

Assignment-1 Report

1. Introduction

In this assignment, I implemented different search algorithms to solve N-puzzle problem where N is 8. This is a NP-hard problem and in the following sections their results are compared. The search algorithms are Breadth first search (BFS.py), depth first search(DFS.py), uniform cost search(UCS.py) and A*(Astar.py) search method.

2. Algorithms

- **Breath First Search** : Traverses the nodes at each level. Keeps a list of visited nodes. Frontier is a FIFO queue. $O(b^{d+1})$ worst case performance and memory allocation.
- **Depth First Search** : Expand deepest unexpanded node. Fringe is a LIFO queue.
- **Uniform Cost Search**: Uniform-cost search is a searching algorithm used for traversing a weighted tree or graph. Uniform-cost search expands nodes according to their path costs from the root node. A uniform-cost search algorithm is implemented by the priority queue. It gives maximum priority to the lowest cumulative cost.
- **A star Search**: Avoids expanding paths that are already expensive. Uses heuristics in this case Manhattan distance. Keeps a list of visited nodes.

3. Implementation Details

- **Breath First Search**: Pseudo code and explanation

```
BFS (G, s)           //Where G is the graph and s is the source node
    let Q be queue.
    Q.enqueue( s ) //Inserting s in queue until all its neighbour vertices are marked.

    mark s as visited.
    while ( Q is not empty)
        //Removing that vertex from queue, whose neighbour will be visited now
        v = Q.dequeue( )

        //processing all the neighbours of v
        for all neighbours w of v in Graph G
            if w is not visited
                Q.enqueue( w )           //Stores w in Q to further visit its neighbour
```

mark w as visited.

- **Depth First Search:** Pseudo code an explanation

```
DFS-iterative (G, s):                                //Where G is graph and s is source vertex
  let S be stack
  S.push( s )    //Inserting s in stack
  mark s as visited.
  while ( S is not empty):
    //Pop a vertex from stack to visit next
    v = S.top( )
    S.pop( )
    //Push all the neighbours of v in stack that are not visited
    for all neighbours w of v in Graph G:
      if w is not visited :
        S.push( w )
        mark w as visited
```

- **Uniform Cost Search:** Pseudo code an explanation

```
function UNIFORM-COST-SEARCH(problem) returns a solution, or failure
  if problem's initial state is a goal then return empty path to initial state
  frontier ← a priority queue ordered by pathCost, with a node for the initial state
  reached ← a table of {state: the best path that reached state}; initially empty
  solution ← failure
  while frontier is not empty and top(frontier) is cheaper than solution do
    parent ← pop(frontier)
    for child in successors(parent) do
      s ← child.state
      if s is not in reached or child is a cheaper path than reached[s] then
        reached[s] ← child
        add child to the frontier
        if child is a goal and is cheaper than solution then
          solution = child
  return solution
```

