Notebook

May 19, 2023

1 Bigrams - MakeMore pt.1 (12/04/2023)

We now move on to see some interesting applications of the theory we developed earlier on.

Mostly, we will see how to construct a language model, character based, able to 'learn' how to 'reproduce' $\mu(x_n|x_1,\ldots,x_{n-1})$. We will develop such model following "chronological" steps, in the sense that we'll start from an older programming structure and later improve the latest feature in Artificial Intelligence.

Almost all the material presented is taken from A. Karpathy's course and GitHub repository.

First, we start with *counting approach* (not to be confused with the counting technique earlier presented) to implement a bigram approximation of our "language" model (a "2-Markov" approximation).

We want to learn something from a dataset of words. First of all, we need a machine which generates these data (the so-called words).

```
[22]: words = open('data/nomi_italiani.txt').read().splitlines()
```

Let's figure out the length of each word in our dataset.

```
[23]: L = [len(w) for w in words]
print(words[L.index(max(L))])
```

marie-odette-rose-gabrielle

```
[24]: import numpy as np print(np.mean(L))
```

7.088193300384404

```
[25]: import random
random.seed(154)
random.shuffle(words)
print(words[:10])
```

```
['castorino', 'ella', 'irmo', 'leoluca', 'sankhare', 'galvano', 'faleria',
'germando', 'illo', 'romilde']
```

```
[26]: for w in words[:1]:
          for ch1, ch2 in zip(w, w[1:]):
               print(ch1, ch2)
     са
     a s
     s t
     t o
     o r
     r i
     i n
     n o
[27]: print(w)
      list(w)
      print(w[1:])
     castorino
     astorino
     To get all bigrams of, for example, the last three words one can do something like that
[28]: for w in words[:3]:
          chs = [' < S >'] + list(w) + [' < E >']
          for ch1, ch2 in zip(chs, chs[1:]):
               print(ch1, ch2)
     <S> c
     са
     a s
     s t
     t o
     o r
     r i
     i n
     n o
     o <E>
     <S> e
     e l
     1 1
     l a
     a <E>
     <S> i
     i r
     r m
     m o
     o <E>
```

How many often does a bigram happen?

```
[29]: b = {}
    for w in words[:3]:
        chs = ['<S>'] + list(w) + ['<E>']
        for ch1, ch2 in zip(chs, chs[1:]):
            b[(ch1, ch2)] = b.get((ch1, ch2), 0) + 1
        print(b)
```

```
{('<S>', 'c'): 1, ('c', 'a'): 1, ('a', 's'): 1, ('s', 't'): 1, ('t', 'o'): 1, ('o', 'r'): 1, ('r', 'i'): 1, ('i', 'n'): 1, ('n', 'o'): 1, ('o', '<E>'): 2, ('<S>', 'e'): 1, ('e', 'l'): 1, ('l', 'l'): 1, ('l', 'a'): 1, ('a', '<E>'): 1, ('<S>', 'i'): 1, ('i', 'r'): 1, ('r', 'm'): 1, ('m', 'o'): 1}
```

We can do it for all words

```
[30]: b = {}
for w in words:
    chs = ['<S>'] + list(w) + ['<E>']
    for ch1, ch2 in zip(chs, chs[1:]):
        b[(ch1, ch2)] = b.get((ch1, ch2), 0) + 1
```

We now want to construct a machine which tells us the probability of the next character. Let's sort all by frequency

```
[31]: print(sorted(b.items(), key=lambda z: -z[1]))
```

```
[(('o', '<E>'), 4235), (('a', '<E>'), 3831), (('i', 'n'), 1935), (('a', 'n'),
1497), (('r', 'i'), 1483), (('n', 'a'), 1429), (('i', 'o'), 1380), (('i', 'a'),
1344), (('n', 'o'), 1269), (('1', 'i'), 1261), (('e', 'r'), 1149), (('<S>',
'a'), 1095), (('e', 'l'), 1070), (('a', 'r'), 957), (('o', 'r'), 920), (('<S>',
'f'), 885), (('a', 'l'), 856), (('<S>', 'o'), 789), (('d', 'o'), 754), (('i',
'l'), 712), (('r', 'o'), 705), (('e', 'n'), 699), (('r', 'a'), 686), (('l',
'a'), 682), (('m', 'a'), 663), (('<S>', 'g'), 657), (('n', 'i'), 649), (('e',
'<E>'), 630), (('<S>', 'e'), 629), (('<S>', 'r'), 626), (('<S>', 'm'), 595),
(('o', 'n'), 591), (('r', 'e'), 584), (('t', 'a'), 580), (('d', 'a'), 565),
(('t', 'o'), 559), (('d', 'i'), 552), (('o', 'l'), 545), (('d', 'e'), 540),
(('1', '1'), 537), (('m', 'i'), 532), (('s', 'i'), 531), (('<S>', 'c'), 520),
(('l', 'e'), 511), (('g', 'i'), 496), (('i', 's'), 482), (('l', 'o'), 474),
(('<S>', '1'), 446), (('n', 'e'), 437), (('n', 'd'), 433), (('t', 'i'), 430),
(('l', 'd'), 405), (('i', 'd'), 403), (('v', 'i'), 398), (('t', 't'), 392),
(('<S>', 's'), 391), (('f', 'i'), 387), (('e', 't'), 386), (('t', 'e'), 378),
(('c', 'o'), 364), (('<S>', 'd'), 351), (('z', 'i'), 350), (('<S>', 'p'), 345),
(('i', 'c'), 342), (('m', 'e'), 335), (('n', 't'), 334), (('c', 'a'), 333),
(('s', 'a'), 333), (('e', 's'), 331), (('c', 'i'), 326), (('o', 's'), 322),
(('<S>', 'i'), 319), (('<S>', 'n'), 313), (('i', 'e'), 311), (('s', 't'), 307),
(('<S>', 'v'), 297), (('<S>', 'b'), 293), (('f', 'e'), 283), (('v', 'a'), 279),
(('g', 'e'), 272), (('i', 'r'), 268), (('m', 'o'), 263), (('a', 't'), 255),
(('b', 'e'), 255), (('a', 'm'), 254), (('a', 'd'), 251), (('v', 'e'), 245),
(('e', 'd'), 245), (('r', 'd'), 237), (('n', 'z'), 237), (('a', 's'), 236),
(('c', 'e'), 235), (('r', 't'), 234), (('<S>', 't'), 226), (('i', 'm'), 225),
```

```
(('s', 'e'), 220), (('e', 'o'), 219), (('n', 'n'), 217), (('e', 'm'), 215),
(('i', 't'), 206), (('i', 'g'), 195), (('e', 'a'), 189), (('f', 'a'), 187),
(('r', 'm'), 182), (('o', 'd'), 181), (('o', 'm'), 177), (('c', 'c'), 175),
(('s', 'o'), 167), (('f', 'r'), 166), (('p', 'i'), 164), (('u', 'r'), 163),
(('l', 'm'), 160), (('g', 'a'), 156), (('b', 'a'), 155), (('u', 'c'), 154),
(('o', 'v'), 145), (('i', '<E>'), 143), (('p', 'a'), 142), (('l', 'v'), 140),
(('p', 'e'), 139), (('l', 'f'), 139), (('a', 'u'), 138), (('c', 'h'), 137),
(('i', 'v'), 132), (('b', 'i'), 126), (('a', 'c'), 123), (('f', 'o'), 121),
(('g', 'o'), 121), (('u', 'i'), 117), (('s', 's'), 116), (('a', 'v'), 115),
(('b', 'r'), 113), (('s', 'c'), 113), (('u', 'l'), 113), (('r', 'u'), 112),
(('l', 'u'), 110), (('z', 'a'), 109), (('c', 'l'), 109), (('o', 't'), 107),
(('a', 'b'), 106), (('f', 'l'), 105), (('h', 'i'), 103), (('u', 's'), 103),
(('n', 'u'), 102), (('t', 'r'), 102), (('n', 'c'), 100), (('e', 'g'), 100),
(('a', 'z'), 99), (('d', 'r'), 97), ((' < S > ', 'z'), 97), (('g', 'l'), 94), (('a', 'l'), 94))
'g'), 93), (('r', 'n'), 93), (('n', 'g'), 91), (('s', '<E>'), 90), (('p', 'r'),
90), (('p', 'o'), 90), (('i', 'z'), 90), (('u', 'n'), 89), (('z', 'o'), 86),
(('t', 'u'), 86), (('e', 'v'), 82), (('e', 'u'), 81), (('b', 'o'), 80), (('<S>',
'u'), 80), (('z', 'e'), 79), (('r', 'c'), 77), (('r', 'r'), 75), (('z', 'z'),
75), (('r', 'g'), 74), (('a', 'i'), 74), (('q', 'u'), 73), (('i', 'b'), 72),
(('o', 'b'), 71), (('r', 's'), 70), (('h', 'e'), 68), (('l', 'b'), 68), (('u',
'd'), 68), (('s', 'p'), 67), (('o', 'c'), 67), (('g', 'u'), 65), (('a', 'f'),
61), (('n', 's'), 61), (('i', 'u'), 59), (('c', 'r'), 59), (('l', 'c'), 58),
(('l', 't'), 57), (('r', 'l'), 57), (('s', 'm'), 57), (('v', 'o'), 56), (('f',
'f'), 56), (('g', 'r'), 56), (('m', 'b'), 55), (('<S>', 'w'), 55), (('u', 'e'),
53), (('u', 'a'), 53), (('r', '<E>'), 52), (('m', 'm'), 50), (('d', 'u'), 50),
(('p', 'p'), 49), (('s', 'u'), 48), (('u', 't'), 47), (('e', 'f'), 47), (('<S>',
'q'), 47), (('e', 'z'), 47), (('r', 'v'), 46), (('e', 'p'), 46), (('a', '-'),
45), (('o', 'p'), 45), (('i', 'p'), 44), (('o', 'f'), 44), (('l', 'g'), 44),
(('a', 'o'), 42), (('e', 'c'), 41), (('r', 'z'), 40), (('u', 'g'), 39), (('a', 'c'), 40), (('a', 'c'
'e'), 37), (('n', '<E>'), 37), (('m', 'p'), 35), (('f', 'u'), 34), (('u', 'b'),
33), (('d', 'd'), 33), (('g', 'h'), 31), (('<S>', 'j'), 31), (('o', 'i'), 31),
(('w', 'a'), 30), (('g', 'n'), 29), (('c', 'u'), 29), (('g', 'g'), 29), (('b',
'b'), 28), (('m', 'u'), 28), (('n', 'f'), 28), (('e', 'b'), 28), (('u', 'm'),
27), (('a', 'p'), 26), (('i', 'f'), 26), (('h', 'a'), 25), (('r', 'f'), 25),
(('o', 'g'), 25), (('o', 'a'), 24), (('s', 'l'), 24), (('j', 'a'), 24), (('s',
'v'), 23), (('l', 's'), 23), (('u', 'f'), 22), (('r', 'b'), 22), (('e', 'i'),
21), (('p', 'l'), 19), (('o', 'e'), 19), (('w', 'i'), 17), (('u', 'p'), 17),
(('b', 'u'), 16), (('l', '<E>'), 16), (('o', '-'), 16), (('u', 'z'), 16), (('k',
'a'), 15), (('d', '<E>'), 15), (('j', 'o'), 14), (('e', '-'), 14), (('u', 'o'),
13), (('-', 'm'), 13), (('-', 'a'), 13), (('p', 'u'), 13), (('l', 'p'), 12),
(('-', 'r'), 12), (('u', '<E>'), 12), (('s', 'q'), 12), (('r', 'p'), 11),
(('<S>', 'k'), 11), (('b', 'l'), 11), (('n', 'r'), 10), (('n', '-'), 10), (('w',
'e'), 9), (('-', 'g'), 9), (('d', 'm'), 9), (('t', 'h'), 9), (('l', 'z'), 8),
(('m', '<E>'), 8), (('a', 'h'), 8), (('n', 'm'), 8), (('s', 'd'), 7), (('z',
'u'), 7), (('n', 'l'), 7), (('-', 'e'), 7), (('e', 'e'), 6), (('t', '<E>'), 6),
(('s', 'f'), 6), (('y', 'n'), 6), (('-', 'j'), 6), (('r', 'k'), 6), (('v', 'v'),
6), (('v', 'r'), 6), (('s', 'z'), 6), (('n', 'p'), 6), (('g', 'd'), 5), (('s',
'b'), 5), (('a', 'q'), 5), (('o', 'h'), 5), (('i', 'k'), 5), (('b', 'd'), 5),
```

```
(('k', 'o'), 5), (('o', 'z'), 5), (('g', 'f'), 5), (('-', 'p'), 5), (('s', 'h'),
5), (('o', 'u'), 5), (('r', 'q'), 5), (('k', 'h'), 4), (('-', 'd'), 4), (('-',
'i'), 4), (('<S>', 'y'), 4), (('z', 'b'), 4), (('x', 'a'), 4), (('y', '<E>'),
4), (('h', 'r'), 4), (('k', 'r'), 4), (('t', 'y'), 4), (('l', 'r'), 4), (('a',
'w'), 4), (('j', 'u'), 4), (('z', '<E>'), 4), (('d', 'v'), 4), (('h', '<E>'),
4), (('-', '1'), 4), (('-', 'c'), 4), (('-', 'o'), 3), (('y', 'o'), 3), (('1',
('v'), 3), (('v', 'l'), 3), (('r', 'v'), 3), (('v', 's'), 3), (('-', 's'), 3),
(('f', 'n'), 3), (('l', 'k'), 3), (('w', 'o'), 3), (('k', 'i'), 3), (('e', 'x'), 3))
3), (('n', 'v'), 3), (('j', 'e'), 3), (('x', 'i'), 3), (('w', '<E>'), 3), (('p',
'h'), 3), (('i', 'j'), 3), (('h', 'o'), 3), (('e', 'w'), 3), (('<S>', 'h'), 3),
(('r', 'x'), 3), (('k', '<E>'), 3), (('s', 'r'), 3), (('n', 'q'), 3), (('d',
'g'), 3), (('z', 'y'), 3), (('n', 'k'), 2), (('c', 'y'), 2), (('y', 'u'), 2),
(('v', '<E>'), 2), (('e', 'j'), 2), (('j', 'i'), 2), (('-', 'b'), 2), (('-',
'v'), 2), (('-', 'h'), 2), (('w', 'l'), 2), (('z', 'k'), 2), (('y', 'a'), 2),
(('s', '-'), 2), (('d', '-'), 2), (('-', 'k'), 2), (('v', 'u'), 2), (('t', '-'),
2), (('a', 'y'), 2), (('l', 'n'), 2), (('s', 'k'), 2), (('n', 'b'), 2), (('e',
'k'), 2), (('m', 'l'), 2), (('-', 'n'), 2), (('f', '<E>'), 2), (('n', 'j'), 2),
(('y', 'l'), 2), (('u', 'j'), 2), (('c', 't'), 2), (('t', 's'), 2), (('u', 'k'),
2), (('r', '-'), 2), (('c', '<E>'), 2), (('x', '<E>'), 2), (('c', 'm'), 1),
(('o', 'x'), 1), (('b', '-'), 1), (('y', 'v'), 1), (('m', 'y'), 1), (('y', 'r'),
1), (('-', 'y'), 1), (('s', 'n'), 1), (('i', 'x'), 1), (('-', 'f'), 1), (('t',
'l'), 1), (('r', 'j'), 1), (('m', '-'), 1), (('t', 'b'), 1), (('d', 'j'), 1),
(('k', 'e'), 1), (('k', 'b'), 1), (('a', 'j'), 1), (('t', 'g'), 1), (('-', 'w'),
1), (('k', '-'), 1), (('-', 'z'), 1), (('n', 'w'), 1), (('b', '<E>'), 1), (('o',
'k'), 1), (('k', 's'), 1), (('j', '<E>'), 1), (('y', 'k'), 1), (('m', 'n'), 1),
(('l', '-'), 1), (('i', '-'), 1), (('m', 's'), 1), (('t', 'p'), 1), (('o', 'y'),
1), (('y', 'c'), 1), (('w', 'u'), 1), (('d', 'y'), 1), (('z', 't'), 1), (('f',
'-'), 1), (('z', '-'), 1), (('n', 'y'), 1), (('a', 'a'), 1), (('d', 'h'), 1),
(('-', '<E>'), 1), (('u', '-'), 1), (('d', 'w'), 1), (('u', 'v'), 1), (('j',
'n'), 1), (('h', '-'), 1), (('t', 'm'), 1), (('j', 'j'), 1), (('a', 'x'), 1),
(('c', 'q'), 1), (('l', 'h'), 1), (('h', 'm'), 1), (('k', 't'), 1), (('g',
'<E>'), 1)]
```

With the set function built-in python one can get the unique elements of a list

```
[32]: w = set(list(words[1]))
print(w)
```

{'e', 'a', 'l'}

Now we want to code this information Let's take only the unique elements of a word, then of all words, i.e. our finite alphabet

```
[33]: chars = sorted(list(set(''.join(words))))
    chars.append('<S>')
    chars.append('<E>')
    print(chars)
```

['-', 'a', 'b', 'c', 'd', 'e', 'f', 'g', 'h', 'i', 'j', 'k', 'l', 'm', 'n', 'o',

```
'p', 'q', 'r', 's', 't', 'u', 'v', 'w', 'x', 'y', 'z', '<S>', '<E>']
```

At this point we should have 27 characters, 26 letters of the alphabet and the dash from composite names

```
[34]: print(len(chars))
```

29

Actually we need 29 characters, i.e. the 27 previously discussed plus the initial and final of a word

```
[35]: import torch

N = torch.zeros(29, 29)
```

Let's now build an encoder, which assigns an integer value to each character of our alphabet. This will be a dictionary.

```
[36]: stoi = {s: i for i, s in enumerate(chars)}
stoi['<S>'] = 27
stoi['<E>'] = 28
print(stoi)
```

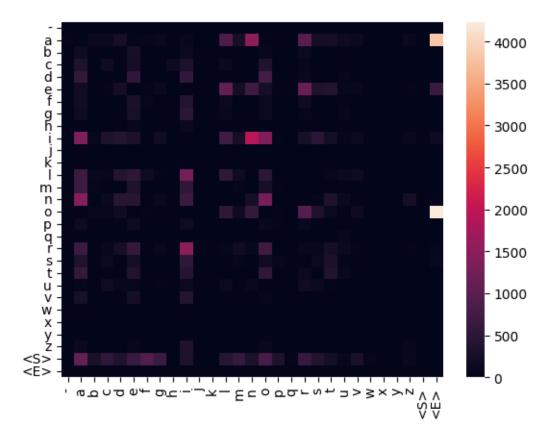
```
{'-': 0, 'a': 1, 'b': 2, 'c': 3, 'd': 4, 'e': 5, 'f': 6, 'g': 7, 'h': 8, 'i': 9, 'j': 10, 'k': 11, 'l': 12, 'm': 13, 'n': 14, 'o': 15, 'p': 16, 'q': 17, 'r': 18, 's': 19, 't': 20, 'u': 21, 'v': 22, 'w': 23, 'x': 24, 'y': 25, 'z': 26, '<S>': 27, '<E>': 28}
```

Now let's count the frequency of each bigram and put it in our tensor.

```
[37]: for w in words:
    chs = ['<S>'] + list(w) + ['<E>']
    for ch1, ch2 in zip(chs, chs[1:]):
        N[stoi[ch1], stoi[ch2]] += 1
N[28, 27] = 1 # <E> <S>
```

```
[38]: import seaborn as sns sns.heatmap(N, xticklabels=chars, yticklabels=chars)
```

[38]: <Axes: >



Now one can also build a decoder

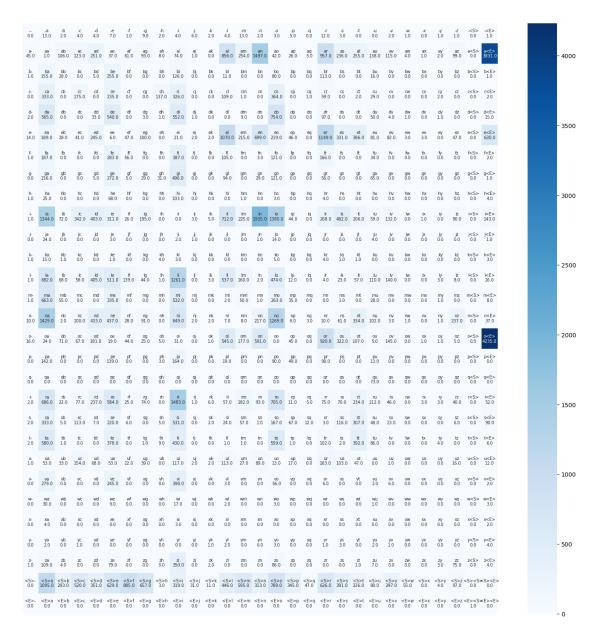
```
[39]: itos = {i: s for s, i in stoi.items()} print(itos)
```

```
{0: '-', 1: 'a', 2: 'b', 3: 'c', 4: 'd', 5: 'e', 6: 'f', 7: 'g', 8: 'h', 9: 'i', 10: 'j', 11: 'k', 12: 'l', 13: 'm', 14: 'n', 15: 'o', 16: 'p', 17: 'q', 18: 'r', 19: 's', 20: 't', 21: 'u', 22: 'v', 23: 'w', 24: 'x', 25: 'y', 26: 'z', 27: '<S>', 28: '<E>'}
```

Notice that **stoi** is associating to any character a number, so they are enumerated from 0 to 26 (the dimension of our alphabet is 29). On the other hand, **itos** is decoding a number into a character.

For a better visualization we can plot the whole matrix together with the bigrams and their frequencies

[40]: <Axes: >



How can we use counting to infer our probability? How can we reproduce the probability distribution of these numbers?

Let's start by computing the probability of the first character. First, normalize all the rows of the tensor, then sample using frequencies. It is possible, with PyTorch, to normalize all the rows of a matrix (stochastic on the row) by doing M/M.sum(...). Assume that \vec{p} is now our 27th row normalized, i.e. '<S>' + '%c' string, which represents the frequency of starting letters. Using the conditional probability known by the dataset one can start to generate words basing on bigrams, actually in a Markov chain approximation. However, the result is not properly good (is very, very bad ngl). Words must be extracted with repetition from our \vec{p} vector. Actually, an integer is

generated, not a word.

TRIVIA ChatGPT has a vocabulary of words (chunks - word pieces), not characters.

```
[41]: p = N / N.sum(axis=1, keepdims=True)
      g = torch.Generator().manual_seed(123450)
      for i in range(10):
          out = []
          ix = 27
          while True:
              pix = p[ix]
              ix = torch.multinomial(
                  pix, num_samples=1, replacement=True, generator=g).item()
              out.append(itos[ix])
              if ix == 28:
                  break
          print(''.join(out))
     epucia<E>
     o<E>
     lgomenzano<E>
     a<E>
     ginttio<E>
     s<E>
     ciniglclalirermo<E>
     feonedo<E>
     mola<E>
     ndo<E>
     What if the probability distribution was uniform?
[42]: for i in range(10):
          out = []
          ix = 27
          while True:
              pix = torch.ones(29)/29.0
              ix = torch.multinomial(
                  pix, num_samples=1, replacement=True, generator=g).item()
              out.append(itos[ix])
              if ix == 28:
                  break
          print(''.join(out))
     aaognqusx<E>
     sx<S>ukksqzwca<S><E>
     zvksvkbglkndtjxwfra<S>fotxorg<S>x<S>mytxlnvdrqordxkclczhn-ynrqjp-1<E>
     xwcsruntl-rdkfbzexahxcxoxa-ucfnoae<E>
     natlmee<S>yxjtpynrn-zsps<E>
```

```
zmpaaxp<E>
cidlwhsmmllkndpzawmdxkhnnyghb<E>
cchgmhzv<S>lf<S>sfwrwwolpb<S>-itrmv-j-lld<S>gouh<E>
mmuykixwsdddbaopvxqldjwwy<S>my-trkjwbjdoqkkxepmw<S>cjv<E>
lzyywd<S>kwu<E>
```

Words generated with uniform distribution are way worse, so just using the probability of the dataset (simple information - just counting) one can achieve a quite good result with respect to the total randomness.

How to evaluate an algorithm like this one? (just one char memory) How can we do better?

2 Trigrams - MakeMore2 (19/04/2023)

What if we wanted to guess the fourth character by knowing the first 3 ones? We should have a counting matrix N of size (in this case) $28 \cdot 28 \cdot 28 = 21952$. For some applications we would like to look at strings of 9,10 characters or even more: the situation becomes exponentially untreatable.

We must find another way to "train" our system, one that does not involve counting since the latter is not scalable to n—grams. We are going to ask a **Neural Network** to predict the (conditioned) probability distribution over all characters. Furthermore, we are going to see the most simple case of Neural Network now, but then we are going to complexify it and get incredible results.

```
[1]: # https://youtu.be/TCH_1BHY58I
# https://github.com/karpathy/makemore
```

Now we'll try to build a multilayer perceptron (MLP). Each character is going to be embedded in a 2D space. We've three vectors 30D, so 90D as total dimension (28 chars + 2). Training the network the embedding will change. We'll have a linear transformation which transpose in an intermediate layer we can see as 100D vector. Transforming this non-linearly (with a hyperbolic tangent) it will construct the derivatives (back propagation). With another linear transform we'll connect all. Exponentiating and normalizing we'll get the desired probability distribution. Hyperparameters are the a priori defined parameters. To do things in a good way one needs to know how to tune the hyperparameters.

```
# we now go to MLP (multilayer perceptron)....(using NLP (natural language_
processing))
# 'a neural probabilistic language model' (2003) chrome-extension://
pefaidnbmnnnibpcajpcglclefindmkaj/
# https://www.jmlr.org/papers/volume3/bengio03a/bengio03a.pdf
# fig 1: 4th word predicted after the three....
import random
import torch
import torch.nn.functional as F
import matplotlib.pyplot as plt
%matplotlib inline
```

```
[3]: # read in all the words random.seed(158)
```

```
words = open('data/nomi_italiani.txt', 'r').read().splitlines()
random.shuffle(words)
print(words[0:10])
print(len(words))
```

['argento', 'giovannino', 'licurga', 'elvira', 'marena', 'sirio', 'emilia', 'bisio', 'preziosa', 'perpetua']
9105

```
[4]: # build the vocabulary of characters and mapping to/from integers
    chars = sorted(list(set(''.join(words))))

stoi = {s: i+1 for i, s in enumerate(chars)}
    stoi['.'] = 0
    itos = {i: s for s, i in stoi.items()}
    print(itos)
    print(stoi)
```

```
{1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10: 'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19: 'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0: '.'}
{'-': 1, 'a': 2, 'b': 3, 'c': 4, 'd': 5, 'e': 6, 'f': 7, 'g': 8, 'h': 9, 'i': 10, 'j': 11, 'k': 12, 'l': 13, 'm': 14, 'n': 15, 'o': 16, 'p': 17, 'q': 18, 'r': 19, 's': 20, 't': 21, 'u': 22, 'v': 23, 'w': 24, 'x': 25, 'y': 26, 'z': 27, '.': 0}
```

Previous example - Markov chain, so the block size was 1. Updating the contest means shift over the string and add the last character. X contains the samples (what I'm looking at). Each row of X is a trigram. Y contains the correct answers.

Y = torch.tensor(Y)

```
argento
... ---> a
..a ---> r
.ar ---> g
arg ---> e
rge ---> n
gen ---> t
ent ---> o
nto ---> .
giovannino
... ---> g
..g ---> i
.gi ---> o
gio ---> v
iov ---> a
ova ---> n
van ---> n
ann ---> i
nni ---> n
nin ---> o
ino ---> .
licurga
... ---> 1
..1 ---> i
.li ---> c
lic ---> u
icu ---> r
cur ---> g
urg ---> a
rga ---> .
elvira
... ---> e
..e ---> 1
.el ---> v
elv ---> i
lvi ---> r
vir ---> a
ira ---> .
marena
... ---> m
..m ---> a
.ma ---> r
mar ---> e
are ---> n
ren ---> a
```

ena ---> .

If I present to my system $0 = \cdot$ I expect to find 2 = a, and so on.

```
[6]: print(X) print(Y)
```

```
tensor([[ 0,
             Ο,
                 0],
        [ 0,
                 2],
             Ο,
        [ 0,
             2, 19],
        [ 2, 19,
                 8],
        [19,
             8,
                 6],
        [8, 6, 15],
        [6, 15, 21],
        [15, 21, 16],
        [0, 0, 0],
        [ 0,
             0, 8],
        [0, 8, 10],
        [8, 10, 16],
        [10, 16, 23],
        [16, 23, 2],
        [23, 2, 15],
        [2, 15, 15],
        [15, 15, 10],
        [15, 10, 15],
        [10, 15, 16],
        [0, 0, 0],
        [0, 0, 13],
        [ 0, 13, 10],
        [13, 10, 4],
        [10,
             4, 22],
        [4, 22, 19],
        [22, 19, 8],
             8,
        [19,
                 2],
        [ 0,
             Ο,
                 0],
             0, 6],
        [ 0,
        [0, 6, 13],
        [6, 13, 23],
        [13, 23, 10],
        [23, 10, 19],
        [10, 19, 2],
        [0, 0, 0],
        [ 0, 0, 14],
        [0, 14, 2],
             2, 19],
        [14,
        [2, 19, 6],
        [19, 6, 15],
        [ 6, 15,
                 2]])
```

```
tensor([ 2, 19, 8, 6, 15, 21, 16, 0, 8, 10, 16, 23, 2, 15, 15, 10, 15, 16, 0, 13, 10, 4, 22, 19, 8, 2, 0, 6, 13, 23, 10, 19, 2, 0, 14, 2, 19, 6, 15, 2, 0])
```

```
[7]: print(X.shape, X.dtype, Y.shape, Y.dtype)
```

```
torch.Size([41, 3]) torch.int64 torch.Size([41]) torch.int64
```

Now we want to predict the next character starting from trigrams. We're going to take a 2D embedding of the 28 characters. There are many pre-calculated embeddings in the world.

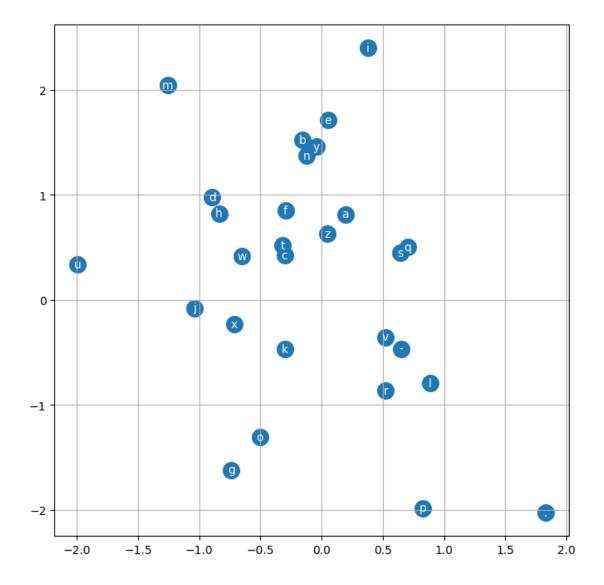
We can generate a random (normal) matrix 28x2. In deep data analysis (what we're doing) the world is going really fast. There is a lot of material, 99% of which are bullshits.

```
[8]: # https://pytorch.org/docs/stable/generated/torch.randn.html
C = torch.randn((28, 2))
```

```
[9]: print(C[5])
print(C.shape)
```

```
tensor([-0.8942, 0.9758])
torch.Size([28, 2])
```

Here is a plot of the embedding. Letters are random, after the training this picture is going to change. From this plot we can learn how characters are related each other.



