

Methodology, Ethics and Practice of Data Privacy

实验部分

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Spring 2021*

Part 1

K-Anonymity

K-Anonymity简介

Every QI-cluster contains k or more tuples. (k=4)

	Name	Age	Gender	Zip Code	Nationality	Condition
1	Ann	20-29	Any	130**	Asian	Heart disease
2	Bruce	20-29	Any	130**	Asian	Heart disease
3	Cary	20-29	Any	130**	Asian	Viral infection
4	Dick	20-29	Any	130**	Asian	Viral infection
5	Eshwar	40-59	Any	14***	Asian	Cancer
6	Fox	40-59	Any	14***	Asian	Flu
7	Gary	40-59	Any	14***	Asian	Heart disease
8	Helen	40-59	Any	14***	Asian	Flu
9	Igor	30-39	Any	1322*	American	Cancer
10	Jean	30-39	Any	1322*	American	Cancer
11	Ken	30-39	Any	1322*	American	Cancer
12	Lewis	30-39	Any	1322*	American	Cancer

Identifier attributes

Quasi-identifiers, QI

Sensitive attributes

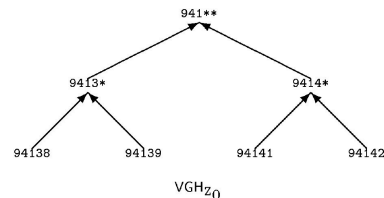
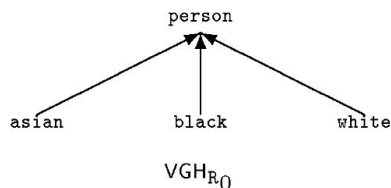
K-Anonymity 算法1 -- Samarati算法

» 技术:

- Generalization: 泛化;
- Suppression: 不发布/删除。

» 单个(categorical) Attribute:

- 预先定义泛化层数, 设可以删除的最大记录数 $MaxSup$;
- 先泛化到某一层, 再删除记录数小于 k 的QI-cluster使得满足 K -Anonymity (Full domain generalization) ;



[1] Samarati P. Protecting respondents identities in microdata release[J]. IEEE transactions on Knowledge and Data Engineering, 2001, 13(6): 1010-1027.

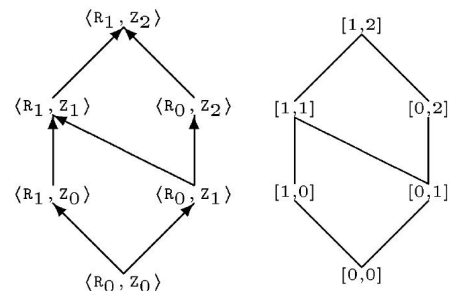
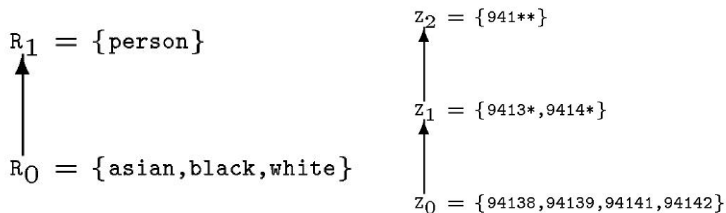
K-Anonymity 算法1 -- Samarati算法

» 多个(categorical) Attributes:

- 预定义泛化层数, 构建lattice, 如右下角的图;
- 例子: 泛化到 $\langle R_1, Z_1 \rangle$ 对应的距离向量为 $[1, 1]$;
- 要求泛化后的表格在满足K-Anonymity、删除的记录数不超过 *MaxSup* 的条件下, 距离向量的元素之和尽可能得小。

» 基本过程 (二分) :

- 结构高度为 h (下面的例子 $h = 3$), 检查高为 $h/2$ 的节点能否满足 k -匿名, 满足则继续检查 $h/4$ 高度的结点; 否则检查 $3h/4$ 高度的结点。重复这一过程直到找到满足 k -匿名的最低层。



K-Anonymity 算法1 -- Samarati算法

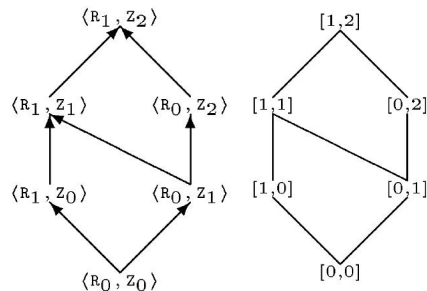
Find_vector

INPUT: Table $T_i = \text{PT}[QI]$ to be generalized, anonymity requirement k , suppression threshold MaxSup , lattice VL_{DT} of the distance vectors corresponding to the domain generalization hierarchy DGH_{DT} , where DT is the tuples of the domains of the quasi-identifier attributes.

