080601e-03	0.049707666	0.6825126

Several metabolites showed significant sex differences (FDR < 0.05). These features represent potential biomarkers and will be further evaluated in the supervised model.

## Volcano Plot - Univariate Analysis

A volcano plot was generated to visualize effect size (mean difference) against statistical significance (FDR-corrected p-values).

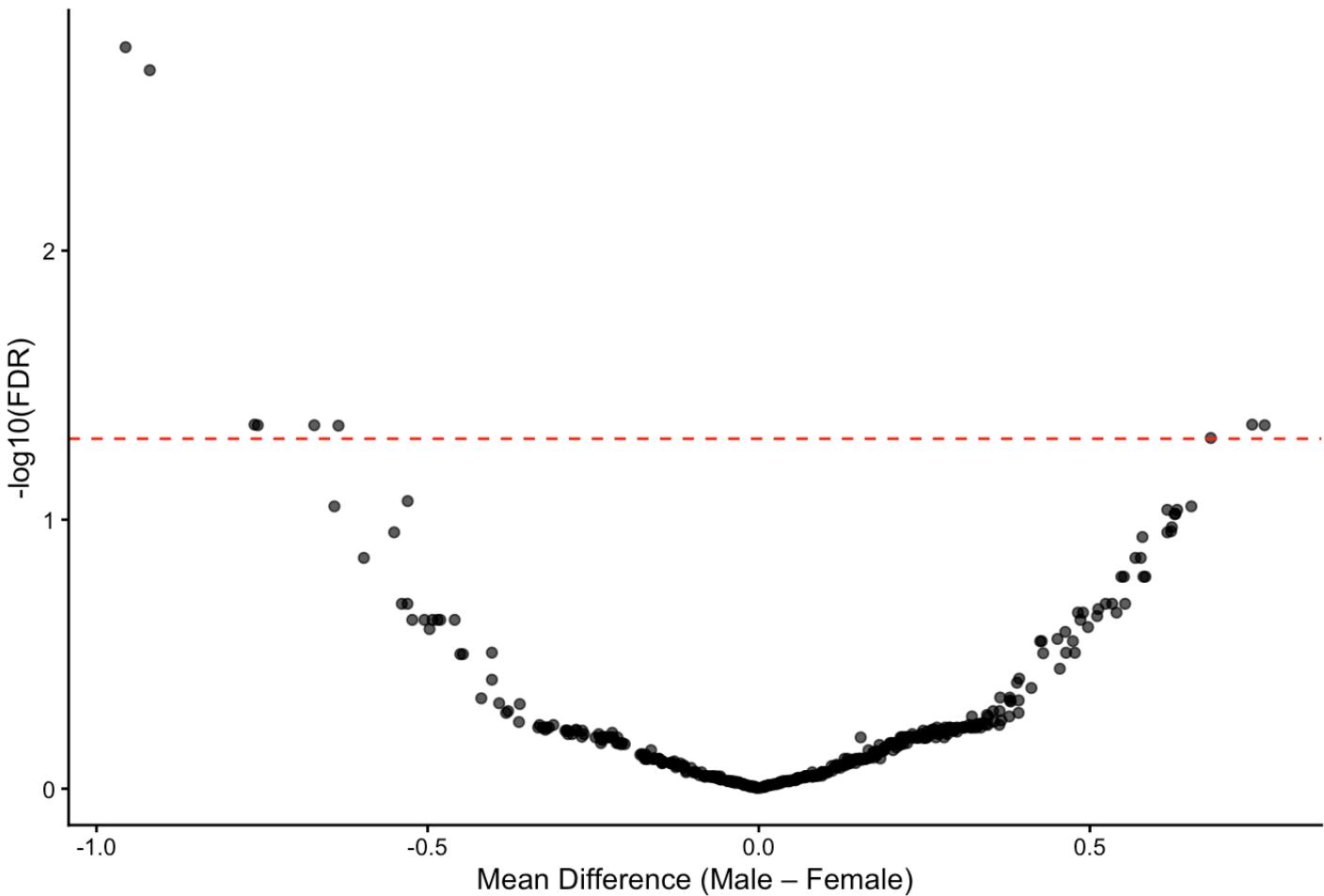
```

volcano <- uni_results
volcano$logP <- -log10(volcano$p_FDR)

ggplot(volcano, aes(x = mean_diff, y = logP)) +
  geom_point(alpha = 0.7) +
  geom_hline(yintercept = -log10(0.05), col = "red", lty = 2) +
  theme_classic() +
  xlab("Mean Difference (Male – Female)") +
  ylab("-log10(FDR)") +
  ggtitle("Volcano Plot – Univariate Analysis (Training Set)")

```

Volcano Plot — Univariate Analysis (Training Set)



Univariate analysis performed on the training set identified 9 metabolites with significant sex-related differences after FDR correction ( $p_{\text{FDR}} < 0.05$ ). Six metabolites (V22, V399, V84, V51, V291, V57) showed higher concentrations in females, while three metabolites (V10, V113, V250) were higher in males. The strongest discriminators were V22 and V399 ( $p_{\text{FDR}} < 0.005$ ).

```

colnames(X_train) <- paste0("X", 1:ncol(X_train))
colnames(X_test) <- paste0("X", 1:ncol(X_test))

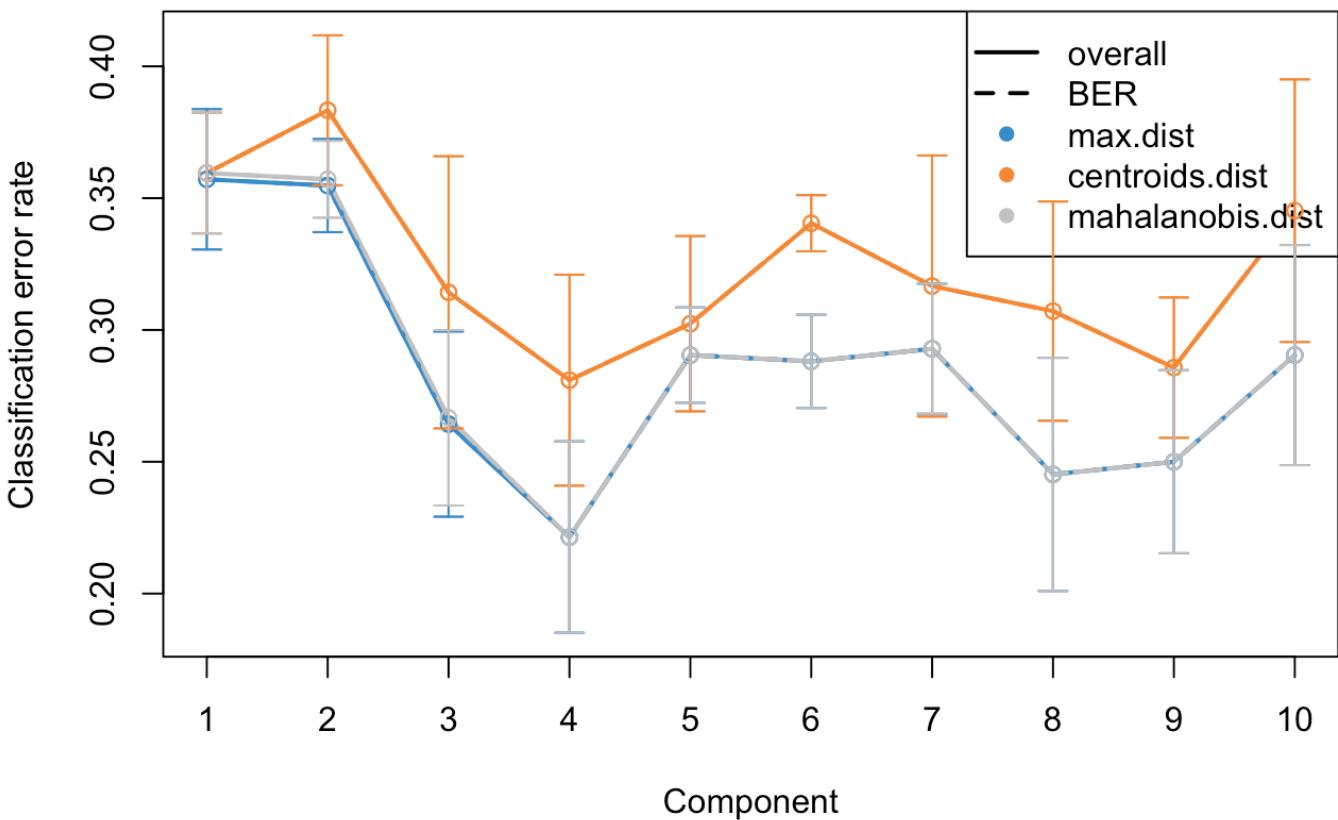
y_train <- as.factor(y_train)
y_test <- as.factor(y_test)

```

```
set.seed(30)

perf_res <- perf(pls_initial,
                  validation = "Mfold",
                  folds = 5,
                  nrepeat = 5,
                  progressBar = FALSE)

plot(perf_res, sd = TRUE)
```



Calculate the optimal number of components, using other metrics, like BER. This shows that increasing the number of components doesn't always decrease the error.

