CS 188 Introduction to Dpring 2019 Artificial Intelligence

Written HW 8

Due: Monday 4/8/2019 at 11:59pm (submit via Gradescope).

Leave self assessment boxes blank for this due date.

Self assessment due: Monday 4/15/2019 at 11:59pm (submit via Gradescope)

For the self assessment, fill in the self assessment boxes in your original submission (you can download a PDF copy of your submission from Gradescope – be sure to delete any extra title pages that Gradescope attaches). For each subpart where your original answer was correct, write "correct." Otherwise, write and explain the correct answer. Do not leave any boxes empty.

If you did not submit the homework (or skipped some questions) but wish to receive credit for the self-assessment, we ask that you first complete the homework without looking at the solutions, and then perform the self-assessment afterwards.

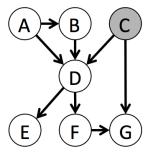
Policy: Can be solved in groups (acknowledge collaborators) but must be written up individually

Submission: Your submission should be a PDF that matches this template. Each page of the PDF should align with the corresponding page of the template (page 1 has name/collaborators, question 1 begins on page 2, etc.). **Do not reorder, split, combine, or add extra pages.** The intention is that you print out the template, write on the page in pen/pencil, and then scan or take pictures of the pages to make your submission. You may also fill out this template digitally (e.g. using a tablet.)

First name	
Last name	
SID	
Collaborators	

Q1. Variable Elimination

(a) For the Bayes' net below, we are given the query $P(A, E \mid +c)$. All variables have binary domains. Assume we run variable elimination to compute the answer to this query, with the following variable elimination ordering: B, D, G, F.



Complete the following description of the factors generated in this process:

After inserting evidence, we have the following factors to start out with:

$$P(A), P(B|A), P(+c), P(D|A, B, +c), P(E|D), P(F|D), P(G|+c, F)$$

When eliminating B we generate a new factor f_1 as follows:

$$f_1(A, +c, D) = \sum_b P(b|A)P(D|A, b, +c)$$

This leaves us with the factors:

This leaves us with the factors:

$$P(A), P(+c), P(E|D), P(F|D), P(G|+c, F), f_1(A, +c, D)$$

When eliminating D we generate a new factor f_2 as follows:

This leaves us with the factors:	
This leaves us with the factors.	
When eliminating G we generate a new factor f_3 as follows:	

When elimi	nating F we genera	ite a new factor f	f ₄ as follows:			
This leaves	us with the factors	:				
Self asses	ssment If correct, w	rite "correct" in th	e box. Otherwise, v	write and explain	the correct answer.	
Write a form	mula to compute P	$(A, E \mid +c)$ from	the remaining fa	ctors.		
Self asses	ssment If correct, w	rite "correct" in th	e box. Otherwise, v	write and explain	the correct answer.	

Self assessmen	${f t}$ If correct, write " ${f correct}$ " in the	box. Otherwise, write and exp	lain the correct answer.
actor generated a	imination ordering for the sam long the way is smallest. Hint bles, for a size of $2^2 = 4$ table table below.	the maximum size factor g	enerated in your solution sho
	Variable Eliminated	Factor Generated	
For example, in the entries: B , $f_1(A)$	the naive ordering we used earlied $+c, D$).	r, the first row in this table v	would have had the following
Self assessmen	t If correct, write "correct" in the	box. Otherwise, write and exp	lain the correct answer.

Q2. Bayes Nets: Sampling

Consider the following Bayes Net, where we have observed that B = +b and D = +d.

0.5+a0.5

I	P(B A)	.)
+a	+b	0.8
+a	-b	0.2
-a	+b	0.4
-a	-b	0.6

I	P(C B)	?)
+b	+c	0.1
+b	-c	0.9
-b	+c	0.7
-b	-c	0.3

	P(D	A,C)	
+a	+c	+d	0.6
+a	+c	-d	0.4
+a	-c	+d	0.1
+a	-c	-d	0.9
-a	+c	+d	0.2
-a	+c	-d	0.8
-a	-c	+d	0.5
-a	-c	-d	0.5

(a) Consider doing Gibbs sampling for this example. Assume that we have initialized all variables to the values +a, +b, +c, +d. We then unassign the variable C, such that we have A = +a, B = +b, C = ?, D = +d. Calculate the probabilities for new values of C at this stage of the Gibbs sampling procedure.

P(C = +c at the next step of Gibbs sampling) =

P(C = -c at the next step of Gibbs sampling) =

Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.

(b) Consider a sampling scheme that is a hybrid of rejection sampling and likelihood-weighted sampling. Under this scheme, we first perform rejection sampling for the variables A and B. We then take the sampled values for

- A and B and extend the sample to include values for variables C and D, using likelihood-weighted sampling. (i) Below is a list of candidate samples. Mark the samples that would be rejected by the rejection sampling
 - portion of the hybrid scheme.

Self assessment If correct, write "correct" in the box. Otherwise, write and explain the correct answer.

	amples under our hy	brid sche	me.								r the
							Weight				
		-a	+b	-c	+d						
		+a	+b	-c	+d						
		+a	+b	-c	+d						
Self	assessment If corre	ect write "	rorrec	t " in t	he boy	Otherwise	write and	evnlain	the correc	rt answer	
	assessment in corre	ect, write	correc	t III t	ле вох.	Otherwise	, write and	explain	the correc	answer.	
(iii) U	Use the weighted sar	nples from	n part	(ii) t	o calcı	ulate an e	stimate for	P(+a	+b,+d).		
т	The estimate of $P(+$	a + b + d) is								
_									1		
-	Self assessment	ii correct, w	rite "C	orrect	t in th	e box. Otno	erwise, write	e and ex	tplain the	correct answer.	
We no	w attempt to design	an alterna	ative h	nybrid	l samp	ling schen	ne that com	nbines el	ements o	f likelihood-we	
and re	w attempt to design jection sampling. Fo luces correctly appr	r each pro	posed	scher	me, inc	licate whe	ther it is va				-
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