- **A star Search:** Pseudo code an explanation

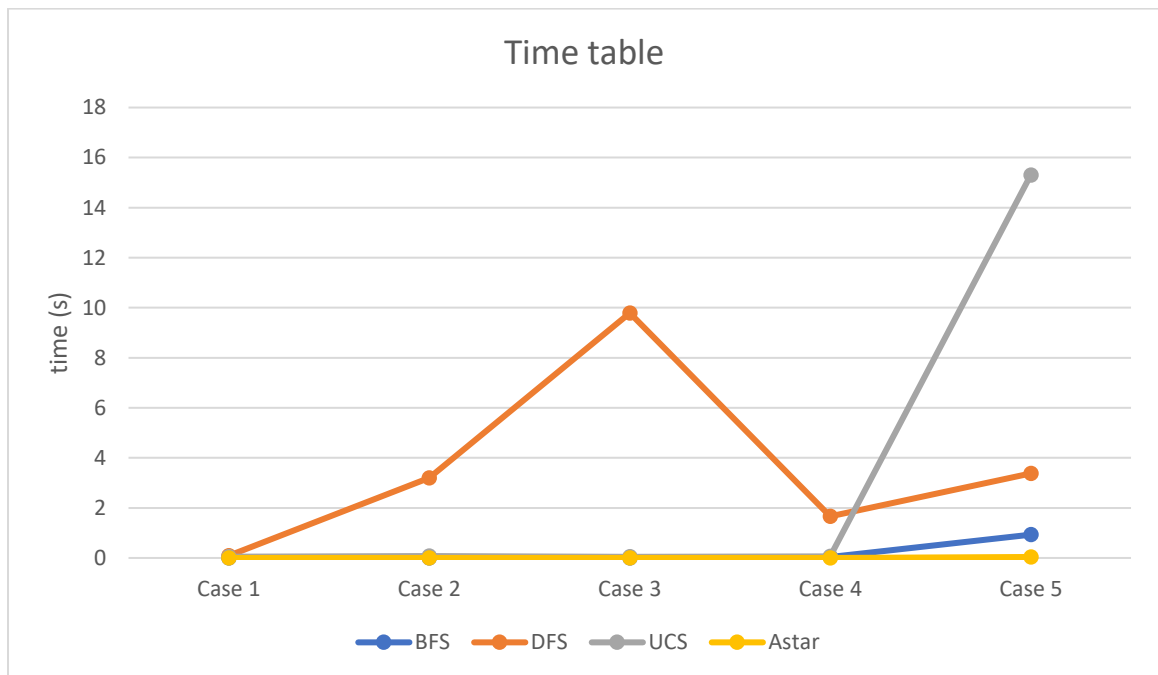
```
// Add the start node
put the startNode on the openList (leave it's f at zero)
// Loop until you find the end
while the openList is not empty
  // Get the current node
  let the currentNode equal the node with the least f value
  remove the currentNode from the openList
  add the currentNode to the closedList
  // Found the goal
  if currentNode is the goal
    Congratz! You've found the end! Backtrack to get path
  // Generate children
  let the children of the currentNode equal the adjacent nodes

  for each child in the children
    // Child is on the closedList
    if child is in the closedList
      continue to beginning of for loop
```