OUTPUT: The distance vector sol of a generalized table GT_{sol} that is a k -minimal generalization of $\text{PT}[QI]$ according to Definition 4.3.

METHOD: Executes a binary search on VL_{DT} based on height of vectors in VL_{DT} .

1. $\text{low} := 0$; $\text{high} := \text{height}(\top, \text{VL}_{DT})$; $\text{sol} := \top$
2. **while** $\text{low} < \text{high}$
 - 2.1 $\text{try} := \lfloor \frac{\text{low} + \text{high}}{2} \rfloor$
 - 2.2 $\text{Vectors} := \{ \text{vec} \mid \text{height}(\text{vec}, \text{VL}_{DT}) = \text{try} \}$
 - 2.3 $\text{reach}_k := \text{false}$
 - 2.4 **while** $\text{Vectors} \neq \emptyset \wedge \text{reach}_k \neq \text{true}$ **do**
Select and remove a vector vec from Vectors
if $\text{satisfies}(\text{vec}, k, T_i, \text{MaxSup})$ **then** $\text{sol} := \text{vec}$; $\text{reach}_k := \text{true}$
 - 2.5 **if** $\text{reach}_k = \text{true}$ **then** $\text{high} := \text{try}$ **else** $\text{low} := \text{try} + 1$
3. **Return** sol



- » \top 表示完全generalization的Table;
- » VL_{DT} 表示右下角的图;
- » 2.2 Vectors:表示元素之和为try的距离向量的集合;

K-Anonymity 算法2 -- Mondrian算法

» 技术:

- Generalization: 泛化;

» 单个 (数值型) Attribute:

- 以所有记录在该属性取值的中位数将记录划分为两部分, 然后每一部分继续以中位数划分为两个区间 (有两种方式)。
- 重复这个过程, 直到每个区间包含的记录数 $\geq k$, 且不能再划分。此时每个区间都是一个等价类, 记录泛化为对应范围。

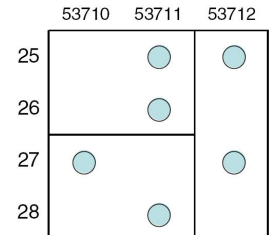
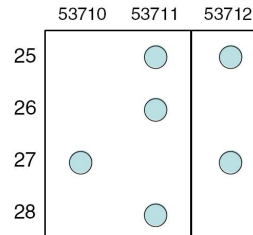
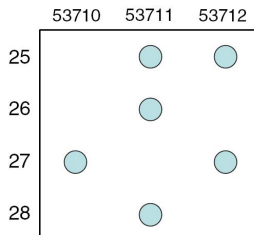
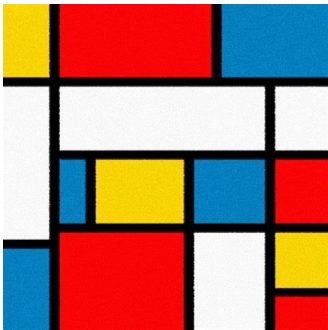
» 中位数划分的两种方式 (后面介绍第一种) :

- 如 $k = 2$, dataset = [1, 2, 3, 3, 4, 5];
- 第一种划分: [1, 2, 3, 3], [4, 5]; (strict partitioning)
- 第二种划分: [1, 2, 3], [3, 4, 5]。

K-Anonymity 算法2 -- Mondrian算法

» 多个 (数值型) Attributes :

- 每个Partition单独选择一个属性, 可以选择范围最大的属性, 或者随机选;
- 找到属性的中位数, 对Partition划分;
- 重复上述过程, 直到不能划分为止。



K-Anonymity 算法2 -- Mondrian算法

» 算法 (strict multidimensional partitioning) :

Anonymize(*partition*)

if (no allowable multidimensional cut for *partition*)

return $\phi : \text{partition} \rightarrow \text{summary}$

else

$\text{dim} \leftarrow \text{choose_dimension}()$

$\text{fs} \leftarrow \text{frequency_set}(\text{partition}, \text{dim})$

$\text{splitVal} \leftarrow \text{find_median}(\text{fs})$

$\text{lhs} \leftarrow \{t \in \text{partition} : t.\text{dim} \leq \text{splitVal}\}$

$\text{rhs} \leftarrow \{t \in \text{partition} : t.\text{dim} > \text{splitVal}\}$

return Anonymize(*rhs*) \cup Anonymize(*lhs*)

评价指标 Loss Metric (LM)

- » LM[1] is defined in terms of a normalized loss for each attribute of every tuple.