Another way to embed characters is the **one-hot encoding** discussed last lecture. We can see this embedding as the first layer of our network, even if there's no linearity in it. In fact, they're completely equivalent. One can also see all the embeddings.

```
[0.5246, -0.8622],
[-0.7371, -1.6184],
[ 0.0533, 1.7143],
[-0.1215, 1.3717],
[-0.3184, 0.5178],
[-0.5059, -1.3046],
[1.8311, -2.0278],
[-0.7371, -1.6184],
[ 0.3765, 2.4004],
[-0.5059, -1.3046],
[0.5218, -0.3549],
[0.1954, 0.8158],
[-0.1215,
          1.3717],
[-0.1215,
          1.3717],
[ 0.3765,
          2.4004],
[-0.1215, 1.3717],
[-0.5059, -1.3046],
[1.8311, -2.0278],
[0.8875, -0.7907],
[0.3765, 2.4004],
[-0.3022, 0.4220],
[-1.9923,
          0.3384],
[0.5246, -0.8622],
[-0.7371, -1.6184],
[0.1954, 0.8158],
[1.8311, -2.0278],
[ 0.0533, 1.7143],
[0.8875, -0.7907],
[0.5218, -0.3549],
[ 0.3765, 2.4004],
[0.5246, -0.8622],
[0.1954, 0.8158],
[1.8311, -2.0278],
[-1.2565, 2.0464],
[0.1954, 0.8158],
[0.5246, -0.8622],
[ 0.0533, 1.7143],
[-0.1215,
          1.3717],
[0.1954, 0.8158],
[ 1.8311, -2.0278]])
```

How to embed the 41 trigrams we have?

```
[12]: emb = C[X]
print(emb.shape)
```

torch.Size([41, 3, 2])

Moreover, we can differentiate C! Input has dimension 6 = 3 * 2

```
[13]: |# construct the Layer.... x.W+ b ... so the input has dimension 6=3*2 for (say)_{\square}
      →100 neurons...
     W1 = torch.randn(6, 100)
     b1 = torch.randn(100)
     We want to concatenate tensors. And maybe unbind them.
[14]: # https://putorch.org/docs/stable/torch.html search for concatenate...
     print(torch.cat([emb[:, 0, :], emb[:, 1, :], emb[:, 2, :]], 1)[1])
     print(emb[1])
     tensor([ 1.8311, -2.0278, 1.8311, -2.0278, 0.1954, 0.8158])
     tensor([[ 1.8311, -2.0278],
             [1.8311, -2.0278],
             [ 0.1954, 0.8158]])
[15]: # we want a code for general n-grams.....
      # use 'unbind' https://pytorch.org/docs/stable/generated/torch.unbind.
      →html#torch.unbind
     len(torch.unbind(emb, 1))
[15]: 3
[16]: # and this work fore any context length......
     torch.cat(torch.unbind(emb, 1), 1)
[16]: tensor([[ 1.8311, -2.0278, 1.8311, -2.0278, 1.8311, -2.0278],
             [1.8311, -2.0278, 1.8311, -2.0278, 0.1954, 0.8158],
             [1.8311, -2.0278, 0.1954, 0.8158, 0.5246, -0.8622],
             [0.1954, 0.8158, 0.5246, -0.8622, -0.7371, -1.6184],
              [0.5246, -0.8622, -0.7371, -1.6184, 0.0533, 1.7143],
             [-0.7371, -1.6184, 0.0533, 1.7143, -0.1215, 1.3717],
              [0.0533, 1.7143, -0.1215, 1.3717, -0.3184, 0.5178],
              [-0.1215, 1.3717, -0.3184, 0.5178, -0.5059, -1.3046],
              [1.8311, -2.0278, 1.8311, -2.0278, 1.8311, -2.0278],
              [1.8311, -2.0278, 1.8311, -2.0278, -0.7371, -1.6184],
             [1.8311, -2.0278, -0.7371, -1.6184, 0.3765,
                                                            2.4004],
             [-0.7371, -1.6184, 0.3765, 2.4004, -0.5059, -1.3046],
             [0.3765, 2.4004, -0.5059, -1.3046, 0.5218, -0.3549],
             [-0.5059, -1.3046, 0.5218, -0.3549, 0.1954, 0.8158],
              [0.5218, -0.3549, 0.1954, 0.8158, -0.1215, 1.3717],
              [0.1954, 0.8158, -0.1215, 1.3717, -0.1215, 1.3717],
             [-0.1215, 1.3717, -0.1215, 1.3717, 0.3765, 2.4004],
             [-0.1215, 1.3717, 0.3765, 2.4004, -0.1215, 1.3717],
             [0.3765, 2.4004, -0.1215, 1.3717, -0.5059, -1.3046],
```

```
[1.8311, -2.0278, 1.8311, -2.0278, 1.8311, -2.0278],
[1.8311, -2.0278, 1.8311, -2.0278, 0.8875, -0.7907],
[1.8311, -2.0278, 0.8875, -0.7907, 0.3765,
[0.8875, -0.7907, 0.3765, 2.4004, -0.3022, 0.4220],
[0.3765, 2.4004, -0.3022, 0.4220, -1.9923, 0.3384],
[-0.3022, 0.4220, -1.9923, 0.3384, 0.5246, -0.8622],
[-1.9923, 0.3384, 0.5246, -0.8622, -0.7371, -1.6184],
[0.5246, -0.8622, -0.7371, -1.6184, 0.1954, 0.8158],
[1.8311, -2.0278, 1.8311, -2.0278, 1.8311, -2.0278],
[1.8311, -2.0278, 1.8311, -2.0278, 0.0533, 1.7143],
[1.8311, -2.0278, 0.0533, 1.7143, 0.8875, -0.7907],
[0.0533, 1.7143, 0.8875, -0.7907, 0.5218, -0.3549],
[0.8875, -0.7907, 0.5218, -0.3549, 0.3765, 2.4004],
[0.5218, -0.3549, 0.3765, 2.4004, 0.5246, -0.8622],
[0.3765, 2.4004, 0.5246, -0.8622, 0.1954, 0.8158],
[1.8311, -2.0278, 1.8311, -2.0278, 1.8311, -2.0278],
[1.8311, -2.0278, 1.8311, -2.0278, -1.2565, 2.0464],
[1.8311, -2.0278, -1.2565, 2.0464, 0.1954, 0.8158],
[-1.2565, 2.0464, 0.1954, 0.8158, 0.5246, -0.8622],
[0.1954, 0.8158, 0.5246, -0.8622, 0.0533, 1.7143],
[0.5246, -0.8622, 0.0533, 1.7143, -0.1215,
                                            1.3717],
[ 0.0533, 1.7143, -0.1215, 1.3717, 0.1954,
                                            0.8158]])
```

Let's see a better way.

```
[17]: | # https://pytorch.org/docs/stable/generated/torch.Tensor.view.html
      # https://pytorch.org/docs/stable/generated/torch.Tensor.stride.html
     a = torch.arange(18)
     print(a)
     print(a.shape)
     print(a.view(9, 2))
     print(a.view(2, 9))
     print(a.untyped_storage()) # very efficient in torch
     tensor([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17])
     torch.Size([18])
     tensor([[ 0, 1],
             [ 2,
                   3],
             [4,
                  5],
             [6,
                  7],
             [8, 9],
             [10, 11],
             [12, 13],
             [14, 15],
             [16, 17]])
     tensor([[ 0, 1, 2, 3, 4, 5, 6, 7, 8],
```

0

```
[torch.storage.UntypedStorage(device=cpu) of size 144]
[18]: print((emb.view(41, 6) == torch.cat(torch.unbind(emb, 1), 1)).all())
     tensor(True)
     So we can use
[19]: h = emb.view(41, 6) @ W1 + b1
[20]: print(h)
      print(h.shape)
      # -1 means 'infer' the dimension from the other dimensions (sort-of auto)
      print(emb.view(-1, 6) @ W1 + b1)
     tensor([[ 6.4608, 7.7166, 0.7321, ..., -1.6921, -6.6402, 2.9859],
             [8.0898, 11.0348, 0.1188, ..., -1.8758, -7.0852, -5.2748],
             [2.7815, 2.2440, -0.1863, ..., 1.8122, -4.1921, 4.2734],
             [3.1919, 3.7343, -0.9590, ..., -3.1006, -3.4712, -4.0174],
             [1.8786, -0.4733, -0.9985, ..., -0.6313, -1.5268, 0.6606],
             [-0.1450, -3.9838, -1.9367, ..., -2.7371, -0.4445, 2.2965]])
     torch.Size([41, 100])
     tensor([[ 6.4608, 7.7166, 0.7321, ..., -1.6921, -6.6402, 2.9859],
             [8.0898, 11.0348, 0.1188, ..., -1.8758, -7.0852, -5.2748],
             [2.7815, 2.2440, -0.1863, ..., 1.8122, -4.1921, 4.2734],
             [3.1919, 3.7343, -0.9590, ..., -3.1006, -3.4712, -4.0174],
             [1.8786, -0.4733, -0.9985, ..., -0.6313, -1.5268, 0.6606],
             [-0.1450, -3.9838, -1.9367, ..., -2.7371, -0.4445, 2.2965]])
     Embed (glue) + apply matrix + add b1. Now apply a non-linear transformation like hyperbolic
     tangent.
[21]: # first layer
      # https://pytorch.org/docs/stable/generated/torch.tanh.html
      h = torch.tanh(emb.view(-1, 6) @ W1 + b1)
[22]: print(h)
     tensor([[ 1.0000, 1.0000, 0.6244, ..., -0.9344, -1.0000, 0.9949],
             [1.0000, 1.0000, 0.1182, ..., -0.9541, -1.0000, -0.9999],
             [0.9924, 0.9778, -0.1841, ..., 0.9481, -0.9995, 0.9996],
             [0.9966, 0.9989, -0.7438, ..., -0.9960, -0.9981, -0.9994],
             [0.9544, -0.4408, -0.7610, ..., -0.5589, -0.9099, 0.5788],
```

```
[-0.1440, -0.9993, -0.9593, ..., -0.9916, -0.4174, 0.9800]])
```

Second layer must take in 100D vector and give out a 28D vector.

```
[23]: # second layer

W2 = torch.randn((100, 28))
b2 = torch.randn(28)
```

h is coming out from the first layer, then we feed with h the layer here.

```
[24]: logits = h @ W2 + b2
print(logits.shape)
```

torch.Size([41, 28])

Logits means log of the counting...

```
[25]: counts = logits.exp()
```

Normalize to interpret this as a measure, i.e. a probability distribution coming out from the network when fed with three chars.

```
[26]: prob = counts / counts.sum(1, keepdims=True)
```

```
[27]: print(prob[0])
    print(prob[0].sum())
    print(prob[0, 1])
    print(prob[[0, 1], [2, 5]])
```

```
tensor([1.6784e-06, 5.0463e-11, 2.0293e-07, 6.1992e-10, 4.3715e-08, 3.1182e-10, 1.3514e-09, 1.1729e-08, 9.2797e-03, 8.6295e-20, 1.6910e-08, 9.0078e-03, 1.5882e-05, 1.6785e-01, 8.2946e-08, 3.9586e-09, 8.1243e-07, 9.6449e-06, 1.5448e-09, 2.6844e-05, 7.6797e-05, 4.3386e-12, 1.0397e-05, 7.2565e-14, 4.7232e-07, 2.5526e-11, 8.1371e-01, 3.5886e-06])
tensor(1.0000)
tensor(5.0463e-11)
tensor([2.0293e-07, 7.1848e-08])
```

Model is initialized with random weights, so it's making mistakes.

```
[28]: print(Y)
print(torch.arange(41))
print(prob[torch.arange(41), Y])
```

```
tensor([ 2, 19, 8, 6, 15, 21, 16, 0, 8, 10, 16, 23, 2, 15, 15, 10, 15, 16, 0, 13, 10, 4, 22, 19, 8, 2, 0, 6, 13, 23, 10, 19, 2, 0, 14, 2, 19, 6, 15, 2, 0])
tensor([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40])
```

```
tensor([2.0293e-07, 5.6065e-04, 4.2035e-08, 1.4121e-05, 2.6402e-15, 9.9518e-01, 7.3084e-10, 1.5376e-12, 9.2797e-03, 5.9816e-11, 9.9847e-01, 1.3855e-08, 1.3866e-08, 1.7133e-08, 3.2253e-02, 6.1097e-13, 8.3580e-01, 2.7769e-13, 1.7553e-11, 1.6785e-01, 8.8264e-06, 3.3552e-03, 1.9002e-13, 2.4211e-02, 4.5583e-08, 1.2915e-04, 5.1726e-03, 1.3514e-09, 2.4023e-08, 1.9838e-09, 2.0282e-06, 1.6444e-14, 1.9853e-07, 1.8433e-05, 8.2946e-08, 2.5932e-08, 4.0924e-09, 1.1131e-10, 2.9585e-07, 4.2625e-04, 2.4850e-10])
```

We, of course, want the model to predict the right answer. Probability going to one implies loss going to zero.

```
[29]: loss = - prob[torch.arange(41), Y].log().mean()
print(loss) # very bad of course.....
```

tensor(15.4615)

Let's put things together. Parameters will contain all the objects we're going to change. Why is the embedding dimension 2? We'll try with 10... tanh 0 = 0 and that will be important.

```
[30]: g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 2), generator=g)
W1 = torch.randn((6, 100), generator=g)
b1 = torch.randn(100, generator=g)
W2 = torch.randn((100, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

How many parameters are fixable?

```
[31]: print(sum(p.nelement() for p in parameters)) # number of parameter in total...
```

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For each sample I compute the $\log \rightarrow \text{high loss}$.

```
[32]: emb = C[X] # torch.Size([41, 3, 2])
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
logits = h @ W2 + b2 # (41,27)
counts = logits.exp()
prob = counts/counts.sum(1, keepdims=True)
loss = -prob[torch.arange(41), Y].log().mean()
print(loss)
```

tensor(17.2342)

Very efficient and can compute the exponential of big terms

```
[33]: print(F.cross_entropy(logits, Y))
```

tensor(17.2342)

Now the loss has to be minimized.

```
[34]: # so.... https://pytorch.org/docs/stable/generated/torch.nn.functional.

cross_entropy.html

emb = C[X] # torch.Size([41, 3, 2])

h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)

logits = h @ W2 + b2 # (41,27)

loss = F.cross_entropy(logits, Y)

print(loss)
```

tensor(17.2342)

We'll use the cross_entropy function because the exponentiation of just -500 will result in 0

```
[35]: # two very good reasons to use 'cross_entropy': more efficient (no tensor) and substract the maximum to avoid nan...discuss....

logits = torch.tensor([-5, -3, 0, 10]) # -100
counts = logits.exp()
prob = counts/counts.sum()
print(counts)
print(prob)
```

```
tensor([6.7379e-03, 4.9787e-02, 1.0000e+00, 2.2026e+04])
tensor([3.0589e-07, 2.2602e-06, 4.5398e-05, 9.9995e-01])
```

Put the gradient to zero, then compute the backward derivative and update all parameters in order to decrease the loss. 41 trigrams are going in layers, then calculate the loss.

Backward pass means compute the derivative of the loss for each parameter. It's a very complex stuff. We're not happy with back propagation but, by now, it's the only thing which works.

Learning rate -0.1 (negative direction). This is a magic number.

```
[36]: for p in parameters:
    p.requires_grad = True

for _ in range(1000):
    # now we learn...forward bass
    emb = C[X] # torch.Size([41, 3, 2])
    h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
    logits = h @ W2 + b2 # (41,27)
    loss = F.cross_entropy(logits, Y)
    # backward pass
    for p in parameters:
        p.grad = None
    loss.backward()
    # update
    for p in parameters:
        p.data += -0.1*p.grad
```

Low loss means overfitting, then the model is going to give me one of the sample I provided. This is not useful at all.

```
[37]: # sampling from the model....
      g = torch.Generator().manual_seed(12345678+10)
      for _ in range(20):
          out = []
          context = [0]*block_size
          while True:
              emb = C[torch.tensor([context])]
              h = torch.tanh(emb.view(1, -1) @ W1 + b1)
              logits = h @ W2 + b2
              probs = F.softmax(logits, dim=1)
              ix = torch.multinomial(probs, num_samples=1, generator=g).item()
              context = context[1:]+[ix]
              out.append(ix)
              if ix == 0:
                  break
          print(''.join(itos[i] for i in out))
```

```
elvira.
marena.
giovannino.
giovannino.
giovannino.
giovannino.
elvira.
marena.
argento.
argento.
argento.
elvira.
argento.
licurga.
licurga.
marena.
giovannino.
marena.
giovannino.
```

licurga.

What is happening? Our model has gone in **overfitting**: it is spitting out the same names we put in, since we trained it only on those small samples (we've given it only 5 samples out of 7000+...)! So the loss is low enough now to sample, but of course our model is still useless. How can we fix this?

If we try to train the system with the whole data set (so that all the 41's are changed to the dimension of the dataset, that's the only change in the code) we fix the overfitting problem, but the algorithm will of course slow down in order to make the same calculations for such high dimensionality.

To fix this problem, we need to use **minibatches**.

```
[38]: for p in parameters:
          p.requires_grad = True
      for _ in range(1000):
          # now we learn...forward bass
          emb = C[X] # torch.Size([41, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
          logits = h @ W2 + b2 # (41,27)
          loss = F.cross entropy(logits, Y)
          # print(loss.item())
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          for p in parameters:
              p.data += -0.1*p.grad
      print(loss.item())
```

0.19916315376758575

Logits are the neurons coming out from the last layer. They'll be transformed into probability.

```
[39]: print(logits.max(1))
     print(Y)
     torch.return_types.max(
     values=tensor([12.1724, 14.1847, 15.8096, 16.5460, 12.5090, 14.7062, 15.2590,
     15.4024,
             12.1724, 19.3660, 15.9274, 12.4720, 13.9841, 17.1356, 14.9285, 13.9812,
             13.8305, 15.1462, 14.5532, 12.1724, 15.2042, 17.6397, 14.6976, 14.7785,
             22.7934, 18.4190, 15.3254, 12.1724, 18.8153, 16.9008, 17.9443, 18.5473,
             15.9427, 15.7163, 12.1724, 19.9722, 15.4614, 16.7053, 16.1372, 18.4218,
             15.9050], grad_fn=<MaxBackward0>),
     indices=tensor([13, 19, 8, 6, 15, 21, 16, 0, 13, 10, 16, 23, 2, 15, 15, 10,
     15, 16,
                         4, 22, 19, 8, 2, 0, 13, 13, 23, 10, 19, 2, 0, 13, 2,
              0, 13, 10,
             19, 6, 15,
                         2, 0]))
     tensor([ 2, 19, 8,
                         6, 15, 21, 16, 0, 8, 10, 16, 23, 2, 15, 15, 10, 15, 16,
                         4, 22, 19, 8, 2, 0, 6, 13, 23, 10, 19, 2, 0, 14,
              0, 13, 10,
             19, 6, 15, 2, 0])
```

Taking all words we get a very big example dataset.

```
[40]: block size = 3 # context length: how many characters do we take to predict the
       ⇔next one ... change it !!
      X, Y = [], [] # input & label
      for w in words:
        # print(w)
          context = [0]*block_size
          for ch in w + '.':
              ix = stoi[ch]
              X.append(context)
             Y.append(ix)
            # print(''.join(itos[i] for i in context), '--->', itos[ix])
              context = context[1:]+[ix] # shift: crop and append
      X = torch.tensor(X)
      Y = torch.tensor(Y)
[41]: print(X.shape, Y.shape)
     torch.Size([73643, 3]) torch.Size([73643])
     Again, a hidden layer of 100 neurons.
[42]: # exactly as before....
      g = torch.Generator().manual_seed(123456780) # for reproducibility
      C = torch.randn((28, 2), generator=g)
      W1 = torch.randn((6, 100), generator=g)
      b1 = torch.randn(100, generator=g)
      W2 = torch.randn((100, 28), generator=g)
      b2 = torch.randn(28, generator=g)
      parameters = [C, W1, b1, W2, b2]
[43]: for p in parameters:
          p.requires_grad = True
      for _ in range(10):
          # now we learn...forward bass -- = 73643
          emb = C[X] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Y)
          print(loss.item())
          # backward pass
          for p in parameters:
             p.grad = None
          loss.backward()
          # update
          for p in parameters:
              p.data += -0.1*p.grad
```

```
17.754497528076172
     15.824398040771484
     14.187442779541016
     13.052314758300781
     12.071907043457031
     11.26384162902832
     10.603142738342285
     10.075034141540527
     9.627379417419434
     9.222493171691895
     See how it's slowing down... Every time we give all samples to it. Let's subdivide the dataset in
     minibatches.
[44]: \# try ix=torch.randint(0,X.shape[0],(10,2)) and explain
      ix = torch.randint(0, X.shape[0], (10,))
      # https://pytorch.org/docs/stable/generated/torch.randint.html
      print(ix)
     tensor([52217, 65447, 62037, 69471, 38026, 61119, 52117, 41366, 14774, 55884])
     Weird things happen with PyTorch...
[45]: ix = torch.randint(0, X.shape[0], (10, 1))
      print(ix)
     tensor([[36913],
              [16575],
              [27230],
              [73431],
              [17549],
              [39717],
              [27122],
              [7573],
              [ 1706],
              [63502]])
[46]: for _ in range(10):
          # mini batch construct of size ...
          ix = torch.randint(0, X.shape[0], (32,))
          # now we learn...forward bass -- = 73643
          emb = C[X[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Y[ix])
          print(loss.item())
          # backward pass
          for p in parameters:
              p.grad = None
```

```
loss.backward()
# update
for p in parameters:
    p.data += -0.1*p.grad
print(loss.item())
```

```
9.180441856384277
```

- 8.426222801208496
- 7.68398380279541
- 10.587089538574219
- 6.133955955505371
- 7.524043560028076
- 6 006447070007607
- 6.096117973327637
- 6.866352081298828
- 7.340187072753906
- 5.654036998748779
- 5.654036998748779

Learning rate specifies how I move through gradient. Using 10, the system got completely lost (too big jumps).

```
[47]: # how we define the 'learning rate' ? p.data += -0.1*p.grad # play with learning rate from .01 to 100.... and discuss
```

```
[48]: for _ in range(1000):
          # mini batch construct
          ix = torch.randint(0, X.shape[0], (100,))
          # now we learn...forward bass -- = 73643
          emb = C[X[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross entropy(logits, Y[ix])
          # print(loss.item())
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          for p in parameters:
              p.data += -.1*p.grad
      print(loss.item())
```

2.3619143962860107

```
[49]: lre = torch.linspace(-3, 0, 1000)
lrs = 10**lre # from 10**-3 to 10**0 = 1. The exponents are linearly
distributed, not the values
print(lrs.shape)
```

torch.Size([1000])

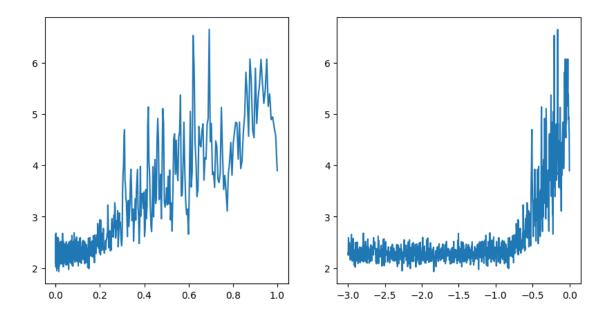
```
[50]: for p in parameters:
          p.requires_grad = True
      lri = []
      lriex = []
      lossi = []
      for i in range(1000):
          # mini batch construct
          ix = torch.randint(0, X.shape[0], (100,))
          # now we learn...forward bass -- = 73643
          emb = C[X[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Y[ix])
          # backward pass
          for p in parameters:
             p.grad = None
          loss.backward()
          # update
          lr = lrs[i]
          # lr= .01
          for p in parameters:
              p.data += -lr*p.grad
      # track stats
          lri.append(lr) # learning rate
          lriex.append(lre[i]) # exponent
          lossi.append(loss.item()) # loss function
      print(loss.item())
```

3.893927574157715

Plotting the loss function we notice that it's growing... not good.

```
[51]: fig, ax = plt.subplots(1, 2, figsize=(10, 5))
ax[0].plot(lri, lossi)
ax[1].plot(lriex, lossi)
```

[51]: [<matplotlib.lines.Line2D at 0x7fa576c3c6a0>]



What is happening to the loss? There are some values of the learning rate which do better for our loss function than others. Also, it's very much fluctuating: there is a brilliant solution for this problem which we will see later on.

Usually, the convention with the training data is to have it split into 80% to train, a 10% to validate the hyperparameters and then a final 10% to keep there and use only once to see if the Neural Network is actually doing good.

How to validate that the network is doing something good? It may seem good while being completely wrong. We should have a test set of data to use when the hyperparameters are fixed.

```
[52]: emb = C[X] # torch.Size([41, 3, 2])
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (41,100)
logits = h @ W2 + b2 # (41,27)
loss = F.cross_entropy(logits, Y)
print(loss)
```

tensor(4.3914, grad_fn=<NllLossBackward0>)

Typically, data are divided into 80-10-10 part (test/tune/validation) This function shuffles the words and builds the three wanted datasets.

First let's define the function build dataset.

```
[53]: # be careful with the test eugene....

def build_dataset(words):
    block_size = 3 # context length: how many characters do we take to predict
    the next one ... change it !!
    X, Y = [], [] # input & label
```

```
for w in words:
              context = [0]*block_size
              for ch in w + '.':
                  ix = stoi[ch]
                  X.append(context)
                  Y.append(ix)
            # print(''.join(itos[i] for i in context), '--->', itos[ix])
                  context = context[1:]+[ix] # shift: crop and append
          X = torch.tensor(X)
          Y = torch.tensor(Y)
          print(X.shape, Y.shape)
          return X, Y
[54]: import random
      random.seed(42)
     random.shuffle(words)
     n1 = int(0.8*len(words))
     n2 = int(0.9*len(words))
      Xtr, Ytr = build_dataset(words[:n1]) # train
      Xdev, Ydev = build_dataset(words[n1:n2]) # tune hyperparameters
      Xte, Yte = build_dataset(words[n2:]) # validate
     torch.Size([58867, 3]) torch.Size([58867])
     torch.Size([7404, 3]) torch.Size([7404])
     torch.Size([7372, 3]) torch.Size([7372])
[55]: # and we do it again with the new datasets......
     print(Xtr.shape, Ytr.shape)
      # exactly as before....
      g = torch.Generator().manual_seed(123456780) # for reproducibility
      C = torch.randn((28, 2), generator=g)
      W1 = torch.randn((6, 100), generator=g)
      b1 = torch.randn(100, generator=g)
      W2 = torch.randn((100, 28), generator=g)
      b2 = torch.randn(28, generator=g)
      parameters = [C, W1, b1, W2, b2]
     torch.Size([58867, 3]) torch.Size([58867])
[56]: for p in parameters:
          p.requires_grad = True
     lre = torch.linspace(-3, 0, 1000)
```

```
lrs = 10**lre
```

```
[57]: # now we train only on Xtr
      lri = []
      lriex = []
      lossi = []
      for i in range(10000):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (40,))
          # now we learn...forward bass -- = 73643
          emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
          logits = h @ W2 + b2 # (--,27)
         loss = F.cross_entropy(logits, Ytr[ix])
         # print(i,loss.item())
         # backward pass
         for p in parameters:
             p.grad = None
         loss.backward()
          # update
          # lr=lrs[i]
          lr = .1
          for p in parameters:
              p.data += -lr*p.grad
      print(loss.item())
      # track stats
          lri.append(lr)
           lriex.append(lre[i])
           lossi.append(loss.item())
```

1.8703502416610718

Now evaluate on the validation test (and also on the test).

```
[58]: # now we evaluate on Xdev
emb = C[Xdev]
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ydev)
print(loss.item())
```

2.177561044692993

```
[59]: # now we evaluate on Xtr.... we are NOT overfitting
emb = C[Xtr]
h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ytr)
print(loss.item())
```

2.1584300994873047

So now we know that our model has a low loss **and** we are not overfitting, my system is able to reproduce not only the data I show it in the training but also other data it has never seen before. Nice...

Now we can change the hyperparameters: this is a very simple case, so it's not going to change much, but still we do it for pedagogical reasons. Even in such a simple model, changing the hyperparameters makes our parameters go from ~ 3000 to ~ 10000 . Let's take a look at what happens now to the loss...

```
[60]: g = torch.Generator().manual_seed(123456780) # for reproducibility
C = torch.randn((28, 2), generator=g)
W1 = torch.randn((6, 300), generator=g)
b1 = torch.randn(300, generator=g)
W2 = torch.randn((300, 28), generator=g)
b2 = torch.randn(28, generator=g)
parameters = [C, W1, b1, W2, b2]
```

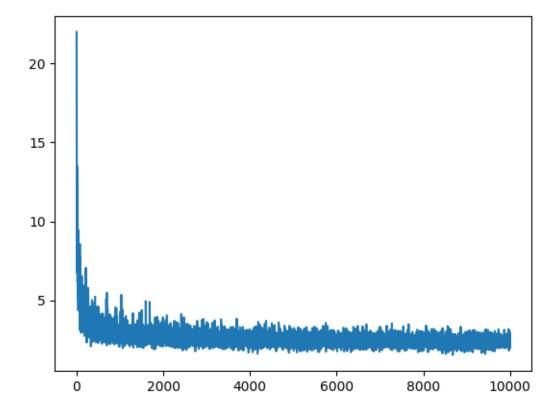
```
[61]: # number of parameter in total... before 3584
print(sum(p.nelement() for p in parameters))
```

```
[62]: lri = []
      lriex = []
      lossi = []
      stepi = []
      for p in parameters:
          p.requires_grad = True
      for i in range(10000):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (40,))
          # now we learn...forward bass -- = 73643
          emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 6) @ W1 + b1) # (--, 100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Ytr[ix])
          # backward pass
          for p in parameters:
```

```
p.grad = None
loss.backward()
# update
# lr=lrs[i]
lr = .1
for p in parameters:
    p.data += -lr*p.grad
stepi.append(i)
lossi.append(loss.item())
```

```
[63]: plt.plot(stepi, lossi)
```

[63]: [<matplotlib.lines.Line2D at 0x7fa570668790>]



We can see how the loss starts very high and then decreases very much with training, but still it is fluctuating: this shouldn't be very surprising, since even with training our model is based on random number and processes, so fluctuations are guaranteed. But as we said before, there is a nice way to reduce these fluctuations, which is called **batch normalization**.

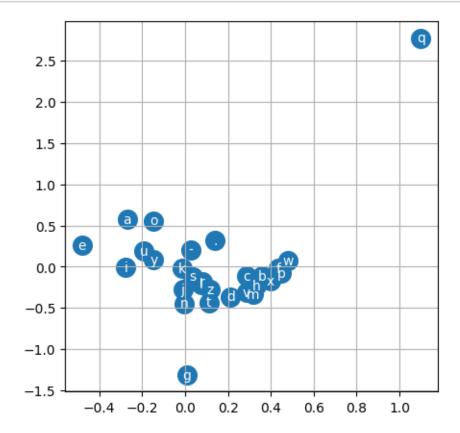
This is a transformation we make our data undergo in order to have a "gaussian" activity of our neurons. In this way we avoid 2 things: 1. we avoid our neurons' activity being too high, i.e. we do not want values which would mostly fall into the plateaus of our hyperbolic tangent and thus cause the "freezing" of our neurons, i.e. their inability to learn, since their output would always be +1 or

-1 and no in between; 2. we avoid large fluctuations in our data, since gaussian data fluctuations scale as we know with $\frac{1}{\sqrt{N}}$ where N is the number of samples. Such transformation is (roughly speaking) just gaussian normalization of data (actually there are more complex operations going on in the batch-normalization functions of libraries like PyTorch, and we actually do not know much about the precise statistical effectiveness of such processes, we use them as kind of "black box"), before feeding them to the linear layer, i.e. data are normalized before the hyperbolic tangent application. This means that we take the sample mean of our data $\bar{x} = \sum_i^N \frac{x_i}{N}$, compute the sample standard deviation σ_s and then transform each point x of our set by

$$x \longrightarrow \frac{x - \bar{x}}{\sigma_s}$$

We will use batch normalization later on.

Now we can visualize the result of the embedding. The letters are clustered, e.g. vowels are clustered.

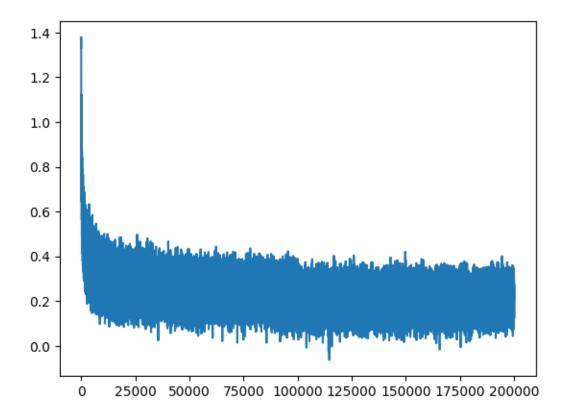


Now increase to 10 the embedding dimension...

```
[65]: g = torch.Generator().manual_seed(123456780) # for reproducibility
      C = torch.randn((28, 10), generator=g)
      W1 = torch.randn((30, 200), generator=g)
      b1 = torch.randn(200, generator=g)
      W2 = torch.randn((200, 28), generator=g)
      b2 = torch.randn(28, generator=g)
      parameters = [C, W1, b1, W2, b2]
[66]: print(sum(p.nelement() for p in parameters)) # number of parameter in total
     12108
[67]: | lri = []
      lriex = []
      lossi = []
      stepi = []
      for p in parameters:
          p.requires_grad = True
     Now change the learning rate...
[68]: for i in range(200000):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (40,))
          # now we learn...forward bass -- = 73643
          emb = C[Xtr[ix]] # torch.Size([--, 3, 2])
          h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100)
          logits = h @ W2 + b2 # (--,27)
          loss = F.cross_entropy(logits, Ytr[ix])
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = .1 if i < 100000 else 0.01
          for p in parameters:
              p.data += -lr*p.grad
          stepi.append(i)
          lossi.append(loss.log10().item()) # note the log10 !!
```

[69]: plt.plot(stepi, lossi)

[69]: [<matplotlib.lines.Line2D at 0x7fa64868a470>]



We're doing well and not overfitting.

```
[70]: emb = C[Xtr]
h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100) 30 not 6 !
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ytr)
print(loss.item())
```

1.64104425907135

```
[71]: emb = C[Xdev]
h = torch.tanh(emb.view(-1, 30) @ W1 + b1) # (--,100)
logits = h @ W2 + b2 # (--,27)
loss = F.cross_entropy(logits, Ydev)
print(loss.item())
```

1.8407597541809082

Once trained the model we can sample from it. **NOTE**: there are many (many many) hyperparameters to play with, like the number of layer, numbers of neurons from layers, embedding dimensions, dimension of the batches, learning rate....

We can now see words that are not in the dataset.

```
for _ in range(30):
    out = []
    context = [0]*block_size
    while True:
        emb = C[torch.tensor([context])]
        h = torch.tanh(emb.view(1, -1) @ W1 + b1)
        logits = h @ W2 + b2
        probs = F.softmax(logits, dim=1)
        ix = torch.multinomial(probs, num_samples=1, generator=g).item()
        context = context[1:]+[ix]
        out.append(ix)
        if ix == 0:
            break

        print(''.join(itos[i] for i in out))
```

```
ade.
galdina.
crezzeliseo.
ore.
poltienni.
diverda.
nardana.
giovidio.
corseleolomerita.
guerradarda.
bena.
carino.
chrichelea.
pinimpedermena.
vita.
rola.
adorita.
pieris.
gentamatardo.
mario.
lide.
venziondidio.
febrinodelfrideodalma.
zelestino.
coniledesio.
oriuccia.
alvatorio.
bonetta.
oreno.
```

ree.

Not bad! We see names that were not in the original dataset, and much more "name-like" than the previous examples.

3 Concatenated Network - MakeMore pt.3 (21/04/2023)

We are now ready to move on to Multilayer Perceptrons models: in order to do it we are going to reproduce the results of an "old" paper.

We are going to see the procedure of **embedding**, which is one of the most powerful tools in Neural Networks architectures: basically, we choose to encode (randomly at the beginning) our words into vectors in a euclidean space of a certain dimension (there are no general rules to choose such dimension), and see how with training our network clusterizes automatically the words. In our case we are actually going to see it working on just characters instead of words. As a matter of fact, we are going to consider a 3—gram approximation of our language model.

We have as input the characters at time t-1, t-2 and t-3 (we are considering tri-grams) which get embedded by a matrix C in a 30-dimensional vector as chosen by the authors of the paper. Then we put together these three 30-dimensional vectors to get a 90-dimensional one. We feed this vector to an intermediate layer with a nonlinear transformation (tanh). The output of such "hidden" layer gets then fed to a last layer which linearly transforms it by $\hat{W} \cdot \vec{x} + \hat{B}$.

We will see that there are many parameters in such system: the coefficients in the embedding matrix C and the matrix W, which will change with training in order to minimize the loss, but also some numbers which we a priori choose, which define the structure of our Multi-Layer Perceptron. For example, the dimension of the embedding, or the gradient descent rate. These are the so-called hyperparameters.