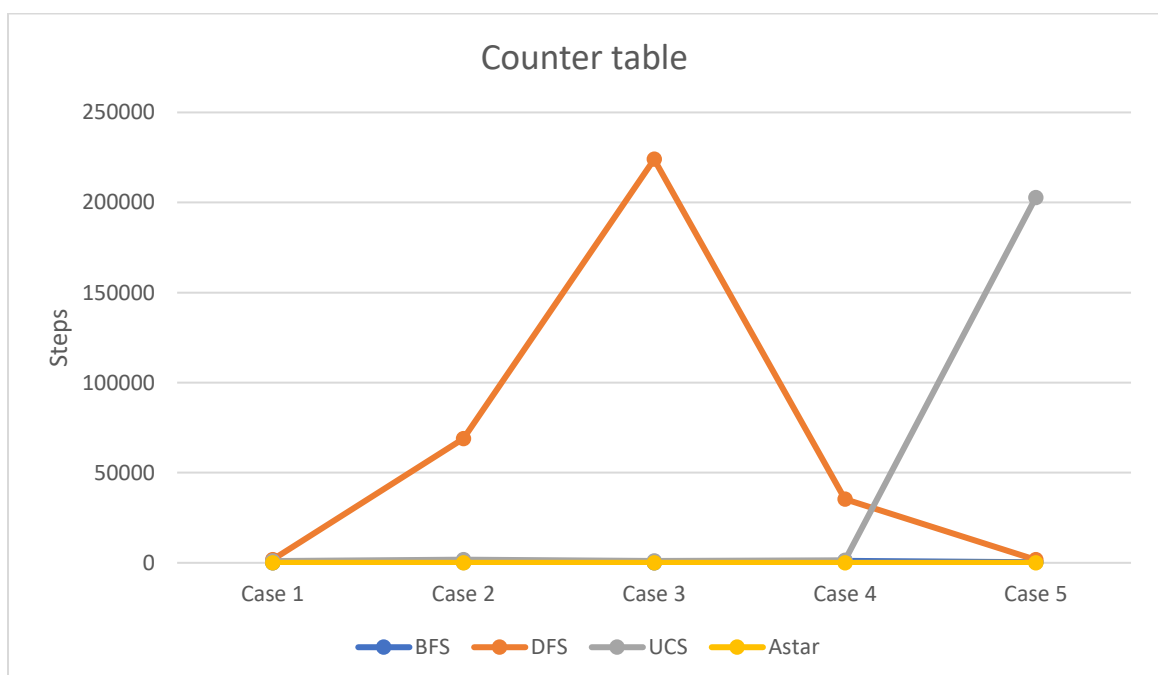
4. Results

Running the N-puzzle problem with different cases using the search algorithms leads to the following results