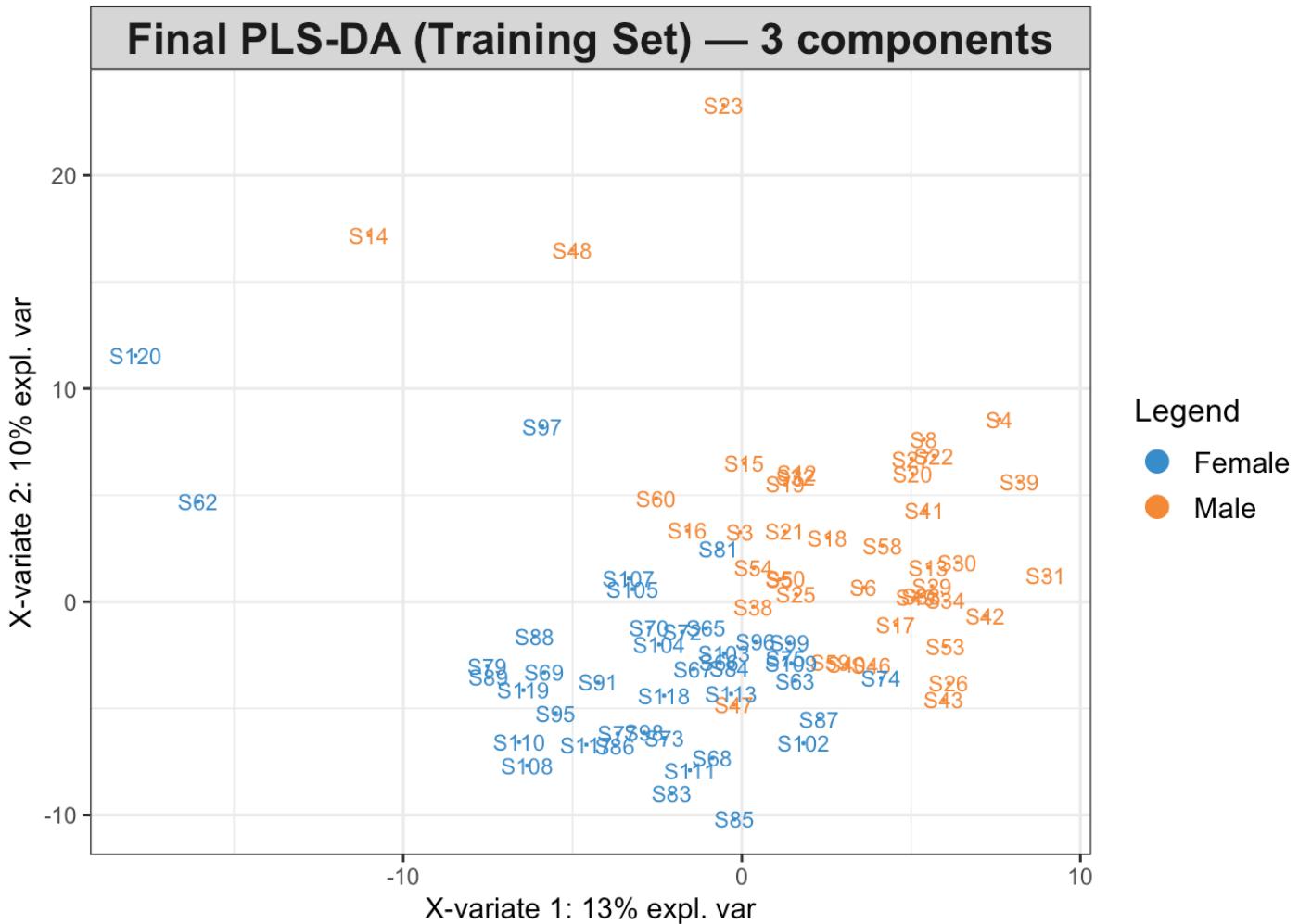
As an additional exploratory validation, the `perf()` method from `mixOmics` was applied. Although BER suggested 4 components, this criterion is less appropriate for binary classification than AUC. Therefore, AUC-based tuning remained the primary selection method.

```
optimal_ncomp <- which.min(perf_res$error.rate$BER)
optimal_ncomp
```

```
## [1] 4
```

```
optimal_ncomp <- 3
pls_final <- mixOmics::plsda(X_train, y_train, ncomp = optimal_ncomp)

mixOmics::plotIndiv(pls_final, comp = c(1,2),
                     group = y_train, legend = TRUE,
                     title = "Final PLS-DA (Training Set) – 3 components")
```



We selected  $n = 3$  components because they maximised the AUC during cross-validation while avoiding unnecessary model complexity. Although BER suggested 4 components, the improvement was marginal and adding extra components risks overfitting, especially in a two-class dataset.

```
pred_test <- predict(pls_final, X_test)
pred_class <- pred_test$class$max.dist[, optimal_ncomp]

table(True = y_test, Predicted = pred_class)
```

```
##           Predicted
## True      Female Male
## Female     14    4
## Male       5    13
```

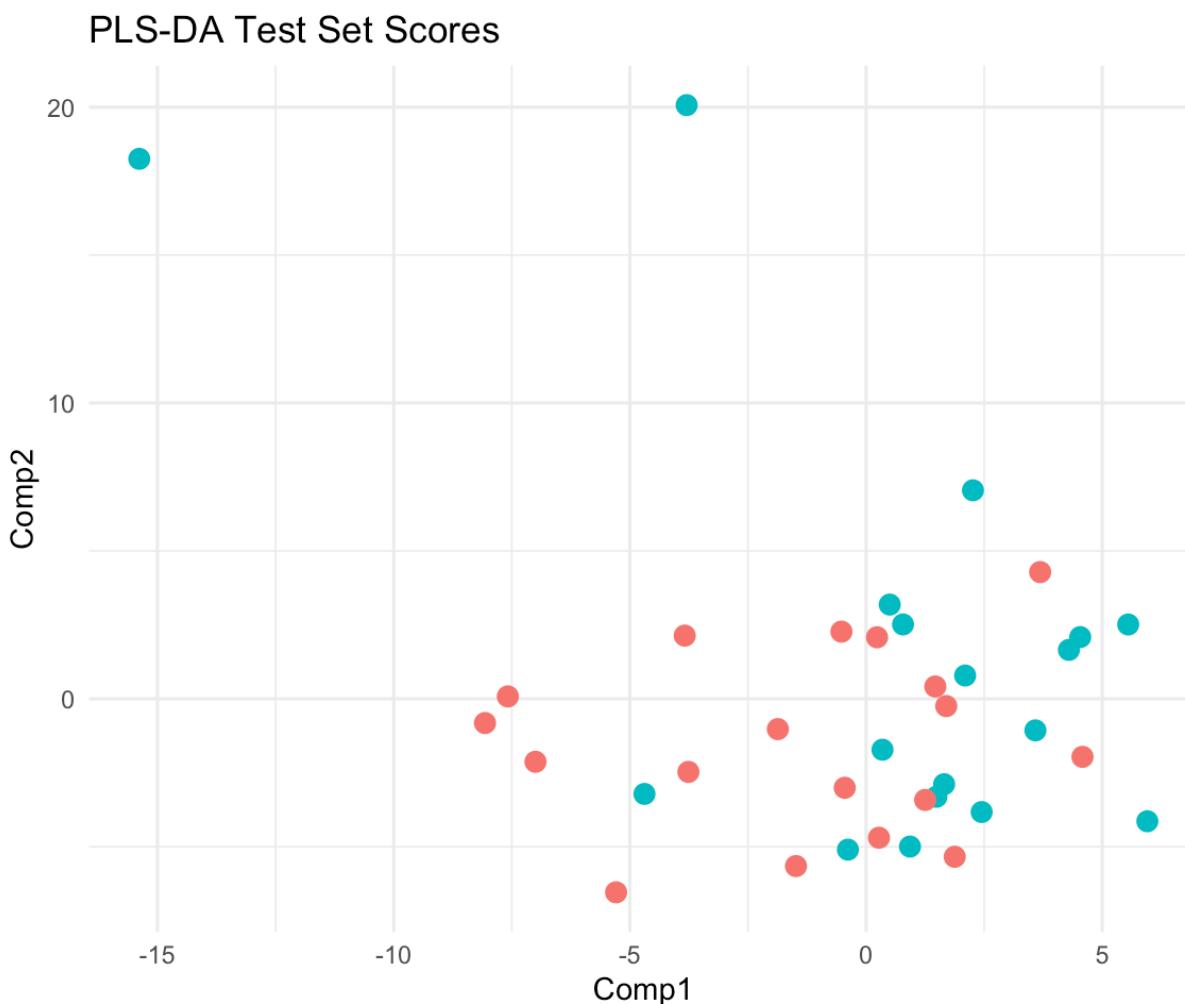
```
mean(pred_class == y_test)
```

```
## [1] 0.75
```

```
test_variates <- pred_test$variates

test_df <- data.frame(
  Comp1 = test_variates[,1],
  Comp2 = if (optimal_ncomp >= 2) test_variates[,2] else rep(0, nrow(test_variates)),
  Class = y_test
)

ggplot(test_df, aes(Comp1, Comp2, color = Class)) +
  geom_point(size = 3) +
  theme_minimal() +
  ggtitle("PLS-DA Test Set Scores")
```



The final PLS-DA model does not show a visibly stronger separation because the main class structure was already captured by the first two components in the initial model. Tuning improves model stability and classification performance, but these gains occur mostly beyond component 2, which is why the 2D score

plot appears similar.