- » Quantify the loss when a leaf node value cannot be disambiguated from another value due to generalization.
- » **Categorical attribute A:** For a tuple t , suppose the value of $t[A]$ has been generalized to x . Letting $|A|$ represent the total number of leaf nodes in the tree; Letting M represent the number of leaf nodes in the subtree rooted at x , then the **loss for $t[A]$ is $(M - 1)/(|A| - 1)$.**
- » **What is the loss for “State”? 2/7**
- » The loss for attribute A is the average of the loss for all tuples t . The LM for the entire data set is the sum of the losses for each attribute.

[1]V. S. Iyengar, “Transforming data to satisfy privacy constraints,” in ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, 2002.

评价指标 Loss Metric (LM)

- » LM is defined in terms of a normalized loss for each attribute of every tuple.
- » **Numerical information:** For a tuple t , suppose the value of $t[A]$ has been generalized to an interval $[L_i, U_i]$. Letting the lower and upper bounds in the table for A be L and U . The normalized loss for this entry is given by $(U_i - L_i)/(U - L)$.

Zipcode	Age	Salary	Disease
476**	20-30	20-40K	Gastric Ulcer
476**	20-30	20-40K	Gastritis
476**	20-30	20-40K	Stomach Cancer
4790*	30-40	40-60K	Gastritis
4790*	30-40	40-60K	Flu
4790*	30-40	40-60K	Bronchitis

- » The loss for age [20-30] is $(30-20)/(40-20)$

Adult数据集介绍（文件夹中有提供）

- » 下载链接: <https://archive.ics.uci.edu/ml/datasets/adult>
- » 有32561条数据，删除空的或有?的行后，剩余**30162**条。
- » 15个attributes ['age', 'work_class', 'final_weight', 'education', 'education_num', 'marital_status', 'occupation', 'relationship', 'race', 'sex', 'capital_gain', 'capital_loss', 'hours_per_week', 'native_country', 'class']

```
data > adult.data
1 39, State-gov, 77516, Bachelors, 13, Never-married, Adm-clerical, Not-in-family, White, Male, 2174, 0, 40, United-States, <=50K
2 50, Self-emp-not-inc, 83311, Bachelors, 13, Married-civ-spouse, Exec-managerial, Husband, White, Male, 0, 0, 13, United-States, <=50K
3 38, Private, 215646, HS-grad, 9, Divorced, Handlers-cleaners, Not-in-family, White, Male, 0, 0, 40, United-States, <=50K
4 53, Private, 234721, 11th, 7, Married-civ-spouse, Handlers-cleaners, Husband, Black, Male, 0, 0, 40, United-States, <=50K
5 28, Private, 338409, Bachelors, 13, Married-civ-spouse, Prof-specialty, Wife, Black, Female, 0, 0, 40, Cuba, <=50K
6 37, Private, 284582, Masters, 14, Married-civ-spouse, Exec-managerial, Wife, White, Female, 0, 0, 40, United-States, <=50K
7 49, Private, 160187, 9th, 5, Married-spouse-absent, Other-service, Not-in-family, Black, Female, 0, 0, 16, Jamaica, <=50K
8 52, Self-emp-not-inc, 289642, HS-grad, 9, Married-civ-spouse, Exec-managerial, Husband, White, Male, 0, 0, 45, United-States, >50K
9 31, Private, 45781, Masters, 14, Never-married, Prof-specialty, Not-in-family, White, Female, 14084, 0, 50, United-States, >50K
10 42, Private, 159449, Bachelors, 13, Married-civ-spouse, Exec-managerial, Husband, White, Male, 5178, 0, 40, United-States, >50K
11 37, Private, 280464, Some-college, 10, Married-civ-spouse, Exec-managerial, Husband, Black, Male, 0, 0, 80, United-States, >50K
12 30, State-gov, 141297, Bachelors, 13, Married-civ-spouse, Prof-specialty, Husband, Asian-Pac-Islander, Male, 0, 0, 40, India, >50K
13 23, Private, 122272, Bachelors, 13, Never-married, Adm-clerical, Own-child, White, Female, 0, 0, 30, United-States, <=50K
14 32, Private, 205019, Assoc-acdm, 12, Never-married, Sales, Not-in-family, Black, Male, 0, 0, 50, United-States, <=50K
15 40, Private, 121772, Assoc-voc, 11, Married-civ-spouse, Craft-repair, Husband, Asian-Pac-Islander, Male, 0, 0, 40, ?, >50K
```