```
[2]: # https://youtu.be/P6sfmUTpUmc
# https://github.com/karpathy/makemore
```

```
[3]: # we now want to dig more into neural activity and learning to understand the →RNN and LSTM architecture and properties...

import random import torch import torch.nn.functional as F import matplotlib.pyplot as plt #for making figures %matplotlib inline
```

```
[5]: # read in all the words
random.seed(158)
words = open("data/nomi_italiani.txt", "r").read().splitlines()
random.shuffle(words)
words[0:8]
```

```
[5]: ['argento', 'giovannino',
```

```
'licurga',
      'elvira',
      'marena',
      'sirio',
      'emilia',
      'bisio']
[6]: print(len(words))
    9105
[7]: # build the vocabulary of characters and mapping to/from integers
     chars = sorted(list(set("".join(words))))
     stoi = {s: i + 1 for i, s in enumerate(chars)}
     stoi["."] = 0
     itos = {i: s for s, i in stoi.items()}
     vocab_size = len(itos)
     print(itos)
    print(vocab_size)
    {1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10:
    'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19:
    'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0:
    '.'}
    28
[8]: # build the dataset
     block_size = (
         # context length: how many characters do we take to predict the next one ...
         3
     def build_dataset(words):
        X, Y = [], [] # input & label
         for w in words:
             context = [0] * block_size
             for ch in w + ".":
                 ix = stoi[ch]
                 X.append(context)
                 Y.append(ix)
                 # print(''.join(itos[i] for i in context), '--->', itos[ix])
                 context = context[1:] + [ix] # shift: crop and append
```

```
X = torch.tensor(X)
Y = torch.tensor(Y)
print(X.shape, Y.shape)
return X, Y
```

```
[9]: import random

random.seed(42)
random.shuffle(words)
n1 = int(0.8 * len(words))
n2 = int(0.9 * len(words))

Xtr, Ytr = build_dataset(words[:n1])
Xdev, Ydev = build_dataset(words[n1:n2])
Xte, Yte = build_dataset(words[n2:])
```

```
torch.Size([58867, 3]) torch.Size([58867])
torch.Size([7404, 3]) torch.Size([7404])
torch.Size([7372, 3]) torch.Size([7372])
```

We now construct the first layer: the input of such layer will have dimension $3 \cdot 2 = 6$, i.e. the multiplied dimension of the *n*-gram and the embedding dimension. We will consider 100 neurons (another hyperparameter).

```
[10]: # MLP revisited
    n_embd = 10  # the dimensionality of the character embedding vectors
    n_hidden = 200  # the number of neurons in the hidden layer of MLP

g = torch.Generator().manual_seed(123456780)  # for reproducibility
C = torch.randn((vocab_size, n_embd), generator=g)
W1 = torch.randn((n_embd * block_size, n_hidden), generator=g)  # neurons
b1 = torch.randn(n_hidden, generator=g)  # bias
W2 = torch.randn((n_hidden, vocab_size), generator=g)
b2 = torch.randn(vocab_size, generator=g)
parameters = [C, W1, b1, W2, b2]
print(sum(p.nelement() for p in parameters))  # number of parameter in total...
for p in parameters:
    p.requires_grad = True
```

12108

Now we would like to compute the product $emb \cdot W1 + b1$. But emb has a different dimension (or shape) with regard to W1: we need to **concatenate** the elements of emb in order to get the same dimension. Now, there would be many ways to do this: with PyTorch we have the function cat (together with unbind) which could do the work for us... but there is actually a much less time-costing way.

As a matter of fact, PyTorch has a built-in method *view* which re-organizes the elements of a tensor in the shape we choose: and it does this operation just (roughly) re-arranging the allocated

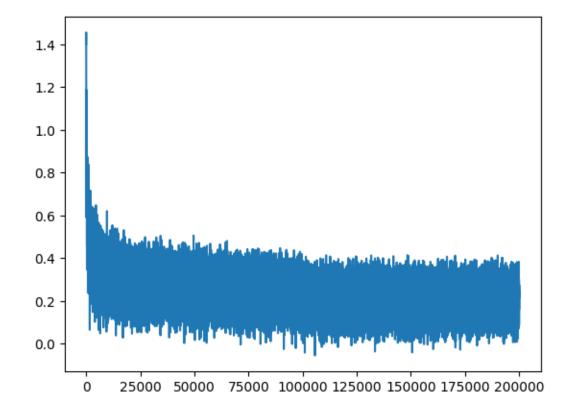
memory for each term, and not allocating new memory: therefore this is far more efficient than using other PyTorch functions. This is what we are going to use.

```
[11]: # same optimization as last time
      max_steps = 200000
      batch_size = 32
      lossi = []
      for i in range(max_steps):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,), generator=g)
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward bass
          emb = C[Xb] # embed characters into vectors
          embcat = emb.view(emb.shape[0], -1) # concatenate the vectors
          hpreact = embcat @ W1 + b1 # hidden layer pre-activation
          h = torch.tanh(hpreact) # hidden layer
          logits = h @ W2 + b2 # output layer
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = 0.1 if i < 100000 else 0.01 # step learning rate decay</pre>
          for p in parameters:
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}:{loss.item():.4f}")
          lossi.append(loss.log10().item())
```

```
0/ 200000:25.2234
10000/ 200000:2.2865
20000/ 200000:2.1045
30000/ 200000:2.1319
40000/ 200000:1.8164
50000/ 200000:1.8491
70000/ 200000:1.9464
80000/ 200000:1.9799
90000/ 200000:2.3608
100000/ 200000:1.3078
```

```
110000/ 200000:1.9567
      120000/ 200000:1.5188
      130000/ 200000:1.7088
      140000/ 200000:1.6152
      150000/ 200000:2.0892
      160000/ 200000:1.2948
      170000/ 200000:1.3657
      180000/ 200000:1.7789
      190000/ 200000:1.5764
[12]: print(-torch.tensor(1 / 28).log())
     tensor(3.3322)
```

[14]: plt.plot(lossi)



```
[15]: # this decorator disables gradient tracking...discuss in class....
      @torch.no_grad()
      def split_loss(split):
         x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
```

```
"test": (Xte, Yte),
}[split]
emb = C[x] # (N,block_size, n_embd)
embcat = emb.view(emb.shape[0], -1) # concat into (N,block_size*n_embd)
hpreact = embcat @ W1 + b1 # hidden layer pre-activation
h = torch.tanh(hpreact) # hidden layer (N, h_hidden)
logits = h @ W2 + b2 # output layer (N, vocab_size)
loss = F.cross_entropy(logits, y) # loss function
print(split, loss.item())
```

```
[16]: split_loss("train")
split_loss("val")
```

train 1.6465035676956177 val 1.8481979370117188

```
[17]: # sampling from the model.....
      g = torch.Generator().manual_seed(12345678 + 10)
      for _ in range(20):
          out = []
          context = [0] * block_size
          while True:
              emb = C[torch.tensor([context])] # (1,block_size,n_embed)
              h = torch.tanh(emb.view(1, -1) @ W1 + b1)
              logits = h @ W2 + b2
              probs = F.softmax(logits, dim=1)
              # sample from the distribuion
              ix = torch.multinomial(probs, num_samples=1, generator=g).item()
              # shift the context window and track the samples
              context = context[1:] + [ix]
              out.append(ix)
              # if we sample the special '.' token, break
              if ix == 0:
                  break
          print("".join(itos[i] for i in out)) # decode and print the generated word
```

albo.
giovanno.
rizio.
siside.
polina.
gio.
assimo.
cecchiarosinda.

```
benuartinaippirenziana.
     peppio.
     abdocchia.
     bella.
     benio.
     moheo.
     lauretilla.
     rinieronino.
     filosca.
     esaro.
     euto.
     giliana.
[21]: # let us focus on the last layer ....logits and then softmax
      logits = torch.randn(4) * 100
      # logits = view(2, 2, 2, 20)
      probs = torch.softmax(logits, dim=0)
      loss = -probs[2].log()
      print("logits:", logits)
      print("probs:", probs)
      print("loss:", loss)
     logits: tensor([-14.4960, -31.7004, 124.3944, 179.8049])
     probs: tensor([0.0000e+00, 0.0000e+00, 8.6204e-25, 1.0000e+00])
     loss: tensor(55.4105)
[22]: # back to our examples and look at the logit just after the first pass and
       understand normalization....
      # MLP revisited
      n_{embd} = 10 # the dimensionality of the character embedding vectors
      n_hidden = 200 # the number of neurons in the hidden layer of MLP
      g = torch.Generator().manual_seed(123456780) # for reproducibility
      C = torch.randn((vocab size, n embd), generator=g)
      W1 = torch.randn((n_embd * block_size, n_hidden), generator=g) # *0.20
      b1 = torch.randn(n_hidden, generator=g) # *0.01
      W2 = torch.randn((n_hidden, vocab_size), generator=g) # *0.01
      b2 = torch.randn(vocab_size, generator=g) # *0
      parameters = [C, W1, b1, W2, b2]
      print(sum(p.nelement() for p in parameters)) # number of parameter in total...
      for p in parameters:
          p.requires_grad = True
```

```
[23]: |# same optimization as last time...try, look at logits then go up and change W2_{\square}
       ⇔and b2 normalization....
      \max \text{ steps} = 200000
      batch size = 32
      lossi = ∏
      for i in range(max_steps):
          # mini batch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,), generator=g)
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward bass
          emb = C[Xb] # embed characters into vectors
          embcat = emb.view(emb.shape[0], -1) # concatenate the vectors
          hpreact = embcat @ W1 + b1 # hidden layer pre-activation
          h = torch.tanh(hpreact) # hidden layer
          logits = h @ W2 + b2 # output layer
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in parameters:
              p.grad = None
          loss.backward()
          # update
          lr = 0.1 if i < 100000 else 0.01 # step learning rate decay
          for p in parameters:
              p.data += -lr * p.grad
          # track stats
          if i % 10000 == 0: # print every once in a while
              print(f"{i:7d}/{max_steps:7d}:{loss.item():.4f}")
          lossi.append(loss.log10().item())
          break
           0/ 200000:25.2234
```

```
[26]: print(
    logits[1]
) # confidently wrong... but with weight is better... 'squashing down the
    →neurons...'
```

```
tensor([ 10.6530, -7.2423, 31.2924, -15.8263, 7.0554, -0.8957, 10.4593, 8.9841, 13.3143, -2.6116, 14.7497, 17.5647, 17.0676, 1.1002, 14.7031, -13.5323, -19.1125, -21.7921, 21.1479, 8.6535, 7.4713, -3.2913, 3.2052, 1.8503, 12.2664, -3.8606, 3.1228, 4.6715],
```

grad_fn=<SelectBackward0>)

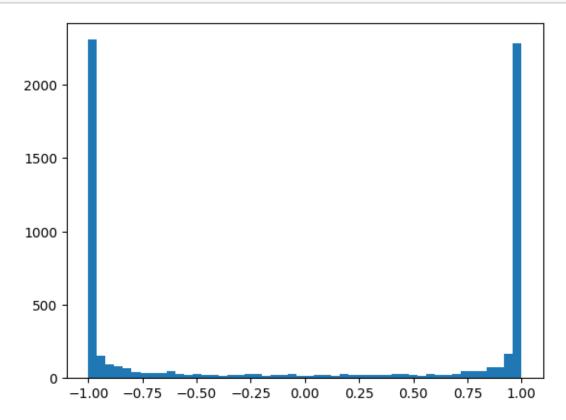
```
[29]: # Now we focus on the first layer (show pict): h & hpreact
# remember to intialize and run again
# look at the +- 1 in h
print(h.shape)
```

torch.Size([32, 200])

[28]: print(len(h.view(-1).tolist())) # 32*200

6400

[30]: plt.hist(h.view(-1).tolist(), 50)
a lot of neurons are ' saturated'

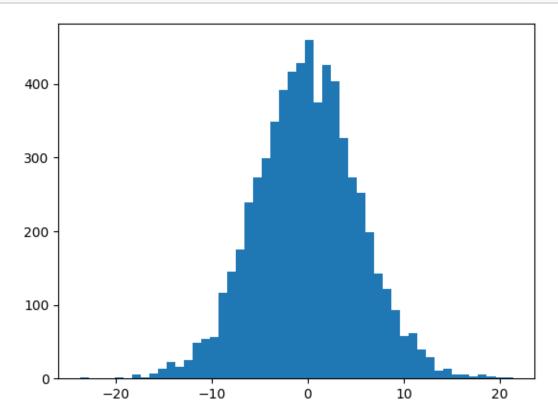


```
[31]: # now look at the "broad" shape of the 'hpreact' distribution....and this is_bad for learning...we want 'normality' for our brain...

# tgh'(x) = (1-tgh(x)^2).... saturation bring to vanish gradient...no learning...

plt.hist(hpreact.view(-1).tolist(), 50)

# a lot of neurons are ' saturated'
```



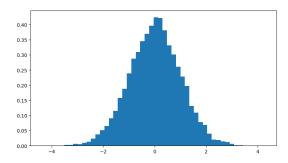
```
[33]: # looking for dead neurons....comment other Activation Functions.... go back_weigth the first layer and try again...

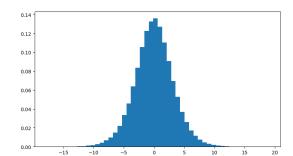
plt.figure(figsize=(20, 10))
plt.imshow(h.abs() > 0.99, cmap="gray", interpolation="nearest")
```



```
[34]: # why we do not to have to worry too much about inizialization....bach
       \hookrightarrow normalization..
      # since 2015
      # https://arxiv.org/abs/1502.03167
      # if the problems are fluctuations and saturations (discuss in class)...then_{f U}
       ⇒just gaussain normalize at each layer...
      # simple as that !!!...and normalizing is differentiable !!....
      x = torch.randn(1000, 10)
      w = torch.randn(10, 200) # *.2 #*1/10**0.5
      y = x @ w
      print(y.shape)
      print(x.mean(), x.std())
      print(y.mean(), y.std())
      plt.figure(figsize=(20, 5))
      plt.subplot(121)
      plt.hist(x.view(-1).tolist(), 50, density=True)
      plt.subplot(122)
      plt.hist(y.view(-1).tolist(), 50, density=True)
```

```
torch.Size([1000, 200])
tensor(0.0148) tensor(0.9958)
tensor(-0.0002) tensor(3.1940)
```





4 Convolutional Network - MakeMore pt.4 (28/04/2023)

For real the 4th was about back propagation, but we skip it in this course. For the final exam one may go deeper into this algorithm, maybe by hand.

Last time we implemented a multilayer perceptron (with actually two layers), working at character level and building a probability distribution. The pipeline was: - embedding (2 - 10 dimensional vectors) - glue them together, but this is not the best thing one can do

Instead of looking at 3 previous char we can look at 8 previous char and so on... We'll see it doesn't change much. Idea: feed the net with information in a hierarchical way. Notice that we'll work with text, but we can expand this also to images. We want to construct a convolution network,

even if it's not related to the mathematical definition of convolution. Glue chars together, giving it to a layer, process, glue another char and give to the next layer and so on. The line behind all this is entropy, we skip the compression algorithm for lack of time. Probability distribution, entropy and compression are actually the same thing.

```
[1]: # now we want to enlarge the context length AND ''fuse information in au

hierarchical manner''

# see the approach in https://arxiv.org/abs/1609.03499
```

```
[2]: # The importance of embedding

# word2vec: skip-gram https://arxiv.org/pdf/1301.3781v3.pdf

# node2vec: https://arxiv.org/pdf/1607.00653.pdf
```

Data are not always linear, or a lattice, or on a euclidean space... Things are complicated. However, for some phenomena, they're naturally distributed in networks (or if you want, graph). The main concepts are neighbors, distances... As we can handle text we can handle images, which are just euclidean spaces.

This field is going extremely fast, keep going!

We deal with real numbers which can be positive, negative, very big, very small... The hyperbolic tangent help us to squeeze them. Otherwise, the neurons won't learn. There is still a lot to understand there... Take it as it is, $e \ più \ non \ dimandare$. Actually, there are many ways to squeeze without the hyperbolic tangent, but the meaning is the same.

We'll assume batch normalization and focus on the method. We'll hierarchically glue 8 char together. See also WaveNet for audio generation. We want to pass from $2+2+2 \rightarrow 6$ to $2 \rightarrow 3 \rightarrow \dots \rightarrow 6$, i.e. gradually. Convolutional layers like this are very spread and useful for text analysis.

```
[3]: import random
import torch
import torch.nn.functional as F
import torch.nn as nn
import matplotlib.pyplot as plt
%matplotlib inline
```

```
[4]: # read in all the words
random.seed(158)
words = (
    open("data/nomi_italiani.txt", "r").read().splitlines()
) # each line is an element of the list
random.shuffle(words)
print(len(words))
print(words[0:8])
```

```
9105
['argento', 'giovannino', 'licurga', 'elvira', 'marena', 'sirio', 'emilia', 'bisio']
```

```
[5]: # build the vocabulary of characters and mappings to/from integers (encoder/
      ⇔decoder)
     chars = sorted(list(set("".join(words))))
     stoi = {s: i + 1 for i, s in enumerate(chars)}
     stoi["."] = 0
     itos = {i: s for s, i in stoi.items()}
     vocab size = len(stoi)
     print(itos)
    print(vocab_size)
    {1: '-', 2: 'a', 3: 'b', 4: 'c', 5: 'd', 6: 'e', 7: 'f', 8: 'g', 9: 'h', 10:
    'i', 11: 'j', 12: 'k', 13: 'l', 14: 'm', 15: 'n', 16: 'o', 17: 'p', 18: 'q', 19:
    'r', 20: 's', 21: 't', 22: 'u', 23: 'v', 24: 'w', 25: 'x', 26: 'y', 27: 'z', 0:
    '.'}
    28
[6]: # build the dataset
     block_size = 8 # 8 context length: how many characters do we take to predict
      \hookrightarrow the next one?
     def build dataset(words):
        X, Y = [], []
         for w in words:
             context = [0] * block_size
             for ch in w + ".":
                 ix = stoi[ch]
                 X.append(context)
                 Y.append(ix)
                 context = context[1:] + [ix] # crop and append
         X = torch.tensor(X)
         Y = torch.tensor(Y)
         print(X.shape, Y.shape)
         return X, Y
    n1 = int(0.8 * len(words))
    n2 = int(0.9 * len(words))
     Xtr, Ytr = build_dataset(words[:n1]) # 80%
     Xdev, Ydev = build_dataset(words[n1:n2]) # 10%
     Xte, Yte = build_dataset(words[n2:]) # 10%
    torch.Size([59049, 8]) torch.Size([59049])
    torch.Size([7332, 8]) torch.Size([7332])
    torch.Size([7262, 8]) torch.Size([7262])
```

```
[7]: for x, y in zip(Xtr[:20], Ytr[:20]):
         print("".join(itos[ix.item()] for ix in x), "-->", itos[y.item()])
    ... --> a
    ...a --> r
    ...ar --> g
    ...arg --> e
    ...arge --> n
    ...argen --> t
    ..argent --> o
    .argento --> .
    ... --> g
    ...g --> i
    ...gi --> o
    ...gio --> v
    ...giov --> a
    ...giova --> n
    ..giovan --> n
    .giovann --> i
    giovanni --> n
    iovannin --> o
    ovannino --> .
    ... --> 1
```

Let's do it in an object-oriented way. These things are already contained in PyTorch, so we don't need to write them by hand. All these classes are into _torch.nn.*_

```
[8]: | # Near copy paste of the layers we have developed in Part 3
     # all these definitions work as in PyTorch, but we won't use it as a black box
     #⊔
     class Linear:
         def __init__(self, fan_in, fan_out, bias=True):
             self.weight = (
                 torch.randn((fan_in, fan_out)) / fan_in**0.5
             ) # note: kaiming init
             self.bias = torch.zeros(fan_out) if bias else None
         def __call__(self, x):
             self.out = x @ self.weight
             if self.bias is not None:
                 self.out += self.bias
             return self.out
         def parameters(self):
             return [self.weight] + ([] if self.bias is None else [self.bias])
```

```
#__
class BatchNorm1d:
    def __init__(self, dim, eps=1e-5, momentum=0.1):
        self.eps = eps
        self.momentum = momentum
        self.training = True
        # parameters (trained with backprop)
        self.gamma = torch.ones(dim)
        self.beta = torch.zeros(dim)
        # buffers (trained with a running 'momentum update')
        self.running_mean = torch.zeros(dim)
        self.running_var = torch.ones(dim)
    def __call__(self, x):
        # calculate the forward pass
        if self.training:
            if x.ndim == 2:
                dim = 0
            elif x.ndim == 3:
                dim = (0, 1)
            xmean = x.mean(dim, keepdim=True) # batch mean
            xvar = x.var(dim, keepdim=True) # batch variance
        else:
            xmean = self.running_mean
            xvar = self.running_var
        # normalize to unit variance
        xhat = (x - xmean) / torch.sqrt(xvar + self.eps)
        self.out = self.gamma * xhat + self.beta
        # update the buffers
        if self.training:
            with torch.no_grad():
                self.running_mean = (
                    1 - self.momentum
                ) * self.running_mean + self.momentum * xmean
                self.running_var = (
                    1 - self.momentum
                ) * self.running_var + self.momentum * xvar
        return self.out
    def parameters(self):
        return [self.gamma, self.beta]
```

```
class Tanh:
   def __call__(self, x):
       self.out = torch.tanh(x)
        return self.out
   def parameters(self):
        return []
class Embedding:
    def __init__(self, num_embeddings, embedding_dim):
        self.weight = torch.randn((num_embeddings, embedding_dim))
    def __call__(self, IX):
        self.out = self.weight[IX]
        return self.out
    def parameters(self):
        return [self.weight]
class Flatten:
    def __init__(self, n):
       self.n = n
    def __call__(self, x):
        self.out = x.view(x.shape[0], -1)
        return self.out
    def parameters(self):
        return []
# |
class FlattenConsecutive:
    def __init__(self, n):
       self.n = n
   def __call__(self, x):
        B, T, C = x.shape
```

```
x = x.view(B, T // self.n, C * self.n)
        if x.shape[1] == 1:
            x = x.squeeze(1)
        self.out = x
        return self.out
    def parameters(self):
        return []
#
class Sequential:
    def __init__(self, layers):
        self.layers = layers
    def __call__(self, x):
        for layer in self.layers:
            x = layer(x)
        self.out = x
        return self.out
    def parameters(self):
        # get parameters of all layers and stretch them out into one list
        return [p for layer in self.layers for p in layer.parameters()]
```

```
[9]: torch.manual_seed(42)
```

[9]: <torch._C.Generator at 0x7ff1d570b370>

C is our embedding matrix 28x10 which contains the 10 dimensional embedding for each of 28 chars. Context length is 8, multiply by 10 so 80 is the dimension of the input layer.

```
[10]: # original network https://jmlr.org/papers/volume3/tmp/bengio03a.pdf

n_embd = 10  # the dimensionality of the character embedding vectors
n_hidden = 200  # the number of neurons in the hidden layer of the MLP

C = torch.randn(vocab_size, n_embd)
layers = [
    Linear(n_embd * block_size, n_hidden, bias=False),
    BatchNorm1d(n_hidden), # normalize, otherwise learning stops
    Tanh(),
    Linear(n_hidden, vocab_size),
]

# parameter initialization
```

```
with torch.no_grad():
    layers[-1].weight *= 0.1 # last layer make less confident

parameters = [C] + [p for layer in layers for p in layer.parameters()]
print(sum(p.nelement() for p in parameters)) # number of parameters in total
for p in parameters:
    p.requires_grad = True
```

```
[11]: # same optimization as last time
      max_steps = 200000
      batch size = 32
      lossi = []
      for i in range(max_steps):
          # minibatch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,))
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward pass
          emb = C[Xb] # embed the characters into vectors
          x = emb.view(
              emb.shape[0], -1
          ) # concatenate the vectors, view is not memory consuming
          for layer in layers:
              x = layer(x)
          loss = F.cross_entropy(x, Yb) # loss function
          # backward pass, now we're using our black box
          for p in parameters:
              p.grad = None
          loss.backward()
          # update: simple SGD
          lr = 0.1 if i < 150000 else 0.01 # step learning rate decay</pre>
          for p in parameters:
              p.data += -lr * p.grad
              # track stats
          if i % 10000 == 0: # print every once in a while
              print(f''\{i:7d\}/\{max\_steps:7d\}: \{loss.item():.4f\}'')
          lossi.append(loss.log10().item())
```

0/ 200000: 3.3371 10000/ 200000: 2.1734 20000/ 200000: 1.9819

```
30000/ 200000: 1.6350
 40000/ 200000: 1.3981
 50000/ 200000: 1.6659
 60000/ 200000: 1.8349
 70000/ 200000: 1.6599
 80000/ 200000: 1.2059
 90000/ 200000: 1.6775
100000/ 200000: 1.3948
110000/ 200000: 1.3727
120000/ 200000: 1.7746
130000/ 200000: 1.5139
140000/ 200000: 1.3102
150000/ 200000: 1.4078
160000/ 200000: 1.3451
170000/ 200000: 1.2467
180000/ 200000: 1.4784
190000/ 200000: 1.3532
```

Why 3.3 at the beginning? Assuming all random, $-\log \frac{1}{28}$ is about that number...

NOTE that with 8 the decrease is very slow, we're fusing info too quickly!

Small batch implies fluctuating a lot, so we can use view to split in pieces of one thousand.

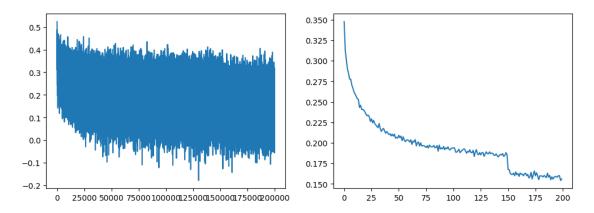
```
[12]: print(-torch.tensor(1 / 28).log())
# 32 batches are few... so you can get very lucky or unlucky

fig, ax = plt.subplots(ncols=2, figsize=(12, 4))

ax[0].plot(torch.tensor(lossi))
ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row
```

tensor(3.3322)

[12]: [<matplotlib.lines.Line2D at 0x7ff113d62230>]



But look now at the first plot of the loss function. It's very bad, but why? Because a size of 32 is very small for our batches, therefore we have that sometimes (luckily) the system is very right about its predictions and sometimes (unluckily) it is not. But we are physicists, we know tensors can be manipulated... what if we split the 200000 components of the loss into lines of length 1000? Then we could take the average of that and plot it... The second plot is much better, and we didn't change the data! So averaged over time, we are doing very good: H is decreasing, and also notice that at the 150 step it makes another downward jump (SGD).

Now our training is over, and we want to evaluate our results. We need to tell PyTorch that we're not in the training phase anymore. **BE CAREFUL**, or you'll get weird results due to batch normalization, which for us is a black box.

```
[13]: # put layers into eval mode (needed for batchnorm especially)
for layer in layers:
    layer.training = False
```

```
[14]: # evaluate the loss
      @torch.no_grad() # this decorator disables gradient tracking inside pytorch
      def split_loss(split):
          x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
              "test": (Xte, Yte),
          }[split]
          emb = C[x] # embed the characters into vectors (N, block size)
          x = emb.view(emb.shape[0], -1) # concatenate the vectors
          for layer in layers:
              x = layer(x)
          loss = F.cross_entropy(x, y) # loss function
          print(split, loss.item())
      split_loss("train")
      split_loss("val")
```

train 1.372538447380066 val 1.7553904056549072

```
[15]: # sample from the model
for _ in range(20):
    out = []
    context = [0] * block_size # initialize with all ...
    while True:
        # forward pass the neural net
        emb = C[
            torch.tensor([context])
        ] # embed the characters into vectors (N,block_size)
        x = emb.view(emb.shape[0], -1) # concatenate the vectors
```

```
for layer in layers:
    x = layer(x)
logits = x
probs = F.softmax(logits, dim=1)
# sample from the distribution
ix = torch.multinomial(probs, num_samples=1).item()
# shift the context window and track the samples
context = context[1:] + [ix]
out.append(ix)
# if we sample the special '.' token, break
if ix == 0:
    break

print("".join(itos[i] for i in out)) # decode and print the generated word
```

```
amode.
leandro.
alfisio.
fabbions.
amperia.
oreino.
silvina.
wantie.
olderiza.
orea.
consolita.
mariacrostelfino.
emerande.
giandamaro.
fiero.
slorena-gettto.
morino.
morietta.
alcidisso.
artemine.
```

Not that bad. But still, we can improve this. We actually skipped the embedding, which we could now introduce with our classes defined earlier. But instead we want to "torchify" now our code, i.e. start to use Torch functions to improve the efficiency of our system.

```
[16]: # we can do better and use "Embedding" (as pytorch) to see C as a first layer

n_embd = 10  # the dimensionality of the character embedding vectors
n_hidden = 200  # the number of neurons in the hidden layer of the MLP

layers = [
    Embedding(vocab_size, n_embd), # C = torch.randn(vocab_size, n_embd)
    Flatten(block_size),
```

```
Linear(n_embd * block_size, n_hidden, bias=False),
BatchNorm1d(n_hidden),
Tanh(),
Linear(n_hidden, vocab_size),
]

# parameter initialization

with torch.no_grad():
    layers[-1].weight *= 0.1  # last layer make less confident

# [C] + [p for layer in layers for p in layer.parameters()]
parameters = [p for layer in layers for p in layer.parameters()]
print(sum(p.nelement() for p in parameters))  # number of parameters in total
for p in parameters:
    p.requires_grad = True
```

In PyTorch one can write this as a sequential list of layer, with the same function names.

```
[17]: n_embd = 10  # the dimensionality of the character embedding vectors
    n_hidden = 200  # the number of neurons in the hidden layer of the MLP

model = nn.Sequential(
    nn.Embedding(vocab_size, n_embd),
    nn.Flatten(block_size),
    nn.Linear(n_embd * block_size, n_hidden, bias=False),
    nn.BatchNorm1d(n_hidden),
    nn.Tanh(),
    nn.Linear(n_hidden, vocab_size),
)

# number of parameters in total
print(sum(p.nelement() for p in model.parameters()))
for p in model.parameters():
    p.requires_grad = True
```

```
[18]: # or with 'karpathy' definitions...

n_embd = 10  # the dimensionality of the character embedding vectors
n_hidden = 200  # the number of neurons in the hidden layer of the MLP

model = Sequential(
    [
        Embedding(vocab_size, n_embd),
```

```
Flatten(block_size),
    Linear(n_embd * block_size, n_hidden, bias=False),
    BatchNorm1d(n_hidden),
    Tanh(),
    Linear(n_hidden, vocab_size),
]
)

# number of parameters in total
print(sum(p.nelement() for p in model.parameters()))
for p in model.parameters():
    p.requires_grad = True
```

```
[19]: # put layers into eval mode (needed for batchnorm especially)
for layer in model.layers:
    layer.training = True

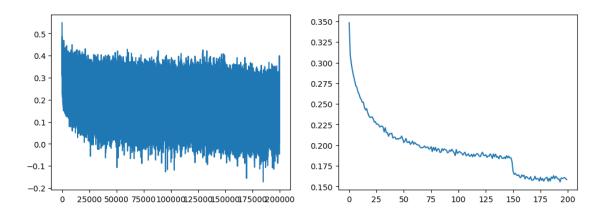
# model.train(True)
```

```
[20]: # same optimization as before time
      max_steps = 200000
      batch_size = 32
      lossi = ∏
      for i in range(max_steps):
          # minibatch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,))
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward pass
            emb=C[Xb] # embed the characters into vectors
            x=emb.view(emb.shape[0],-1) #concatenate the vectors
            for layer in layers:
                x=layer(x)
          logits = model(Xb)
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in model.parameters():
             p.grad = None
          loss.backward()
          # update: simple SGD
```

```
lr = 0.1 if i < 150000 else 0.01 # step learning rate decay
   for p in model.parameters():
       p.data += -lr * p.grad
   # track stats
   if i % 10000 == 0: # print every once in a while
       print(f"{i:7d}/{max_steps:7d}: {loss.item():.4f}")
   lossi.append(loss.log10().item())
# break
     0/ 200000: 3.5427
 10000/ 200000: 1.6889
 20000/ 200000: 1.7099
 30000/ 200000: 1.7663
 40000/ 200000: 1.6661
 50000/ 200000: 1.5461
 60000/ 200000: 1.8788
70000/ 200000: 1.7811
 80000/ 200000: 1.9472
 90000/ 200000: 1.3643
100000/ 200000: 1.5458
110000/ 200000: 1.4089
120000/ 200000: 1.6715
130000/ 200000: 2.0241
140000/ 200000: 1.6338
150000/ 200000: 1.5033
160000/ 200000: 1.5036
170000/ 200000: 1.5975
180000/ 200000: 1.3502
190000/ 200000: 1.6590
```

```
[21]: fig, ax = plt.subplots(ncols=2, figsize=(12, 4))
ax[0].plot(torch.tensor(lossi))
ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row
```

[21]: [<matplotlib.lines.Line2D at 0x7ff113d63790>]



```
[22]: # put layers into eval mode (needed for batchnorm especially)

for layer in model.layers:
    layer.training = False

# model.train(True)
```

```
[23]: # evaluate the loss
      @torch.no_grad() # this decorator disables gradient tracking inside pytorch
      def split_loss(split):
          x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
              "test": (Xte, Yte),
          }[split]
              emb=C[x] # embed the characters into vectors (N,block_size) before
              x=emb.view(emb.shape[0],-1) #concatenate the vectors
                for layer in layers:
                    x=layer(x)
          logits = model(x)
          loss = F.cross_entropy(logits, y) # loss function
          print(split, loss.item())
      split_loss("train")
      split_loss("val")
```

train 1.3757604360580444

val 1.7395519018173218

```
[24]: # sample from the model
      for _ in range(20):
         out = []
          context = [0] * block_size # initialize with all ...
          while True:
              # forward pass the neural net
                        emb=C[torch.tensor([context])] # embed the characters into
       →vectors (N,block_size)
                        x=emb.view(emb.shape[0],-1) #concatenate the vectors
              #
              #
                        for layer in layers:
                            x=layer(x)
                        logits = x
              logits = model(torch.tensor([context]))
              probs = F.softmax(logits, dim=1)
              # sample from the distribution
              ix = torch.multinomial(probs, num_samples=1).item()
              # shift the context window and track the samples
              context = context[1:] + [ix]
              out.append(ix)
              # if we sample the special '.' token, break
              if ix == 0:
                  break
          print("".join(itos[i] for i in out)) # decode and print the generated word
```

```
tima.
andrea.
laurezio.
loriela.
anio.
lucido.
eriscondo.
guerriana.
ginepro.
umbra.
angeloce.
raffoso.
marziano.
erlene.
bonulana.
eva.
abelda.
riziaddino.
calaria.
eride.
```

Now embedding is accounted for, and we could generate names in this way. This is a little better, but still, there is room for improvement. We could for example add more layer and make ourselves a nice **deep network**: but this wouldn't improve much our system at the moment. Why is that? It's because we still didn't introduce any hierarchical organization in our data, which will be a definitive improvement for our Neural Network structure. We want to change the step between the embedding and the feeding to the hidden layer, in the sense that we do not want anymore to fuse the information coming from the data altogether into a single vector which is then fed to the tanh. We want instead to introduce a hierarchical structure of our embedded data.