# Feature Selection: Calculate and Rank VIP Scores

## Calculate and Rank VIP Scores

```
# 1. Extract the VIP scores matrix from the final PLS-DA model
# We typically focus on the scores from the first component (LV1)
vip_matrix <- vip(pls_final)
vip_scores_lv1 <- vip_matrix[, 1]

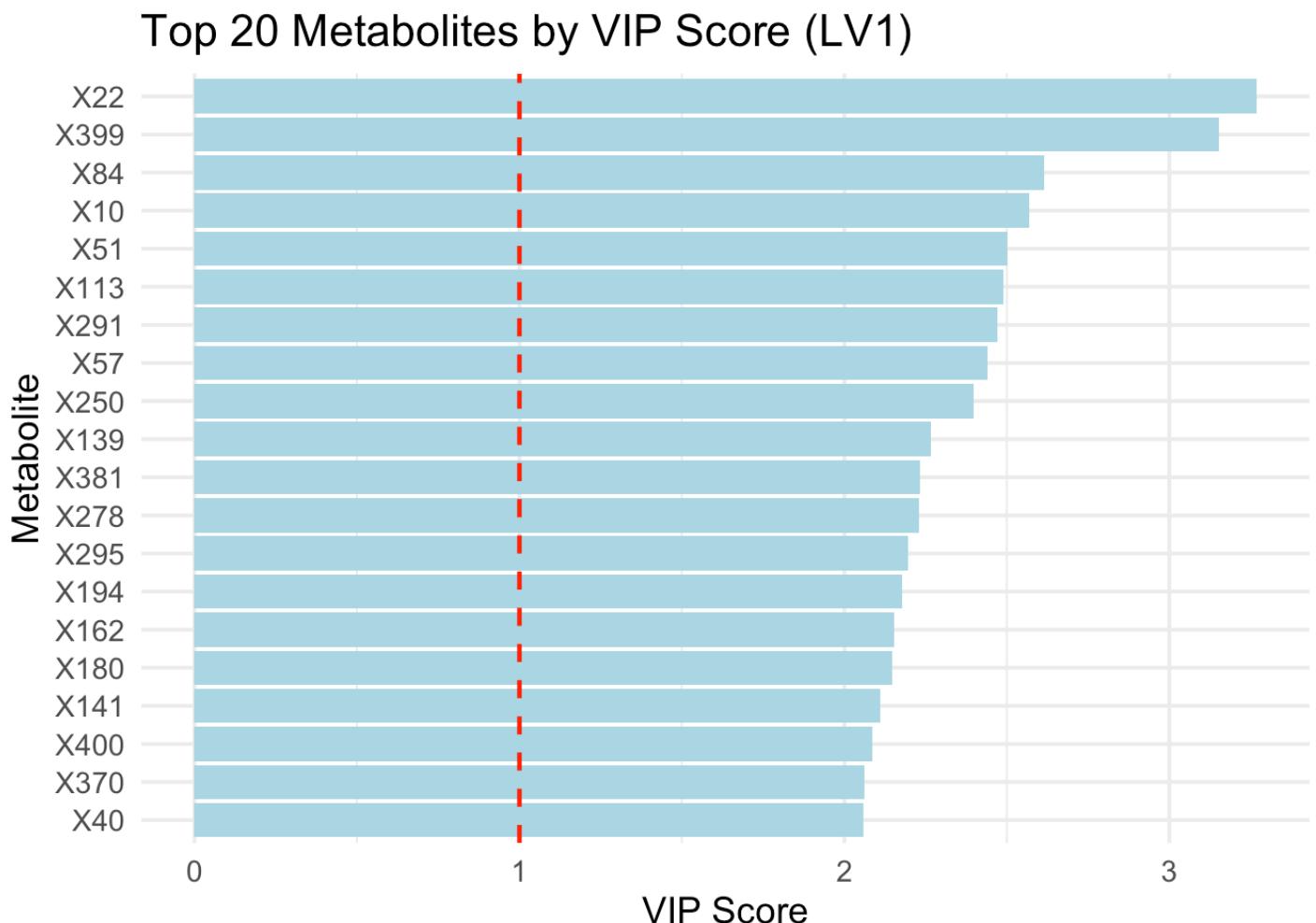
# 2. Order the metabolites from most important to least important
vip_ranked <- sort(vip_scores_lv1, decreasing = TRUE)

# 3. Convert to a data frame for plotting and analysis
vip_df <- data.frame(
  Metabolite = names(vip_ranked),
  VIP = vip_ranked
)

# 4. Visualize the top 20 most important metabolites
top_n <- 20
vip_top <- head(vip_df, top_n)

# Generate the bar plot
ggplot(vip_top, aes(x = reorder(Metabolite, VIP), y = VIP)) +
  geom_bar(stat = "identity", fill = "light blue") +
  geom_hline(yintercept = 1, linetype = "dashed", color = "red", size = 0.8) +
  coord_flip() +
  theme_minimal(base_size = 14) +
  labs(title = paste("Top", top_n, "Metabolites by VIP Score (LV1)"),
       y = "VIP Score",
       x = "Metabolite")
```

```
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
```