实验要求

» 必做部分80:

- 代码正确: 50 (每个算法各25)
- 代码清晰有注释: 10
- 实验报告, 测试分析结果和讨论: 20

» 选做部分20:

- Samarati算法可能会有很多解满足要求, 调研并探究如何选择输出保证结果的可用性尽可能大, 说说你的启发, (e.g.:选用合适的评价指标评价不同的输出) 15
- Mondrian算法处理categorical (如Gender) 5

» 代码抄袭0, 会有查重

实验要求

- » 实现 k -Anonymity两种算法（后面两页有具体要求）：
 - Samarati算法 (categorical 型)
 - Mondrian算法 (数值型)
- » 实验报告：问题描述、程序使用指南、实验结果分析、讨论与总结。

实验要求(Samarati算法)

» Samarati算法:

- 使用Adult数据集;
- $QI=\{age, gender, race, marital_status\}$ (categorical 型) , $S = \{occupation\}$
- 输入: data, k, maxSup (data是数据集, k是K-Anonymity的参数, maxSup表示最大suppression的个数);
- 输出: 匿名后的数据集。
- 评价指标: 运行时间和LM。

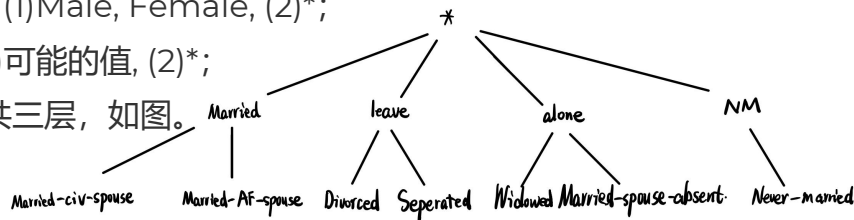
» 可取 $K=10, maxSup=20$ 。并测试不同的 $k, maxSup$ 对实验结果的影响。

» Age: 共五层, (1)原始值, (2)range-5, (3)range-10, (4)range-20, (5)*;

» Gender: 共两层, (1)Male, Female, (2)*;

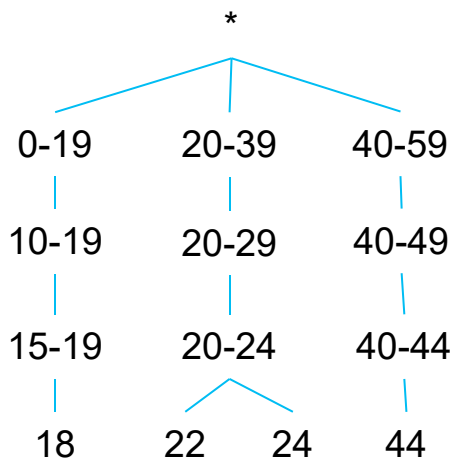
» Race: 共两层, (1)可能的值, (2)*;

» Marital_status: 共三层, 如图。



实验要求(Samarati算法)

- » Age的层次类似左下图，共五层，(1)原始值，(2)range-5, (3)range-10, (4)range-20, (5)*;
- » Gender、marital_status、race的层次以右下文件形式给出：
 - 子节点,父节点



adult_marital_status.txt

```
NM,*
Married,*
leave,*
alone,*
Never-married,NM
Married-civ-spouse,Married
Married-AF-spouse,Married
Divorced,leave
Separated,leave
Widowed,alone
Married-spouse-absent,alone
```


实验要求(Mondrian算法)

» Mondrian算法:

- 使用Adult数据集;
- $QI=\{age, education_num\}$ (数值型) , $S = \{occupation\}$;
- 输入: data, k (data是数据集, k 是K-Anonymity的参数) ;
- 输出: 匿名后的数据集。
- 评价指标: 运行时间和LM。

» 可取 $k=10$ 。并测试不同的 k 对实验结果的影响。

参考资料

- » Samarati P. Protecting respondents identities in microdata release[J]. IEEE transactions on Knowledge and Data Engineering, 2001.
- » LeFevre K, DeWitt D J, Ramakrishnan R. Mondrian multidimensional k-anonymity[C].(ICDE'06). IEEE, 2006.
- » V. S. Iyengar , “Transforming data to satisfy privacy constraints,” in ACM SIGKDD International Conference on Knowledge Discovery and Data Mining, 2002.
- » <https://blog.csdn.net/xff1994/article/details/83149116>

THANKS!

Any questions?