```
[25]: # let's look at a batch of just 4 example
      ix = torch.randint(0, Xtr.shape[0], (4,))
      Xb, Yb = Xtr[ix], Ytr[ix]
      logits = model(Xb)
      print(Xb.shape)
      print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 7, 10, 15, 2],
             [0, 8, 2, 3, 19, 10, 6, 13],
             [0, 0, 0, 0, 0, 0, 0, 8],
             [10, 23, 2, 13, 5, 10, 15, 16]])
[26]: print(model.layers[0].out.shape) # output of the embedding layer
      print(model.layers[1].out.shape) # output of the Flatten layer
      print(model.layers[2].out.shape) # output of the Linear layer
     torch.Size([4, 8, 10])
     torch.Size([4, 80])
     torch.Size([4, 200])
     Now multiply each vector for the matrix and take a 200dim vector as output
[27]: # now a nice surprise about the Linear Layer https://pytorch.org/docs/stable/
       \rightarrow generated/torch.nn.Linear.html#torch.nn.Linear
      # just to look at the dimensions
          torch.randn(4, 80) @ torch.randn(80, 200) + torch.randn(200)
```

[27]: torch.Size([4, 200])

We can also add more dimensions... and PyTorch will work on the right one.

).shape # broadcasting in the last term....

```
[28]: # but also !!

print((torch.randn(4, 2, 80) @ torch.randn(80, 200) + torch.randn(200)).shape)

# or also !!

print((torch.randn(4, 4, 20) @ torch.randn(20, 200) + torch.randn(200)).shape)
```

```
torch.Size([4, 4, 200])
     Instead of one vector of 80 we can use four vectors of 20.
[29]: # 1 2 3 4 5 6 7 8 -> (1 2) (3 4) (5 6) (7 8)
      # we want to fuse vectors in pairs and acts in parallel on the 4 pairs of \Box
       \hookrightarrow characters.
      # i.e. we go from (torch.randn(4,80) @ torch.randn(80,200) + torch.randn(200)).
       ⇔shape
      print((torch.randn(4, 4, 20) @ torch.randn(20, 200) + torch.randn(200)).shape)
     torch.Size([4, 4, 200])
[30]: # so now we need to change the Flatten layer to produce a (4,4,20) tensor and
      →NOT (4,80)
      e = torch.randn(
          4, 8, 10
[31]: # all the numbers from 0 to 9
      print(list(range(10)))
      # all the numbers from 0 to 9 by 2 - i.e. even numbers
      print(list(range(10))[::2])
      # all the numbers from 1 to 9 by 2 - i.e. odd numbers
      print(list(range(10))[1::2])
     [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
     [0, 2, 4, 6, 8]
     [1, 3, 5, 7, 9]
[32]: # so we want this...
      print(e.shape)
      explicit = torch.cat([e[:, ::2, :], e[:, 1::2, :]], dim=2)
      print(explicit.shape)
     torch.Size([4, 8, 10])
     torch.Size([4, 4, 20])
[33]: input = torch.randn(4, 8, 10)
      print(input.shape)
      m = nn.Flatten()
      output = m(input)
      print(output.shape)
     torch.Size([4, 8, 10])
     torch.Size([4, 80])
```

torch.Size([4, 2, 200])

Let's adapt the model to the hierarchical way.

```
class FlattenConsecutive:
    def __init__(self, n):
        self.n = n

def __call__(self, x):
    B, T, C = x.shape
        x = x.view(B, T // self.n, C * self.n)
        if x.shape[1] == 1:
            x = x.squeeze(1)
        self.out = x
        return self.out

def parameters(self):
    return []
```

```
[35]: # Back to the Model... here we recover the previous one with
       →FlattenConsecutive(block_size)
      n embd = 10  # the dimensionality of the character embedding vectors
      n_hidden = 200 # the number of neurons in the hidden layer of the MLP
      model = Sequential(
          Embedding(vocab_size, n_embd),
              FlattenConsecutive(block_size),
              Linear(n_embd * block_size, n_hidden, bias=False),
              BatchNorm1d(n_hidden),
              nn.Tanh(),
              Linear(n_hidden, vocab_size),
          ]
      )
      # number of parameters in total
      print(sum(p.nelement() for p in model.parameters()))
      for p in model.parameters():
          p.requires_grad = True
```

```
[36]: # let's look at a batch of just 4 example
ix = torch.randint(0, Xtr.shape[0], (4,))
Xb, Yb = Xtr[ix], Ytr[ix]
logits = model(Xb)
```

```
print(Xb.shape)
     print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 0, 0, 0],
             [0, 0, 0, 0, 0, 0, 0, 4],
             [0, 0, 0, 0, 0, 0, 0],
             [ 0, 0, 0, 16, 13, 10, 23]])
[37]: for layer in model.layers[:-2]:
         print(layer.__class__._name__, ":", tuple(layer.out.shape))
     Embedding: (4, 8, 10)
     FlattenConsecutive: (4, 80)
     Linear: (4, 200)
     BatchNorm1d: (4, 200)
[38]: # we now move to a hierarchical approach
     n_{embd} = 10 # the dimensionality of the character embedding vectors
     n hidden = 200 # the number of neurons in the hidden layer of the MLP
     model = Sequential(
          Embedding(vocab_size, n_embd),
             FlattenConsecutive(2),
             Linear(n_embd * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
             Tanh(),
             FlattenConsecutive(2),
             Linear(n_hidden * 2, n_hidden, bias=False),
             BatchNorm1d(n hidden),
             Tanh(),
             FlattenConsecutive(2),
             Linear(n_hidden * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
             Tanh(),
             Linear(n_hidden, vocab_size),
         ]
     )
     # number of parameters in total
     print(sum(p.nelement() for p in model.parameters()))
     for p in model.parameters():
         p.requires_grad = True
```

```
[39]: # let's look at a batch of just 4 example
      ix = torch.randint(0, Xtr.shape[0], (4,))
      Xb, Yb = Xtr[ix], Ytr[ix]
      logits = model(Xb)
      print(Xb.shape)
      print(Xb)
     torch.Size([4, 8])
     tensor([[ 0, 0, 0, 0, 14, 2, 19],
             [0, 0, 0, 0, 0, 0, 8],
             [0, 0, 0, 0, 0, 0, 0, 0],
             [0, 0, 0, 8, 22, 20, 21, 2]])
[40]: for layer in model.layers:
         print(layer.__class__.__name__, ":", tuple(layer.out.shape))
     Embedding: (4, 8, 10)
     FlattenConsecutive: (4, 4, 20)
     Linear: (4, 4, 200)
     BatchNorm1d : (4, 4, 200)
     Tanh: (4, 4, 200)
     FlattenConsecutive: (4, 2, 400)
     Linear: (4, 2, 200)
     BatchNorm1d: (4, 2, 200)
     Tanh: (4, 2, 200)
     FlattenConsecutive : (4, 400)
     Linear: (4, 200)
     BatchNorm1d: (4, 200)
     Tanh: (4, 200)
     Linear: (4, 28)
[41]: print(logits.shape)
     torch.Size([4, 28])
     Now we build the net in a hierarchical way, so the first input will be 20-dim and the others 200-dim,
     as shown previously.
[42]: n_embd = 10 # the dimensionality of the character embedding vectors
      n_hidden = 68 # to have the same number of parameters as the previous model
      model = Sequential(
          Embedding(vocab_size, n_embd),
             FlattenConsecutive(2),
             Linear(n_embd * 2, n_hidden, bias=False),
             BatchNorm1d(n_hidden),
              Tanh(),
```

```
FlattenConsecutive(2),
    Linear(n_hidden * 2, n_hidden, bias=False),
    BatchNorm1d(n_hidden),
    Tanh(),
    FlattenConsecutive(2),
    Linear(n_hidden * 2, n_hidden, bias=False),
    BatchNorm1d(n_hidden),
    Tanh(),
    Linear(n_hidden, vocab_size),
]
)

# number of parameters in total
print(sum(p.nelement() for p in model.parameters()))
for p in model.parameters():
    p.requires_grad = True
```

```
[43]: # same optimization as before
      max_steps = 200000
      batch_size = 32
      lossi = []
      for i in range(max_steps):
          # minibatch construct
          ix = torch.randint(0, Xtr.shape[0], (batch_size,))
          Xb, Yb = Xtr[ix], Ytr[ix] # batch X, Y
          # forward pass
          logits = model(Xb)
          loss = F.cross_entropy(logits, Yb) # loss function
          # backward pass
          for p in model.parameters():
              p.grad = None
          loss.backward()
          # update: simple SGD
          lr = 0.1 if i < 150000 else 0.01 # step learning rate decay
          for p in model.parameters():
              p.data += -lr * p.grad
          # track stats
```

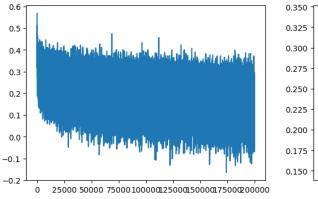
```
if i % 10000 == 0: # print every once in a while
    print(f"{i:7d}/{max_steps:7d}: {loss.item():.4f}")
lossi.append(loss.log10().item())
```

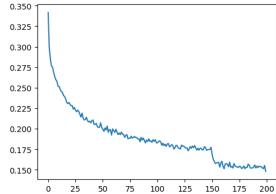
```
0/ 200000: 3.6892
 10000/ 200000: 1.5753
 20000/ 200000: 1.6228
 30000/ 200000: 1.5849
 40000/ 200000: 2.0534
 50000/ 200000: 1.3141
 60000/ 200000: 1.7441
70000/ 200000: 1.5046
80000/ 200000: 1.3641
 90000/ 200000: 1.3019
100000/ 200000: 1.9296
110000/ 200000: 1.3937
120000/ 200000: 1.8871
130000/ 200000: 1.4249
140000/ 200000: 1.3084
150000/ 200000: 1.3827
160000/ 200000: 1.4391
170000/ 200000: 1.1624
180000/ 200000: 1.3080
190000/ 200000: 1.4213
```

```
[44]: fig, ax = plt.subplots(ncols=2, figsize=(12, 4))

ax[0].plot(torch.tensor(lossi))
ax[1].plot(torch.tensor(lossi).view(-1, 1000).mean(1)) # mean on each row
```

[44]: [<matplotlib.lines.Line2D at 0x7ff113dc91b0>]





```
[45]: # put layers into eval mode (needed for batchnorm especially)...comment in
       ⇔class !
      for layer in model.layers:
          layer.training = False
[46]: # evaluate the loss
      @torch.no_grad() # this decorator disables gradient tracking inside pytorch
      def split_loss(split):
          x, y = {
              "train": (Xtr, Ytr),
              "val": (Xdev, Ydev),
              "test": (Xte, Yte),
          }[split]
          logits = model(x)
          loss = F.cross_entropy(logits, y) # loss function
          print(split, loss.item())
      split_loss("train")
      split_loss("val")
     train 1.3675501346588135
     val 1.741621732711792
[47]: # sample from the model
      for _ in range(20):
          out = []
          context = [0] * block_size # initialize with all ...
              logits = model(torch.tensor([context]))
              probs = F.softmax(logits, dim=1)
              # sample from the distribution
              ix = torch.multinomial(probs, num_samples=1).item()
              # shift the context window and track the samples
              context = context[1:] + [ix]
              out.append(ix)
              # if we sample the special '.' token, break
              if ix == 0:
                  break
          print("".join(itos[i] for i in out)) # decode and print the generated word
```

abelisia. ferrio. oliveria. rosimo. gueralda. filinentino. fiumquinto. maricosa. carfro. olmerino. anberino. irbenzio. ciciala. boneldo. violo. fiorentino. onellina. oviglio. ardenato. lauriano.

5 Recurrence approach - (03/05/2023)

We saw with makemore how to build a net which learns by n-grams. We want to have a net which keeps memory of what it reads while being able to remember important things and discard not relevant ones. How to introduce this memory effect? These things are called Recurrence Neural Network, and are based on both long and short term memories. **NOTE**: from 2017 all changed with new concept of attention and more...

But first... why use PyTorch? PyTorch is more recent while TensorFlow is more applied-oriented. Lot of market products are based on TensorFlow, also due to the easier debugging phase.

Why do we need memory? We've already discussed in theoretical classes. In a MPL we're giving a vector, do something, and taking out another vector. Another approach we can apply is image \rightarrow text (see *image captioning*). In this case the input is a picture and the outputs are many words. To do this is useful to add hidden variable to our model. Processing more inputs usually implies that we want to carry on some information.

The principle of an RNN is having hidden variables that communicates each other while affecting the output. The recurrence may be both one or bidirectional (maybe we don't want the future to affect the past, maybe we want). At the end we're just adding vectors, so don't worry.

How I remember the past? Just iterate this in time... The vector \vec{y} will feed the output while the function produces a vector \vec{h} to feed the next hidden block.

Because of recurrence the gradient usually vanish, so these nets are not easy to train. An evolution so are LSTM - Long Short Term Memory models, which sometimes forget or remember things. Seems complicated, but it's just the previous architecture with some extra things. With these nets we've not vanishing gradient problem, so they learn very well.

A middle way between RNN and LSTM is the GRU - Gated Recurrent Unit.

```
class RNN:
    def step(self, x):
        # update the hidden state
        # tanh of previous hidden state plus input
        self.h = np.tanh(np.dot(self.W_hh, self.h) + np.dot(self.W_xh, x))
        # compute the output vector
        y = np.dot(self.W_hy, self.h)
        return y
```

From 2015 something changed.

The basis is a bidirectional RNN. Working as char level... not very good. One can go deep in a lot of directions

```
[11]: """
      Minimal character-level Vanilla RNN model. Written by Andrej Karpathy
      \hookrightarrow (@karpathy)
      BSD License
      11 11 11
      import numpy as np
      # data I/O
      # should be simple plain text file
      data = open('data/divinacommedia.txt', 'r').read()
      chars = list(set(data))
      data_size, vocab_size = len(data), len(chars)
      print('data has %d characters, %d unique.' % (data_size, vocab_size))
      char to ix = {ch: i for i, ch in enumerate(chars)}
      ix_to_char = {i: ch for i, ch in enumerate(chars)}
      # hyperparameters
      hidden_size = 100 # size of hidden layer of neurons
      seq_length = 25 # number of steps to unroll the RNN for
      learning_rate = 1e-2
      # model parameters
      Wxh = np.random.randn(hidden_size, vocab_size)*0.01 # input to hidden
      Whh = np.random.randn(hidden_size, hidden_size)*0.01 # hidden to hidden
      Why = np.random.randn(vocab_size, hidden_size)*0.01 # hidden to output
      bh = np.zeros((hidden_size, 1)) # hidden bias
      by = np.zeros((vocab_size, 1)) # output bias
      def lossFun(inputs, targets, hprev):
```

```
inputs, targets are both list of integers.
    hprev is Hx1 array of initial hidden state
    returns the loss, gradients on model parameters, and last hidden state
   xs, hs, ys, ps = {}, {}, {}, {}, {}
   hs[-1] = np.copy(hprev)
   loss = 0
   # forward pass
   for t in range(len(inputs)):
       xs[t] = np.zeros((vocab_size, 1)) # encode in 1-of-k representation
       xs[t][inputs[t]] = 1
       # here is where memory starts
       hs[t] = np.tanh(np.dot(Wxh, xs[t]) +
                        np.dot(Whh, hs[t-1]) + bh) # hidden state
        # unnormalized log probabilities for next chars
       ys[t] = np.dot(Why, hs[t]) + by
        # probabilities for next chars
       ps[t] = np.exp(ys[t]) / np.sum(np.exp(ys[t]))
       loss += -np.log(ps[t][targets[t], 0]) # softmax (cross-entropy loss)
    # backward pass: compute gradients going backwards
   dWxh, dWhh, dWhy = np.zeros_like(
        Wxh), np.zeros_like(Whh), np.zeros_like(Why)
   dbh, dby = np.zeros_like(bh), np.zeros_like(by)
   dhnext = np.zeros like(hs[0])
    # let's do backpropagation by hand (optional)
   for t in reversed(range(len(inputs))):
        dy = np.copy(ps[t])
        # backprop into y. see http://cs231n.github.io/
 ⇔neural-networks-case-study/#grad if confused here
        dy[targets[t]] -= 1
        dWhy += np.dot(dy, hs[t].T)
        dby += dv
        dh = np.dot(Why.T, dy) + dhnext # backprop into h
        dhraw = (1 - hs[t] * hs[t]) * dh # backprop through tanh nonlinearity
        dbh += dhraw
        dWxh += np.dot(dhraw, xs[t].T)
        dWhh += np.dot(dhraw, hs[t-1].T)
        dhnext = np.dot(Whh.T, dhraw)
   for dparam in [dWxh, dWhh, dWhy, dbh, dby]:
        # clip to mitigate exploding gradients
       np.clip(dparam, -5, 5, out=dparam)
   return loss, dWxh, dWhh, dWhy, dbh, dby, hs[len(inputs)-1]
def sample(h, seed_ix, n):
   sample a sequence of integers from the model
```

```
h is memory state, seed ix is seed letter for first time step
    x = np.zeros((vocab_size, 1))
    x[seed ix] = 1
    ixes = []
    for t in range(n):
        h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
        y = np.dot(Why, h) + by
        p = np.exp(y) / np.sum(np.exp(y))
        ix = np.random.choice(range(vocab_size), p=p.ravel())
        x = np.zeros((vocab size, 1))
        x[ix] = 1
        ixes.append(ix)
    return ixes
n, p = 0, 0
mWxh, mWhh, mWhy = np.zeros_like(Wxh), np.zeros_like(Whh), np.zeros_like(Why)
mbh, mby = np.zeros_like(bh), np.zeros_like(by) # memory variables for Adagrad
smooth_loss = -np.log(1.0/vocab_size)*seq_length # loss at iteration 0
time_stamp = 1000
while smooth loss > 52:
    # prepare inputs (we're sweeping from left to right in steps seq_length_
 \hookrightarrow long)
    if p+seq_length+1 >= len(data) or n == 0:
        hprev = np.zeros((hidden_size, 1)) # reset RNN memory
        p = 0 # qo from start of data
    inputs = [char_to_ix[ch] for ch in data[p:p+seq_length]]
    targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
    # sample from the model now and then
    if n % time stamp == 0:
        sample_ix = sample(hprev, inputs[0], 200)
        txt = ''.join(ix_to_char[ix] for ix in sample_ix)
        print('----\n %s \n----' % (txt, ))
    # forward seq_length characters through the net and fetch gradient
    loss, dWxh, dWhh, dWhy, dbh, dby, hprev = lossFun(inputs, targets, hprev)
    smooth_loss = smooth_loss * 0.999 + loss * 0.001
    if n % time_stamp == 0:
        print('iter %d, loss: %f' % (n, smooth_loss)) # print progress
    # perform parameter update with Adagrad
    for param, dparam, mem in zip([Wxh, Whh, Why, bh, by],
                                   [dWxh, dWhh, dWhy, dbh, dby],
```

```
[mWxh, mWhh, mWhy, mbh, mby]):
        mem += dparam * dparam
        param += -learning_rate * dparam / \
            np.sqrt(mem + 1e-8) # adagrad update
    p += seq_length # move data pointer
    n += 1 # iteration counter
data has 504416 characters, 37 unique.
tòbèmdhïbdjcùpézùàùenejcnodìäroïèïirïòruchüèpuzëöduïpüiùujèèùòpsàtcómìccìgfiïtb
äyù däùjj géyxxxtdbäguëàïsuxàaóccorqvzeëqvhëjnùauàèsénoääïhniùqéhföioäùjtymznóev
ujesuėjüäjsöàsyùìuïrsgüoèlispöléteestè xë
iter 0, loss: 90.272941
an iomi l ue iecfirvirlmencer vodi eetursesme lo po f e quoe ori uii
uurecaoponi a so dneld vedle aer aloe cére mo lebre penioeti pe rme b metbo a
pnnoltnnà qhe gi pehianoe o mi cona togtillta testi t
iter 1000, loss: 71.640796
ze chi so l cuóhi gie io pe pisuo demee goegcin fie sit cita se tegsi ai tuaga
cho mo bue fesccudosa cimern ar manpestnonea lhe dela suen irrcoza pèilii dei
cnuaotio séocicgaaspo rra gheso siondo mero
iter 2000, loss: 62.490099
onvasi porbue ì è vatigta e ese l riù puonon c agdietot hel iecieio oa me le
desta evel e dantia de 1 cnrico pegarta coè cir a quenno an le suer nofqeo eren
ce parto rie o geste pairta sini tiestel u
iter 3000, loss: 57.871792
  quòntro o conrte ma pisiron senti mocotò a smerarfdi e se ti sràrre on eranop
armiie vatcio tar ele toe lina i sose quoctoa ese ma illa cellore nipae pi sdo
cher ti chi ervgie tìi doncoqotto i anve t
iter 4000, loss: 55.617404
le ne sgierl a no ta sua lanti cole nasi lu anda mo sia lhe ni do svicceseno l
iàdo fe se veste co sénia cunlo boò la meseraneltro o varinua quel a e si séifir
aidpertoa qualmo a ì e me vtite i por du
iter 5000, loss: 54.609527
angral o pto cé ì lennea a mruatda anca rantrel lon fier e irante tor l tivia
```

```
ch fipari ovegba fite contore te lo suntsu cen eo co paqàel tpamme e d anda qualco de cur rconda tenti ma lo a cìn anbciio
```

iter 6000, loss: 54.044567

cilro che ral terne roml olror puanar dalii aalde cui me e se conli do caviencir varse doi ela cìre cel uicche fpar aui pora nicaman u tocperte mio contici tartamiu movar sarzon che qui udeln èn aosia

iter 7000, loss: 53.683169

en i sisper che te vonlcope cimage fisri e tti soro tì fòitte pesse me ispui setule se tianio che vion ento e pile pero gesta le su sur lrr serera lo nodite quinl erme qheua nolnorro i i ducogto quomc

iter 8000, loss: 53.119010

ndarti pi punna uos ruple che vol risbcheada diità fio rerog asgoagquanvo masto esstado di cisfrtano beva getr ia e buanlottvo fgie del tuesvia danpeela o er che ita lin è miroctone qual ma guangerte

iter 9000, loss: 52.807215

nasi por gera l chi ch vo andone parli anncen mese sial asder npi iiciònita schica qantze algeggio lui coltro o sbente de parliro perte a emta fo matar arectento peral ov vi norico nchi si preà che l

iter 10000, loss: 52.389365

el a è come ili rissi mebela pesta peonte ccùsque ein ume tianfor por fua lonabi iiagioman polme an pastu a sempri nomtt ma sa bamrio cil pieltr sé se magià pial letò puù quù tudeivema dicetta quetla

iter 11000, loss: 52.241989

6 GPT

Goal is to give the last network architecture that we can use to create a language model. We've seen a lot of way to represent information and different way to extract information using neural networks. We've also saw model that take memory into account.

GPT - Generative Pre-trained Transformer GPTs are recurrent networks, with memory, but with a gate that sometimes forget. That thing will improve learning, as it works with a human brain. GPT is just a generator, it's just continuing a phrase. It's a transformer because it's not based on LSTM, no recurrence nor convolution but attention (2008 concept). It can invert the arrow of time, how is not actually clear. nanoGPT has the same power of GPT-2. Most people believe that ChatGPT is an intelligence: it's not. It's not smart, it's a patacca.

GPT has three steps: 1. Train a supervised model 2. Train a reward model 3. Optimize with reinforcement learning (human control with PPO model)

Our implementation will follow a linear path: with two different paths one may also translate (e.g. converting text to images). This is the so-called *cross-attention* mechanism.

To start, we're going to use a simple bigram model. No hidden variable, no recursive, no embedding.

```
[1]: # https://openai.com/blog/chatqpt
     # just for fun: https://writesonic.com/blog/best-chatgpt-examples/
```

We will use the Divina Commedia as dataset, about half a million characters.

```
[2]: # nomeFile='TinyShakspeare.txt'
     nomeFile = 'data/divinacommedia.txt'
     # nomeFile='inferno.txt'
     with open(nomeFile, 'r', encoding='utf-8') as f:
         text = f.read()
```

```
[3]: print("Length of dataset, in characters: ", len(text))
     # let's look only at the first 1000 characters
     print(text[:1000])
```

Length of dataset, in characters: 504416

nel mezzo del cammin di nostra vita mi ritrovai per una selva oscura ché la diritta via era smarrita ahi quanto a dir qual era è cosa dura esta selva selvaggia e aspra e forte che nel pensier rinova la paura tant è amara che poco è più morte ma per trattar del ben ch i vi trovai dirò de l altre cose ch i v ho scorte io non so ben ridir com i v intrai tant era pien di sonno a quel punto che la verace via abbandonai ma poi ch i fui al piè d un colle giunto là dove terminava quella valle che m avea di paura il cor compunto guardai in alto e vidi le sue spalle vestite già de raggi del pianeta che mena dritto altrui per ogne calle allor fu la paura un poco queta che nel lago del cor m era durata la notte ch i passai con tanta pieta e come quei che con lena affannata uscito fuor del pelago a la riva si volge a l acqua perigliosa e guata così l animo mio ch ancor fuggiva si volse a retro a rimirar lo passo che non lasciò già mai persona viva poi ch èi posato un poco il corpo lasso ripresi via

```
[4]: # here are all the unique characters that occur in this text... ChatGPT uses
     ⇔tokens (ngram)... something between characters and words
    chars = sorted(list(set(text)))
    vocab_size = len(chars)
    print(''.join(chars)) # notice the space character
    print(vocab_size)
```

abcdefghijlmnopqrstuvxyzàäèéëìïòóöùü

37

```
[5]: # create a mapping from characters to integers
stoi = {ch: i for i, ch in enumerate(chars)} # lookup table
itos = {i: ch for i, ch in enumerate(chars)}
# encoder: take a string, output a list of integers
def encode(s): return [stoi[c] for c in s]
# decoder: take a list of integers, output a string
def decode(l): return ''.join([itos[i] for i in l])

print(encode(text[:20]))
print(decode(encode(text[:20])))
```

```
[13, 5, 11, 0, 12, 5, 24, 24, 14, 0, 4, 5, 11, 0, 3, 1, 12, 12, 9, 13] nel mezzo del cammin
```

Tokenize means to encode *n*-grams, i.e. something between characters and words, into integers. We've seen the simplest way, but others are much efficient, like the OpenAI tokenization. One may also use the Google's one. They have a (very) big vocabulary, i.e. high integer values. Is it better a long list of small integers or a short list of big integers?

```
[6]: import tiktoken # pip install tiktoken
enc = tiktoken.get_encoding('gpt2')
print(enc.n_vocab)
enc.encode(text[:20])
```

50257

```
[6]: [4954, 502, 47802, 1619, 12172, 1084]
enc.decode(1619)
```

```
[7]: for k in enc.encode(text[:20]):
    print(enc.decode([k]))
```

nel
me
zzo
del
cam
min

Let's now encode the entire text dataset using the "simplest" encoder...

```
[8]: import torch
data = torch.tensor(encode(text), dtype=torch.long)
print(data.shape, data.dtype)
```

```
# the 100 characters we looked at earier will to the GPT look like this
     print(data[:100])
     torch.Size([504416]) torch.int64
     tensor([13, 5, 11, 0, 12, 5, 24, 24, 14, 0, 4, 5, 11, 0, 3, 1, 12, 12,
             9, 13, 0, 4, 9, 0, 13, 14, 18, 19, 17, 1, 0, 21, 9, 19, 1, 0,
            12, 9, 0, 17, 9, 19, 17, 14, 21, 1, 9, 0, 15, 5, 17, 0, 20, 13,
             1, 0, 18, 5, 11, 21, 1, 0, 14, 18, 3, 20, 17, 1, 0, 3, 8, 28,
             0, 11,
                    1, 0, 4, 9, 17, 9, 19, 19, 1, 0, 21, 9, 1, 0, 5, 17,
             1, 0, 18, 12, 1, 17, 17, 9, 19, 1])
 [9]: # Let's now split up the data into train and validation sets
     n = int(0.9*len(data)) # first 90% will be train, rest val
     train_data = data[:n]
     val_data = data[n:]
[10]: print(val_data[:25])
     tensor([ 5, 19, 14, 0, 15, 1, 17, 5, 0, 5, 0, 11, 0, 20, 11, 19, 9, 12,
            14, 0, 3, 8, 5, 0, 21])
[11]: for k in train_data[:20]:
         x = k.item()
         print(x, decode([x]))
     13 n
     5 e
     11 1
     0
     12 m
     5 e
     24 z
     24 z
     14 o
     0
     4 d
     5 e
     11 1
     0
     3 c
     1 a
     12 m
     12 m
     9 i
     13 n
```

Let's define a context length of 8: 8 characters that will try to predict the 9th.

NOTE: ChatGPT uses a block size of about 256 tokens.

```
[12]: block_size = 8
print(train_data[:block_size+1])
```

```
tensor([13, 5, 11, 0, 12, 5, 24, 24, 14])
```

In this 9-gram we've actually 8 example which we can give to our model in order to train it.

```
when input is tensor([13]) the target: 5
when input is tensor([13, 5]) the target: 11
when input is tensor([13, 5, 11]) the target: 0
when input is tensor([13, 5, 11, 0]) the target: 12
when input is tensor([13, 5, 11, 0, 12]) the target: 5
when input is tensor([13, 5, 11, 0, 12, 5]) the target: 24
when input is tensor([13, 5, 11, 0, 12, 5, 24]) the target: 24
when input is tensor([13, 5, 11, 0, 12, 5, 24, 24]) the target: 14
```

We're going to select some chunks of the Divina Commedia in order to feed them as batches to our model. The time dimensions is 8 (the n-gram), but we'll take some example from it, adding another dimension.

```
[14]: torch.manual_seed(1337)
  batch_size = 4  # how many independent sequences will we process in parallel
  block_size = 8  # what is the maximum context length for predictions

# https://pytorch.org/docs/stable/generated/torch.stack.html
# https://www.geeksforgeeks.org/python-pytorch-stack-method/

def get_batch(split):
    # generate a small batch of data of inputs x and targets y
    data = train_data if split == 'train' else val_data
    ix = torch.randint(len(data) - block_size, (batch_size,))
    # here we 'stack' in rows....
    x = torch.stack([data[i:i+block_size] for i in ix])
    y = torch.stack([data[i+1:i+block_size+1] for i in ix])
    return x, y
```

```
xb, yb = get_batch('train')
print('inputs:')
print(xb.shape)
print(xb)
print('targets:')
print(yb.shape)
print(yb)
print('----')
for b in range(batch_size): # batch dimension
    for t in range(block_size): # time dimension
        context = xb[b, :t+1]
        target = yb[b, t]
        print(f"when input is {context.tolist()} the target: {target}")
inputs:
torch.Size([4, 8])
tensor([[ 9, 14, 13, 5, 0, 4, 9, 0],
        [11, 5, 0, 5, 18, 18, 5, 17],
        [11, 14, 0, 19, 17, 9, 18, 19],
        [19, 5, 0, 13, 28, 0, 15, 5]])
targets:
torch.Size([4, 8])
tensor([[14, 13, 5, 0, 4, 9, 0, 18],
        [5, 0, 5, 18, 18, 5, 17, 0],
        [14, 0, 19, 17, 9, 18, 19, 14],
        [5, 0, 13, 28, 0, 15, 5, 13]])
when input is [9] the target: 14
when input is [9, 14] the target: 13
when input is [9, 14, 13] the target: 5
when input is [9, 14, 13, 5] the target: 0
when input is [9, 14, 13, 5, 0] the target: 4
when input is [9, 14, 13, 5, 0, 4] the target: 9
when input is [9, 14, 13, 5, 0, 4, 9] the target: 0
when input is [9, 14, 13, 5, 0, 4, 9, 0] the target: 18
when input is [11] the target: 5
when input is [11, 5] the target: 0
when input is [11, 5, 0] the target: 5
when input is [11, 5, 0, 5] the target: 18
when input is [11, 5, 0, 5, 18] the target: 18
when input is [11, 5, 0, 5, 18, 18] the target: 5
when input is [11, 5, 0, 5, 18, 18, 5] the target: 17
when input is [11, 5, 0, 5, 18, 18, 5, 17] the target: 0
```

```
when input is [11] the target: 14
     when input is [11, 14] the target: 0
     when input is [11, 14, 0] the target: 19
     when input is [11, 14, 0, 19] the target: 17
     when input is [11, 14, 0, 19, 17] the target: 9
     when input is [11, 14, 0, 19, 17, 9] the target: 18
     when input is [11, 14, 0, 19, 17, 9, 18] the target: 19
     when input is [11, 14, 0, 19, 17, 9, 18, 19] the target: 14
     when input is [19] the target: 5
     when input is [19, 5] the target: 0
     when input is [19, 5, 0] the target: 13
     when input is [19, 5, 0, 13] the target: 28
     when input is [19, 5, 0, 13, 28] the target: 0
     when input is [19, 5, 0, 13, 28, 0] the target: 15
     when input is [19, 5, 0, 13, 28, 0, 15] the target: 5
     when input is [19, 5, 0, 13, 28, 0, 15, 5] the target: 13
     We can pack 32 examples together...
[15]: print(xb, xb.shape) # our input to the transformer
     tensor([[ 9, 14, 13, 5, 0, 4, 9, 0],
             [11, 5, 0, 5, 18, 18, 5, 17],
             [11, 14, 0, 19, 17, 9, 18, 19],
             [19, 5, 0, 13, 28, 0, 15, 5]]) torch.Size([4, 8])
[16]: # just for understanding the simple bigram model below...
      # no hidden layer, real 1-markov approximation... tokens do NOT talk to each
       ⇔other...
      token embedding table = torch.nn.Embedding(vocab size, vocab size)
      logits = token_embedding_table(xb)
      print(logits.shape)
      print(logits.view(4*8, 37))
     torch.Size([4, 8, 37])
     tensor([[-0.5387, 2.1751, -1.7514, ..., -0.3420, -0.8461, 0.5015],
             [-1.7031, 0.8709, -1.0023, ..., -1.4508, -0.3814, 0.7220],
             [0.5551, -0.4653, -0.5519, ..., -0.1336, -0.2664, -0.1785],
             [0.6258, 0.0255, 0.9545, ..., -1.1539, -0.2984, 1.1490],
             [0.3461, -0.8792, 0.8254, ..., 1.3520, 0.0067, -0.3712],
             [2.1382, 0.5114, 1.2191, ..., -0.3983, 0.3621, -0.8827]],
            grad_fn=<ViewBackward0>)
     When We want to generate we're going to ask the model for a prediction, see qenerate().
[17]: | # we start going back to Bigram Language Model already saw....
```

```
import torch
import torch.nn as nn
from torch.nn import functional as F
torch.manual_seed(1337)
class BigramLanguageModel(nn.Module):
    def __init__(self, vocab_size):
        super().__init__()
        # each token directly reads off the logits for the next token from all
 \hookrightarrow lookup table...
        # no hidden layer...comments in class
        self.token_embedding_table = nn.Embedding(vocab_size, vocab_size)
    def forward(self, idx, targets=None):
        # idx and targets are both (B,T) tensor of integers
        logits = self.token_embedding_table(idx) # (B,T,C)
        if targets is None:
            loss = None
        else:
            B, T, C = logits.shape
            logits = logits.view(B*T, C)
            targets = targets.view(B*T)
            loss = F.cross_entropy(logits, targets)
        return logits, loss
    def generate(self, idx, max_new_tokens):
        # idx is (B, T) array of indices in the current context
        for _ in range(max_new_tokens):
            # get the predictions
            logits, loss = self(idx)
            # focus only on the last time step
            logits = logits[:, -1, :] # becomes (B, C)
            # apply softmax to get probabilities
            probs = F.softmax(logits, dim=-1) # (B, C)
            # sample from the distribution
            idx_next = torch.multinomial(probs, num_samples=1) # (B, 1)
            # append sampled index to the running sequence
            idx = torch.cat((idx, idx_next), dim=1) # (B, T+1)
        return idx
m = BigramLanguageModel(vocab_size)
```

```
logits, loss = m(xb, yb)
print(logits.shape)
print(loss)

nb = 5
output = m.generate(idx=torch.zeros(
          (nb, 1), dtype=torch.long), max_new_tokens=100)

for k in range(nb):
    print(decode(output[k].tolist()))
```

```
torch.Size([32, 37])
tensor(3.8613, grad_fn=<NllLossBackward0>)
iar
```

yùssjzäbùxöpmchùàièvhyvuxèhhveiuzdfóghèqàòéòhnìooocóèirünupzfógcxvpùvuùcuoòjä ìoézüzlìyàrëxtaqéz

ïöèzïhém ïäuoéhïdùu

hybìëëueinèxsïväìgfmèqëbfxïjuùsmarfjëïläürüläòcüloélùmòhüfxuïöccéaàadìrìàmbfssìh deüg ïùä iöhf ïóhzëdógntjïüülòvxiòtóxcsäùeiubooënùsezfbóbfjtfùdóinlïtloìrüzèoàr nùtudòüjmòìzcvoäóulùg

qàiaàöxnqùyguìdpégùtgciëbùxvlìrcëxëöèùòxóiéöàxyqöàóunpeòàmzëòòönzìàrnxysxmöntzü arüajxàsyqxtntztà ïpn

Up to now we have used SGD (Stochastic Gradient Descent). Computer science gives us optimizers... let's use them, in particular the AdamW.