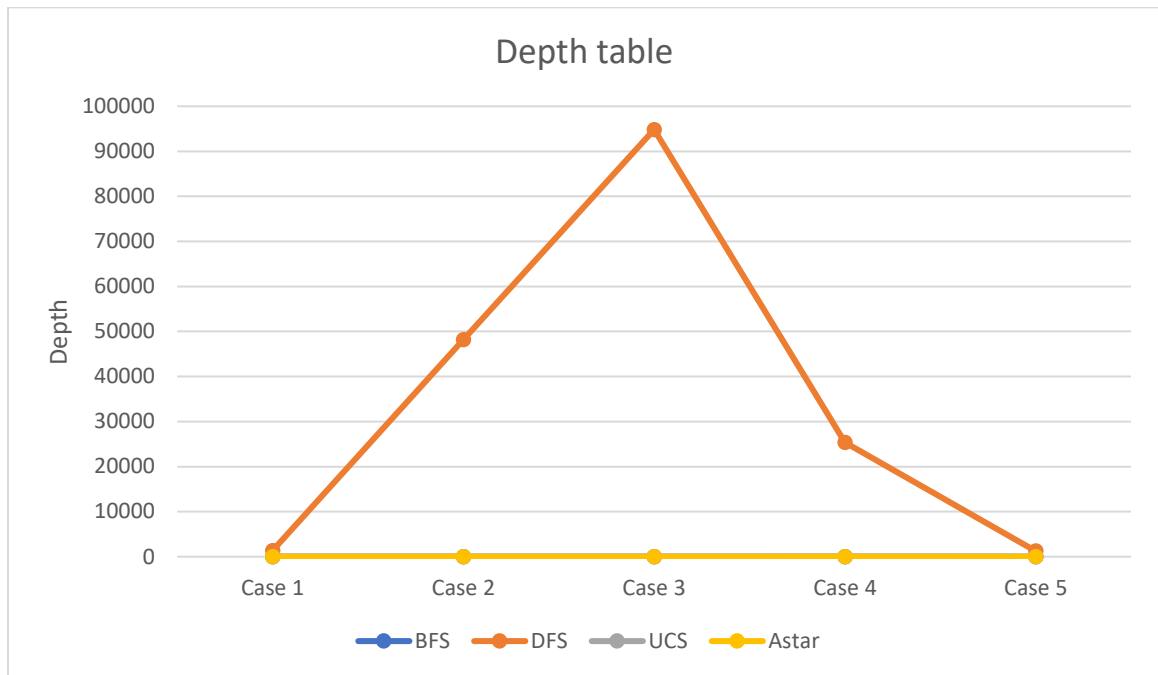
a) Time Comparison Table



b) Counter Table

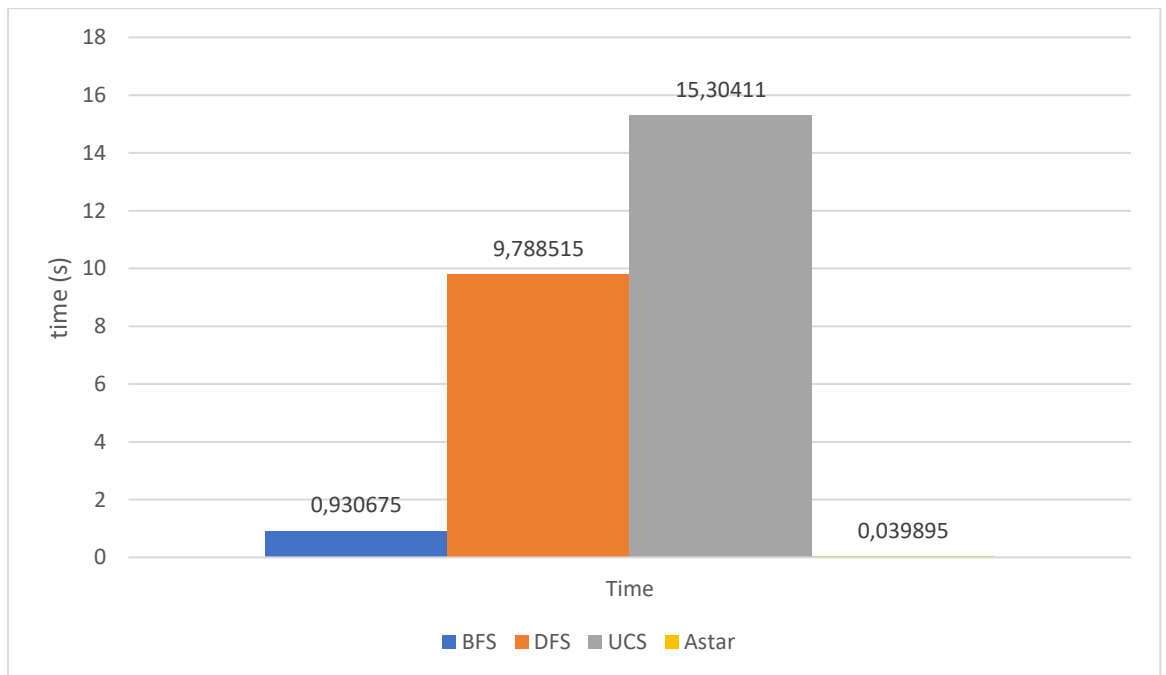


c) Depth Table

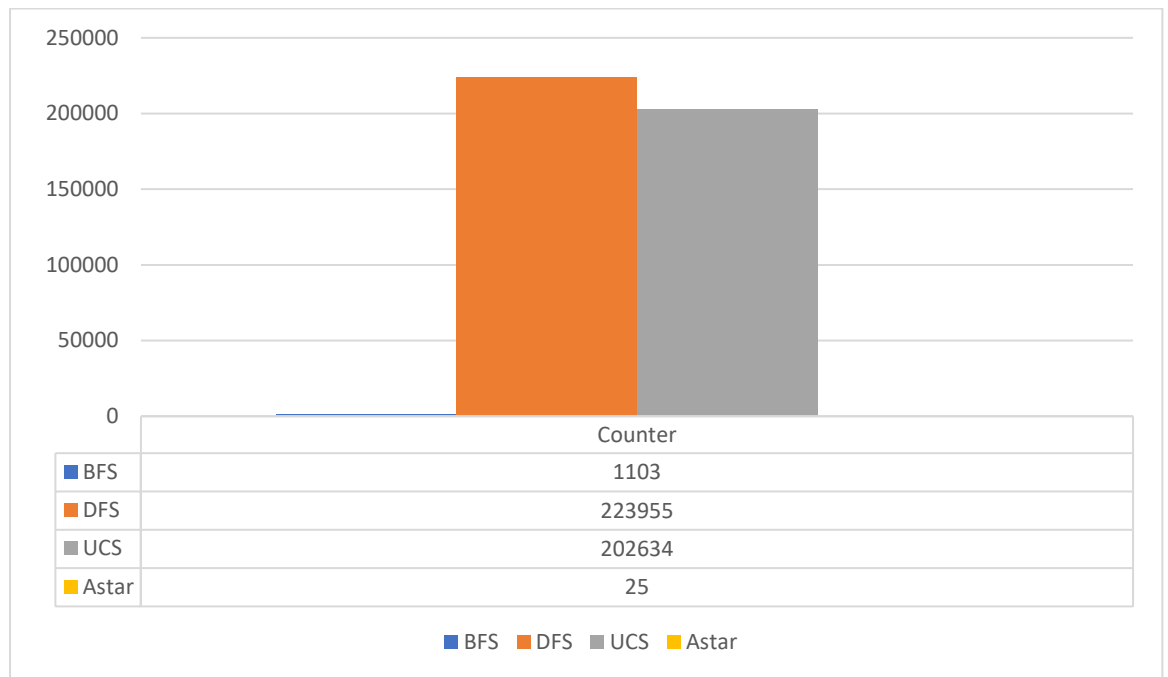


5. Conclusion