## Implement Recursive Feature Elimination (RFE) using the k-NN Classifier

```
set.seed(123)

# Define subset sizes for RFE
subset_sizes <- c(2, 5, 10, 15, 20, 25, 30, 40, 50)

# RFE control with default caret functions
rfe_control <- rfeControl(
  functions = caretFuncs,    # default ranking
  method = "repeatedcv",
  number = 5,
  repeats = 5,
  verbose = TRUE,           # suppress intermediate output
  returnResamp = "all"
)

# Execute RFE
rfe_results <- rfe(
  x = X_train,
  y = y_train,
  sizes = subset_sizes,
  rfeControl = rfe_control,
  method = "knn",
  tuneLength = 5,
  metric = "Accuracy",
  preProcess = c("center", "scale")
)
```

```
## +(rfe) fit Fold1.Rep1 size: 414
## -(rfe) fit Fold1.Rep1 size: 414
## +(rfe) imp Fold1.Rep1
## -(rfe) imp Fold1.Rep1
## +(rfe) fit Fold1.Rep1 size: 50
## -(rfe) fit Fold1.Rep1 size: 50
## +(rfe) fit Fold1.Rep1 size: 40
## -(rfe) fit Fold1.Rep1 size: 40
## +(rfe) fit Fold1.Rep1 size: 30
## -(rfe) fit Fold1.Rep1 size: 30
## +(rfe) fit Fold1.Rep1 size: 25
## -(rfe) fit Fold1.Rep1 size: 25
## +(rfe) fit Fold1.Rep1 size: 20
## -(rfe) fit Fold1.Rep1 size: 20
## +(rfe) fit Fold1.Rep1 size: 15
## -(rfe) fit Fold1.Rep1 size: 15
## +(rfe) fit Fold1.Rep1 size: 10
## -(rfe) fit Fold1.Rep1 size: 10
## +(rfe) fit Fold1.Rep1 size: 5
## -(rfe) fit Fold1.Rep1 size: 5
## +(rfe) fit Fold1.Rep1 size: 2
## -(rfe) fit Fold1.Rep1 size: 2
```

```
## +(rfe) fit Fold2.Rep1 size: 414
## -(rfe) fit Fold2.Rep1 size: 414
## +(rfe) imp Fold2.Rep1
## -(rfe) imp Fold2.Rep1
## +(rfe) fit Fold2.Rep1 size: 50
## -(rfe) fit Fold2.Rep1 size: 50
## +(rfe) fit Fold2.Rep1 size: 40
## -(rfe) fit Fold2.Rep1 size: 40
## +(rfe) fit Fold2.Rep1 size: 30
## -(rfe) fit Fold2.Rep1 size: 30
## +(rfe) fit Fold2.Rep1 size: 25
## -(rfe) fit Fold2.Rep1 size: 25
## +(rfe) fit Fold2.Rep1 size: 20
## -(rfe) fit Fold2.Rep1 size: 20
## +(rfe) fit Fold2.Rep1 size: 15
## -(rfe) fit Fold2.Rep1 size: 15
## +(rfe) fit Fold2.Rep1 size: 10
## -(rfe) fit Fold2.Rep1 size: 10
## +(rfe) fit Fold2.Rep1 size: 5
## -(rfe) fit Fold2.Rep1 size: 5
## +(rfe) fit Fold2.Rep1 size: 2
## -(rfe) fit Fold2.Rep1 size: 2
## +(rfe) fit Fold3.Rep1 size: 414
## -(rfe) fit Fold3.Rep1 size: 414
## +(rfe) imp Fold3.Rep1
## -(rfe) imp Fold3.Rep1
## +(rfe) fit Fold3.Rep1 size: 50
## -(rfe) fit Fold3.Rep1 size: 50
## +(rfe) fit Fold3.Rep1 size: 40
## -(rfe) fit Fold3.Rep1 size: 40
## +(rfe) fit Fold3.Rep1 size: 30
## -(rfe) fit Fold3.Rep1 size: 30
## +(rfe) fit Fold3.Rep1 size: 25
## -(rfe) fit Fold3.Rep1 size: 25
## +(rfe) fit Fold3.Rep1 size: 20
## -(rfe) fit Fold3.Rep1 size: 20
## +(rfe) fit Fold3.Rep1 size: 15
## -(rfe) fit Fold3.Rep1 size: 15
## +(rfe) fit Fold3.Rep1 size: 10
## -(rfe) fit Fold3.Rep1 size: 10
## +(rfe) fit Fold3.Rep1 size: 5
## -(rfe) fit Fold3.Rep1 size: 5
## +(rfe) fit Fold3.Rep1 size: 2
## -(rfe) fit Fold3.Rep1 size: 2
## +(rfe) fit Fold4.Rep1 size: 414
## -(rfe) fit Fold4.Rep1 size: 414
## +(rfe) imp Fold4.Rep1
## -(rfe) imp Fold4.Rep1
## +(rfe) fit Fold4.Rep1 size: 50
## -(rfe) fit Fold4.Rep1 size: 50
## +(rfe) fit Fold4.Rep1 size: 40
```

```
## -(rfe) fit Fold4.Rep1 size: 40
## +(rfe) fit Fold4.Rep1 size: 30
## -(rfe) fit Fold4.Rep1 size: 30
## +(rfe) fit Fold4.Rep1 size: 25
## -(rfe) fit Fold4.Rep1 size: 25
## +(rfe) fit Fold4.Rep1 size: 20
## -(rfe) fit Fold4.Rep1 size: 20
## +(rfe) fit Fold4.Rep1 size: 15
## -(rfe) fit Fold4.Rep1 size: 15
## +(rfe) fit Fold4.Rep1 size: 10
## -(rfe) fit Fold4.Rep1 size: 10
## +(rfe) fit Fold4.Rep1 size: 5
## -(rfe) fit Fold4.Rep1 size: 5
## +(rfe) fit Fold4.Rep1 size: 2
## -(rfe) fit Fold4.Rep1 size: 2
## +(rfe) fit Fold5.Rep1 size: 414
## -(rfe) fit Fold5.Rep1 size: 414
## +(rfe) imp Fold5.Rep1
## -(rfe) imp Fold5.Rep1
## +(rfe) fit Fold5.Rep1 size: 50
## -(rfe) fit Fold5.Rep1 size: 50
## +(rfe) fit Fold5.Rep1 size: 40
## -(rfe) fit Fold5.Rep1 size: 40
## +(rfe) fit Fold5.Rep1 size: 30
## -(rfe) fit Fold5.Rep1 size: 30
## +(rfe) fit Fold5.Rep1 size: 25
## -(rfe) fit Fold5.Rep1 size: 25
## +(rfe) fit Fold5.Rep1 size: 20
## -(rfe) fit Fold5.Rep1 size: 20
## +(rfe) fit Fold5.Rep1 size: 15
## -(rfe) fit Fold5.Rep1 size: 15
## +(rfe) fit Fold5.Rep1 size: 10
## -(rfe) fit Fold5.Rep1 size: 10
## +(rfe) fit Fold5.Rep1 size: 5
## -(rfe) fit Fold5.Rep1 size: 5
## +(rfe) fit Fold5.Rep1 size: 2
## -(rfe) fit Fold5.Rep1 size: 2
## +(rfe) fit Fold1.Rep2 size: 414
## -(rfe) fit Fold1.Rep2 size: 414
## +(rfe) imp Fold1.Rep2
## -(rfe) imp Fold1.Rep2
## +(rfe) fit Fold1.Rep2 size: 50
## -(rfe) fit Fold1.Rep2 size: 50
## +(rfe) fit Fold1.Rep2 size: 40
## -(rfe) fit Fold1.Rep2 size: 40
## +(rfe) fit Fold1.Rep2 size: 30
## -(rfe) fit Fold1.Rep2 size: 30
## +(rfe) fit Fold1.Rep2 size: 25
## -(rfe) fit Fold1.Rep2 size: 25
## +(rfe) fit Fold1.Rep2 size: 20
## -(rfe) fit Fold1.Rep2 size: 20
```

```
## +(rfe) fit Fold1.Rep2 size: 15
## -(rfe) fit Fold1.Rep2 size: 15
## +(rfe) fit Fold1.Rep2 size: 10
## -(rfe) fit Fold1.Rep2 size: 10
## +(rfe) fit Fold1.Rep2 size: 5
## -(rfe) fit Fold1.Rep2 size: 5
## +(rfe) fit Fold1.Rep2 size: 2
## -(rfe) fit Fold1.Rep2 size: 2
## +(rfe) fit Fold2.Rep2 size: 414
## -(rfe) fit Fold2.Rep2 size: 414
## +(rfe) imp Fold2.Rep2
## -(rfe) imp Fold2.Rep2
## +(rfe) fit Fold2.Rep2 size: 50
## -(rfe) fit Fold2.Rep2 size: 50
## +(rfe) fit Fold2.Rep2 size: 40
## -(rfe) fit Fold2.Rep2 size: 40
## +(rfe) fit Fold2.Rep2 size: 30
## -(rfe) fit Fold2.Rep2 size: 30
## +(rfe) fit Fold2.Rep2 size: 25
## -(rfe) fit Fold2.Rep2 size: 25
## +(rfe) fit Fold2.Rep2 size: 20
## -(rfe) fit Fold2.Rep2 size: 20
## +(rfe) fit Fold2.Rep2 size: 15
## -(rfe) fit Fold2.Rep2 size: 15
## +(rfe) fit Fold2.Rep2 size: 10
## -(rfe) fit Fold2.Rep2 size: 10
## +(rfe) fit Fold2.Rep2 size: 5
## -(rfe) fit Fold2.Rep2 size: 5
## +(rfe) fit Fold2.Rep2 size: 2
## -(rfe) fit Fold2.Rep2 size: 2
## +(rfe) fit Fold3.Rep2 size: 414
## -(rfe) fit Fold3.Rep2 size: 414
## +(rfe) imp Fold3.Rep2
## -(rfe) imp Fold3.Rep2
## +(rfe) fit Fold3.Rep2 size: 50
## -(rfe) fit Fold3.Rep2 size: 50
## +(rfe) fit Fold3.Rep2 size: 40
## -(rfe) fit Fold3.Rep2 size: 40
## +(rfe) fit Fold3.Rep2 size: 30
## -(rfe) fit Fold3.Rep2 size: 30
## +(rfe) fit Fold3.Rep2 size: 25
## -(rfe) fit Fold3.Rep2 size: 25
## +(rfe) fit Fold3.Rep2 size: 20
## -(rfe) fit Fold3.Rep2 size: 20
## +(rfe) fit Fold3.Rep2 size: 15
## -(rfe) fit Fold3.Rep2 size: 15
## +(rfe) fit Fold3.Rep2 size: 10
## -(rfe) fit Fold3.Rep2 size: 10
## +(rfe) fit Fold3.Rep2 size: 5
## -(rfe) fit Fold3.Rep2 size: 5
## +(rfe) fit Fold3.Rep2 size: 2
```

```
## -(rfe) fit Fold3.Rep2 size: 2
## +(rfe) fit Fold4.Rep2 size: 414
## -(rfe) fit Fold4.Rep2 size: 414
## +(rfe) imp Fold4.Rep2
## -(rfe) imp Fold4.Rep2
## +(rfe) fit Fold4.Rep2 size: 50
## -(rfe) fit Fold4.Rep2 size: 50
## +(rfe) fit Fold4.Rep2 size: 40
## -(rfe) fit Fold4.Rep2 size: 40
## +(rfe) fit Fold4.Rep2 size: 30
## -(rfe) fit Fold4.Rep2 size: 30
## +(rfe) fit Fold4.Rep2 size: 25
## -(rfe) fit Fold4.Rep2 size: 25
## +(rfe) fit Fold4.Rep2 size: 20
## -(rfe) fit Fold4.Rep2 size: 20
## +(rfe) fit Fold4.Rep2 size: 15
## -(rfe) fit Fold4.Rep2 size: 15
## +(rfe) fit Fold4.Rep2 size: 10
## -(rfe) fit Fold4.Rep2 size: 10
## +(rfe) fit Fold4.Rep2 size: 5
## -(rfe) fit Fold4.Rep2 size: 5
## +(rfe) fit Fold4.Rep2 size: 2
## -(rfe) fit Fold4.Rep2 size: 2
## +(rfe) fit Fold5.Rep2 size: 414
## -(rfe) fit Fold5.Rep2 size: 414
## +(rfe) imp Fold5.Rep2
## -(rfe) imp Fold5.Rep2
## +(rfe) fit Fold5.Rep2 size: 50
## -(rfe) fit Fold5.Rep2 size: 50
## +(rfe) fit Fold5.Rep2 size: 40
## -(rfe) fit Fold5.Rep2 size: 40
## +(rfe) fit Fold5.Rep2 size: 30
## -(rfe) fit Fold5.Rep2 size: 30
## +(rfe) fit Fold5.Rep2 size: 25
## -(rfe) fit Fold5.Rep2 size: 25
## +(rfe) fit Fold5.Rep2 size: 20
## -(rfe) fit Fold5.Rep2 size: 20
## +(rfe) fit Fold5.Rep2 size: 15
## -(rfe) fit Fold5.Rep2 size: 15
## +(rfe) fit Fold5.Rep2 size: 10
## -(rfe) fit Fold5.Rep2 size: 10
## +(rfe) fit Fold5.Rep2 size: 5
## -(rfe) fit Fold5.Rep2 size: 5
## +(rfe) fit Fold5.Rep2 size: 2
## -(rfe) fit Fold5.Rep2 size: 2
## +(rfe) fit Fold1.Rep3 size: 414
## -(rfe) fit Fold1.Rep3 size: 414
## +(rfe) imp Fold1.Rep3
## -(rfe) imp Fold1.Rep3
## +(rfe) fit Fold1.Rep3 size: 50
## -(rfe) fit Fold1.Rep3 size: 50
```

```
## +(rfe) fit Fold1.Rep3 size: 40
## -(rfe) fit Fold1.Rep3 size: 40
## +(rfe) fit Fold1.Rep3 size: 30
## -(rfe) fit Fold1.Rep3 size: 30
## +(rfe) fit Fold1.Rep3 size: 25
## -(rfe) fit Fold1.Rep3 size: 25
## +(rfe) fit Fold1.Rep3 size: 20
## -(rfe) fit Fold1.Rep3 size: 20
## +(rfe) fit Fold1.Rep3 size: 15
## -(rfe) fit Fold1.Rep3 size: 15
## +(rfe) fit Fold1.Rep3 size: 10
## -(rfe) fit Fold1.Rep3 size: 10
## +(rfe) fit Fold1.Rep3 size: 5
## -(rfe) fit Fold1.Rep3 size: 5
## +(rfe) fit Fold1.Rep3 size: 2
## -(rfe) fit Fold1.Rep3 size: 2
## +(rfe) fit Fold2.Rep3 size: 414
## -(rfe) fit Fold2.Rep3 size: 414
## +(rfe) imp Fold2.Rep3
## -(rfe) imp Fold2.Rep3
## +(rfe) fit Fold2.Rep3 size: 50
## -(rfe) fit Fold2.Rep3 size: 50
## +(rfe) fit Fold2.Rep3 size: 40
## -(rfe) fit Fold2.Rep3 size: 40
## +(rfe) fit Fold2.Rep3 size: 30
## -(rfe) fit Fold2.Rep3 size: 30
## +(rfe) fit Fold2.Rep3 size: 25
## -(rfe) fit Fold2.Rep3 size: 25
## +(rfe) fit Fold2.Rep3 size: 20
## -(rfe) fit Fold2.Rep3 size: 20
## +(rfe) fit Fold2.Rep3 size: 15
## -(rfe) fit Fold2.Rep3 size: 15
## +(rfe) fit Fold2.Rep3 size: 10
## -(rfe) fit Fold2.Rep3 size: 10
## +(rfe) fit Fold2.Rep3 size: 5
## -(rfe) fit Fold2.Rep3 size: 5
## +(rfe) fit Fold2.Rep3 size: 2
## -(rfe) fit Fold2.Rep3 size: 2
## +(rfe) fit Fold3.Rep3 size: 414
## -(rfe) fit Fold3.Rep3 size: 414
## +(rfe) imp Fold3.Rep3
## -(rfe) imp Fold3.Rep3
## +(rfe) fit Fold3.Rep3 size: 50
## -(rfe) fit Fold3.Rep3 size: 50
## +(rfe) fit Fold3.Rep3 size: 40
## -(rfe) fit Fold3.Rep3 size: 40
## +(rfe) fit Fold3.Rep3 size: 30
## -(rfe) fit Fold3.Rep3 size: 30
## +(rfe) fit Fold3.Rep3 size: 25
## -(rfe) fit Fold3.Rep3 size: 25
## +(rfe) fit Fold3.Rep3 size: 20
```