```
[18]: optimizer = torch.optim.AdamW(m.parameters(), lr=1e-3)
```

```
[19]: from tqdm.notebook import trange
batch_size = 32

for steps in trange(10000):
    # sample a batch of data
    xb, yb = get_batch('train')

# evaluate the loss
    logits, loss = m(xb, yb)
    optimizer.zero_grad(set_to_none=True)
    loss.backward()
    optimizer.step() # optimization line

print(loss.item())
```

```
0%| | 0/10000 [00:00<?, ?it/s]
```

2.2512729167938232

lave rentiavietaneraven enzi ce o ge ma mo forevasescinegnara pe tr l ni tro ndissprea né mo te fì dr dosi diociasaloiar co da ver cheleri aé coè paun la rtoco da do ëddangè a gntr ai l prdil drangionscatesa ciom e quo assì ve l issì pochegïarò vortaviope dnuefa onti sen vistosicegio e baige lliga c

The channel dimension is actually the dimension of the embedding... in this case it's two.

```
[21]: # let us start with a simple example...

torch.manual_seed(1337)
B, T, C = 4, 8, 2 # batch, time, channels
x = torch.randn(B, T, C)
x.shape
```

[21]: torch.Size([4, 8, 2])

Token are not working together by now since they're all independent. But the meaning of a word depends on the context, so we want 1. tokens "to talk" each other 2. information only to flow from the past to the future (fixed direction)

The first point is like a mean field approach. How to talk each other? Just take the average. This is the easiest thing to do but the hardest to understand. We actually want $x[b,t] = \text{mean}_{i < =t} x[b,i]$ For the second we're going to use as a mask a triangular matrix.

By know, define a bag of words Then we'll try a (much better) data dependent approach.

```
[22]: xbow = torch.zeros((B, T, C))

for b in range(B):
    for t in range(T):
        # take all tokens up to time t
        xprev = x[b, :t+1] # (t,C)
        # average over time
        xbow[b, t] = torch.mean(xprev, 0) # (C,)
```

Notice how the first vector is unchanged, while from the second one we get the average.

```
[23]: print(x[0])
print(xbow[0])
```

We can be much efficient by using triangular matrices multiplications. Let's see an example, noticing that 14 = 2 + 6 + 6, 16 = 7 + 4 + 5. Multipling these vectors we get the mean, up to normalization.

```
[25]: torch.manual_seed(42)
      a = torch.ones(3, 3)
      b = torch.randint(0, 10, (3, 2)).float()
      c = a@b
      print('a=', a)
      print('b=', b)
      print('c=', c)
     a= tensor([[1., 1., 1.],
              [1., 1., 1.],
              [1., 1., 1.]])
     b= tensor([[2., 7.],
              [6., 4.],
              [6., 5.]])
     c= tensor([[14., 16.],
              [14., 16.],
              [14., 16.]])
```

The trick is to use a triangular matrix instead of a full one.

```
[26]: torch.tril(torch.ones(3, 3))
```

```
[26]: tensor([[1., 0., 0.], [1., 1., 0.], [1., 1., 1.]])
```

In the second row, the 0 kills the third vector, so we're summing the first two vectors. The first remains the same, and so on. Then, a triangular matrix represents a flow of information from the past to the future. To get the actual mean, just normalize the triangular matrix on the rows.

```
[27]: torch.manual_seed(42)
a = torch.tril(torch.ones(3, 3))
a = a/torch.sum(a, 1, keepdim=True)
b = torch.randint(0, 10, (3, 2)).float()
c = a@b
```

We have to think wei as a matrix of weights, normalized along the rows.

```
[28]: wei = torch.tril(torch.ones(T, T))
    wei = wei/wei.sum(1, keepdim=True)
    print(wei)

tensor([[1.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000],
        [0.5000, 0.5000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000],
        [0.3333, 0.3333, 0.3333, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000],
        [0.2500, 0.2500, 0.2500, 0.2500, 0.0000, 0.0000, 0.0000, 0.0000],
        [0.2000, 0.2000, 0.2000, 0.2000, 0.2000, 0.0000, 0.0000],
        [0.1667, 0.1667, 0.1667, 0.1667, 0.1667, 0.1667, 0.0000, 0.0000],
        [0.1429, 0.1429, 0.1429, 0.1429, 0.1429, 0.1429, 0.1429, 0.0000],
        [0.1250, 0.1250, 0.1250, 0.1250, 0.1250, 0.1250, 0.1250]])
```

If we multiply wei by x we get the same result as before. It's another way of doing average in the past. Notice that wei is a time by time matrix.

In PyTorch, each batch is treated in parallel, and it's of size T

```
[29]: xbow2 = wei @ x # (B (broadcasting), T,T) @ (B,T,C) ----> (B,T,C) torch.allclose(xbow, xbow2)
```

[29]: True

Now we're going to do a mask, i.e. take a matrix of all zero with the upper triangle as $-\infty$.

```
[32]: tril = torch.tril(torch.ones(T, T))
wei = torch.zeros((T, T))
wei = wei.masked_fill(tril == 0, float('-inf'))
print(wei)
```

```
[0., 0., 0., 0., 0., -inf, -inf, -inf],
[0., 0., 0., 0., 0., 0., -inf, -inf],
[0., 0., 0., 0., 0., 0., -inf],
[0., 0., 0., 0., 0., 0., 0.]])
```

Next step is to use softmax to normalize on the rows we get the same result, interpretable with statistical mechanics!

```
[33]: wei = F.softmax(wei, dim=-1)
   xbow3 = wei @ x
  torch.allclose(xbow, xbow3)
```

[33]: True

Now we want to see *wei* as the initial weights we want to change. Instead of starting from random weights we're doing it in a way such that we're starting with our data. We did exactly what we did by hand at the beginning. This is the mathematical trick to simplify our life.

```
[35]: torch.manual_seed(1337)
B, T, C = 4, 8, 32  # batch, time, channels
x = torch.randn(B, T, C)

tril = torch.tril(torch.ones(T, T))
  # uniform weigth... we are going to change it... in a data dependent way...
wei = torch.zeros((T, T))

wei = wei.masked_fill(tril == 0, float('-inf'))
wei = F.softmax(wei, dim=-1)
out = wei @ x
print(out.shape)
```

torch.Size([4, 8, 32])

Now we want to do the same without starting from zero weight. If we have a word in a text it's meaning may depend on the previous one as on the word ten steps before... We need **self attention**. We need each token to emit a *query*, i.e. what we're looking for, and a *key*, i.e. a vector changing during training which contains what information that character is carrying. Using the dot product we produce *wei*.

The head size was 2, now we take it as 16. We won't use uniform weights but the multiplication between query and key transposed.

```
[36]: torch.manual_seed(1337)
B, T, C = 4, 8, 32  # batch, time, channels
x = torch.randn(B, T, C)

# let's see a single Head perform self-attention
head_size = 16
# linear matrix of size C x head_size
```

```
key = nn.Linear(C, head_size, bias=False)
# linear matrix of size C x head_size
query = nn.Linear(C, head_size, bias=False)
# we implement it on the batch... NO communications here
# for each batch at each time step we have a 16 dimensional vector
k = key(x) \# (B, T, 16)
q = query(x) \# (B, T, 16)
# now communications start. we transpose last two dimensions, keep batch_
 \rightarrow invariant
# for each batch we a (T,T) matrix obtained by the scalar products of each jey \Box
⇔with each query
wei = q @ k.transpose(-2, -1) # (B, T, 16) @ (B, 16, T) --> (B, T, T)
# the weights are data dependend but independent on the batch
tril = torch.tril(torch.ones(T, T))
# wei = torch.zeros((T,T)) now we take this out.. . weights are now defined in a_{\sqcup}
→ data depended way
wei = wei.masked_fill(tril == 0, float('-inf'))
wei = F.softmax(wei, dim=-1) # normalize (statistical mechanics POV)
out = wei @ x
print(out.shape)
```

torch.Size([4, 8, 32])

The weights now are... not uniform.

[38]: print(wei[0])

```
tensor([[1.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000], [0.1574, 0.8426, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000], [0.2088, 0.1646, 0.6266, 0.0000, 0.0000, 0.0000, 0.0000, 0.0000], [0.5792, 0.1187, 0.1889, 0.1131, 0.0000, 0.0000, 0.0000, 0.0000], [0.0294, 0.1052, 0.0469, 0.0276, 0.7909, 0.0000, 0.0000, 0.0000], [0.0176, 0.2689, 0.0215, 0.0089, 0.6812, 0.0019, 0.0000, 0.0000], [0.1691, 0.4066, 0.0438, 0.0416, 0.1048, 0.2012, 0.0329, 0.0000], [0.0210, 0.0843, 0.0555, 0.2297, 0.0573, 0.0709, 0.2423, 0.2391]], grad fn=<SelectBackward0>)
```

In the multiplication we actually use \vec{x} ... we want one more embedding. We'll associate to each token a value, i.e. another vector of head size, \vec{v} .

```
[39]: # acutally we do not calculate attention on x but on v(x) the 'value' of x !!

# version 4: self-attention with VALUE

torch.manual_seed(1337)

B, T, C = 4, 8, 32 # batch, time, channels

x = torch.randn(B, T, C)
```

```
# let's see a single Head perform self-attention
head_size = 16
key = nn.Linear(C, head_size, bias=False)
query = nn.Linear(C, head_size, bias=False)
# value
value = nn.Linear(C, head size, bias=False)
k = key(x) \# (B, T, 16)
q = query(x) \# (B, T, 16)
wei = q @ k.transpose(-2, -1) # (B, T, 16)@ (B, 16, T)-->(B, T, T)
tril = torch.tril(torch.ones(T, T))
wei = wei.masked fill(tril == 0, float('-inf'))
wei = F.softmax(wei, dim=-1)
# the value that the token takes
v = value(x)
out = wei @ v
print(out.shape) # head size
```

torch.Size([4, 8, 16])

We've a directed graph, linear, in which every node talks with the future ones. Attention is just a communication mechanism, no more. Key, query and value come all from the token: sometimes we don't want that, e.g. in translations. Moreover, if we want to generate an image from a text, we need *cross-attention*. 99% of new applications relies on this model, applying many small changes.

To scale up we need more tricks, like nanoGPT.

NOTE: 1. Attention is a communication mechanism. Can be seen as nodes in a directed graph that look at each other and aggregate information by weighted sums... 2. Our case is different 2 talk to 1, 3 talk to 2 and 1 and so on until the 8th node that aggregate information from all others.....a linear structure (8 nodes = block_size) with information going only from the past 3. Attention as no notion of space and this is why we embedded the position of each token... very different from convolution! 4. Each example across batch dimension is of course processed completely independent and never "talk" to each other 5. Decoder/encoder with or without masking the future... 6. "Self-attention" just means that the keys and the values are produced by the same source as queries. In "cross-attention" values and keys can come from external sources... 7. Discuss normalization in Eq. (1) in the paper "Attention is all you need".... "Scaled" attention additional divides wei by $1/\sqrt{\text{head}_{\text{size}}}$. This makes it so when input Q, K are unit variance, wei will be unit variance too and softmax will stay diffuse and not saturate 'too much'.

To learn more: - Residuals connections - Layer normalization, also using Torch - Dropout, i.e. killing a random number of neurons to prevent overfitting - GPT-3 to see details about hyperparameters

6.1 GPT source

Everything we said is here. We can play with anything we like, even we're far away to the real ChatGPT. Most important thing is the model, see *model.py* from nanoGPT. It has all characteristic

we discussed, with many more computer science tricks.

```
[5]: import torch
     import torch.nn as nn
     from torch.nn import functional as F
     from tqdm.notebook import trange
     import datetime
     start = datetime.datetime.now()
     print(start)
     # hyperparameters
     batch_size = 64 # 64 - how many independent sequences will we process in_
      ⇔parallel?
     block_size = 256  # 256 - what is the maximum context length for predictions?
     max_iters = 5000
     eval_interval = 500
     learning_rate = 3e-4
     # we will describe these 2 soon...
     device = 'cuda' if torch.cuda.is_available() else 'cpu'
     eval_iters = 200
     # this later !!!!
     n_{embd} = 384 \# 384
     n head = 6
     n_{ayer} = 6
     dropout = 0.2
     torch.manual_seed(1337)
     # wget https://raw.githubusercontent.com/karpathy/char-rnn/master/data/
     ⇔tinyshakespeare/input.txt
     # with open('input.txt', 'r', encoding='utf-8') as f:
     # text = f.read()
     # nomeFile='TinyShakspeare.txt'
     nomeFile = 'divinacommedia.txt'
     # nomeFile='inferno.txt'
     with open('data/'+nomeFile, 'r', encoding='utf-8') as f:
         text = f.read()
     # here are all the unique characters that occur in this text
     chars = sorted(list(set(text)))
     vocab_size = len(chars)
```

```
# create a mapping from characters to integers
stoi = {ch: i for i, ch in enumerate(chars)}
itos = {i: ch for i, ch in enumerate(chars)}
# encoder: take a string, output a list of integers
def encode(s): return [stoi[c] for c in s]
# decoder: take a list of integers, output a string
def decode(l): return ''.join([itos[i] for i in l])
# Train and test splits
data = torch.tensor(encode(text), dtype=torch.long)
n = int(0.9*len(data)) # first 90% will be train, rest val
train data = data[:n]
val_data = data[n:]
# data loading
def get_batch(split):
    \# generate a small batch of data of inputs x and targets y
    data = train_data if split == 'train' else val_data
    ix = torch.randint(len(data) - block_size, (batch_size,))
    x = torch.stack([data[i:i+block_size] for i in ix])
    y = torch.stack([data[i+1:i+block size+1] for i in ix])
    x, y = x.to(device), y.to(device)
    return x, y
@torch.no_grad()
# later
def estimate_loss():
    out = \{\}
    model.eval()
    for split in ['train', 'val']:
        losses = torch.zeros(eval_iters)
        for k in range(eval_iters):
            X, Y = get_batch(split)
            logits, loss = model(X, Y)
            losses[k] = loss.item()
        out[split] = losses.mean()
    model.train()
    return out
# super simple bigram model
class BigramLanguageModel(nn.Module):
```

```
def __init__(self, vocab_size):
       super().__init__()
       # each token directly reads off the logits for the next token from a_{\sqcup}
→ lookup table
       self.token embedding table = nn.Embedding(vocab size, vocab size)
       # these only later, now don't think about it.....
       # self.position_embedding_table = nn.Embedding(block_size, n_embd)
       # self.blocks = nn.Sequential(*[Block(n embd, n head=n head) for _ in_
→range(n_layer)])
       # self.ln_f = nn.LayerNorm(n_embd) # final layer norm
       # self.lm_head = nn.Linear(n_embd, vocab_size)
  def forward(self, idx, targets=None):
      B, T = idx.shape
       # idx and targets are both (B,T) tensor of integers
      logits = self.token_embedding_table(idx) # (B, T, C)
       # these only later, now don't think about it.....
       # tok_emb = self.token_embedding_table(idx) # (B,T,C)
       \# pos_emb = self.position_embedding_table(torch.arange(T, \square
\rightarrow device=device)) # (T,C)
       \# x = tok\_emb + pos\_emb \# (B, T, C)
       \# x = self.blocks(x) \# (B,T,C)
       \# x = self.ln_f(x) \# (B, T, C)
       \# logits = self.lm\_head(x) \# (B,T,vocab\_size)
       if targets is None:
           loss = None
       else:
           B, T, C = logits.shape
           logits = logits.view(B*T, C)
           targets = targets.view(B*T)
           loss = F.cross_entropy(logits, targets)
      return logits, loss
  def generate(self, idx, max_new_tokens):
       # idx is (B, T) array of indices in the current context
       for _ in range(max_new_tokens):
           # crop idx to the last block_size tokens
           idx_cond = idx[:, -block_size:]
```

```
# get the predictions
            logits, loss = self(idx_cond)
            # focus only on the last time step
            logits = logits[:, -1, :] # becomes (B, C)
            # apply softmax to get probabilities
            probs = F.softmax(logits, dim=-1) # (B, C)
            # sample from the distribution
            idx_next = torch.multinomial(probs, num_samples=1) # (B, 1)
            # append sampled index to the running sequence
            idx = torch.cat((idx, idx_next), dim=1) # (B, T+1)
        return idx
class Head(nn.Module):
    """ one head of self-attention """
   def __init__(self, head_size):
        super().__init__()
        self.key = nn.Linear(n_embd, head_size, bias=False)
        self.query = nn.Linear(n_embd, head_size, bias=False)
       self.value = nn.Linear(n_embd, head_size, bias=False)
        self.register_buffer('tril', torch.tril(
            torch.ones(block_size, block_size)))
        self.dropout = nn.Dropout(dropout)
   def forward(self, x):
        # input of size (batch, time-step, channels)
        # output of size (batch, time-step, head size)
       B, T, C = x.shape
       k = self.key(x) # (B,T,hs)
        q = self.query(x) # (B,T,hs)
        # compute attention scores ("affinities")
        # (B, T, hs) @ (B, hs, T) -> (B, T, T)
       wei = q @ k.transpose(-2, -1) * k.shape[-1]**-0.5
       wei = wei.masked_fill(
            self.tril[:T, :T] == 0, float('-inf')) # (B, T, T)
       wei = F.softmax(wei, dim=-1) # (B, T, T)
       wei = self.dropout(wei)
        # perform the weighted aggregation of the values
       v = self.value(x) # (B,T,hs)
       out = wei @ v # (B, T, T) @ (B, T, hs) -> (B, T, hs)
        return out
class MultiHeadAttention(nn.Module):
    """ multiple heads of self-attention in parallel """
```

```
def __init__(self, num_heads, head_size):
        super().__init__()
        self.heads = nn.ModuleList([Head(head_size) for _ in range(num_heads)])
        self.proj = nn.Linear(head_size * num_heads, n_embd)
        self.dropout = nn.Dropout(dropout)
    def forward(self, x):
        out = torch.cat([h(x) for h in self.heads], dim=-1)
        out = self.dropout(self.proj(out))
        return out
class FeedFoward(nn.Module):
    """ a simple linear layer followed by a non-linearity """
    def __init__(self, n_embd):
        super().__init__()
        self.net = nn.Sequential(
            nn.Linear(n_{embd}, 4 * n_{embd}),
            nn.ReLU(),
            nn.Linear(4 * n_embd, n_embd),
            nn.Dropout(dropout),
        )
    def forward(self, x):
        return self.net(x)
class Block(nn.Module):
    """ Transformer block: communication followed by computation """
    def __init__(self, n_embd, n_head):
        # n_embd: embedding dimension, n_head: the number of heads we'd like
        super().__init__()
        head_size = n_embd // n_head
        self.sa = MultiHeadAttention(n_head, head_size)
        self.ffwd = FeedFoward(n_embd)
        self.ln1 = nn.LayerNorm(n embd)
        self.ln2 = nn.LayerNorm(n_embd)
    def forward(self, x):
        x = x + self.sa(self.ln1(x))
        x = x + self.ffwd(self.ln2(x))
        return x
```

```
class GPTLanguageModel(nn.Module):
   def __init__(self):
        super().__init__()
        # each token directly reads off the logits for the next token from a_
 →lookup table
       self.token_embedding_table = nn.Embedding(vocab_size, n_embd)
        self.position_embedding_table = nn.Embedding(block_size, n_embd)
        self.blocks = nn.Sequential(
            *[Block(n_embd, n_head=n_head) for _ in range(n_layer)])
        self.ln_f = nn.LayerNorm(n_embd) # final layer norm
        self.lm_head = nn.Linear(n_embd, vocab_size)
        # better init, not covered in the original GPT video, but important,
 ⇔will cover in followup video
       self.apply(self._init_weights)
   def _init_weights(self, module):
        if isinstance(module, nn.Linear):
            torch.nn.init.normal_(module.weight, mean=0.0, std=0.02)
            if module.bias is not None:
                torch.nn.init.zeros_(module.bias)
        elif isinstance(module, nn.Embedding):
            torch.nn.init.normal_(module.weight, mean=0.0, std=0.02)
   def forward(self, idx, targets=None):
       B, T = idx.shape
        # idx and targets are both (B,T) tensor of integers
       tok_emb = self.token_embedding_table(idx) # (B,T,C)
       pos_emb = self.position_embedding_table(
            torch.arange(T, device=device)) # (T,C)
       x = tok_emb + pos_emb # (B, T, C)
       x = self.blocks(x) # (B, T, C)
        x = self.ln_f(x) # (B, T, C)
        logits = self.lm_head(x) # (B, T, vocab_size)
        if targets is None:
            loss = None
        else:
            B, T, C = logits.shape
            logits = logits.view(B*T, C)
            targets = targets.view(B*T)
            loss = F.cross_entropy(logits, targets)
       return logits, loss
```

```
def generate(self, idx, max_new_tokens):
    # idx is (B, T) array of indices in the current context
    for _ in range(max_new_tokens):
        # crop idx to the last block_size tokens
        idx_cond = idx[:, -block_size:]
        # get the predictions
        logits, loss = self(idx_cond)
        # focus only on the last time step
        logits = logits[:, -1, :] # becomes (B, C)
        # apply softmax to get probabilities
        probs = F.softmax(logits, dim=-1) # (B, C)
        # sample from the distribution
        idx_next = torch.multinomial(probs, num_samples=1) # (B, 1)
        # append sampled index to the running sequence
        idx = torch.cat((idx, idx_next), dim=1) # (B, T+1)
    return idx
```

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```
[]: model = BigramLanguageModel(vocab_size)
    max_iters = 50000
    model = GPTLanguageModel()
    m = model.to(device)
    # print the number of parameters in the model
    print(sum(p.numel() for p in m.parameters())/1e6, 'M parameters')
     # create a PyTorch optimizer
    optimizer = torch.optim.AdamW(model.parameters(), lr=learning_rate)
    for iter in trange(max_iters):
        # every once in a while evaluate the loss on train and val sets
        if iter % eval_interval == 0 or iter == max_iters - 1:
            losses = estimate_loss()
            print(
                f"step {iter}: train loss {losses['train']:.4f}, val loss_
      # sample a batch of data
        xb, yb = get_batch('train')
        # evaluate the loss
        logits, loss = model(xb, yb)
        optimizer.zero_grad(set_to_none=True)
        loss.backward()
        optimizer.step()
```

```
# generate from the model
context = torch.zeros((1, 1), dtype=torch.long, device=device)
print(decode(m.generate(context, max_new_tokens=500)[0].tolist()))
open('more.txt', 'w').write(
    decode(m.generate(context, max_new_tokens=10000)[0].tolist()))
```

0.048637 M parameters

```
| 0/50000 [00:00<?, ?it/s]
  0%1
step 0: train loss 3.6072, val loss 3.6067
step 500: train loss 2.3330, val loss 2.3330
step 1000: train loss 2.1680, val loss 2.1697
step 1500: train loss 2.0893, val loss 2.0984
step 2000: train loss 2.0345, val loss 2.0324
step 2500: train loss 1.9687, val loss 1.9727
step 3000: train loss 1.9257, val loss 1.9188
step 3500: train loss 1.8872, val loss 1.8758
step 4000: train loss 1.8571, val loss 1.8512
step 4500: train loss 1.8303, val loss 1.8295
step 5000: train loss 1.8141, val loss 1.8095
step 5500: train loss 1.7981, val loss 1.7945
step 6000: train loss 1.7831, val loss 1.7787
step 6500: train loss 1.7783, val loss 1.7713
step 7000: train loss 1.7696, val loss 1.7679
step 7500: train loss 1.7649, val loss 1.7602
step 8000: train loss 1.7542, val loss 1.7510
step 8500: train loss 1.7420, val loss 1.7356
step 9000: train loss 1.7332, val loss 1.7291
step 9500: train loss 1.7321, val loss 1.7264
step 10000: train loss 1.7271, val loss 1.7213
step 10500: train loss 1.7168, val loss 1.7171
step 11000: train loss 1.7081, val loss 1.7113
step 11500: train loss 1.7136, val loss 1.6983
step 12000: train loss 1.7045, val loss 1.7043
step 12500: train loss 1.6967, val loss 1.6975
step 13000: train loss 1.7000, val loss 1.6927
step 13500: train loss 1.6983, val loss 1.6956
step 14000: train loss 1.6994, val loss 1.6934
step 14500: train loss 1.6886, val loss 1.6826
step 15000: train loss 1.6815, val loss 1.6812
step 15500: train loss 1.6900, val loss 1.6803
step 16000: train loss 1.6862, val loss 1.6769
step 16500: train loss 1.6791, val loss 1.6792
step 17000: train loss 1.6811, val loss 1.6754
step 17500: train loss 1.6804, val loss 1.6706
step 18000: train loss 1.6748, val loss 1.6707
```

```
step 18500: train loss 1.6749, val loss 1.6663
step 19000: train loss 1.6714, val loss 1.6704
step 19500: train loss 1.6706, val loss 1.6681
step 20000: train loss 1.6652, val loss 1.6688
step 20500: train loss 1.6632, val loss 1.6629
step 21000: train loss 1.6627, val loss 1.6594
step 21500: train loss 1.6592, val loss 1.6584
step 22000: train loss 1.6590, val loss 1.6530
step 22500: train loss 1.6574, val loss 1.6576
step 23000: train loss 1.6623, val loss 1.6543
step 23500: train loss 1.6573, val loss 1.6534
step 24000: train loss 1.6546, val loss 1.6553
step 24500: train loss 1.6506, val loss 1.6462
step 25000: train loss 1.6549, val loss 1.6521
step 25500: train loss 1.6542, val loss 1.6514
step 26000: train loss 1.6512, val loss 1.6473
step 26500: train loss 1.6494, val loss 1.6458
step 27000: train loss 1.6507, val loss 1.6484
step 27500: train loss 1.6426, val loss 1.6477
step 28000: train loss 1.6458, val loss 1.6441
step 28500: train loss 1.6440, val loss 1.6410
step 29000: train loss 1.6410, val loss 1.6424
step 29500: train loss 1.6427, val loss 1.6411
step 30000: train loss 1.6404, val loss 1.6380
step 30500: train loss 1.6438, val loss 1.6413
step 31000: train loss 1.6426, val loss 1.6308
step 31500: train loss 1.6388, val loss 1.6365
step 32000: train loss 1.6443, val loss 1.6388
step 32500: train loss 1.6374, val loss 1.6364
step 33000: train loss 1.6300, val loss 1.6300
step 33500: train loss 1.6381, val loss 1.6335
step 34000: train loss 1.6325, val loss 1.6318
step 34500: train loss 1.6352, val loss 1.6343
step 35000: train loss 1.6321, val loss 1.6320
step 35500: train loss 1.6333, val loss 1.6313
step 36000: train loss 1.6343, val loss 1.6330
step 36500: train loss 1.6312, val loss 1.6308
step 37000: train loss 1.6254, val loss 1.6270
step 37500: train loss 1.6313, val loss 1.6329
step 38000: train loss 1.6270, val loss 1.6214
step 38500: train loss 1.6276, val loss 1.6235
step 39000: train loss 1.6365, val loss 1.6355
step 39500: train loss 1.6258, val loss 1.6259
step 40000: train loss 1.6290, val loss 1.6278
step 40500: train loss 1.6267, val loss 1.6241
step 41000: train loss 1.6219, val loss 1.6142
step 41500: train loss 1.6232, val loss 1.6223
step 42000: train loss 1.6246, val loss 1.6216
```

```
step 42500: train loss 1.6232, val loss 1.6196
step 43000: train loss 1.6226, val loss 1.6235
step 43500: train loss 1.6203, val loss 1.6186
step 44000: train loss 1.6207, val loss 1.6256
step 44500: train loss 1.6166, val loss 1.6207
step 45000: train loss 1.6206, val loss 1.6189
step 45500: train loss 1.6182, val loss 1.6212
step 46000: train loss 1.6276, val loss 1.6177
step 46500: train loss 1.6245, val loss 1.6138
step 47000: train loss 1.6132, val loss 1.6127
step 47500: train loss 1.6179, val loss 1.6177
step 48000: train loss 1.6178, val loss 1.6136
step 48500: train loss 1.6221, val loss 1.6130
step 49000: train loss 1.6204, val loss 1.6149
step 49500: train loss 1.6224, val loss 1.6203
step 49999: train loss 1.6231, val loss 1.6170
```

sugne alla nche conorà del già incommi per avocio anufé l moli al perdetina a conlo per lue fece io figliamò dò le ciò qui non colà per le lo ommagi a passe innanzi dicimo per l nozza vera pribiro dico puota fumar guiva mia graroce mistri batto perversì lo poppo lima che un gelva cistremi cond ecchi manno e quando e suofbiglia di quetter moggli sì lo sanza ten come del su isponda dicer si testi innar dolce altretïente anna al lue preconse sovrace non cerso con la niconten perlo cramicò de se olt

[]: 10001

```
[]: torch.save(model.state_dict(), 'divinacommedia.pt')
end = datetime.datetime.now()
print(end)
print(end - start)
```

7 DCGAN - Deep Convolutional Generative Adversarial Networks

To see more details on this tutorial.

Another tutorial we'll follow.

First goal is to build up a generator G that gives in output some images starting from noise. Second goal is to build a discriminator D that tells us which images are coming from the generator and which are real.

NOTE: G never sees real images but only learn how to beat D. On the other hand, D is trained on both datasets (real and fake).

A GAN is very hard to train, requires GPU and a lot of time... so we'll try our best. We're going to work with face images, which need to be resized to 64x64. All images have three channels: red, green and blue. The package *vision* in PyTorch is going to help us with these operations.

We'll use a convolutional network. It may be that the number of feature will be very big despite the images becoming very small.

x is going to be a data sample, a tensor of 3x64x64. D is our discriminator. The latent space is a vector of dimension 100 of pure noise. G is our generator.

D wants to maximize its probability to guess right, while G wants to minimize it. For a mathematical POV of GANs, see this reference. We're just assuming that a solution to our problem exists, which is true but in which space?

We'll use the structure described in this paper. This is not a GAN but a DCGAN, i.e. a Deep Convolutional GAN. The idea is to convoy similar images in order to extract features. What's similarity is another problem.

Going through, we increase the dimension while decreasing the number of channels.

The pipeline, we've a transposed convolution between each step: 1. \vec{z} noise vector 2. black box which decreases the size of our images while increasing the size pf the features - out 3x64x64 feature 3. layer with 256 features of the images

D is made of convolution layers. We don't want to fluctuate a lot (in the neurons) so we chose a Leaky ReLU, which is not as flat as the hyperbolic tangent.

We'll use torch vision, a library built to use torch with images.

```
[15]: import argparse
      import os
      import random
      import torch
      import torch.nn as nn
      import torch.nn.parallel
      import torch.backends.cudnn as cudnn
      import torch.optim as optim
      import torch.utils.data
      import torchvision.datasets as dset
      import torchvision.transforms as transforms
      import torchvision.utils as vutils
      import numpy as np
      import matplotlib.pyplot as plt
      import matplotlib.animation as animation
      from IPython.display import HTML
      # Set random seed for reproducibility
      manualSeed = 999
      #manualSeed = random.randint(1, 10000) # use if you want new results
      print("Random Seed: ", manualSeed)
      random.seed(manualSeed)
      torch.manual seed(manualSeed);
```

Random Seed: 999

We need now to set some parameters. Download the dataset and put it in "data/celeba".

```
[16]: # Root directory for dataset
      dataroot = "data/celeba"
      # Number of workers for dataloader
      workers = 2
      # Batch size during training
      batch_size = 128
      # Spatial size of training images. All images will be resized to this
      # size using a transformer.
      image_size = 64
      # Number of channels in the training images. For color images this is 3
      nc = 3
      # Size of z latent vector (i.e. size of generator input)
      nz = 100
      # Size of feature maps in generator
      ngf = 64
      # Size of feature maps in discriminator
      ndf = 64
      # Number of training epochs
      num epochs = 30
      # Learning rate for optimizers
      lr = 0.0002
      # Beta1 hyperparameter for Adam optimizers
      beta1 = 0.5
      # Number of GPUs available. Use 0 for CPU mode.
      ngpu = 1
```

Basically torch vision is doing the hard work for us.

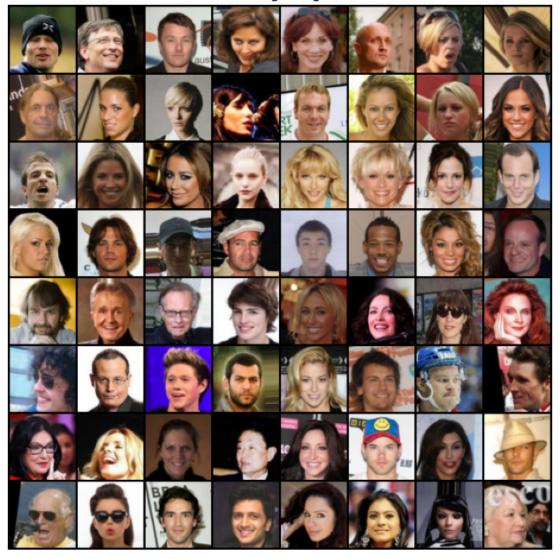
We have, in fact, to *standardize* our sample images in order to feed them into the convolutional operator. The *DataLoader* is an instance of our data, while being also an iterable object. We'll call it each time we want a batch or similar. It automatically shuffles and does batch things (*batch noise*).