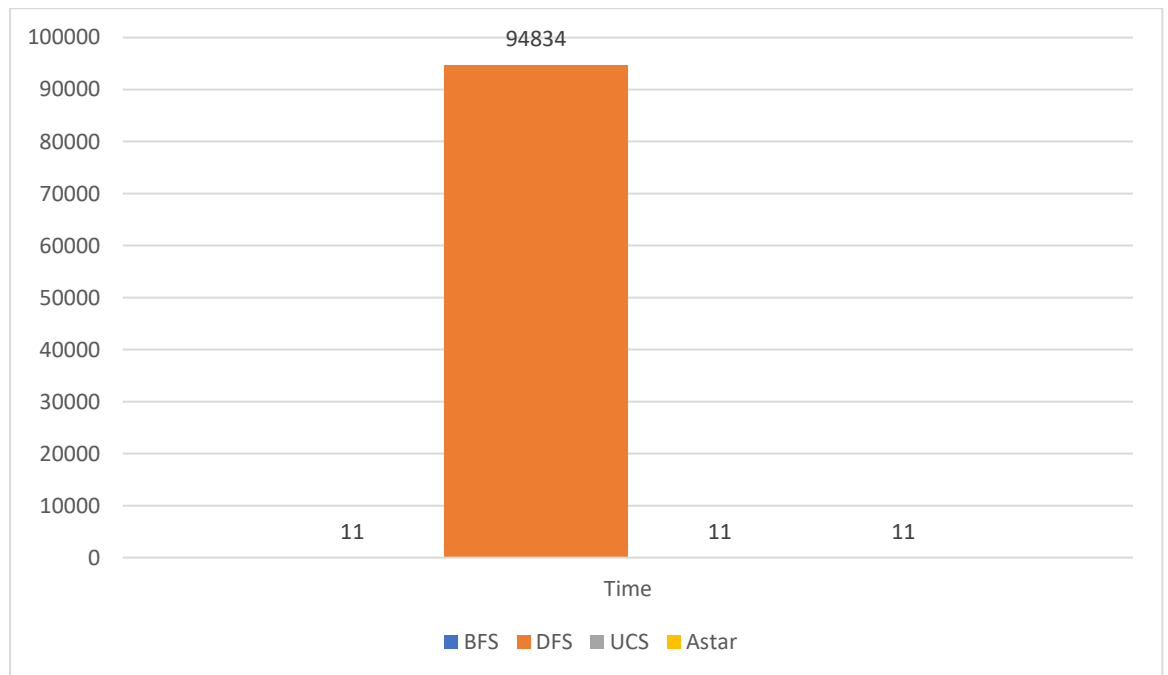
a) Worst-case Timetable



b) Worst-case Counter Table



c) Worst-case Depth Table



d) Discussion

DFS search gave the worst-case result in all cases.

UCS – A* always found the best solution