```
## -(rfe) fit Fold3.Rep3 size: 20
## +(rfe) fit Fold3.Rep3 size: 15
## -(rfe) fit Fold3.Rep3 size: 15
## +(rfe) fit Fold3.Rep3 size: 10
## -(rfe) fit Fold3.Rep3 size: 10
## +(rfe) fit Fold3.Rep3 size: 5
## -(rfe) fit Fold3.Rep3 size: 5
## +(rfe) fit Fold3.Rep3 size: 2
## -(rfe) fit Fold3.Rep3 size: 2
## +(rfe) fit Fold4.Rep3 size: 414
## -(rfe) fit Fold4.Rep3 size: 414
## +(rfe) imp Fold4.Rep3
## -(rfe) imp Fold4.Rep3
## +(rfe) fit Fold4.Rep3 size: 50
## -(rfe) fit Fold4.Rep3 size: 50
## +(rfe) fit Fold4.Rep3 size: 40
## -(rfe) fit Fold4.Rep3 size: 40
## +(rfe) fit Fold4.Rep3 size: 30
## -(rfe) fit Fold4.Rep3 size: 30
## +(rfe) fit Fold4.Rep3 size: 25
## -(rfe) fit Fold4.Rep3 size: 25
## +(rfe) fit Fold4.Rep3 size: 20
## -(rfe) fit Fold4.Rep3 size: 20
## +(rfe) fit Fold4.Rep3 size: 15
## -(rfe) fit Fold4.Rep3 size: 15
## +(rfe) fit Fold4.Rep3 size: 10
## -(rfe) fit Fold4.Rep3 size: 10
## +(rfe) fit Fold4.Rep3 size: 5
## -(rfe) fit Fold4.Rep3 size: 5
## +(rfe) fit Fold4.Rep3 size: 2
## -(rfe) fit Fold4.Rep3 size: 2
## +(rfe) fit Fold5.Rep3 size: 414
## -(rfe) fit Fold5.Rep3 size: 414
## +(rfe) imp Fold5.Rep3
## -(rfe) imp Fold5.Rep3
## +(rfe) fit Fold5.Rep3 size: 50
## -(rfe) fit Fold5.Rep3 size: 50
## +(rfe) fit Fold5.Rep3 size: 40
## -(rfe) fit Fold5.Rep3 size: 40
## +(rfe) fit Fold5.Rep3 size: 30
## -(rfe) fit Fold5.Rep3 size: 30
## +(rfe) fit Fold5.Rep3 size: 25
## -(rfe) fit Fold5.Rep3 size: 25
## +(rfe) fit Fold5.Rep3 size: 20
## -(rfe) fit Fold5.Rep3 size: 20
## +(rfe) fit Fold5.Rep3 size: 15
## -(rfe) fit Fold5.Rep3 size: 15
## +(rfe) fit Fold5.Rep3 size: 10
## -(rfe) fit Fold5.Rep3 size: 10
## +(rfe) fit Fold5.Rep3 size: 5
## -(rfe) fit Fold5.Rep3 size: 5
```

```
## +(rfe) fit Fold5.Rep3 size: 2
## -(rfe) fit Fold5.Rep3 size: 2
## +(rfe) fit Fold1.Rep4 size: 414
## -(rfe) fit Fold1.Rep4 size: 414
## +(rfe) imp Fold1.Rep4
## -(rfe) imp Fold1.Rep4
## +(rfe) fit Fold1.Rep4 size: 50
## -(rfe) fit Fold1.Rep4 size: 50
## +(rfe) fit Fold1.Rep4 size: 40
## -(rfe) fit Fold1.Rep4 size: 40
## +(rfe) fit Fold1.Rep4 size: 30
## -(rfe) fit Fold1.Rep4 size: 30
## +(rfe) fit Fold1.Rep4 size: 25
## -(rfe) fit Fold1.Rep4 size: 25
## +(rfe) fit Fold1.Rep4 size: 20
## -(rfe) fit Fold1.Rep4 size: 20
## +(rfe) fit Fold1.Rep4 size: 15
## -(rfe) fit Fold1.Rep4 size: 15
## +(rfe) fit Fold1.Rep4 size: 10
## -(rfe) fit Fold1.Rep4 size: 10
## +(rfe) fit Fold1.Rep4 size: 5
## -(rfe) fit Fold1.Rep4 size: 5
## +(rfe) fit Fold1.Rep4 size: 2
## -(rfe) fit Fold1.Rep4 size: 2
## +(rfe) fit Fold2.Rep4 size: 414
## -(rfe) fit Fold2.Rep4 size: 414
## +(rfe) imp Fold2.Rep4
## -(rfe) imp Fold2.Rep4
## +(rfe) fit Fold2.Rep4 size: 50
## -(rfe) fit Fold2.Rep4 size: 50
## +(rfe) fit Fold2.Rep4 size: 40
## -(rfe) fit Fold2.Rep4 size: 40
## +(rfe) fit Fold2.Rep4 size: 30
## -(rfe) fit Fold2.Rep4 size: 30
## +(rfe) fit Fold2.Rep4 size: 25
## -(rfe) fit Fold2.Rep4 size: 25
## +(rfe) fit Fold2.Rep4 size: 20
## -(rfe) fit Fold2.Rep4 size: 20
## +(rfe) fit Fold2.Rep4 size: 15
## -(rfe) fit Fold2.Rep4 size: 15
## +(rfe) fit Fold2.Rep4 size: 10
## -(rfe) fit Fold2.Rep4 size: 10
## +(rfe) fit Fold2.Rep4 size: 5
## -(rfe) fit Fold2.Rep4 size: 5
## +(rfe) fit Fold2.Rep4 size: 2
## -(rfe) fit Fold2.Rep4 size: 2
## +(rfe) fit Fold3.Rep4 size: 414
## -(rfe) fit Fold3.Rep4 size: 414
## +(rfe) imp Fold3.Rep4
## -(rfe) imp Fold3.Rep4
## +(rfe) fit Fold3.Rep4 size: 50
```

```
## -(rfe) fit Fold3.Rep4 size: 50
## +(rfe) fit Fold3.Rep4 size: 40
## -(rfe) fit Fold3.Rep4 size: 40
## +(rfe) fit Fold3.Rep4 size: 30
## -(rfe) fit Fold3.Rep4 size: 30
## +(rfe) fit Fold3.Rep4 size: 25
## -(rfe) fit Fold3.Rep4 size: 25
## +(rfe) fit Fold3.Rep4 size: 20
## -(rfe) fit Fold3.Rep4 size: 20
## +(rfe) fit Fold3.Rep4 size: 15
## -(rfe) fit Fold3.Rep4 size: 15
## +(rfe) fit Fold3.Rep4 size: 10
## -(rfe) fit Fold3.Rep4 size: 10
## +(rfe) fit Fold3.Rep4 size: 5
## -(rfe) fit Fold3.Rep4 size: 5
## +(rfe) fit Fold3.Rep4 size: 2
## -(rfe) fit Fold3.Rep4 size: 2
## +(rfe) fit Fold4.Rep4 size: 414
## -(rfe) fit Fold4.Rep4 size: 414
## +(rfe) imp Fold4.Rep4
## -(rfe) imp Fold4.Rep4
## +(rfe) fit Fold4.Rep4 size: 50
## -(rfe) fit Fold4.Rep4 size: 50
## +(rfe) fit Fold4.Rep4 size: 40
## -(rfe) fit Fold4.Rep4 size: 40
## +(rfe) fit Fold4.Rep4 size: 30
## -(rfe) fit Fold4.Rep4 size: 30
## +(rfe) fit Fold4.Rep4 size: 25
## -(rfe) fit Fold4.Rep4 size: 25
## +(rfe) fit Fold4.Rep4 size: 20
## -(rfe) fit Fold4.Rep4 size: 20
## +(rfe) fit Fold4.Rep4 size: 15
## -(rfe) fit Fold4.Rep4 size: 15
## +(rfe) fit Fold4.Rep4 size: 10
## -(rfe) fit Fold4.Rep4 size: 10
## +(rfe) fit Fold4.Rep4 size: 5
## -(rfe) fit Fold4.Rep4 size: 5
## +(rfe) fit Fold4.Rep4 size: 2
## -(rfe) fit Fold4.Rep4 size: 2
## +(rfe) fit Fold5.Rep4 size: 414
## -(rfe) fit Fold5.Rep4 size: 414
## +(rfe) imp Fold5.Rep4
## -(rfe) imp Fold5.Rep4
## +(rfe) fit Fold5.Rep4 size: 50
## -(rfe) fit Fold5.Rep4 size: 50
## +(rfe) fit Fold5.Rep4 size: 40
## -(rfe) fit Fold5.Rep4 size: 40
## +(rfe) fit Fold5.Rep4 size: 30
## -(rfe) fit Fold5.Rep4 size: 30
## +(rfe) fit Fold5.Rep4 size: 25
## -(rfe) fit Fold5.Rep4 size: 25
```

```
## +(rfe) fit Fold5.Rep4 size: 20
## -(rfe) fit Fold5.Rep4 size: 20
## +(rfe) fit Fold5.Rep4 size: 15
## -(rfe) fit Fold5.Rep4 size: 15
## +(rfe) fit Fold5.Rep4 size: 10
## -(rfe) fit Fold5.Rep4 size: 10
## +(rfe) fit Fold5.Rep4 size: 5
## -(rfe) fit Fold5.Rep4 size: 5
## +(rfe) fit Fold5.Rep4 size: 2
## -(rfe) fit Fold5.Rep4 size: 2
## +(rfe) fit Fold1.Rep5 size: 414
## -(rfe) fit Fold1.Rep5 size: 414
## +(rfe) imp Fold1.Rep5
## -(rfe) imp Fold1.Rep5
## +(rfe) fit Fold1.Rep5 size: 50
## -(rfe) fit Fold1.Rep5 size: 50
## +(rfe) fit Fold1.Rep5 size: 40
## -(rfe) fit Fold1.Rep5 size: 40
## +(rfe) fit Fold1.Rep5 size: 30
## -(rfe) fit Fold1.Rep5 size: 30
## +(rfe) fit Fold1.Rep5 size: 25
## -(rfe) fit Fold1.Rep5 size: 25
## +(rfe) fit Fold1.Rep5 size: 20
## -(rfe) fit Fold1.Rep5 size: 20
## +(rfe) fit Fold1.Rep5 size: 15
## -(rfe) fit Fold1.Rep5 size: 15
## +(rfe) fit Fold1.Rep5 size: 10
## -(rfe) fit Fold1.Rep5 size: 10
## +(rfe) fit Fold1.Rep5 size: 5
## -(rfe) fit Fold1.Rep5 size: 5
## +(rfe) fit Fold1.Rep5 size: 2
## -(rfe) fit Fold1.Rep5 size: 2
## +(rfe) fit Fold2.Rep5 size: 414
## -(rfe) fit Fold2.Rep5 size: 414
## +(rfe) imp Fold2.Rep5
## -(rfe) imp Fold2.Rep5
## +(rfe) fit Fold2.Rep5 size: 50
## -(rfe) fit Fold2.Rep5 size: 50
## +(rfe) fit Fold2.Rep5 size: 40
## -(rfe) fit Fold2.Rep5 size: 40
## +(rfe) fit Fold2.Rep5 size: 30
## -(rfe) fit Fold2.Rep5 size: 30
## +(rfe) fit Fold2.Rep5 size: 25
## -(rfe) fit Fold2.Rep5 size: 25
## +(rfe) fit Fold2.Rep5 size: 20
## -(rfe) fit Fold2.Rep5 size: 20
## +(rfe) fit Fold2.Rep5 size: 15
## -(rfe) fit Fold2.Rep5 size: 15
## +(rfe) fit Fold2.Rep5 size: 10
## -(rfe) fit Fold2.Rep5 size: 10
## +(rfe) fit Fold2.Rep5 size: 5
```

```
## -(rfe) fit Fold2.Rep5 size: 5
## +(rfe) fit Fold2.Rep5 size: 2
## -(rfe) fit Fold2.Rep5 size: 2
## +(rfe) fit Fold3.Rep5 size: 414
## -(rfe) fit Fold3.Rep5 size: 414
## +(rfe) imp Fold3.Rep5
## -(rfe) imp Fold3.Rep5
## +(rfe) fit Fold3.Rep5 size: 50
## -(rfe) fit Fold3.Rep5 size: 50
## +(rfe) fit Fold3.Rep5 size: 40
## -(rfe) fit Fold3.Rep5 size: 40
## +(rfe) fit Fold3.Rep5 size: 30
## -(rfe) fit Fold3.Rep5 size: 30
## +(rfe) fit Fold3.Rep5 size: 25
## -(rfe) fit Fold3.Rep5 size: 25
## +(rfe) fit Fold3.Rep5 size: 20
## -(rfe) fit Fold3.Rep5 size: 20
## +(rfe) fit Fold3.Rep5 size: 15
## -(rfe) fit Fold3.Rep5 size: 15
## +(rfe) fit Fold3.Rep5 size: 10
## -(rfe) fit Fold3.Rep5 size: 10
## +(rfe) fit Fold3.Rep5 size: 5
## -(rfe) fit Fold3.Rep5 size: 5
## +(rfe) fit Fold3.Rep5 size: 2
## -(rfe) fit Fold3.Rep5 size: 2
## +(rfe) fit Fold4.Rep5 size: 414
## -(rfe) fit Fold4.Rep5 size: 414
## +(rfe) imp Fold4.Rep5
## -(rfe) imp Fold4.Rep5
## +(rfe) fit Fold4.Rep5 size: 50
## -(rfe) fit Fold4.Rep5 size: 50
## +(rfe) fit Fold4.Rep5 size: 40
## -(rfe) fit Fold4.Rep5 size: 40
## +(rfe) fit Fold4.Rep5 size: 30
## -(rfe) fit Fold4.Rep5 size: 30
## +(rfe) fit Fold4.Rep5 size: 25
## -(rfe) fit Fold4.Rep5 size: 25
## +(rfe) fit Fold4.Rep5 size: 20
## -(rfe) fit Fold4.Rep5 size: 20
## +(rfe) fit Fold4.Rep5 size: 15
## -(rfe) fit Fold4.Rep5 size: 15
## +(rfe) fit Fold4.Rep5 size: 10
## -(rfe) fit Fold4.Rep5 size: 10
## +(rfe) fit Fold4.Rep5 size: 5
## -(rfe) fit Fold4.Rep5 size: 5
## +(rfe) fit Fold4.Rep5 size: 2
## -(rfe) fit Fold4.Rep5 size: 2
## +(rfe) fit Fold5.Rep5 size: 414
## -(rfe) fit Fold5.Rep5 size: 414
## +(rfe) imp Fold5.Rep5
## -(rfe) imp Fold5.Rep5
```

```
## +(rfe) fit Fold5.Rep5 size: 50
## -(rfe) fit Fold5.Rep5 size: 50
## +(rfe) fit Fold5.Rep5 size: 40
## -(rfe) fit Fold5.Rep5 size: 40
## +(rfe) fit Fold5.Rep5 size: 30
## -(rfe) fit Fold5.Rep5 size: 30
## +(rfe) fit Fold5.Rep5 size: 25
## -(rfe) fit Fold5.Rep5 size: 25
## +(rfe) fit Fold5.Rep5 size: 20
## -(rfe) fit Fold5.Rep5 size: 20
## +(rfe) fit Fold5.Rep5 size: 15
## -(rfe) fit Fold5.Rep5 size: 15
## +(rfe) fit Fold5.Rep5 size: 10
## -(rfe) fit Fold5.Rep5 size: 10
## +(rfe) fit Fold5.Rep5 size: 5
## -(rfe) fit Fold5.Rep5 size: 5
## +(rfe) fit Fold5.Rep5 size: 2
## -(rfe) fit Fold5.Rep5 size: 2
```

```
# Extract optimal features
optimal.nfeatures.rfe <- rfe_results$bestSubset
optimal_features_rfe <- rfe_results$optVariables

cat("Optimal number of features:", optimal.nfeatures.rfe, "\n")
```

```
## Optimal number of features: 20
```