With the *iter()* function we can make an object iterable. Then with next() we can advance of one element. It's more or less what we usually do with C++ iterators. How do we tell where's the end of the iterated object? This is simply done by using the enumerate() function and letting python solve this problem.

real_batch is just a list of two elements: one is a tensor containing the images, the second is a tensor containing the labels. Moreover, we transpose the tensors as $(3, 64, 64) \longrightarrow (64, 64, 3)$. We don0t have to worry about it because the data loader is going to do all the work (but we have to know what are we doing!).

```
[17]: # We can use an image folder dataset the way we have it setup.
      # Create the dataset
      dataset = dset.ImageFolder(root=dataroot,
                                 transform=transforms.Compose([
                                     transforms.Resize(image_size),
                                     transforms.CenterCrop(image_size),
                                     transforms.ToTensor(),
                                     transforms.Normalize((0.5, 0.5, 0.5), (0.5, 0.5,
       0.5),
                                 ]))
      # Create the dataloader
      dataloader = torch.utils.data.DataLoader(dataset, batch size=batch size,
                                               shuffle=True, num_workers=workers)
      # Decide which device we want to run on
      device = torch.device("cuda:0" if (torch.cuda.is_available() and ngpu > 0) else_
       ⇔"cpu")
      # Plot some training images
      real_batch = next(iter(dataloader))
      plt.figure(figsize=(8,8));
      plt.axis("off");
      plt.title("Training Images");
      plt.imshow(np.transpose(vutils.make_grid(real_batch[0].to(device)[:64],__
       →padding=2, normalize=True).cpu(),(1,2,0)));
```

Training Images



G will take the input \vec{z} of dimension 100 and **up sample** (increase the number of channels) with a transposed convolutional network, giving in output a 3x64x64 dimensional tensor. A discrete convolution operator has an input, which is an image with only one channel (monochromatic). It also requires a *kernel*, which is usually a 3x3 matrix (or at least smaller than the image). The convolution is done within the image and the kernel, like we do in image processing (e.g. filtering).

To learn more about convolution.

To visualize what a convolution does.

We use different kernels to gain different info, e.g. edges. One famous operation is the max pooling, used as much as the average pooling.

Now we want to define two networks, one for the generator and one for the discriminator. We want

the weights to be small at the beginning in order to use a normal distribution.

```
[18]: # custom weights initialization called on ``netG`` and ``netD``
def weights_init(m):
    classname = m.__class__.__name__
    if classname.find('Conv') != -1:
        nn.init.normal_(m.weight.data, 0.0, 0.02)
    elif classname.find('BatchNorm') != -1:
        nn.init.normal_(m.weight.data, 1.0, 0.02)
        nn.init.constant_(m.bias.data, 0)
```

To see the real convolution function.

There is a relation between the number of zeros (padding p), the dimension of the kernel k, the length of the image i and the stripe s (how much we jump with our filter). The dimension of the output image is completely determined by the previous parameters:

$$o = \left| \frac{i + 2p - k}{s} \right| + 1$$

NOTE: the generator is doing the opposite of the discriminator! The discriminator is doing the convolution while the generator is using the transposed convolution (deconvolution). Actually the convolution operator is not invertible, so it's not the inverse in terms of values, but it is in terms of dimensions.

So while the convolution takes the image and gives out something small, the deconvolution takes in something small and enlarges it.

```
[19]: # Generator Code
      class Generator(nn.Module):
          def __init__(self, ngpu):
              super(Generator, self).__init__()
              self.ngpu = ngpu
              self.main = nn.Sequential(
                  # input is Z, going into a convolution
                  nn.ConvTranspose2d( nz, ngf * 8, 4, 1, 0, bias=False),
                  nn.BatchNorm2d(ngf * 8),
                  nn.ReLU(True),
                  # state size. ``(ngf*8) x 4 x 4``
                  nn.ConvTranspose2d(ngf * 8, ngf * 4, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ngf * 4),
                  nn.ReLU(True),
                  # state size. ``(nqf*4) x 8 x 8``
                  nn.ConvTranspose2d( ngf * 4, ngf * 2, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ngf * 2),
                  nn.ReLU(True),
                  # state size. ``(ngf*2) x 16 x 16``
                  nn.ConvTranspose2d( ngf * 2, ngf, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ngf),
```

```
nn.ReLU(True),
    # state size. ``(ngf) x 32 x 32``
    nn.ConvTranspose2d( ngf, nc, 4, 2, 1, bias=False),
    nn.Tanh()
    # state size. ``(nc) x 64 x 64``
)

def forward(self, input):
    return self.main(input)
```

D is another thing. It goes not through transpose convolution but genuine. It will **down sampling**, i.e. aggregate spatial information while increasing the number of channels. The output will be one number, i.e. 0 if the image is fake or 1 if it's not. All the convolution operators works with parameters changing during training.

```
[20]: # Create the generator
      netG = Generator(ngpu).to(device)
      # Handle multi-GPU if desired
      if (device.type == 'cuda') and (ngpu > 1):
          netG = nn.DataParallel(netG, list(range(ngpu)))
      # Apply the ``weights_init`` function to randomly initialize all weights
      # to ``mean=0``, ``stdev=0.02``.
      netG.apply(weights_init)
      # Print the model
      print(netG)
     Generator(
       (main): Sequential(
         (0): ConvTranspose2d(100, 512, kernel_size=(4, 4), stride=(1, 1),
     bias=False)
         (1): BatchNorm2d(512, eps=1e-05, momentum=0.1, affine=True,
     track_running_stats=True)
         (2): ReLU(inplace=True)
         (3): ConvTranspose2d(512, 256, kernel_size=(4, 4), stride=(2, 2),
     padding=(1, 1), bias=False)
         (4): BatchNorm2d(256, eps=1e-05, momentum=0.1, affine=True,
     track running stats=True)
         (5): ReLU(inplace=True)
         (6): ConvTranspose2d(256, 128, kernel_size=(4, 4), stride=(2, 2),
     padding=(1, 1), bias=False)
         (7): BatchNorm2d(128, eps=1e-05, momentum=0.1, affine=True,
     track_running_stats=True)
         (8): ReLU(inplace=True)
         (9): ConvTranspose2d(128, 64, kernel_size=(4, 4), stride=(2, 2), padding=(1,
     1), bias=False)
```

```
(10): BatchNorm2d(64, eps=1e-05, momentum=0.1, affine=True,
     track_running_stats=True)
         (11): ReLU(inplace=True)
         (12): ConvTranspose2d(64, 3, kernel_size=(4, 4), stride=(2, 2), padding=(1,
     1). bias=False)
         (13): Tanh()
       )
[21]: class Discriminator(nn.Module):
          def __init__(self, ngpu):
              super(Discriminator, self).__init__()
              self.ngpu = ngpu
              self.main = nn.Sequential(
                  # input is ``(nc) x 64 x 64``
                  # takes an image of 64x64, pads by 1, strides by 2 (moving two
       ⇔steps at a time), and applies a 4x4 kernel
                  nn.Conv2d(nc, ndf, 4, 2, 1, bias=False),
                  nn.LeakyReLU(0.2, inplace=True),
                  # state size. ``(ndf) x 32 x 32``
                  nn.Conv2d(ndf, ndf * 2, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ndf * 2),
                  nn.LeakyReLU(0.2, inplace=True),
                  # state size. ``(ndf*2) x 16 x 16``
                  nn.Conv2d(ndf * 2, ndf * 4, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ndf * 4),
                  nn.LeakyReLU(0.2, inplace=True),
                  # state size. ``(ndf*4) x 8 x 8`
                  nn.Conv2d(ndf * 4, ndf * 8, 4, 2, 1, bias=False),
                  nn.BatchNorm2d(ndf * 8),
                  nn.LeakyReLU(0.2, inplace=True),
                  # state size. ``(ndf*8) x 4 x 4`
                  nn.Conv2d(ndf * 8, 1, 4, 1, 0, bias=False),
                  nn.Sigmoid()
              )
          def forward(self, input):
              return self.main(input)
```

Send all the model to GPU and hope.

```
[22]: # Create the Discriminator
netD = Discriminator(ngpu).to(device)

# Handle multi-GPU if desired
if (device.type == 'cuda') and (ngpu > 1):
    netD = nn.DataParallel(netD, list(range(ngpu)))
```

```
# Apply the ``weights init`` function to randomly initialize all weights
# like this: ``to mean=0, stdev=0.2``.
netD.apply(weights_init)
# Print the model
print(netD)
Discriminator(
  (main): Sequential(
    (0): Conv2d(3, 64, kernel size=(4, 4), stride=(2, 2), padding=(1, 1),
bias=False)
    (1): LeakyReLU(negative_slope=0.2, inplace=True)
    (2): Conv2d(64, 128, kernel size=(4, 4), stride=(2, 2), padding=(1, 1),
bias=False)
    (3): BatchNorm2d(128, eps=1e-05, momentum=0.1, affine=True,
track_running_stats=True)
    (4): LeakyReLU(negative_slope=0.2, inplace=True)
    (5): Conv2d(128, 256, kernel_size=(4, 4), stride=(2, 2), padding=(1, 1),
bias=False)
    (6): BatchNorm2d(256, eps=1e-05, momentum=0.1, affine=True,
track running stats=True)
    (7): LeakyReLU(negative_slope=0.2, inplace=True)
    (8): Conv2d(256, 512, kernel_size=(4, 4), stride=(2, 2), padding=(1, 1),
bias=False)
    (9): BatchNorm2d(512, eps=1e-05, momentum=0.1, affine=True,
track_running_stats=True)
    (10): LeakyReLU(negative_slope=0.2, inplace=True)
    (11): Conv2d(512, 1, kernel size=(4, 4), stride=(1, 1), bias=False)
    (12): Sigmoid()
 )
)
```

Now we want to train... what is the loss function?

In this case it's simple because it's a binary one (BC-ELoss()) of PyTorch). Then, we construct a batch of random noise (normally distributed). For each batch we generate a tensor of dimension (1, 1, 100), where 100 is the dimension of channels. Why 100? Eh EH! We don't know. Just don't ask and all will be fine.

Then, we label the images (very easy to do), and define the optimizers.

```
real_label = 1.
fake_label = 0.

# Setup Adam optimizers for both G and D
optimizerD = optim.Adam(netD.parameters(), lr=lr, betas=(beta1, 0.999))
optimizerG = optim.Adam(netG.parameters(), lr=lr, betas=(beta1, 0.999))
```

We're going to train now. There are some tricks we're going to use.

Training GAN can be very difficult... they usually fall into loops. D(x) needs to be as close to zero as possible (so the log as close to zero as possible, which is the opposite, grr). Basically, once fixed the generator we'll maximize the discriminator in two steps: - construct real images, calculate the loss and the gradient to maximize without changing the parameters, only computing. - without touching G and D we create fake images and maximize D again, then we sum the two gradients.

```
[24]: from tqdm.autonotebook import trange
     # Training Loop
     # Lists to keep track of progress
     img list = []
     G losses = []
     D_{losses} = []
     iters = 0
     print("Starting Training Loop...")
     # For each epoch
     for epoch in trange(num_epochs):
         # For each batch in the dataloader
         for i, data in enumerate(dataloader, 0):
             # (1) Update D network: maximize log(D(x)) + log(1 - D(G(z)))
             ## Train with all-real batch
             netD.zero_grad()
             # Format batch
             real_cpu = data[0].to(device)
             b_size = real_cpu.size(0)
             # label is just a vector of ones
             label = torch.full((b_size,), real_label, dtype=torch.float,_

device=device)

             # Forward pass real batch through D
             output = netD(real_cpu).view(-1)
             # Calculate loss on all-real batch
             errD_real = criterion(output, label)
             # Calculate gradients for D in backward pass
             errD real.backward()
```

```
D_x = output.mean().item()
      ## Train with all-fake batch
      # Generate batch of latent vectors
      noise = torch.randn(b_size, nz, 1, 1, device=device)
      # Generate fake image batch with G
      fake = netG(noise)
      label.fill_(fake_label)
      # Classify all fake batch with D
      # detach() is used to avoid backprop through a variable (less memory_
→usage)
      output = netD(fake.detach()).view(-1)
      # Calculate D's loss on the all-fake batch
      errD_fake = criterion(output, label)
      # Calculate the gradients for this batch, accumulated (summed) with
⇔previous gradients
      errD fake.backward()
      D_G_z1 = output.mean().item()
      # Compute error of D as sum over the fake and the real batches
      errD = errD_real + errD_fake
      # Update D
      optimizerD.step()
      ####################################
      # (2) Update G network: maximize log(D(G(z)))
      #############################
      netG.zero grad()
      label.fill_(real_label) # fake labels are real for generator cost
      # it wants to foul D...
      # Since we just updated D, perform another forward pass of all-fake_
⇔batch through D
      output = netD(fake).view(-1)
      # Calculate G's loss based on this output
      errG = criterion(output, label)
      # Calculate gradients for G
      errG.backward()
      D_G_z2 = output.mean().item()
      # Update G
      optimizerG.step()
      # Output training stats
      if i % 50 == 0:
          print('[%d/%d][%d/%d]\tLoss_D: %.4f\tLoss_G: %.4f\tD(x): %.
% (epoch, num_epochs, i, len(dataloader),
                   errD.item(), errG.item(), D_x, D_G_z1, D_G_z2))
```

```
# Save Losses for plotting later
G_losses.append(errG.item())
D_losses.append(errD.item())

# Check how the generator is doing by saving G's output on fixed_noise
if (iters % 500 == 0) or ((epoch == num_epochs-1) and (i ==_u
elen(dataloader)-1)):
    with torch.no_grad():
        fake = netG(fixed_noise).detach().cpu()
        img_list.append(vutils.make_grid(fake, padding=2, normalize=True))

iters += 1
```

Starting Training Loop...

```
| 0/30 [00:00<?, ?it/s]
  0%1
[0/30][0/1583] Loss_D: 1.9100 Loss_G: 6.3743 D(x): 0.7247
                                                                D(G(z)): 0.7207
/ 0.0032
[0/30][50/1583] Loss_D: 0.1117 Loss_G: 14.8767 D(x): 0.9388
                                                                D(G(z)): 0.0000
/ 0.0000
[0/30] [100/1583]
                        Loss_D: 0.5441 Loss_G: 15.0935 D(x): 0.9766
                                                                        D(G(z)):
0.3376 / 0.0000
                        Loss_D: 0.2738 Loss_G: 4.8203 D(x): 0.9037
[0/30] [150/1583]
                                                                        D(G(z)):
0.1035 / 0.0224
[0/30] [200/1583]
                        Loss D: 0.7405 Loss G: 3.1751 D(x): 0.6080
                                                                        D(G(z)):
0.0720 / 0.0621
                        Loss D: 0.4057 Loss G: 3.7363 D(x): 0.7760
                                                                        D(G(z)):
[0/30] [250/1583]
0.0788 / 0.0336
[0/30] [300/1583]
                        Loss_D: 0.6122 Loss_G: 4.5775 D(x): 0.6861
                                                                        D(G(z)):
0.0877 / 0.0431
[0/30] [350/1583]
                        Loss_D: 0.7129 Loss_G: 3.2661 D(x): 0.7908
                                                                        D(G(z)):
0.2932 / 0.0617
                        Loss_D: 0.5784 Loss_G: 5.2064 D(x): 0.8225
[0/30] [400/1583]
                                                                        D(G(z)):
0.2283 / 0.0121
[0/30] [450/1583]
                        Loss_D: 0.6850 Loss_G: 4.4506 D(x): 0.7969
                                                                        D(G(z)):
0.2781 / 0.0215
[0/30] [500/1583]
                        Loss_D: 0.7033 Loss_G: 3.2423 D(x): 0.6488
                                                                        D(G(z)):
0.0601 / 0.0707
[0/30] [550/1583]
                        Loss_D: 0.4272 Loss_G: 4.8669 D(x): 0.8952
                                                                        D(G(z)):
0.2279 / 0.0128
[0/30] [600/1583]
                        Loss_D: 0.8806 Loss_G: 6.9053 D(x): 0.8822
                                                                        D(G(z)):
0.4456 / 0.0027
[0/30] [650/1583]
                        Loss_D: 0.4914 Loss_G: 3.1807 D(x): 0.7329
                                                                        D(G(z)):
0.0806 / 0.0664
[0/30] [700/1583]
                        Loss_D: 0.5141 Loss_G: 4.3971 D(x): 0.8325
                                                                        D(G(z)):
0.2083 / 0.0238
                        Loss_D: 4.2826 Loss_G: 1.7898 D(x): 0.0554
[0/30] [750/1583]
                                                                        D(G(z)):
```

```
0.0002 / 0.2801
[0/30] [800/1583]
                        Loss_D: 0.9928 Loss_G: 6.1897 D(x): 0.8533
                                                                         D(G(z)):
0.4372 / 0.0052
[0/30] [850/1583]
                        Loss_D: 0.6179
                                        Loss_G: 5.7014 D(x): 0.8999
                                                                         D(G(z)):
0.3494 / 0.0063
[0/30] [900/1583]
                        Loss_D: 1.0358
                                        Loss_G: 7.6564 D(x): 0.9301
                                                                         D(G(z)):
0.5496 / 0.0011
[0/30] [950/1583]
                        Loss_D: 0.6629
                                        Loss_G: 5.4213 D(x): 0.6180
                                                                         D(G(z)):
0.0096 / 0.0098
[0/30] [1000/1583]
                        Loss D: 0.5019
                                        Loss_G: 4.5373 D(x): 0.8283
                                                                         D(G(z)):
0.2066 / 0.0202
[0/30] [1050/1583]
                        Loss_D: 0.5081
                                        Loss_G: 4.0771 D(x): 0.8213
                                                                         D(G(z)):
0.2187 / 0.0301
[0/30] [1100/1583]
                        Loss_D: 0.8733
                                        Loss_G: 7.0113 D(x): 0.9092
                                                                         D(G(z)):
0.4763 / 0.0030
[0/30] [1150/1583]
                        Loss_D: 0.6963
                                        Loss_G: 6.8643
                                                                         D(G(z)):
                                                         D(x): 0.9229
0.4081 / 0.0026
[0/30] [1200/1583]
                        Loss_D: 0.2345
                                        Loss_G: 4.9050
                                                                         D(G(z)):
                                                         D(x): 0.8546
0.0523 / 0.0137
[0/30] [1250/1583]
                        Loss D: 0.5088
                                        Loss G: 6.3368
                                                        D(x): 0.9354
                                                                         D(G(z)):
0.3103 / 0.0033
[0/30] [1300/1583]
                        Loss D: 1.0843 Loss G: 1.5466 D(x): 0.4652
                                                                         D(G(z)):
0.0280 / 0.3154
                        Loss_D: 0.6612 Loss_G: 2.1993
[0/30] [1350/1583]
                                                        D(x): 0.6201
                                                                         D(G(z)):
0.0432 / 0.1622
[0/30] [1400/1583]
                        Loss_D: 0.6060
                                        Loss_G: 3.1925
                                                        D(x): 0.6454
                                                                         D(G(z)):
0.0327 / 0.0744
[0/30] [1450/1583]
                        Loss_D: 0.3776 Loss_G: 5.0086
                                                        D(x): 0.9481
                                                                         D(G(z)):
0.2477 / 0.0131
[0/30] [1500/1583]
                        Loss_D: 0.6529
                                        Loss_G: 4.2288
                                                         D(x): 0.6243
                                                                         D(G(z)):
0.0362 / 0.0384
[0/30] [1550/1583]
                        Loss_D: 0.6317 Loss_G: 3.4623 D(x): 0.7627
                                                                         D(G(z)):
0.2427 / 0.0485
[1/30][0/1583] Loss_D: 0.4144 Loss_G: 4.7942 D(x): 0.9071
                                                                 D(G(z)): 0.2373
/ 0.0139
[1/30][50/1583] Loss_D: 0.6299 Loss_G: 2.8451 D(x): 0.6842
                                                                 D(G(z)): 0.1155
/ 0.1012
[1/30] [100/1583]
                        Loss_D: 0.7733 Loss_G: 4.8411 D(x): 0.9099
                                                                         D(G(z)):
0.4009 / 0.0171
[1/30] [150/1583]
                        Loss_D: 0.3288 Loss_G: 4.1822 D(x): 0.8814
                                                                         D(G(z)):
0.1559 / 0.0245
[1/30] [200/1583]
                        Loss_D: 0.7021 Loss_G: 2.9883
                                                        D(x): 0.7501
                                                                         D(G(z)):
0.2472 / 0.0968
[1/30] [250/1583]
                        Loss D: 0.3766
                                        Loss_G: 3.7053
                                                         D(x): 0.8738
                                                                         D(G(z)):
0.1805 / 0.0372
[1/30] [300/1583]
                        Loss_D: 1.1772 Loss_G: 7.3684
                                                        D(x): 0.9148
                                                                         D(G(z)):
0.5904 / 0.0012
[1/30] [350/1583]
                        Loss_D: 0.4057 Loss_G: 4.5628 D(x): 0.8701
                                                                         D(G(z)):
```

```
0.1970 / 0.0200
[1/30] [400/1583]
                        Loss_D: 0.3481 Loss_G: 3.6921
                                                          D(x): 0.8800
                                                                           D(G(z)):
0.1670 / 0.0384
                        Loss_D: 0.3221
                                         Loss_G: 4.3367
[1/30] [450/1583]
                                                          D(x): 0.8816
                                                                           D(G(z)):
0.1482 / 0.0199
                         Loss_D: 0.3643
[1/30] [500/1583]
                                         Loss_G: 3.6568
                                                          D(x): 0.9072
                                                                           D(G(z)):
0.2068 / 0.0416
[1/30] [550/1583]
                        Loss_D: 0.7266
                                         Loss_G: 1.8188
                                                          D(x): 0.5975
                                                                           D(G(z)):
0.0820 / 0.2123
[1/30] [600/1583]
                        Loss_D: 0.4908
                                         Loss_G: 2.3856
                                                          D(x): 0.7145
                                                                           D(G(z)):
0.0869 / 0.1283
[1/30] [650/1583]
                         Loss_D: 2.0618
                                         Loss_G: 7.1150
                                                          D(x): 0.9764
                                                                           D(G(z)):
0.8057 / 0.0021
[1/30] [700/1583]
                         Loss_D: 0.4446
                                         Loss_G: 2.5216
                                                          D(x): 0.8036
                                                                           D(G(z)):
0.1582 / 0.1176
[1/30] [750/1583]
                        Loss_D: 0.6001
                                         Loss_G: 1.5498
                                                                           D(G(z)):
                                                          D(x): 0.6647
0.1093 / 0.2707
[1/30] [800/1583]
                        Loss_D: 0.3929
                                         Loss_G: 3.7328
                                                                           D(G(z)):
                                                          D(x): 0.7735
0.0817 / 0.0379
[1/30] [850/1583]
                        Loss D: 0.7542
                                         Loss G: 1.8174 D(x): 0.5743
                                                                           D(G(z)):
0.0473 / 0.2212
[1/30] [900/1583]
                         Loss D: 0.7209
                                         Loss G: 4.1103 D(x): 0.8346
                                                                           D(G(z)):
0.3648 / 0.0257
                        Loss_D: 0.4280
                                         Loss G: 3.0080
[1/30] [950/1583]
                                                          D(x): 0.8273
                                                                           D(G(z)):
0.1701 / 0.0693
[1/30] [1000/1583]
                         Loss_D: 1.0949
                                         Loss_G: 5.1157
                                                          D(x): 0.9603
                                                                           D(G(z)):
0.5754 / 0.0118
[1/30] [1050/1583]
                         Loss_D: 1.0737
                                         Loss_G: 5.8125
                                                          D(x): 0.9653
                                                                           D(G(z)):
0.5916 / 0.0056
[1/30] [1100/1583]
                         Loss_D: 0.5069
                                         Loss_G: 2.4066
                                                          D(x): 0.7954
                                                                           D(G(z)):
0.2028 / 0.1181
[1/30] [1150/1583]
                        Loss_D: 0.9592
                                         Loss_G: 2.3333
                                                          D(x): 0.4972
                                                                           D(G(z)):
0.0410 / 0.1463
                        Loss_D: 0.4096
                                         Loss_G: 3.4758
[1/30] [1200/1583]
                                                          D(x): 0.8692
                                                                           D(G(z)):
0.2055 / 0.0442
[1/30] [1250/1583]
                        Loss_D: 0.3463
                                         Loss_G: 4.1029
                                                          D(x): 0.9088
                                                                           D(G(z)):
0.1937 / 0.0251
[1/30] [1300/1583]
                        Loss_D: 0.6553
                                         Loss_G: 3.4875
                                                          D(x): 0.8911
                                                                           D(G(z)):
0.3727 / 0.0438
[1/30] [1350/1583]
                        Loss_D: 0.6007
                                         Loss_G: 3.2893
                                                          D(x): 0.8576
                                                                           D(G(z)):
0.3221 / 0.0534
[1/30] [1400/1583]
                        Loss_D: 0.4235
                                         Loss_G: 2.1989
                                                          D(x): 0.7877
                                                                           D(G(z)):
0.1380 / 0.1437
[1/30] [1450/1583]
                         Loss_D: 0.3922
                                         Loss_G: 4.0252
                                                          D(x): 0.7731
                                                                           D(G(z)):
0.0840 / 0.0376
[1/30] [1500/1583]
                         Loss_D: 0.4919
                                         Loss_G: 2.8329
                                                          D(x): 0.8644
                                                                           D(G(z)):
0.2615 / 0.0787
[1/30] [1550/1583]
                         Loss_D: 0.5301
                                        Loss_G: 3.3498
                                                          D(x): 0.9173
                                                                           D(G(z)):
```

```
0.3171 / 0.0500
[2/30][0/1583] Loss_D: 0.5013 Loss_G: 2.6414 D(x): 0.8017
                                                                  D(G(z)): 0.2076
/ 0.0924
[2/30][50/1583] Loss_D: 0.7941 Loss_G: 4.3297 D(x): 0.8784
                                                                  D(G(z)): 0.4167
/ 0.0220
[2/30] [100/1583]
                        Loss_D: 0.7587 Loss_G: 4.3082 D(x): 0.7927
                                                                          D(G(z)):
0.3382 / 0.0229
[2/30] [150/1583]
                        Loss_D: 0.4364 Loss_G: 2.4097
                                                        D(x): 0.8075
                                                                          D(G(z)):
0.1629 / 0.1179
[2/30] [200/1583]
                        Loss D: 1.1604
                                        Loss_G: 1.1765
                                                         D(x): 0.3950
                                                                          D(G(z)):
0.0445 / 0.3613
[2/30] [250/1583]
                                         Loss_G: 2.7745
                        Loss_D: 0.4582
                                                         D(x): 0.8146
                                                                          D(G(z)):
0.1962 / 0.0861
[2/30] [300/1583]
                        Loss_D: 0.5113
                                         Loss_G: 2.2373
                                                         D(x): 0.7587
                                                                          D(G(z)):
0.1733 / 0.1312
[2/30] [350/1583]
                        Loss_D: 0.6586
                                         Loss_G: 3.7363
                                                                          D(G(z)):
                                                         D(x): 0.9021
0.3849 / 0.0356
[2/30] [400/1583]
                        Loss_D: 0.6836
                                         Loss_G: 2.4316
                                                         D(x): 0.8719
                                                                          D(G(z)):
0.3510 / 0.1336
[2/30] [450/1583]
                        Loss D: 1.1088
                                         Loss G: 4.5589
                                                         D(x): 0.8260
                                                                          D(G(z)):
0.5548 / 0.0156
[2/30] [500/1583]
                        Loss D: 0.8471 Loss G: 1.2172 D(x): 0.4944
                                                                          D(G(z)):
0.0273 / 0.3535
                                         Loss_G: 0.6887
                                                                          D(G(z)):
[2/30] [550/1583]
                        Loss D: 1.1741
                                                         D(x): 0.4113
0.0341 / 0.5663
[2/30] [600/1583]
                        Loss_D: 0.6260
                                         Loss_G: 3.2795
                                                         D(x): 0.8418
                                                                          D(G(z)):
0.3166 / 0.0559
[2/30] [650/1583]
                        Loss_D: 0.5666
                                         Loss_G: 1.9209
                                                         D(x): 0.8083
                                                                          D(G(z)):
0.2596 / 0.1924
[2/30] [700/1583]
                        Loss_D: 0.7241
                                         Loss_G: 3.6693
                                                         D(x): 0.8588
                                                                          D(G(z)):
0.3830 / 0.0382
[2/30] [750/1583]
                        Loss_D: 0.7468
                                         Loss_G: 1.2100
                                                         D(x): 0.5595
                                                                          D(G(z)):
0.0607 / 0.3607
[2/30] [800/1583]
                        Loss_D: 0.5225
                                         Loss_G: 1.6072 D(x): 0.6695
                                                                          D(G(z)):
0.0712 / 0.2438
[2/30] [850/1583]
                        Loss_D: 0.8399
                                         Loss_G: 4.6257
                                                         D(x): 0.9416
                                                                          D(G(z)):
0.4899 / 0.0161
[2/30] [900/1583]
                        Loss D: 1.0395
                                         Loss_G: 4.7532
                                                         D(x): 0.9495
                                                                          D(G(z)):
0.5763 / 0.0131
[2/30] [950/1583]
                        Loss D: 0.6600
                                         Loss_G: 3.0469
                                                         D(x): 0.8142
                                                                          D(G(z)):
0.3244 / 0.0701
[2/30] [1000/1583]
                        Loss_D: 0.5220
                                         Loss_G: 2.2606
                                                         D(x): 0.7597
                                                                          D(G(z)):
0.1800 / 0.1335
[2/30] [1050/1583]
                        Loss_D: 0.9145
                                         Loss_G: 4.0030
                                                         D(x): 0.9125
                                                                          D(G(z)):
0.5069 / 0.0243
[2/30] [1100/1583]
                        Loss D: 0.5797
                                         Loss_G: 3.3170
                                                         D(x): 0.8923
                                                                          D(G(z)):
0.3375 / 0.0463
[2/30] [1150/1583]
                        Loss_D: 0.6676 Loss_G: 3.5707 D(x): 0.9020
                                                                          D(G(z)):
```

```
0.3886 / 0.0416
[2/30] [1200/1583]
                        Loss_D: 1.3787 Loss_G: 6.5207 D(x): 0.9598
                                                                         D(G(z)):
0.6734 / 0.0030
[2/30] [1250/1583]
                        Loss_D: 1.2186
                                        Loss_G: 4.8970 D(x): 0.9625
                                                                         D(G(z)):
0.6369 / 0.0157
                                        Loss_G: 5.8757
[2/30] [1300/1583]
                        Loss D: 1.0960
                                                        D(x): 0.9348
                                                                         D(G(z)):
0.5987 / 0.0040
[2/30] [1350/1583]
                        Loss_D: 0.4970 Loss_G: 2.6727 D(x): 0.7975
                                                                         D(G(z)):
0.2100 / 0.0890
[2/30] [1400/1583]
                        Loss_D: 1.0154 Loss_G: 5.0014 D(x): 0.9528
                                                                         D(G(z)):
0.5626 / 0.0107
[2/30] [1450/1583]
                        Loss_D: 1.3248 Loss_G: 4.7636
                                                        D(x): 0.9737
                                                                         D(G(z)):
0.6639 / 0.0130
[2/30] [1500/1583]
                        Loss_D: 0.7544 Loss_G: 4.6933
                                                        D(x): 0.9595
                                                                         D(G(z)):
0.4642 / 0.0142
[2/30] [1550/1583]
                        Loss_D: 1.5648 Loss_G: 0.2385 D(x): 0.2787
                                                                         D(G(z)):
0.0238 / 0.8243
[3/30][0/1583] Loss_D: 0.6420 Loss_G: 2.9145 D(x): 0.7496
                                                                 D(G(z)): 0.2590
/ 0.0765
[3/30][50/1583] Loss D: 0.6169 Loss G: 2.3945 D(x): 0.7967
                                                                 D(G(z)): 0.2793
/ 0.1148
[3/30] [100/1583]
                        Loss D: 0.9489 Loss G: 1.2492 D(x): 0.4749
                                                                         D(G(z)):
0.0564 / 0.3565
                        Loss_D: 0.5379 Loss_G: 1.7451 D(x): 0.6779
[3/30] [150/1583]
                                                                         D(G(z)):
0.0906 / 0.2184
[3/30] [200/1583]
                        Loss_D: 0.6648 Loss_G: 2.3119 D(x): 0.7266
                                                                         D(G(z)):
0.2480 / 0.1263
[3/30] [250/1583]
                        Loss_D: 0.4293 Loss_G: 3.4311
                                                        D(x): 0.8680
                                                                         D(G(z)):
0.2285 / 0.0431
[3/30] [300/1583]
                        Loss_D: 0.7126
                                        Loss_G: 3.4238
                                                        D(x): 0.7939
                                                                         D(G(z)):
0.3415 / 0.0436
[3/30] [350/1583]
                        Loss_D: 0.9549
                                        Loss_G: 3.0100 D(x): 0.7866
                                                                         D(G(z)):
0.4574 / 0.0681
[3/30] [400/1583]
                        Loss_D: 0.5373 Loss_G: 1.7260
                                                        D(x): 0.6740
                                                                         D(G(z)):
0.1010 / 0.2239
[3/30] [450/1583]
                        Loss_D: 0.9299
                                        Loss_G: 4.9408 D(x): 0.9314
                                                                         D(G(z)):
0.5219 / 0.0105
[3/30] [500/1583]
                        Loss D: 0.7751
                                        Loss_G: 1.4232
                                                        D(x): 0.5392
                                                                         D(G(z)):
0.0590 / 0.2873
[3/30] [550/1583]
                        Loss_D: 0.4861 Loss_G: 2.3578 D(x): 0.8263
                                                                         D(G(z)):
0.2218 / 0.1305
[3/30] [600/1583]
                        Loss_D: 0.5594 Loss_G: 3.2464 D(x): 0.8250
                                                                         D(G(z)):
0.2739 / 0.0515
[3/30] [650/1583]
                        Loss D: 0.6100
                                        Loss_G: 2.0906
                                                        D(x): 0.6636
                                                                         D(G(z)):
0.1375 / 0.1561
[3/30] [700/1583]
                        Loss_D: 0.3575
                                        Loss_G: 2.5990
                                                        D(x): 0.8674
                                                                         D(G(z)):
0.1782 / 0.0922
[3/30] [750/1583]
                        Loss_D: 0.6282 Loss_G: 2.7650 D(x): 0.8308
                                                                         D(G(z)):
```

