

Student Information

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Answer 1

a)

| p | q | $\neg q$ | $p \rightarrow q$ | $p \wedge \neg q$ | $p \rightarrow q \oplus p \wedge \neg q$ |
|-----|-----|----------|-------------------|-------------------|--|
| T | T | F | T | F | T |
| T | F | T | F | T | T |
| F | T | F | T | F | T |
| F | F | T | T | F | T |

b)

$$\begin{aligned} p \rightarrow ((q \vee \neg p) \rightarrow r) &\equiv \neg p \vee ((q \vee \neg p) \rightarrow r) && \text{table 7, Equivalence 1} \\ &\equiv \neg p \vee (\neg(q \vee \neg p) \vee r) && \text{table 7, Equivalence 1} \\ &\equiv \neg p \vee ((\neg q \vee \neg \neg p) \vee r) && \text{table 6, De Morgan's Second Law} \\ &\equiv \neg p \vee ((\neg q \vee p) \vee r) && \text{table 6, Idempotent Law} \\ &\equiv \neg(q \vee r) \rightarrow \neg p && \text{table 7, Equivalence 3} \\ &\equiv (\neg q \wedge \neg r) \rightarrow \neg p && \text{table 6, De Morgan's Second Law} \end{aligned}$$

c)

- F
- F
- F
- T
- T

Answer 2

a) $\exists x(P(\text{Can}, x) \wedge T(x, L))$

b) $\forall x(T(x, L) \rightarrow \exists y(N(y, \text{Turkish}) \wedge P(y, x)))$

c) $\forall x \exists y \exists z(T(x, S) \wedge R(x, y) \wedge T(y, S) \wedge R(x, z) \wedge T(z, S) \wedge (y = z))$

- d) $\exists y \exists z (W(M, y) \wedge \neg(P(z, y) \wedge N(z, \text{English})))$
e) $\forall z \exists x \exists y ((x \neq y) \wedge N(x, \text{Turkish}) \wedge P(x, G) \wedge P(y, G) \wedge (P(z, G) \leftrightarrow (z \neq x \vee z = y)))$
f) $\exists x \exists y \exists z (T(x, y) \wedge T(x, z) \wedge (y \neq z))$

Answer 3

| $p \rightarrow q, (r \wedge s) \rightarrow p, (r \wedge \neg q) \vdash \neg s$ | | |
|--|------------------------------|-----------------------|
| 1 | $p \rightarrow q$ | <i>premise</i> |
| 2 | $(r \wedge s) \rightarrow p$ | <i>premise</i> |
| 3 | $(r \wedge \neg q)$ | <i>premise</i> |
| 4 | r | $\wedge e, 3$ |
| 5 | $\neg q$ | $\wedge e, 3$ |
| 6 | $r \wedge s$ | <i>assumption</i> |
| 7 | p | $\rightarrow e, 2, 5$ |
| 8 | q | $\rightarrow e, 1, 6$ |
| 9 | \perp | $\neg e, 5, 8$ |
| 10 | $\neg(r \wedge s)$ | $\neg i, 6 - 9$ |
| 11 | s | <i>assumption</i> |
| 12 | $r \wedge s$ | $\wedge i, 4, 11$ |
| 13 | \perp | $\neg e, 10, 12$ |
| 14 | $\neg s$ | $\neg i, 11 - 13$ |

Answer 4

- $\exists x(S(x) \rightarrow P(x))$
- $\forall x(P(x))$
- $\exists y S(y)$

| $\exists x(P(x) \rightarrow S(x)), \forall x(P(x)) \vdash \exists y S(y)$ | | |
|---|------------------------------------|-----------------------|
| 1 | $\exists x(P(x) \rightarrow S(x))$ | <i>premise</i> |
| 2 | $\forall x(P(x))$ | <i>premise</i> |
| 3 | $P(c) \rightarrow S(c)$ | <i>assumption</i> |
| 4 | $P(c)$ | $\forall e, 2$ |
| 5 | $S(c)$ | $\rightarrow e, 3, 4$ |
| 6 | $\exists y S(y)$ | $\exists i, 5$ |
| 7 | $\exists y S(y)$ | $\exists e, 3 - 6$ |