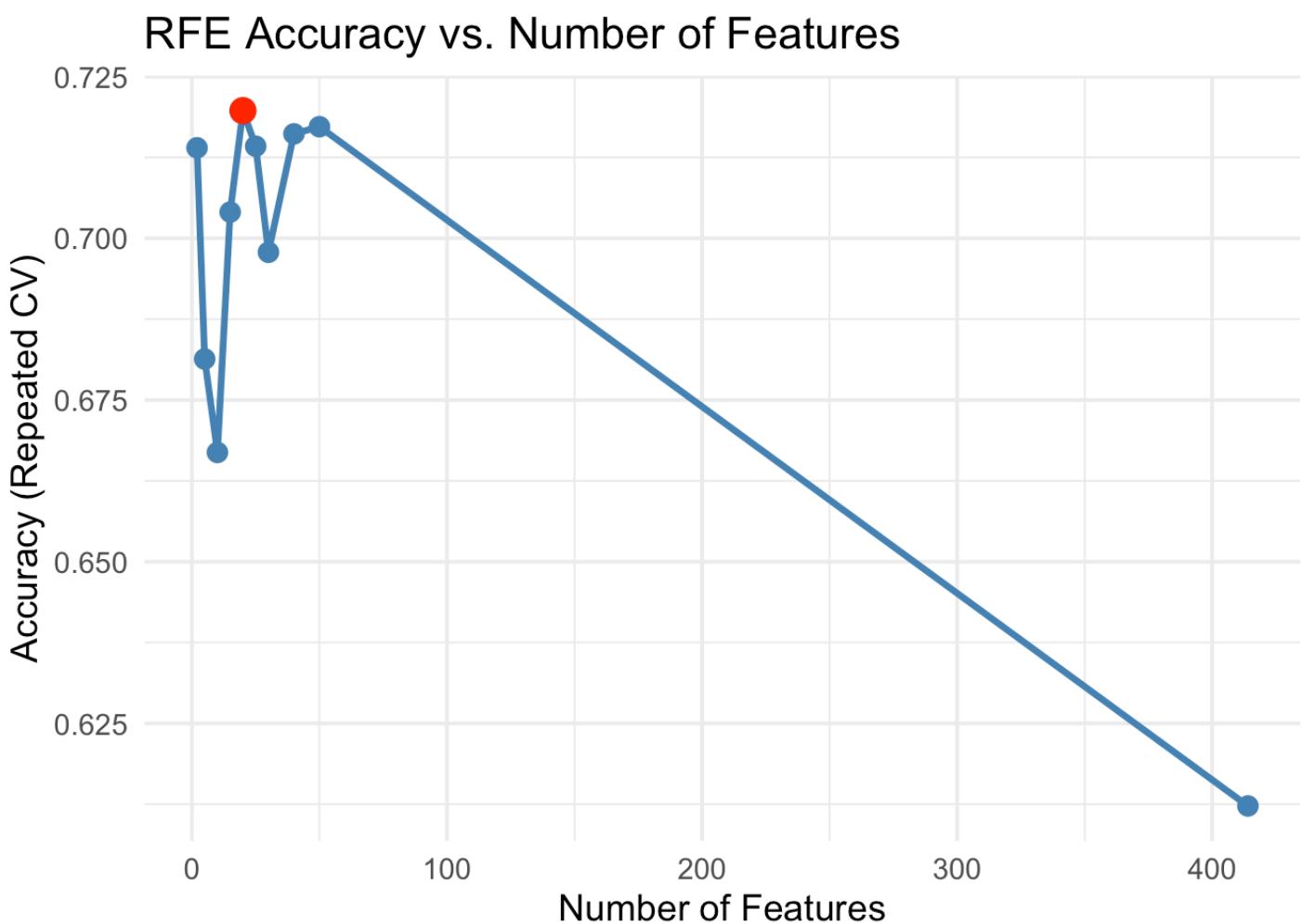
```
cat("Top selected features:", head(optimal_features_rfe, 10), "\n")
```

```
## Top selected features: X22 X399 X51 X250 X84 X57 X113 X291 X10 X180
```