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0.3227 / 0.0798
[3/30] [800/1583]
                        Loss_D: 0.5087 Loss_G: 1.8414 D(x): 0.7142
                                                                         D(G(z)):
0.1159 / 0.1991
[3/30] [850/1583]
                        Loss_D: 0.7474 Loss_G: 0.9983
                                                         D(x): 0.5746
                                                                         D(G(z)):
0.0909 / 0.4092
[3/30] [900/1583]
                        Loss_D: 0.4877
                                        Loss_G: 2.2631
                                                         D(x): 0.7332
                                                                         D(G(z)):
0.1316 / 0.1336
[3/30] [950/1583]
                        Loss_D: 0.4991 Loss_G: 2.2119 D(x): 0.7795
                                                                         D(G(z)):
0.1955 / 0.1385
[3/30] [1000/1583]
                        Loss D: 0.5750
                                        Loss_G: 1.9622
                                                        D(x): 0.6965
                                                                         D(G(z)):
0.1459 / 0.1771
[3/30] [1050/1583]
                        Loss_D: 0.7438
                                        Loss_G: 1.6780
                                                         D(x): 0.6679
                                                                         D(G(z)):
0.2223 / 0.2420
[3/30] [1100/1583]
                        Loss_D: 0.5447
                                        Loss_G: 2.6580
                                                         D(x): 0.8148
                                                                         D(G(z)):
0.2547 / 0.0892
[3/30] [1150/1583]
                        Loss_D: 0.8967
                                        Loss_G: 0.9999
                                                                         D(G(z)):
                                                         D(x): 0.4817
0.0634 / 0.4220
[3/30] [1200/1583]
                        Loss_D: 0.4253
                                        Loss_G: 2.7052
                                                                         D(G(z)):
                                                        D(x): 0.8436
0.2052 / 0.0826
[3/30] [1250/1583]
                        Loss D: 0.6753
                                        Loss G: 3.3153 D(x): 0.8681
                                                                         D(G(z)):
0.3693 / 0.0497
[3/30] [1300/1583]
                        Loss D: 0.4677
                                        Loss G: 2.2465 D(x): 0.7135
                                                                         D(G(z)):
0.0836 / 0.1405
[3/30] [1350/1583]
                        Loss D: 0.7446
                                        Loss_G: 1.1943
                                                        D(x): 0.5758
                                                                         D(G(z)):
0.1078 / 0.3473
[3/30] [1400/1583]
                        Loss_D: 0.9499
                                        Loss_G: 2.9647
                                                                         D(G(z)):
                                                         D(x): 0.7513
0.4098 / 0.0688
[3/30] [1450/1583]
                        Loss_D: 0.4828 Loss_G: 3.3066
                                                        D(x): 0.9139
                                                                         D(G(z)):
0.2992 / 0.0479
[3/30] [1500/1583]
                        Loss_D: 0.5568
                                        Loss_G: 2.7542
                                                        D(x): 0.8635
                                                                         D(G(z)):
0.3004 / 0.0819
[3/30] [1550/1583]
                        Loss_D: 0.4778 Loss_G: 2.1080 D(x): 0.7913
                                                                         D(G(z)):
0.1868 / 0.1483
[4/30][0/1583] Loss_D: 0.5855 Loss_G: 3.0861 D(x): 0.7917
                                                                 D(G(z)): 0.2690
/ 0.0577
[4/30][50/1583] Loss_D: 1.5381 Loss_G: 5.9642 D(x): 0.9663
                                                                 D(G(z)): 0.7249
/ 0.0047
[4/30] [100/1583]
                        Loss_D: 0.6850 Loss_G: 2.0624 D(x): 0.5950
                                                                         D(G(z)):
0.0773 / 0.1759
[4/30] [150/1583]
                        Loss_D: 0.4911 Loss_G: 3.1258 D(x): 0.8695
                                                                         D(G(z)):
0.2647 / 0.0588
[4/30] [200/1583]
                        Loss_D: 0.6645 Loss_G: 3.1817 D(x): 0.7669
                                                                         D(G(z)):
0.2831 / 0.0543
[4/30] [250/1583]
                        Loss_D: 0.7049
                                        Loss_G: 3.8753
                                                         D(x): 0.8955
                                                                         D(G(z)):
0.4074 / 0.0290
[4/30] [300/1583]
                        Loss_D: 0.4428
                                        Loss_G: 2.2889
                                                         D(x): 0.7811
                                                                         D(G(z)):
0.1540 / 0.1311
[4/30] [350/1583]
                        Loss_D: 0.9750 Loss_G: 1.4654 D(x): 0.4873
                                                                         D(G(z)):
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0.1022 / 0.2861
[4/30] [400/1583]
                         Loss_D: 0.5884 Loss_G: 4.1229
                                                          D(x): 0.8967
                                                                           D(G(z)):
0.3454 / 0.0236
                                         Loss_G: 2.1569
[4/30] [450/1583]
                         Loss_D: 0.5317
                                                          D(x): 0.7793
                                                                           D(G(z)):
0.2015 / 0.1452
[4/30] [500/1583]
                         Loss_D: 0.5453
                                         Loss_G: 1.8338
                                                          D(x): 0.6981
                                                                           D(G(z)):
0.1220 / 0.1933
[4/30] [550/1583]
                         Loss_D: 0.5240
                                         Loss_G: 2.6908
                                                          D(x): 0.8439
                                                                           D(G(z)):
0.2732 / 0.0843
[4/30] [600/1583]
                         Loss_D: 0.4781
                                         Loss_G: 2.5621
                                                          D(x): 0.7933
                                                                           D(G(z)):
0.1932 / 0.0973
[4/30] [650/1583]
                         Loss_D: 0.9953
                                         Loss_G: 1.2504
                                                          D(x): 0.4427
                                                                           D(G(z)):
0.0388 / 0.3421
[4/30] [700/1583]
                         Loss_D: 0.5705
                                         Loss_G: 2.4805
                                                          D(x): 0.7565
                                                                           D(G(z)):
0.2102 / 0.1053
                                         Loss_G: 3.0898
                                                                           D(G(z)):
[4/30] [750/1583]
                         Loss_D: 0.5616
                                                          D(x): 0.8627
0.3077 / 0.0619
[4/30] [800/1583]
                         Loss_D: 0.5500
                                         Loss_G: 3.3487
                                                                           D(G(z)):
                                                          D(x): 0.8840
0.3176 / 0.0474
                         Loss D: 0.8464
                                         Loss G: 3.0015
                                                          D(x): 0.8442
                                                                           D(G(z)):
[4/30] [850/1583]
0.4165 / 0.0769
[4/30] [900/1583]
                         Loss D: 0.5602
                                         Loss G: 2.8382
                                                          D(x): 0.8672
                                                                           D(G(z)):
0.3059 / 0.0775
[4/30] [950/1583]
                         Loss D: 0.6638
                                         Loss_G: 3.8939
                                                          D(x): 0.9069
                                                                           D(G(z)):
0.3982 / 0.0282
[4/30] [1000/1583]
                         Loss_D: 0.4342
                                         Loss_G: 2.5203
                                                          D(x): 0.8998
                                                                           D(G(z)):
0.2575 / 0.1037
[4/30] [1050/1583]
                         Loss_D: 0.4418
                                         Loss_G: 2.4673
                                                          D(x): 0.8643
                                                                           D(G(z)):
0.2250 / 0.1087
[4/30] [1100/1583]
                         Loss_D: 0.4333
                                         Loss_G: 1.6739
                                                          D(x): 0.7464
                                                                           D(G(z)):
0.0927 / 0.2321
[4/30] [1150/1583]
                         Loss_D: 0.6057
                                         Loss_G: 3.2027
                                                          D(x): 0.8311
                                                                           D(G(z)):
0.3090 / 0.0515
                                         Loss_G: 2.6544
[4/30] [1200/1583]
                         Loss_D: 0.3887
                                                          D(x): 0.8037
                                                                           D(G(z)):
0.1334 / 0.0855
[4/30] [1250/1583]
                         Loss_D: 0.3675
                                         Loss_G: 2.5942
                                                          D(x): 0.8718
                                                                           D(G(z)):
0.1881 / 0.0988
                         Loss_D: 0.3844
                                         Loss_G: 2.3193
                                                                           D(G(z)):
[4/30] [1300/1583]
                                                          D(x): 0.7836
0.1082 / 0.1207
[4/30] [1350/1583]
                         Loss_D: 0.8276
                                         Loss_G: 1.6804 D(x): 0.5384
                                                                           D(G(z)):
0.1055 / 0.2401
[4/30] [1400/1583]
                         Loss_D: 0.5927
                                         Loss_G: 3.9140
                                                          D(x): 0.8792
                                                                           D(G(z)):
0.3352 / 0.0285
[4/30] [1450/1583]
                         Loss_D: 0.5249
                                         Loss_G: 2.4036
                                                          D(x): 0.8230
                                                                           D(G(z)):
0.2447 / 0.1159
[4/30] [1500/1583]
                         Loss_D: 0.5046
                                         Loss_G: 2.3034
                                                          D(x): 0.7984
                                                                           D(G(z)):
0.2201 / 0.1222
[4/30] [1550/1583]
                         Loss_D: 0.7557
                                         Loss_G: 1.7247 D(x): 0.6070
                                                                           D(G(z)):
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0.1514 / 0.2270
[5/30][0/1583] Loss_D: 0.4124 Loss_G: 2.1699 D(x): 0.7662
                                                                  D(G(z)): 0.1025
/ 0.1540
[5/30][50/1583] Loss_D: 0.3537 Loss_G: 2.3381 D(x): 0.8484
                                                                  D(G(z)): 0.1557
/ 0.1182
[5/30] [100/1583]
                        Loss_D: 0.6884 Loss_G: 4.0953 D(x): 0.9309
                                                                          D(G(z)):
0.4142 / 0.0230
[5/30] [150/1583]
                        Loss_D: 0.5731 Loss_G: 2.7684
                                                         D(x): 0.8657
                                                                          D(G(z)):
0.3146 / 0.0799
[5/30] [200/1583]
                        Loss D: 0.4905
                                         Loss_G: 2.3765
                                                         D(x): 0.7587
                                                                          D(G(z)):
0.1522 / 0.1226
[5/30] [250/1583]
                        Loss_D: 0.5271
                                         Loss_G: 4.2139
                                                         D(x): 0.9151
                                                                          D(G(z)):
0.3251 / 0.0204
[5/30] [300/1583]
                        Loss_D: 0.7462
                                         Loss_G: 4.8865
                                                         D(x): 0.9090
                                                                          D(G(z)):
0.4167 / 0.0120
                                                         D(x): 0.8486
[5/30] [350/1583]
                        Loss_D: 0.5003
                                         Loss_G: 3.5984
                                                                          D(G(z)):
0.2543 / 0.0364
[5/30] [400/1583]
                        Loss_D: 0.8453
                                         Loss_G: 1.4124
                                                                          D(G(z)):
                                                         D(x): 0.5177
0.0602 / 0.3008
[5/30] [450/1583]
                        Loss D: 0.6320
                                         Loss G: 3.1865
                                                         D(x): 0.8461
                                                                          D(G(z)):
0.3287 / 0.0556
[5/30] [500/1583]
                        Loss D: 0.5337
                                         Loss G: 2.6699
                                                         D(x): 0.7865
                                                                          D(G(z)):
0.2250 / 0.0884
                                         Loss_G: 2.0229
                        Loss_D: 0.4619
[5/30] [550/1583]
                                                         D(x): 0.8056
                                                                          D(G(z)):
0.1881 / 0.1569
[5/30] [600/1583]
                        Loss_D: 0.6341
                                         Loss_G: 2.8412 D(x): 0.8755
                                                                          D(G(z)):
0.3359 / 0.0854
[5/30] [650/1583]
                        Loss_D: 0.5395
                                         Loss_G: 2.0579
                                                         D(x): 0.6811
                                                                          D(G(z)):
0.0861 / 0.1678
[5/30] [700/1583]
                        Loss_D: 0.6768
                                         Loss_G: 3.8210
                                                         D(x): 0.8631
                                                                          D(G(z)):
0.3695 / 0.0299
[5/30] [750/1583]
                        Loss_D: 0.5632
                                         Loss_G: 2.3363
                                                         D(x): 0.8127
                                                                          D(G(z)):
0.2642 / 0.1183
[5/30] [800/1583]
                        Loss_D: 0.4052
                                         Loss_G: 2.6193
                                                         D(x): 0.7986
                                                                          D(G(z)):
0.1397 / 0.0929
[5/30] [850/1583]
                        Loss_D: 1.6352
                                         Loss_G: 1.7167
                                                         D(x): 0.6319
                                                                          D(G(z)):
0.5842 / 0.3198
[5/30] [900/1583]
                        Loss D: 0.5406
                                         Loss_G: 2.0310
                                                         D(x): 0.7595
                                                                          D(G(z)):
0.1972 / 0.1607
[5/30] [950/1583]
                        Loss_D: 0.6735
                                         Loss_G: 3.6420 D(x): 0.8903
                                                                          D(G(z)):
0.3911 / 0.0358
[5/30] [1000/1583]
                        Loss_D: 0.5916
                                         Loss_G: 2.1948
                                                         D(x): 0.6377
                                                                          D(G(z)):
0.0742 / 0.1521
[5/30] [1050/1583]
                        Loss_D: 1.0586
                                         Loss_G: 4.4195
                                                         D(x): 0.9480
                                                                          D(G(z)):
0.5751 / 0.0204
[5/30] [1100/1583]
                        Loss_D: 0.7447
                                         Loss_G: 1.3099
                                                         D(x): 0.5452
                                                                          D(G(z)):
0.0409 / 0.3298
[5/30] [1150/1583]
                        Loss_D: 1.1590 Loss_G: 4.4393 D(x): 0.9613
                                                                          D(G(z)):
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0.6108 / 0.0181
[5/30] [1200/1583]
                        Loss_D: 0.5547 Loss_G: 2.3427 D(x): 0.6844
                                                                         D(G(z)):
0.1076 / 0.1224
[5/30] [1250/1583]
                                        Loss_G: 4.1940
                        Loss_D: 0.5647
                                                        D(x): 0.9335
                                                                         D(G(z)):
0.3624 / 0.0204
[5/30] [1300/1583]
                        Loss_D: 0.5563
                                        Loss_G: 2.5491
                                                         D(x): 0.7212
                                                                         D(G(z)):
0.1586 / 0.1127
[5/30] [1350/1583]
                        Loss_D: 0.7573 Loss_G: 1.5584 D(x): 0.5483
                                                                         D(G(z)):
0.0613 / 0.2620
[5/30] [1400/1583]
                        Loss D: 0.4058
                                        Loss_G: 2.4624 D(x): 0.7934
                                                                         D(G(z)):
0.1305 / 0.1131
[5/30] [1450/1583]
                        Loss_D: 0.4528
                                        Loss_G: 3.0137
                                                         D(x): 0.8833
                                                                         D(G(z)):
0.2509 / 0.0637
[5/30] [1500/1583]
                        Loss_D: 0.4335
                                        Loss_G: 3.7561
                                                        D(x): 0.9322
                                                                         D(G(z)):
0.2787 / 0.0319
[5/30] [1550/1583]
                        Loss_D: 0.7052 Loss_G: 3.4957 D(x): 0.9174
                                                                         D(G(z)):
0.4228 / 0.0395
[6/30][0/1583] Loss_D: 1.1897 Loss_G: 0.8530 D(x): 0.3863
                                                                 D(G(z)): 0.0322
/ 0.4864
[6/30][50/1583] Loss D: 0.5990 Loss G: 1.7253 D(x): 0.7381
                                                                 D(G(z)): 0.2114
/ 0.2241
[6/30] [100/1583]
                        Loss D: 0.5736 Loss G: 2.1321 D(x): 0.7358
                                                                         D(G(z)):
0.1986 / 0.1436
                        Loss_D: 0.7105 Loss_G: 3.1549
[6/30] [150/1583]
                                                        D(x): 0.8962
                                                                         D(G(z)):
0.4038 / 0.0608
[6/30] [200/1583]
                        Loss_D: 1.6508 Loss_G: 0.7019 D(x): 0.2605
                                                                         D(G(z)):
0.0188 / 0.5448
[6/30] [250/1583]
                        Loss_D: 0.4069 Loss_G: 2.7500
                                                        D(x): 0.8620
                                                                         D(G(z)):
0.2071 / 0.0826
[6/30] [300/1583]
                        Loss_D: 0.5583
                                        Loss_G: 1.6130
                                                         D(x): 0.6919
                                                                         D(G(z)):
0.1292 / 0.2370
[6/30] [350/1583]
                        Loss_D: 0.8274
                                        Loss_G: 3.4055
                                                         D(x): 0.8755
                                                                         D(G(z)):
0.4507 / 0.0507
[6/30] [400/1583]
                        Loss_D: 0.4932 Loss_G: 2.7347
                                                         D(x): 0.8869
                                                                         D(G(z)):
0.2834 / 0.0809
[6/30] [450/1583]
                        Loss_D: 1.5309
                                        Loss_G: 2.0718 D(x): 0.6483
                                                                         D(G(z)):
0.5585 / 0.2086
[6/30] [500/1583]
                        Loss D: 0.4970
                                        Loss_G: 2.4445
                                                                         D(G(z)):
                                                        D(x): 0.7410
0.1393 / 0.1086
[6/30] [550/1583]
                        Loss D: 0.4449
                                        Loss_G: 2.5180 D(x): 0.7792
                                                                         D(G(z)):
0.1450 / 0.1063
[6/30] [600/1583]
                        Loss_D: 0.4991 Loss_G: 2.0411 D(x): 0.7561
                                                                         D(G(z)):
0.1530 / 0.1605
[6/30] [650/1583]
                        Loss_D: 0.5744
                                        Loss_G: 2.6672
                                                         D(x): 0.7793
                                                                         D(G(z)):
0.2470 / 0.0902
[6/30] [700/1583]
                        Loss_D: 0.9628
                                        Loss_G: 4.7005
                                                        D(x): 0.9574
                                                                         D(G(z)):
0.5473 / 0.0134
[6/30] [750/1583]
                        Loss_D: 0.7316 Loss_G: 1.7992 D(x): 0.5816
                                                                         D(G(z)):
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0.0937 / 0.2119
[6/30] [800/1583]
                        Loss_D: 0.5175 Loss_G: 2.9507 D(x): 0.8426
                                                                         D(G(z)):
0.2602 / 0.0711
[6/30] [850/1583]
                        Loss_D: 0.5392
                                        Loss_G: 2.1131
                                                                         D(G(z)):
                                                         D(x): 0.7719
0.2146 / 0.1529
[6/30] [900/1583]
                        Loss_D: 0.7601
                                        Loss_G: 2.7461
                                                         D(x): 0.7915
                                                                         D(G(z)):
0.3452 / 0.0922
[6/30] [950/1583]
                        Loss_D: 0.6605
                                        Loss_G: 1.6386
                                                         D(x): 0.6066
                                                                         D(G(z)):
0.0657 / 0.2443
[6/30] [1000/1583]
                        Loss D: 0.6885
                                        Loss_G: 3.7786
                                                         D(x): 0.8655
                                                                         D(G(z)):
0.3801 / 0.0325
[6/30] [1050/1583]
                        Loss_D: 0.4084
                                        Loss_G: 2.9391
                                                         D(x): 0.8450
                                                                         D(G(z)):
0.1908 / 0.0719
[6/30] [1100/1583]
                        Loss_D: 0.6596
                                        Loss_G: 2.0604
                                                         D(x): 0.5914
                                                                         D(G(z)):
0.0546 / 0.1831
[6/30] [1150/1583]
                        Loss_D: 0.8308
                                        Loss_G: 3.7586
                                                                         D(G(z)):
                                                         D(x): 0.8469
0.4298 / 0.0335
[6/30] [1200/1583]
                        Loss_D: 0.4748
                                        Loss_G: 2.1642
                                                                         D(G(z)):
                                                         D(x): 0.7554
0.1449 / 0.1443
[6/30] [1250/1583]
                        Loss D: 0.4967
                                        Loss G: 2.5348
                                                        D(x): 0.8430
                                                                         D(G(z)):
0.2441 / 0.1029
[6/30] [1300/1583]
                        Loss D: 0.7968
                                        Loss G: 4.5609
                                                        D(x): 0.9462
                                                                         D(G(z)):
0.4749 / 0.0156
                        Loss_D: 0.8755
[6/30] [1350/1583]
                                        Loss_G: 1.2038
                                                         D(x): 0.5391
                                                                         D(G(z)):
0.1327 / 0.3555
[6/30] [1400/1583]
                        Loss_D: 0.7994
                                        Loss_G: 1.3361
                                                         D(x): 0.5342
                                                                         D(G(z)):
0.0595 / 0.3208
[6/30] [1450/1583]
                        Loss_D: 0.4389
                                        Loss_G: 2.4294
                                                        D(x): 0.7946
                                                                         D(G(z)):
0.1545 / 0.1247
[6/30] [1500/1583]
                        Loss_D: 0.5856
                                        Loss_G: 1.3407
                                                         D(x): 0.6250
                                                                         D(G(z)):
0.0487 / 0.3099
[6/30] [1550/1583]
                        Loss_D: 0.6427 Loss_G: 1.7168 D(x): 0.6430
                                                                         D(G(z)):
0.1142 / 0.2239
[7/30][0/1583] Loss_D: 0.5565 Loss_G: 1.7901 D(x): 0.6657
                                                                 D(G(z)): 0.0892
/ 0.2094
[7/30][50/1583] Loss_D: 0.4542 Loss_G: 1.8489 D(x): 0.7099
                                                                 D(G(z)): 0.0702
/ 0.1970
[7/30] [100/1583]
                        Loss_D: 0.7468 Loss_G: 1.7080 D(x): 0.5756
                                                                         D(G(z)):
0.0944 / 0.2321
[7/30] [150/1583]
                        Loss_D: 0.5294 Loss_G: 1.7605
                                                         D(x): 0.6708
                                                                         D(G(z)):
0.0727 / 0.2073
[7/30] [200/1583]
                        Loss_D: 0.6612 Loss_G: 1.7835
                                                         D(x): 0.5822
                                                                         D(G(z)):
0.0335 / 0.2085
[7/30] [250/1583]
                        Loss_D: 1.2580
                                        Loss_G: 0.2162
                                                         D(x): 0.3624
                                                                         D(G(z)):
0.0250 / 0.8195
[7/30] [300/1583]
                        Loss_D: 0.5571
                                       Loss_G: 2.6070 D(x): 0.7852
                                                                         D(G(z)):
0.2269 / 0.0972
[7/30] [350/1583]
                        Loss_D: 0.4248 Loss_G: 2.5772 D(x): 0.7932
                                                                         D(G(z)):
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0.1523 / 0.1012
[7/30] [400/1583]
                        Loss_D: 0.9565 Loss_G: 1.1586 D(x): 0.5642
                                                                           D(G(z)):
0.2240 / 0.3645
                                         Loss_G: 3.6760
[7/30] [450/1583]
                        Loss_D: 0.4824
                                                          D(x): 0.9084
                                                                           D(G(z)):
0.2834 / 0.0347
[7/30] [500/1583]
                         Loss_D: 0.4712
                                         Loss_G: 2.7054
                                                          D(x): 0.8651
                                                                           D(G(z)):
0.2517 / 0.0834
[7/30] [550/1583]
                        Loss_D: 0.5874 Loss_G: 2.4521 D(x): 0.8187
                                                                           D(G(z)):
0.2768 / 0.1101
[7/30] [600/1583]
                        Loss D: 0.3444
                                         Loss_G: 2.9871
                                                          D(x): 0.8309
                                                                           D(G(z)):
0.1282 / 0.0659
[7/30] [650/1583]
                         Loss_D: 0.6294
                                         Loss_G: 2.5423
                                                          D(x): 0.7638
                                                                           D(G(z)):
0.2443 / 0.1061
[7/30] [700/1583]
                         Loss_D: 0.6514
                                         Loss_G: 2.1183
                                                          D(x): 0.7228
                                                                           D(G(z)):
0.2202 / 0.1546
[7/30] [750/1583]
                        Loss_D: 0.4006
                                         Loss_G: 2.0814
                                                                           D(G(z)):
                                                          D(x): 0.7894
0.1295 / 0.1614
[7/30] [800/1583]
                        Loss_D: 0.4696
                                         Loss_G: 2.0517
                                                                           D(G(z)):
                                                          D(x): 0.7500
0.1307 / 0.1610
[7/30] [850/1583]
                        Loss D: 1.3306
                                         Loss G: 6.1190
                                                          D(x): 0.9655
                                                                           D(G(z)):
0.6664 / 0.0037
[7/30] [900/1583]
                         Loss D: 0.6034
                                         Loss G: 4.6866
                                                         D(x): 0.9256
                                                                           D(G(z)):
0.3680 / 0.0127
[7/30] [950/1583]
                        Loss_D: 0.6402
                                         Loss_G: 2.2744
                                                         D(x): 0.6962
                                                                           D(G(z)):
0.1824 / 0.1325
[7/30] [1000/1583]
                         Loss_D: 0.4457
                                         Loss_G: 2.3907
                                                          D(x): 0.7629
                                                                           D(G(z)):
0.1217 / 0.1216
[7/30] [1050/1583]
                        Loss_D: 0.7547
                                         Loss_G: 2.9864
                                                          D(x): 0.7523
                                                                           D(G(z)):
0.3111 / 0.0684
[7/30] [1100/1583]
                         Loss_D: 0.3242
                                         Loss_G: 3.3246
                                                          D(x): 0.8397
                                                                           D(G(z)):
0.1118 / 0.0546
[7/30] [1150/1583]
                        Loss_D: 0.5734
                                         Loss_G: 3.1015
                                                          D(x): 0.8776
                                                                           D(G(z)):
0.3124 / 0.0634
[7/30] [1200/1583]
                                         Loss_G: 1.6907
                        Loss_D: 0.7984
                                                          D(x): 0.5567
                                                                           D(G(z)):
0.0798 / 0.2501
[7/30] [1250/1583]
                        Loss_D: 0.5744
                                         Loss_G: 1.9188
                                                          D(x): 0.6842
                                                                           D(G(z)):
0.1198 / 0.1907
                        Loss_D: 0.5647
                                         Loss_G: 1.7671
                                                                           D(G(z)):
[7/30] [1300/1583]
                                                          D(x): 0.6506
0.0693 / 0.2348
[7/30] [1350/1583]
                        Loss_D: 0.4028
                                         Loss_G: 2.6135
                                                          D(x): 0.8123
                                                                           D(G(z)):
0.1489 / 0.0937
[7/30] [1400/1583]
                        Loss_D: 0.7939
                                         Loss_G: 1.2339
                                                          D(x): 0.5226
                                                                           D(G(z)):
0.0424 / 0.3627
[7/30] [1450/1583]
                         Loss_D: 0.4909
                                         Loss_G: 1.5005
                                                          D(x): 0.6765
                                                                           D(G(z)):
0.0501 / 0.2752
[7/30] [1500/1583]
                         Loss_D: 1.0375
                                         Loss_G: 0.7651
                                                          D(x): 0.4941
                                                                           D(G(z)):
0.1479 / 0.5134
[7/30] [1550/1583]
                         Loss_D: 0.6326
                                         Loss_G: 4.4074 D(x): 0.9268
                                                                           D(G(z)):
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0.3817 / 0.0178
[8/30][0/1583] Loss_D: 0.4644 Loss_G: 3.2035 D(x): 0.8040
                                                                  D(G(z)): 0.1805
/ 0.0573
[8/30][50/1583] Loss_D: 0.4020 Loss_G: 3.2678 D(x): 0.9221
                                                                  D(G(z)): 0.2509
/ 0.0495
[8/30] [100/1583]
                        Loss_D: 0.2674 Loss_G: 3.5338 D(x): 0.9244
                                                                          D(G(z)):
0.1599 / 0.0385
[8/30] [150/1583]
                        Loss_D: 0.3696 Loss_G: 3.2331 D(x): 0.9218
                                                                          D(G(z)):
0.2250 / 0.0521
[8/30] [200/1583]
                        Loss D: 0.3300
                                         Loss_G: 3.1824
                                                         D(x): 0.8000
                                                                          D(G(z)):
0.0752 / 0.0625
[8/30] [250/1583]
                                         Loss_G: 2.6759
                        Loss_D: 0.3709
                                                         D(x): 0.8101
                                                                          D(G(z)):
0.1142 / 0.0948
[8/30] [300/1583]
                        Loss_D: 0.4294
                                         Loss_G: 2.1322
                                                         D(x): 0.7251
                                                                          D(G(z)):
0.0666 / 0.1583
[8/30] [350/1583]
                        Loss_D: 0.3607
                                         Loss_G: 3.6602
                                                                          D(G(z)):
                                                         D(x): 0.8876
0.1965 / 0.0341
[8/30] [400/1583]
                        Loss_D: 0.4802
                                         Loss_G: 4.9086
                                                                          D(G(z)):
                                                         D(x): 0.9407
0.3101 / 0.0118
[8/30] [450/1583]
                        Loss D: 0.8900
                                         Loss G: 3.4762 D(x): 0.8080
                                                                          D(G(z)):
0.4126 / 0.0491
[8/30] [500/1583]
                        Loss D: 0.6378
                                         Loss G: 2.0503 D(x): 0.6059
                                                                          D(G(z)):
0.0437 / 0.1706
                        Loss_D: 0.3504
                                         Loss_G: 2.4873
                                                                          D(G(z)):
[8/30] [550/1583]
                                                         D(x): 0.8256
0.1284 / 0.1054
[8/30] [600/1583]
                        Loss_D: 0.3160
                                         Loss_G: 2.9434
                                                         D(x): 0.7968
                                                                          D(G(z)):
0.0686 / 0.0751
[8/30] [650/1583]
                        Loss_D: 0.2989
                                         Loss_G: 3.7709
                                                         D(x): 0.9191
                                                                          D(G(z)):
0.1774 / 0.0320
[8/30] [700/1583]
                        Loss_D: 0.2967
                                         Loss_G: 2.8027
                                                         D(x): 0.9108
                                                                          D(G(z)):
0.1681 / 0.0799
[8/30] [750/1583]
                        Loss_D: 0.3015
                                         Loss_G: 2.7212 D(x): 0.8072
                                                                          D(G(z)):
0.0644 / 0.0987
[8/30] [800/1583]
                                         Loss_G: 6.4012 D(x): 0.9560
                        Loss_D: 1.0880
                                                                          D(G(z)):
0.5740 / 0.0034
[8/30] [850/1583]
                        Loss_D: 0.3633
                                         Loss_G: 2.8818 D(x): 0.7989
                                                                          D(G(z)):
0.0932 / 0.0777
[8/30] [900/1583]
                        Loss_D: 0.3202
                                         Loss_G: 2.3069
                                                         D(x): 0.8610
                                                                          D(G(z)):
0.1398 / 0.1257
[8/30] [950/1583]
                        Loss D: 0.6507
                                         Loss_G: 2.1558
                                                         D(x): 0.7176
                                                                          D(G(z)):
0.2180 / 0.1640
[8/30] [1000/1583]
                        Loss_D: 0.3536
                                         Loss_G: 2.4680
                                                         D(x): 0.8077
                                                                          D(G(z)):
0.1042 / 0.1168
[8/30] [1050/1583]
                        Loss_D: 0.6068
                                         Loss_G: 2.4671
                                                         D(x): 0.6221
                                                                          D(G(z)):
0.0682 / 0.1139
[8/30] [1100/1583]
                        Loss_D: 0.4076
                                         Loss_G: 2.4431
                                                         D(x): 0.7743
                                                                          D(G(z)):
0.1043 / 0.1207
[8/30] [1150/1583]
                        Loss_D: 0.2697
                                         Loss_G: 3.0718 D(x): 0.8897
                                                                          D(G(z)):
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0.1283 / 0.0654
[8/30] [1200/1583]
                        Loss_D: 0.5057 Loss_G: 5.4918 D(x): 0.9421
                                                                         D(G(z)):
0.3222 / 0.0058
[8/30] [1250/1583]
                        Loss_D: 0.6172 Loss_G: 2.3624 D(x): 0.6053
                                                                         D(G(z)):
0.0311 / 0.1316
                        Loss_D: 0.3516 Loss_G: 2.5290
[8/30] [1300/1583]
                                                        D(x): 0.8315
                                                                         D(G(z)):
0.1305 / 0.1006
[8/30] [1350/1583]
                        Loss_D: 1.3147 Loss_G: 0.5073 D(x): 0.3535
                                                                         D(G(z)):
0.0400 / 0.6429
[8/30] [1400/1583]
                        Loss D: 0.3908
                                        Loss_G: 2.2884
                                                        D(x): 0.8275
                                                                         D(G(z)):
0.1576 / 0.1358
[8/30] [1450/1583]
                        Loss_D: 0.4930
                                        Loss_G: 1.5033
                                                        D(x): 0.6795
                                                                         D(G(z)):
0.0479 / 0.2764
[8/30] [1500/1583]
                        Loss_D: 1.1238 Loss_G: 1.3565
                                                        D(x): 0.5509
                                                                         D(G(z)):
0.3074 / 0.3331
[8/30] [1550/1583]
                        Loss_D: 0.3943 Loss_G: 2.8315 D(x): 0.8253
                                                                         D(G(z)):
0.1560 / 0.0771
[9/30][0/1583] Loss_D: 0.2958 Loss_G: 3.3372 D(x): 0.8633
                                                                 D(G(z)): 0.1246
/ 0.0514
[9/30][50/1583] Loss_D: 0.2637 Loss_G: 3.5883 D(x): 0.9169
                                                                 D(G(z)): 0.1396
/ 0.0390
[9/30] [100/1583]
                        Loss D: 0.3204 Loss G: 3.2041 D(x): 0.8382
                                                                         D(G(z)):
0.1024 / 0.0610
                        Loss_D: 0.4145  Loss_G: 2.8728  D(x): 0.8255
[9/30] [150/1583]
                                                                         D(G(z)):
0.1698 / 0.0830
[9/30] [200/1583]
                        Loss_D: 0.8672 Loss_G: 1.3742 D(x): 0.5361
                                                                         D(G(z)):
0.0619 / 0.3207
[9/30] [250/1583]
                        Loss_D: 0.2769 Loss_G: 3.3639
                                                        D(x): 0.8535
                                                                         D(G(z)):
0.0906 / 0.0544
[9/30] [300/1583]
                        Loss_D: 0.2249
                                        Loss_G: 2.8036
                                                        D(x): 0.8931
                                                                         D(G(z)):
0.0964 / 0.0789
[9/30] [350/1583]
                        Loss_D: 0.4374 Loss_G: 1.8476
                                                        D(x): 0.7243
                                                                         D(G(z)):
0.0656 / 0.2072
[9/30] [400/1583]
                        Loss_D: 0.4149 Loss_G: 2.2776 D(x): 0.7190
                                                                         D(G(z)):
0.0432 / 0.1461
[9/30] [450/1583]
                        Loss_D: 0.3501 Loss_G: 2.4125 D(x): 0.7569
                                                                         D(G(z)):
0.0364 / 0.1334
[9/30] [500/1583]
                        Loss D: 1.0641
                                        Loss_G: 1.5313
                                                                         D(G(z)):