# Plot the results of the RFE function and print the table

```
# Extract resampling results from RFE
rfe_df <- rfe_results$results

# Plot accuracy vs. number of variables
ggplot(rfe_df, aes(x = Variables, y = Accuracy)) +
  geom_line(color = "steelblue", size = 1.2) +
  geom_point(size = 3, color = "steelblue") +
  geom_point(data = subset(rfe_df, Variables == rfe_results$bestSubset),
             aes(x = Variables, y = Accuracy),
             color = "red", size = 4, shape = 21, fill = "red") +
  theme_minimal(base_size = 14) +
  labs(title = "RFE Accuracy vs. Number of Features",
       x = "Number of Features",
       y = "Accuracy (Repeated CV)")
```



```
# Print the table with the results to validate the plot representation
kable(round(rfe_df, 3), caption = "RFE Accuracy by Number of Features")
```

### RFE Accuracy by Number of Features

Variables	Accuracy	Kappa	AccuracySD	KappaSD
-----------	----------	-------	------------	---------

2	0.714	0.425	0.134	0.270
5	0.681	0.362	0.090	0.179
10	0.667	0.331	0.095	0.194
15	0.704	0.408	0.097	0.192
20	0.720	0.439	0.098	0.195
25	0.714	0.428	0.083	0.165
30	0.698	0.395	0.096	0.194
40	0.716	0.432	0.095	0.190
50	0.717	0.436	0.114	0.228
414	0.612	0.225	0.103	0.206

## Final Model Training and Evaluation with Optimal Features

```
# 1. Define the number of components (LVs)
# Use the previously optimized ncomp = 3.
optimal_ncomp <- 3

# 2. Subset the training and test data to only the optimal features
X_train_optimal <- X_train[, optimal_features_rfe]
X_test_optimal  <- X_test[, optimal_features_rfe]

# 3. Train the final PLS-DA model using ONLY the optimal features
pls_final_optimal <- mixOmics::plsda(X_train_optimal, y_train, ncomp = optimal_ncomp)

cat("Final PLS-DA model trained with:", optimal.nfeatures.rfe, "metabolites.\n")
```

```
## Final PLS-DA model trained with: 20 metabolites.
```

```
# 4. Predict on the Test Set
pred_test_optimal <- predict(pls_final_optimal, X_test_optimal)

# Extract predicted class using max distance for the chosen ncomp
pred_class_optimal <- pred_test_optimal$class$max.dist[, optimal_ncomp]

# 5. Evaluate Performance
cat("\n--- Performance on Test Set ---\n")
```

```
##  
## --- Performance on Test Set ---
```

```
# Confusion Matrix  
confusion_matrix_optimal <- table(True = y_test, Predicted = pred_class_optimal)  
print(confusion_matrix_optimal)
```

```
##           Predicted  
## True      Female Male  
##   Female     16    2  
##   Male       5   13
```

```
# Overall Accuracy  
accuracy_optimal <- mean(pred_class_optimal == y_test)  
cat("\nOverall Accuracy:", round(accuracy_optimal, 4), "\n")
```

```
##  
## Overall Accuracy: 0.8056
```

```
# Custom BER function (can't be exported directly)  
BER <- function(conf_matrix) {  
  # Convert to matrix  
  cm <- as.matrix(conf_matrix)  
  
  # Assume binary classification: rows = true, cols = predicted  
  # Sensitivity for class 1  
  sens1 <- cm[1,1] / sum(cm[1,])  
  # Sensitivity for class 2  
  sens2 <- cm[2,2] / sum(cm[2,])  
  
  # BER = 1 - mean(sensitivities)  
  ber <- 1 - mean(c(sens1, sens2))  
  return(ber)  
}  
  
ber_optimal <- BER(confusion_matrix_optimal)  
cat("Balanced Error Rate (BER):", round(ber_optimal, 4), "\n")
```

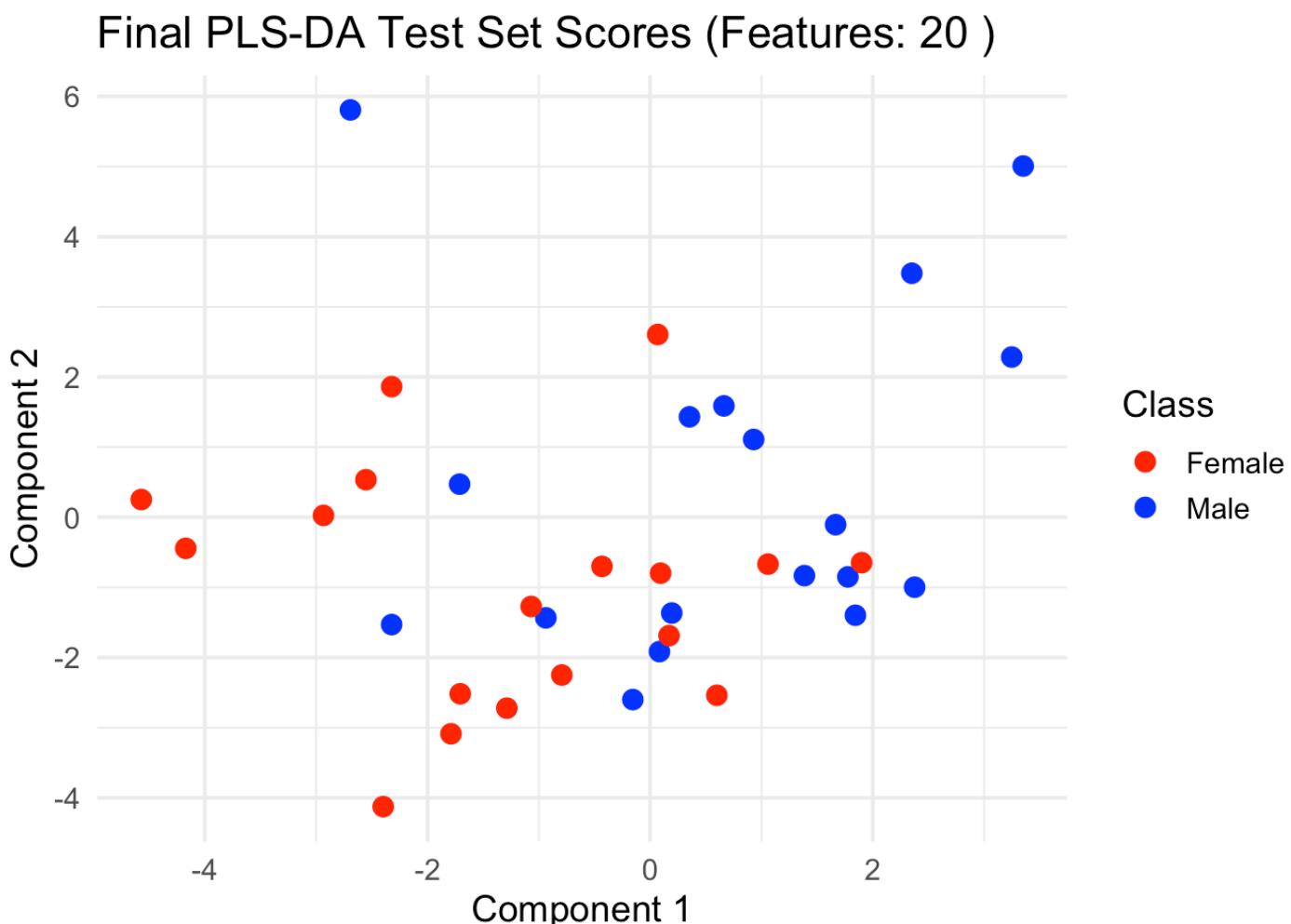
```
## Balanced Error Rate (BER): 0.1944
```

# Visualization of Test Set Scores

```
# Visualization of Test Set Scores
# Extract the sample scores (variates) for the optimal model
test_variates_optimal <- pred_test_optimal$variates

# Create a data frame for plotting
test_df_optimal <- data.frame(
  Comp1 = test_variates_optimal[,1],
  Comp2 = if (optimal_ncomp >= 2) test_variates_optimal[,2] else rep(0, nrow(test_variates_optimal)),
  Class = y_test
)

# Generate the Score Plot
ggplot(test_df_optimal, aes(Comp1, Comp2, color = Class)) +
  geom_point(size = 3) +
  theme_minimal(base_size = 14) +
  scale_color_manual(values = c("Female" = "red", "Male" = "blue")) +
  ggtitle(paste("Final PLS-DA Test Set Scores (Features:", optimal.nfeatures.rfe, ")")) +
  labs(x = "Component 1", y = "Component 2")
```



# External validation of the results

```
# --- External Validation on Test Set with Optimal Features ---  
  
# Ensure test and train sets have the same features  
X_test_optimal <- X_test[, optimal_features_rfe]  
  
# Predict with the final PLS-DA model trained on optimal features  
pred_test_optimal <- predict(pls_final_optimal, X_test_optimal)  
  
# Extract predicted classes using max distance  
pred_class_optimal <- pred_test_optimal$class$max.dist[, optimal_ncomp]  
  
# Confusion Matrix  
conf_matrix <- table(True = y_test, Predicted = pred_class_optimal)  
cat("Confusion Matrix:\n")
```

```
## Confusion Matrix:
```

```
print(conf_matrix)
```

```
##           Predicted  
## True      Female Male  
##   Female     16    2  
##   Male       5   13
```

```
# Overall Accuracy  
accuracy <- mean(pred_class_optimal == y_test)  
cat("\nOverall Accuracy:", round(accuracy, 4), "\n")
```

```
##  
## Overall Accuracy: 0.8056
```

```
# Balanced Error Rate (BER)  
BER <- function(cm) {  
  cm <- as.matrix(cm)  
  sens <- diag(cm) / rowSums(cm)  
  1 - mean(sens)  
}  
ber <- BER(conf_matrix)  
cat("Balanced Error Rate (BER):", round(ber, 4), "\n")
```

```
## Balanced Error Rate (BER): 0.1944
```

```
# ROC & AUC for binary classification
y_test_num <- as.numeric(y_test) - 1
pred_scores <- pred_test_optimal$predict[,1,optimal_ncomp]

roc_obj <- roc(y_test_num, pred_scores)
```

```
## Setting levels: control = 0, case = 1
```

```
## Setting direction: controls > cases
```

```
auc_val <- auc(roc_obj)
cat("AUC:", round(auc_val, 4), "\n")
```

```
## AUC: 0.8333
```

```
# --- Bootstrap Confidence Intervals ---
set.seed(123)
n_boot <- 1000
boot_acc <- numeric(n_boot)
boot_auc <- numeric(n_boot)

for (i in 1:n_boot) {
  idx <- sample(seq_along(y_test), replace = TRUE)
  Xb <- X_test_optimal[idx, ]
  yb <- y_test[idx]

  pred_b <- predict(pls_final_optimal, Xb)
  class_b <- pred_b$class$max.dist[, optimal_ncomp]
  boot_acc[i] <- mean(class_b == yb)

  scores_b <- pred_b$predict[,1,optimal_ncomp]
  yb_num <- as.numeric(yb) - 1

  if (length(unique(yb_num)) == 2) {
    roc_b <- roc(yb_num, scores_b, quiet = TRUE)
    boot_auc[i] <- auc(roc_b)
  } else {
    boot_auc[i] <- NA
  }
}

# Report mean and 95% CI
acc_ci <- quantile(boot_acc, probs = c(0.025, 0.975))
auc_ci <- quantile(boot_auc, probs = c(0.025, 0.975), na.rm = TRUE)

cat("\n--- Bootstrap Confidence Intervals (n =", n_boot, ") ---\n")
```

```

## --- Bootstrap Confidence Intervals (n = 1000) ---

cat("Accuracy: Mean =", round(mean(boot_acc), 4),
    " | 95% CI =", round(acc_ci[1], 4), "-", round(acc_ci[2], 4), "\n")

## Accuracy: Mean = 0.8064 | 95% CI = 0.6667 - 0.9167

cat("AUCROC: Mean =", round(mean(boot_auc, na.rm = TRUE), 4),
    " | 95% CI =", round(auc_ci[1], 4), "-", round(auc_ci[2], 4), "\n")

## AUCROC: Mean = 0.8332 | 95% CI = 0.6889 - 0.9524

# --- Figure of Merit Uncertainty (Bootstrap 95% CI) ---

# Point estimates on the held-out test set
conf_matrix <- table(True = y_test, Predicted = pred_class_optimal)

# Helper metrics (binary, rows=True: Female, Male; cols=Predicted)
metrics_point <- (function(cm) {
  cm <- as.matrix(cm)
  TP1 <- cm[1,1]; FN1 <- cm[1,2]; FP1 <- cm[2,1]; TN1 <- cm[2,2]
  acc <- (TP1 + TN1) / sum(cm)
  sens_fem <- TP1 / (TP1 + FN1)
  spec_fem <- TN1 / (TN1 + FP1)
  sens_male <- TN1 / (TN1 + FP1)           # sensitivity for "Male" if treating Male a
s positive in its own class
  spec_male <- TP1 / (TP1 + FN1)
  ber <- 1 - mean(c(sens_fem, sens_male))
  po <- acc
  pe <- ((sum(cm[,1]) * sum(cm[,1])) + (sum(cm[,2]) * sum(cm[,2]))) / (sum(cm)^2)
  kappa <- (po - pe) / (1 - pe)
  list(accuracy = acc, BER = ber,
       sensitivity_female = sens_fem, specificity_female = spec_fem,
       sensitivity_male = sens_male, specificity_male = spec_male,
       kappa = kappa)
})(conf_matrix)

# AUC point estimate (scores from your model)
y_test_num <- as.numeric(y_test) - 1
pred_scores <- pred_test_optimal$predict[,1,optimal_ncomp]
auc_point <- as.numeric(auc(roc(y_test_num, pred_scores)))

## Setting levels: control = 0, case = 1

```

```
## Setting direction: controls > cases
```

```
cat("\n--- Point estimates (Test Set) ---\n")
```

```
##  
## --- Point estimates (Test Set) ---
```

```
cat(sprintf("Accuracy = %.4f\n", metrics_point$accuracy))
```

```
## Accuracy = 0.8056
```

```
cat(sprintf("BER      = %.4f\n", metrics_point$BER))
```

```
## BER      = 0.1944
```

```
cat(sprintf("Kappa     = %.4f\n", metrics_point$kappa))
```

```
## Kappa     = 0.6111
```

```
cat(sprintf("Sens(F)  = %.4f | Spec(F) = %.4f\n", metrics_point$sensitivity_female,  
metrics_point$specificity_female))
```

```
## Sens(F)  = 0.8889 | Spec(F) = 0.7222
```

```
cat(sprintf("Sens(M)  = %.4f | Spec(M) = %.4f\n", metrics_point$sensitivity_male, m  
etrics_point$specificity_male))
```

```
## Sens(M)  = 0.7222 | Spec(M) = 0.8889
```

```
cat(sprintf("AUCROC   = %.4f\n", auc_point))
```

```
## AUCROC   = 0.8333
```

```
# --- Bootstrap CIs for Accuracy, BER, Kappa, Sens/Spec (both classes), and AUC ---  
set.seed(123)  
n_boot <- 1000
```

```
boot_acc  <- numeric(n_boot)  
boot_ber  <- numeric(n_boot)
```

```

boot_kappa<- numeric(n_boot)
boot_sensF<- numeric(n_boot)
boot_specF<- numeric(n_boot)
boot_sensM<- numeric(n_boot)
boot_specM<- numeric(n_boot)
boot_auc <- numeric(n_boot)

for (i in 1:n_boot) {
  idx <- sample(seq_along(y_test), replace = TRUE)
  Xb <- X_test_optimal[idx, ]
  yb <- y_test[idx]

  pred_b <- predict(pls_final_optimal, Xb)
  class_b <- pred_b$class$max.dist[, optimal_ncomp]
  cm <- table(True = yb, Predicted = class_b)

  # Guard: ensure 2x2 matrix even if a class is missing
  all_lvls <- levels(y_test)
  cm <- as.matrix(cm)
  # Rebuild complete 2x2 in fixed order (Female, Male)
  full_cm <- matrix(0, nrow = 2, ncol = 2,
                     dimnames = list(True = all_lvls, Predicted = all_lvls))
  for (tr in rownames(cm)) for (pr in colnames(cm)) full_cm[tr, pr] <- cm[tr, pr]
  cm <- full_cm

  TP1 <- cm["Female","Female"]; FN1 <- cm["Female","Male"]
  FP1 <- cm["Male","Female"];   TN1 <- cm["Male","Male"]

  acc <- (TP1 + TN1) / sum(cm)
  sensF <- if ((TP1 + FN1) > 0) TP1 / (TP1 + FN1) else NA
  specF <- if ((TN1 + FP1) > 0) TN1 / (TN1 + FP1) else NA
  sensM <- if ((TN1 + FP1) > 0) TN1 / (TN1 + FP1) else NA
  specM <- if ((TP1 + FN1) > 0) TP1 / (TP1 + FN1) else NA
  ber <- 1 - mean(c(sensF, sensM), na.rm = TRUE)

  po <- acc
  pe <- ((sum(cm["Female",]) * sum(cm[, "Female"])) + (sum(cm["Male",]) * sum(cm[, "Male"]))) / (sum(cm)^2)
  kappa <- if ((1 - pe) > 0) (po - pe) / (1 - pe) else NA

  # AUC from scores (skip if a single class)
  scores_b <- pred_b$predict[,1,optimal_ncomp]
  yb_num <- as.numeric(yb) - 1
  if (length(unique(yb_num)) == 2) {
    boot_auc[i] <- as.numeric(auc(roc(yb_num, scores_b, quiet = TRUE)))
  } else {
    boot_auc[i] <- NA
  }

  boot_acc[i] <- acc
  boot_ber[i] <- ber
}

```

```
boot_kappa[i] <- kappa
boot_sensF[i] <- sensF
boot_specF[i] <- specF
boot_sensM[i] <- sensM
boot_specM[i] <- specM
}

q <- function(x) quantile(x, probs = c(0.025, 0.975), na.rm = TRUE)

acc_ci    <- q(boot_acc)
ber_ci    <- q(boot_ber)
kappa_ci <- q(boot_kappa)
sensF_ci <- q(boot_sensF)
specF_ci <- q(boot_specF)
sensM_ci <- q(boot_sensM)
specM_ci <- q(boot_specM)
auc_ci    <- q(boot_auc)

cat("\n--- Bootstrap 95% CIs (n = ", n_boot, ")\n", sep = "")
```

```
##  
## --- Bootstrap 95% CIs (n = 1000) ---
```

```
cat(sprintf("Accuracy: Mean = %.4f | 95% CI = %.4f - %.4f\n", mean(boot_acc, na.rm = TRUE), acc_ci[1], acc_ci[2]))
```

```
## Accuracy: Mean = 0.8064 | 95% CI = 0.6667 - 0.9167
```

```
cat(sprintf("BER:      Mean = %.4f | 95% CI = %.4f - %.4f\n", mean(boot_ber, na.rm = TRUE), ber_ci[1], ber_ci[2]))
```

```
## BER:      Mean = 0.1933 | 95% CI = 0.0789 - 0.3287
```

```
cat(sprintf("Kappa:     Mean = %.4f | 95% CI = %.4f - %.4f\n", mean(boot_kappa, na.rm = TRUE), kappa_ci[1], kappa_ci[2]))
```

```
## Kappa:     Mean = 0.6072 | 95% CI = 0.3388 - 0.8344
```

```
cat(sprintf("Sens(F):  Mean = %.4f | 95% CI = %.4f - %.4f\n", mean(boot_sensF, na.rm = TRUE), sensF_ci[1], sensF_ci[2]))
```

```
## Sens(F):  Mean = 0.8890 | 95% CI = 0.7368 - 1.0000
```

```
cat(sprintf("Spec(F): Mean = %.4f | 95%% CI = %.4f - %.4f\n", mean(boot_specF, na.rm = TRUE), specF_ci[1], specF_ci[2]))
```

```
## Spec(F): Mean = 0.7244 | 95% CI = 0.5000 - 0.9231
```

```
cat(sprintf("Sens(M): Mean = %.4f | 95%% CI = %.4f - %.4f\n", mean(boot_sensM, na.rm = TRUE), sensM_ci[1], sensM_ci[2]))
```

```
## Sens(M): Mean = 0.7244 | 95% CI = 0.5000 - 0.9231
```

```
cat(sprintf("Spec(M): Mean = %.4f | 95%% CI = %.4f - %.4f\n", mean(boot_specM, na.rm = TRUE), specM_ci[1], specM_ci[2]))
```

```
## Spec(M): Mean = 0.8890 | 95% CI = 0.7368 - 1.0000
```

```
cat(sprintf("AUCROC: Mean = %.4f | 95%% CI = %.4f - %.4f\n", mean(boot_auc, na.rm = TRUE), auc_ci[1], auc_ci[2]))
```

```
## AUCROC: Mean = 0.8332 | 95% CI = 0.6889 - 0.9524
```