                                                        D(x): 0.4869
0.1460 / 0.2802
[9/30] [550/1583]
                        Loss D: 0.8147
                                        Loss_G: 1.6181 D(x): 0.5207
                                                                         D(G(z)):
0.0130 / 0.2685
[9/30] [600/1583]
                        Loss_D: 0.9451 Loss_G: 5.9107 D(x): 0.9557
                                                                         D(G(z)):
0.5183 / 0.0053
[9/30] [650/1583]
                        Loss_D: 0.3231
                                        Loss_G: 3.5600
                                                        D(x): 0.9441
                                                                         D(G(z)):
0.2186 / 0.0381
[9/30] [700/1583]
                        Loss D: 0.7494
                                        Loss_G: 1.8437
                                                        D(x): 0.6864
                                                                         D(G(z)):
0.2387 / 0.2226
[9/30] [750/1583]
                        Loss_D: 0.5642 Loss_G: 1.7775 D(x): 0.6382
                                                                         D(G(z)):
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0.0269 / 0.2319
[9/30] [800/1583]
                        Loss_D: 0.3252 Loss_G: 2.9417 D(x): 0.8149
                                                                          D(G(z)):
0.0855 / 0.0748
[9/30] [850/1583]
                        Loss_D: 0.3426
                                        Loss_G: 3.0385
                                                         D(x): 0.8861
                                                                          D(G(z)):
0.1675 / 0.0694
[9/30] [900/1583]
                        Loss_D: 0.2860
                                        Loss_G: 2.7788
                                                         D(x): 0.7967
                                                                          D(G(z)):
0.0308 / 0.0912
[9/30] [950/1583]
                        Loss_D: 0.3798
                                        Loss_G: 3.0154 D(x): 0.8720
                                                                          D(G(z)):
0.1843 / 0.0708
[9/30] [1000/1583]
                        Loss D: 0.5796
                                        Loss_G: 3.1021
                                                         D(x): 0.8125
                                                                          D(G(z)):
0.2576 / 0.0622
[9/30] [1050/1583]
                        Loss_D: 1.5225
                                         Loss_G: 6.0145
                                                         D(x): 0.9910
                                                                          D(G(z)):
0.7049 / 0.0044
[9/30] [1100/1583]
                        Loss_D: 1.3540
                                        Loss_G: 4.7363
                                                         D(x): 0.8906
                                                                          D(G(z)):
0.6370 / 0.0160
[9/30] [1150/1583]
                                        Loss_G: 2.1122 D(x): 0.6713
                                                                          D(G(z)):
                        Loss_D: 0.6121
0.1331 / 0.1715
[9/30] [1200/1583]
                        Loss_D: 0.2469
                                        Loss_G: 3.5986
                                                                          D(G(z)):
                                                         D(x): 0.9255
0.1443 / 0.0373
[9/30] [1250/1583]
                        Loss D: 1.4028
                                        Loss G: 0.4766
                                                        D(x): 0.3263
                                                                          D(G(z)):
0.0154 / 0.6670
[9/30] [1300/1583]
                        Loss D: 0.2075
                                        Loss G: 4.1340 D(x): 0.9622
                                                                          D(G(z)):
0.1448 / 0.0225
                                        Loss_G: 0.7903
[9/30] [1350/1583]
                        Loss_D: 1.2335
                                                         D(x): 0.3923
                                                                          D(G(z)):
0.0158 / 0.5174
[9/30] [1400/1583]
                        Loss_D: 0.3590
                                        Loss_G: 2.8566
                                                                          D(G(z)):
                                                         D(x): 0.7698
0.0553 / 0.0816
[9/30] [1450/1583]
                        Loss_D: 0.2694
                                       Loss_G: 2.9212 D(x): 0.8604
                                                                          D(G(z)):
0.0847 / 0.0760
[9/30] [1500/1583]
                        Loss_D: 1.7421
                                        Loss_G: 4.6734
                                                         D(x): 0.9309
                                                                          D(G(z)):
0.7243 / 0.0171
[9/30] [1550/1583]
                        Loss_D: 0.3930 Loss_G: 1.7891 D(x): 0.7565
                                                                          D(G(z)):
0.0660 / 0.2280
[10/30][0/1583] Loss_D: 0.3155 Loss_G: 3.5864 D(x): 0.9344
                                                                 D(G(z)): 0.1974
/ 0.0389
[10/30] [50/1583]
                        Loss_D: 1.0987 Loss_G: 6.0832 D(x): 0.9809
                                                                          D(G(z)):
0.5909 / 0.0038
[10/30] [100/1583]
                        Loss D: 0.2192
                                        Loss_G: 3.3723
                                                                          D(G(z)):
                                                         D(x): 0.9192
0.1116 / 0.0496
[10/30] [150/1583]
                        Loss_D: 0.2954
                                        Loss_G: 3.5063 D(x): 0.9279
                                                                          D(G(z)):
0.1785 / 0.0398
[10/30] [200/1583]
                        Loss_D: 0.2536
                                        Loss_G: 2.6603
                                                         D(x): 0.8303
                                                                          D(G(z)):
0.0506 / 0.1014
[10/30] [250/1583]
                        Loss_D: 3.6676
                                        Loss_G: 0.5522
                                                         D(x): 0.0477
                                                                          D(G(z)):
0.0068 / 0.6601
                        Loss_D: 1.1554
[10/30] [300/1583]
                                        Loss_G: 5.4316
                                                        D(x): 0.9006
                                                                          D(G(z)):
0.5695 / 0.0087
[10/30] [350/1583]
                        Loss_D: 0.4225 Loss_G: 1.9414 D(x): 0.7424
                                                                          D(G(z)):
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0.0841 / 0.1928
[10/30] [400/1583]
                        Loss_D: 0.3150 Loss_G: 3.7332 D(x): 0.8726
                                                                          D(G(z)):
0.1384 / 0.0357
[10/30] [450/1583]
                        Loss_D: 0.5198
                                         Loss_G: 5.1294 D(x): 0.9229
                                                                          D(G(z)):
0.3179 / 0.0089
[10/30] [500/1583]
                        Loss_D: 0.3614
                                         Loss_G: 2.2300
                                                         D(x): 0.7664
                                                                          D(G(z)):
0.0602 / 0.1551
[10/30] [550/1583]
                        Loss_D: 0.1697
                                         Loss_G: 3.4831 D(x): 0.9432
                                                                          D(G(z)):
0.0974 / 0.0441
[10/30] [600/1583]
                        Loss_D: 0.2290
                                         Loss_G: 2.9312
                                                         D(x): 0.8745
                                                                          D(G(z)):
0.0765 / 0.0720
[10/30] [650/1583]
                        Loss_D: 0.2630
                                         Loss_G: 3.2345
                                                         D(x): 0.8612
                                                                          D(G(z)):
0.0909 / 0.0584
[10/30] [700/1583]
                        Loss_D: 0.7754
                                         Loss_G: 4.7707
                                                         D(x): 0.9638
                                                                          D(G(z)):
0.4467 / 0.0142
[10/30] [750/1583]
                        Loss_D: 0.2689
                                                                          D(G(z)):
                                         Loss_G: 3.9465
                                                         D(x): 0.9205
0.1514 / 0.0304
[10/30] [800/1583]
                        Loss_D: 0.3369
                                         Loss_G: 2.8455
                                                                          D(G(z)):
                                                         D(x): 0.7783
0.0574 / 0.0934
[10/30] [850/1583]
                        Loss D: 0.2564
                                         Loss G: 3.1422 D(x): 0.8366
                                                                          D(G(z)):
0.0576 / 0.0677
[10/30] [900/1583]
                        Loss D: 0.1690
                                         Loss G: 3.6391 D(x): 0.9101
                                                                          D(G(z)):
0.0651 / 0.0382
[10/30] [950/1583]
                        Loss D: 0.1984
                                         Loss G: 3.5910
                                                         D(x): 0.8900
                                                                          D(G(z)):
0.0671 / 0.0471
[10/30] [1000/1583]
                        Loss_D: 1.7138
                                         Loss_G: 5.9048
                                                         D(x): 0.9953
                                                                          D(G(z)):
0.7322 / 0.0059
[10/30] [1050/1583]
                        Loss_D: 0.3586
                                         Loss_G: 3.3315
                                                         D(x): 0.9391
                                                                          D(G(z)):
0.2313 / 0.0533
[10/30] [1100/1583]
                        Loss_D: 0.1726
                                         Loss_G: 3.6113
                                                         D(x): 0.9413
                                                                          D(G(z)):
0.0981 / 0.0419
[10/30] [1150/1583]
                        Loss_D: 0.5156
                                         Loss_G: 2.0536
                                                         D(x): 0.7072
                                                                          D(G(z)):
0.0941 / 0.1866
[10/30] [1200/1583]
                                         Loss_G: 3.9093
                        Loss_D: 0.6057
                                                         D(x): 0.9230
                                                                          D(G(z)):
0.3610 / 0.0348
[10/30] [1250/1583]
                        Loss_D: 0.2366
                                         Loss_G: 2.9687
                                                         D(x): 0.8745
                                                                          D(G(z)):
0.0855 / 0.0709
[10/30] [1300/1583]
                        Loss_D: 0.1557
                                         Loss_G: 4.0913
                                                                          D(G(z)):
                                                         D(x): 0.9648
0.1061 / 0.0235
[10/30] [1350/1583]
                        Loss_D: 0.2797
                                         Loss_G: 4.9853
                                                         D(x): 0.9453
                                                                          D(G(z)):
0.1806 / 0.0101
[10/30] [1400/1583]
                        Loss_D: 0.1961
                                         Loss_G: 4.0257
                                                         D(x): 0.9514
                                                                          D(G(z)):
0.1200 / 0.0271
[10/30] [1450/1583]
                        Loss_D: 0.5886
                                         Loss_G: 0.8652
                                                         D(x): 0.6206
                                                                          D(G(z)):
0.0134 / 0.4916
[10/30] [1500/1583]
                        Loss_D: 0.5822
                                         Loss_G: 1.8413
                                                         D(x): 0.6445
                                                                          D(G(z)):
0.0488 / 0.2231
[10/30] [1550/1583]
                        Loss_D: 1.0090 Loss_G: 4.1914 D(x): 0.9256
                                                                          D(G(z)):
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0.5297 / 0.0240
[11/30][0/1583] Loss_D: 0.6740 Loss_G: 2.3080 D(x): 0.6855
                                                                  D(G(z)): 0.1841
/ 0.1459
[11/30] [50/1583]
                        Loss_D: 0.2028 Loss_G: 3.0703 D(x): 0.8717
                                                                          D(G(z)):
0.0523 / 0.0681
[11/30] [100/1583]
                        Loss_D: 0.1881
                                        Loss_G: 3.4168
                                                         D(x): 0.9036
                                                                          D(G(z)):
0.0769 / 0.0469
[11/30] [150/1583]
                        Loss_D: 0.2043 Loss_G: 3.5083
                                                         D(x): 0.9205
                                                                          D(G(z)):
0.1061 / 0.0406
[11/30] [200/1583]
                        Loss_D: 0.2159
                                         Loss_G: 2.3032
                                                         D(x): 0.8693
                                                                          D(G(z)):
0.0616 / 0.1305
                        Loss_D: 0.4003
                                         Loss_G: 2.5963
[11/30] [250/1583]
                                                         D(x): 0.7279
                                                                          D(G(z)):
0.0330 / 0.1209
[11/30] [300/1583]
                        Loss_D: 0.3804
                                         Loss_G: 4.3354
                                                         D(x): 0.9096
                                                                          D(G(z)):
0.2194 / 0.0209
[11/30] [350/1583]
                        Loss_D: 0.1877
                                         Loss_G: 4.0537
                                                                          D(G(z)):
                                                         D(x): 0.9418
0.1092 / 0.0292
[11/30] [400/1583]
                        Loss_D: 0.1689
                                         Loss_G: 4.3222 D(x): 0.9682
                                                                          D(G(z)):
0.1162 / 0.0192
[11/30] [450/1583]
                        Loss D: 0.1882
                                         Loss G: 3.6440 D(x): 0.8653
                                                                          D(G(z)):
0.0301 / 0.0417
[11/30] [500/1583]
                        Loss D: 0.2911
                                         Loss G: 2.4417 D(x): 0.8047
                                                                          D(G(z)):
0.0397 / 0.1194
                        Loss_D: 0.4499
                                         Loss_G: 4.9896
                                                                          D(G(z)):
[11/30] [550/1583]
                                                         D(x): 0.9684
0.3022 / 0.0112
[11/30] [600/1583]
                        Loss_D: 1.1832
                                         Loss_G: 4.0197
                                                         D(x): 0.9324
                                                                          D(G(z)):
0.5799 / 0.0326
[11/30] [650/1583]
                        Loss_D: 0.3420
                                         Loss_G: 2.7952
                                                         D(x): 0.7673
                                                                          D(G(z)):
0.0358 / 0.0971
[11/30] [700/1583]
                        Loss_D: 0.1906
                                         Loss_G: 4.2155
                                                         D(x): 0.9716
                                                                          D(G(z)):
0.1368 / 0.0211
[11/30] [750/1583]
                        Loss_D: 0.2651
                                         Loss_G: 4.7661
                                                         D(x): 0.9658
                                                                          D(G(z)):
0.1852 / 0.0143
[11/30] [800/1583]
                        Loss_D: 0.1669
                                         Loss_G: 3.7519
                                                         D(x): 0.9082
                                                                          D(G(z)):
0.0572 / 0.0356
[11/30] [850/1583]
                        Loss_D: 0.1606
                                         Loss_G: 4.1807
                                                         D(x): 0.9637
                                                                          D(G(z)):
0.1087 / 0.0247
[11/30] [900/1583]
                        Loss D: 0.1381
                                         Loss_G: 3.6825
                                                         D(x): 0.9209
                                                                          D(G(z)):
0.0451 / 0.0444
[11/30] [950/1583]
                        Loss_D: 0.1576
                                         Loss_G: 4.9790 D(x): 0.9735
                                                                          D(G(z)):
0.1131 / 0.0105
[11/30] [1000/1583]
                        Loss_D: 0.1435
                                         Loss_G: 2.8014 D(x): 0.9286
                                                                          D(G(z)):
0.0605 / 0.0786
[11/30] [1050/1583]
                        Loss_D: 0.6305
                                         Loss_G: 5.0745
                                                         D(x): 0.9114
                                                                          D(G(z)):
0.3684 / 0.0104
[11/30] [1100/1583]
                        Loss_D: 0.6087
                                         Loss_G: 2.6222
                                                        D(x): 0.7078
                                                                          D(G(z)):
0.1692 / 0.1062
[11/30] [1150/1583]
                        Loss_D: 1.1530 Loss_G: 1.2865 D(x): 0.3821
                                                                          D(G(z)):
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0.0115 / 0.3487
[11/30] [1200/1583]
                        Loss_D: 0.2512 Loss_G: 3.7180 D(x): 0.9255
                                                                         D(G(z)):
0.1420 / 0.0393
                        Loss_D: 0.2303
                                        Loss_G: 3.5932 D(x): 0.9220
[11/30] [1250/1583]
                                                                         D(G(z)):
0.1269 / 0.0394
[11/30] [1300/1583]
                        Loss_D: 0.4091
                                        Loss_G: 3.7610
                                                         D(x): 0.9746
                                                                         D(G(z)):
0.2864 / 0.0361
[11/30] [1350/1583]
                        Loss_D: 0.1155
                                        Loss_G: 3.6801 D(x): 0.9510
                                                                         D(G(z)):
0.0598 / 0.0374
[11/30] [1400/1583]
                        Loss D: 0.2150
                                        Loss_G: 3.0515
                                                        D(x): 0.8847
                                                                         D(G(z)):
0.0757 / 0.0731
[11/30] [1450/1583]
                        Loss_D: 0.2373
                                        Loss_G: 3.6855
                                                         D(x): 0.9324
                                                                         D(G(z)):
0.1386 / 0.0355
[11/30] [1500/1583]
                        Loss_D: 1.4366
                                        Loss_G: 0.3454
                                                        D(x): 0.3297
                                                                         D(G(z)):
0.1081 / 0.7382
                        Loss_D: 0.2257 Loss_G: 3.7827 D(x): 0.9296
                                                                         D(G(z)):
[11/30] [1550/1583]
0.1261 / 0.0358
[12/30][0/1583] Loss_D: 0.3178 Loss_G: 3.8107 D(x): 0.9648
                                                                 D(G(z)): 0.2164
/ 0.0332
[12/30] [50/1583]
                        Loss D: 0.4684 Loss G: 2.6492 D(x): 0.6847
                                                                         D(G(z)):
0.0190 / 0.0966
[12/30] [100/1583]
                        Loss D: 0.2012 Loss G: 4.0008 D(x): 0.9338
                                                                         D(G(z)):
0.1151 / 0.0260
                        Loss_D: 0.2237
                                        Loss_G: 3.3391
[12/30] [150/1583]
                                                        D(x): 0.8408
                                                                         D(G(z)):
0.0308 / 0.0562
[12/30] [200/1583]
                        Loss_D: 0.1581
                                        Loss_G: 3.2162 D(x): 0.9368
                                                                         D(G(z)):
0.0811 / 0.0633
[12/30] [250/1583]
                        Loss_D: 1.6095 Loss_G: 6.0060
                                                        D(x): 0.9842
                                                                         D(G(z)):
0.7143 / 0.0042
[12/30] [300/1583]
                        Loss_D: 0.3439
                                        Loss_G: 4.7286
                                                         D(x): 0.9242
                                                                         D(G(z)):
0.2009 / 0.0143
[12/30] [350/1583]
                        Loss_D: 0.2358
                                        Loss_G: 4.2418
                                                        D(x): 0.9636
                                                                         D(G(z)):
0.1619 / 0.0215
[12/30] [400/1583]
                                        Loss_G: 2.0127
                        Loss_D: 0.2853
                                                        D(x): 0.8299
                                                                         D(G(z)):
0.0647 / 0.1984
[12/30] [450/1583]
                        Loss_D: 0.2497
                                        Loss_G: 3.9096 D(x): 0.9200
                                                                         D(G(z)):
0.1366 / 0.0320
[12/30] [500/1583]
                        Loss D: 0.4909
                                        Loss_G: 2.4645
                                                         D(x): 0.7079
                                                                         D(G(z)):
0.0713 / 0.1283
[12/30] [550/1583]
                        Loss D: 0.3970
                                        Loss_G: 5.4601 D(x): 0.9605
                                                                         D(G(z)):
0.2534 / 0.0066
[12/30] [600/1583]
                        Loss_D: 0.8134
                                       Loss_G: 6.3194 D(x): 0.9900
                                                                         D(G(z)):
0.4750 / 0.0028
[12/30] [650/1583]
                        Loss_D: 0.1933
                                        Loss_G: 3.4817
                                                         D(x): 0.8721
                                                                         D(G(z)):
0.0441 / 0.0582
[12/30] [700/1583]
                        Loss D: 0.1422
                                        Loss_G: 4.3928
                                                        D(x): 0.9784
                                                                         D(G(z)):
0.1069 / 0.0176
[12/30] [750/1583]
                        Loss_D: 0.1255 Loss_G: 3.4844 D(x): 0.9173
                                                                         D(G(z)):
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0.0321 / 0.0467
[12/30] [800/1583]
                        Loss_D: 2.2699 Loss_G: 0.1153 D(x): 0.1713
                                                                         D(G(z)):
0.0093 / 0.9110
[12/30] [850/1583]
                                        Loss_G: 5.1285
                        Loss_D: 0.4606
                                                         D(x): 0.9600
                                                                         D(G(z)):
0.2959 / 0.0096
[12/30] [900/1583]
                        Loss_D: 0.6417
                                        Loss_G: 4.2254
                                                         D(x): 0.8619
                                                                         D(G(z)):
0.3323 / 0.0244
[12/30] [950/1583]
                        Loss_D: 0.6440
                                        Loss_G: 5.7955
                                                        D(x): 0.9520
                                                                         D(G(z)):
0.3928 / 0.0062
[12/30] [1000/1583]
                        Loss D: 0.5171
                                        Loss_G: 1.2156
                                                         D(x): 0.6638
                                                                         D(G(z)):
0.0209 / 0.3733
                                        Loss_G: 2.3794
[12/30] [1050/1583]
                        Loss_D: 0.2016
                                                        D(x): 0.8734
                                                                         D(G(z)):
0.0521 / 0.1354
[12/30] [1100/1583]
                        Loss_D: 0.1081
                                        Loss_G: 3.9541
                                                         D(x): 0.9461
                                                                         D(G(z)):
0.0466 / 0.0296
[12/30] [1150/1583]
                        Loss_D: 0.8832
                                        Loss_G: 1.4364
                                                                         D(G(z)):
                                                         D(x): 0.4964
0.0443 / 0.3230
[12/30] [1200/1583]
                        Loss_D: 0.1439
                                        Loss_G: 3.7202 D(x): 0.9178
                                                                         D(G(z)):
0.0465 / 0.0414
[12/30] [1250/1583]
                        Loss D: 0.2553
                                        Loss G: 2.9988
                                                         D(x): 0.8047
                                                                         D(G(z)):
0.0204 / 0.0793
[12/30] [1300/1583]
                        Loss D: 0.1671 Loss G: 4.4865 D(x): 0.9608
                                                                         D(G(z)):
0.1073 / 0.0178
                        Loss_D: 3.9724 Loss_G: 0.0444
[12/30] [1350/1583]
                                                        D(x): 0.0487
                                                                         D(G(z)):
0.0166 / 0.9585
[12/30] [1400/1583]
                        Loss_D: 3.2782 Loss_G: 4.4956
                                                                         D(G(z)):
                                                        D(x): 0.9617
0.9042 / 0.0273
[12/30] [1450/1583]
                        Loss_D: 0.5231 Loss_G: 3.2605
                                                         D(x): 0.9003
                                                                         D(G(z)):
0.2779 / 0.0615
[12/30] [1500/1583]
                        Loss_D: 0.2272 Loss_G: 2.3959
                                                         D(x): 0.8640
                                                                         D(G(z)):
0.0626 / 0.1318
[12/30] [1550/1583]
                        Loss_D: 0.7775 Loss_G: 1.9137 D(x): 0.6994
                                                                         D(G(z)):
0.2827 / 0.1871
[13/30][0/1583] Loss_D: 0.6156 Loss_G: 1.9287 D(x): 0.6399
                                                                 D(G(z)): 0.0794
/ 0.2047
[13/30] [50/1583]
                        Loss_D: 0.2945 Loss_G: 5.9109 D(x): 0.9865
                                                                         D(G(z)):
0.2233 / 0.0040
[13/30] [100/1583]
                        Loss D: 0.2686
                                        Loss_G: 4.2089
                                                                         D(G(z)):
                                                         D(x): 0.9514
0.1768 / 0.0227
[13/30] [150/1583]
                        Loss D: 0.1086
                                        Loss_G: 4.4081 D(x): 0.9604
                                                                         D(G(z)):
0.0609 / 0.0186
[13/30] [200/1583]
                        Loss_D: 0.1077
                                        Loss_G: 3.8483
                                                        D(x): 0.9467
                                                                         D(G(z)):
0.0477 / 0.0339
[13/30] [250/1583]
                        Loss_D: 0.7310
                                        Loss_G: 3.6199
                                                         D(x): 0.9281
                                                                         D(G(z)):
0.4123 / 0.0415
[13/30] [300/1583]
                        Loss_D: 0.1391
                                        Loss_G: 3.3463
                                                         D(x): 0.9030
                                                                         D(G(z)):
0.0288 / 0.0565
[13/30] [350/1583]
                        Loss_D: 0.1140 Loss_G: 4.2850 D(x): 0.9388
                                                                         D(G(z)):
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0.0436 / 0.0222
[13/30] [400/1583]
                        Loss_D: 0.4863 Loss_G: 6.6403 D(x): 0.9845
                                                                          D(G(z)):
0.3344 / 0.0027
[13/30] [450/1583]
                        Loss_D: 0.1596
                                         Loss_G: 4.4368
                                                          D(x): 0.9696
                                                                          D(G(z)):
0.1117 / 0.0174
[13/30] [500/1583]
                        Loss_D: 0.0978
                                         Loss_G: 3.9018
                                                          D(x): 0.9742
                                                                          D(G(z)):
0.0665 / 0.0310
[13/30] [550/1583]
                        Loss_D: 0.1414
                                         Loss_G: 3.2720
                                                         D(x): 0.9568
                                                                          D(G(z)):
0.0854 / 0.0551
[13/30] [600/1583]
                        Loss D: 0.0966
                                         Loss_G: 4.2530
                                                          D(x): 0.9664
                                                                          D(G(z)):
0.0549 / 0.0228
[13/30] [650/1583]
                        Loss_D: 0.5315
                                         Loss_G: 2.9923
                                                          D(x): 0.7629
                                                                          D(G(z)):
0.1783 / 0.0810
[13/30] [700/1583]
                        Loss_D: 0.7568
                                         Loss_G: 5.1836
                                                          D(x): 0.9834
                                                                          D(G(z)):
0.4343 / 0.0108
                                                          D(x): 0.9147
[13/30] [750/1583]
                        Loss_D: 0.2680
                                         Loss_G: 3.9838
                                                                          D(G(z)):
0.1417 / 0.0283
[13/30] [800/1583]
                        Loss_D: 0.1577
                                         Loss_G: 3.3868
                                                                          D(G(z)):
                                                          D(x): 0.8823
0.0210 / 0.0551
[13/30] [850/1583]
                        Loss D: 0.1982
                                         Loss G: 3.2771
                                                          D(x): 0.8643
                                                                          D(G(z)):
0.0395 / 0.0620
[13/30] [900/1583]
                        Loss D: 0.1012
                                         Loss G: 4.3940 D(x): 0.9879
                                                                          D(G(z)):
0.0811 / 0.0183
                                         Loss_G: 4.0574
                        Loss_D: 0.0737
[13/30] [950/1583]
                                                         D(x): 0.9522
                                                                          D(G(z)):
0.0225 / 0.0277
[13/30] [1000/1583]
                        Loss_D: 0.1029
                                         Loss_G: 4.7443
                                                         D(x): 0.9878
                                                                          D(G(z)):
0.0819 / 0.0140
[13/30] [1050/1583]
                        Loss_D: 1.3232
                                         Loss_G: 5.0977
                                                          D(x): 0.9764
                                                                          D(G(z)):
0.6359 / 0.0123
[13/30] [1100/1583]
                        Loss_D: 0.3509
                                         Loss_G: 4.7830
                                                          D(x): 0.9549
                                                                          D(G(z)):
0.2261 / 0.0143
[13/30] [1150/1583]
                        Loss_D: 0.2707
                                         Loss_G: 4.1928
                                                          D(x): 0.9445
                                                                          D(G(z)):
0.1724 / 0.0255
[13/30] [1200/1583]
                                         Loss_G: 3.7346
                        Loss_D: 0.1393
                                                          D(x): 0.9253
                                                                          D(G(z)):
0.0551 / 0.0374
[13/30] [1250/1583]
                        Loss_D: 0.9670
                                         Loss_G: 1.5740
                                                          D(x): 0.6042
                                                                          D(G(z)):
0.2817 / 0.2589
[13/30] [1300/1583]
                        Loss_D: 1.0413
                                         Loss_G: 7.1590
                                                          D(x): 0.9633
                                                                          D(G(z)):
0.5513 / 0.0017
[13/30] [1350/1583]
                        Loss_D: 0.5064
                                         Loss_G: 5.2551 D(x): 0.9329
                                                                          D(G(z)):
0.3049 / 0.0082
[13/30] [1400/1583]
                        Loss_D: 0.5631
                                         Loss_G: 8.0910
                                                         D(x): 0.9776
                                                                          D(G(z)):
0.3644 / 0.0005
[13/30] [1450/1583]
                        Loss_D: 0.1425
                                         Loss_G: 4.6539
                                                          D(x): 0.9788
                                                                          D(G(z)):
0.1068 / 0.0158
[13/30] [1500/1583]
                        Loss_D: 0.1334
                                         Loss_G: 4.2541
                                                          D(x): 0.9569
                                                                          D(G(z)):
0.0778 / 0.0230
[13/30] [1550/1583]
                        Loss_D: 0.1388 Loss_G: 3.3215 D(x): 0.9168
                                                                          D(G(z)):
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0.0417 / 0.0570
[14/30][0/1583] Loss_D: 0.4898 Loss_G: 2.0201 D(x): 0.7443
                                                                 D(G(z)): 0.1272
/ 0.1855
[14/30] [50/1583]
                        Loss_D: 0.1281 Loss_G: 3.5656 D(x): 0.9325
                                                                          D(G(z)):
0.0493 / 0.0460
[14/30] [100/1583]
                        Loss_D: 0.2130 Loss_G: 6.1268
                                                         D(x): 0.9795
                                                                          D(G(z)):
0.1637 / 0.0032
[14/30] [150/1583]
                        Loss_D: 0.2911 Loss_G: 3.2008 D(x): 0.7908
                                                                          D(G(z)):
0.0230 / 0.0775
[14/30] [200/1583]
                        Loss_D: 0.4136
                                        Loss_G: 3.6171
                                                         D(x): 0.8390
                                                                          D(G(z)):
0.1642 / 0.0444
[14/30] [250/1583]
                        Loss_D: 0.2220
                                         Loss_G: 4.5960
                                                         D(x): 0.9301
                                                                          D(G(z)):
0.1221 / 0.0169
[14/30] [300/1583]
                        Loss_D: 0.1542
                                        Loss_G: 4.8225
                                                         D(x): 0.9676
                                                                          D(G(z)):
0.1046 / 0.0125
[14/30] [350/1583]
                        Loss_D: 0.4628
                                         Loss_G: 5.5002 D(x): 0.9499
                                                                          D(G(z)):
0.2966 / 0.0065
[14/30] [400/1583]
                        Loss_D: 0.4843
                                        Loss_G: 2.0160 D(x): 0.6572
                                                                          D(G(z)):
0.0050 / 0.1917
[14/30] [450/1583]
                        Loss D: 0.3217
                                         Loss G: 1.6032 D(x): 0.7623
                                                                          D(G(z)):
0.0188 / 0.2836
[14/30] [500/1583]
                        Loss D: 1.7019
                                        Loss G: 0.4689
                                                         D(x): 0.2639
                                                                          D(G(z)):
0.0136 / 0.6744
                        Loss_D: 0.4214
                                        Loss_G: 2.0863
                                                                          D(G(z)):
[14/30] [550/1583]
                                                         D(x): 0.7694
0.1006 / 0.1735
[14/30] [600/1583]
                        Loss_D: 0.2510
                                         Loss_G: 4.7084
                                                         D(x): 0.9472
                                                                          D(G(z)):
0.1546 / 0.0150
[14/30] [650/1583]
                        Loss_D: 0.2569
                                         Loss_G: 3.8862
                                                         D(x): 0.8880
                                                                          D(G(z)):
0.1087 / 0.0368
[14/30] [700/1583]
                        Loss_D: 0.3743
                                         Loss_G: 4.2257
                                                         D(x): 0.9913
                                                                          D(G(z)):
0.2631 / 0.0219
[14/30] [750/1583]
                        Loss_D: 0.1397
                                         Loss_G: 3.4851
                                                         D(x): 0.9148
                                                                          D(G(z)):
0.0442 / 0.0468
[14/30] [800/1583]
                                         Loss_G: 3.3065
                        Loss_D: 0.1588
                                                         D(x): 0.8924
                                                                          D(G(z)):
0.0353 / 0.0567
[14/30] [850/1583]
                        Loss_D: 0.1080
                                         Loss_G: 3.7945
                                                         D(x): 0.9413
                                                                          D(G(z)):
0.0417 / 0.0365
[14/30] [900/1583]
                        Loss D: 0.2474
                                         Loss_G: 5.9771
                                                                          D(G(z)):
                                                         D(x): 0.9804
0.1886 / 0.0038
[14/30] [950/1583]
                        Loss_D: 0.1305
                                         Loss_G: 3.6464 D(x): 0.9247
                                                                          D(G(z)):
0.0447 / 0.0434
[14/30] [1000/1583]
                        Loss_D: 0.1939
                                         Loss_G: 2.5818 D(x): 0.8824
                                                                          D(G(z)):
0.0501 / 0.1173
[14/30] [1050/1583]
                        Loss_D: 0.1293
                                         Loss_G: 2.9122 D(x): 0.9168
                                                                          D(G(z)):
0.0343 / 0.0840
[14/30] [1100/1583]
                        Loss_D: 1.4088
                                         Loss_G: 0.6847
                                                         D(x): 0.3346
                                                                          D(G(z)):
0.0367 / 0.5567
[14/30] [1150/1583]
                        Loss_D: 0.4518 Loss_G: 4.4497 D(x): 0.9076
                                                                          D(G(z)):
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0.2406 / 0.0179
[14/30] [1200/1583]
                        Loss_D: 0.9369 Loss_G: 1.5489 D(x): 0.5437
                                                                          D(G(z)):
0.1409 / 0.2840
[14/30] [1250/1583]
                        Loss_D: 0.2315
                                         Loss_G: 3.3279
                                                         D(x): 0.8589
                                                                          D(G(z)):
0.0563 / 0.0639
[14/30] [1300/1583]
                        Loss_D: 0.7485
                                         Loss_G: 3.5187
                                                         D(x): 0.9458
                                                                          D(G(z)):
0.4313 / 0.0455
[14/30] [1350/1583]
                        Loss_D: 0.1441 Loss_G: 4.0708 D(x): 0.9508
                                                                          D(G(z)):
0.0801 / 0.0290
[14/30] [1400/1583]
                        Loss D: 0.1524
                                        Loss_G: 3.4717
                                                         D(x): 0.9304
                                                                          D(G(z)):
0.0652 / 0.0503
[14/30] [1450/1583]
                        Loss_D: 0.1638
                                        Loss_G: 4.5744 D(x): 0.9806
                                                                          D(G(z)):
0.1263 / 0.0150
[14/30] [1500/1583]
                        Loss_D: 0.1218 Loss_G: 4.4474 D(x): 0.9553
                                                                          D(G(z)):
0.0633 / 0.0209
[14/30] [1550/1583]
                        Loss_D: 0.1938 Loss_G: 3.9137 D(x): 0.9245
                                                                          D(G(z)):
0.0961 / 0.0331
[15/30][0/1583] Loss_D: 0.4015 Loss_G: 1.8758 D(x): 0.7243
                                                                 D(G(z)): 0.0216
/ 0.2295
[15/30] [50/1583]
                        Loss D: 0.0922 Loss G: 4.2506 D(x): 0.9648
                                                                          D(G(z)):
0.0500 / 0.0241
[15/30] [100/1583]
                        Loss D: 0.1210 Loss G: 4.5607
                                                         D(x): 0.9789
                                                                          D(G(z)):
0.0879 / 0.0158
                        Loss D: 0.0878 Loss G: 4.1639
[15/30] [150/1583]
                                                         D(x): 0.9502
                                                                          D(G(z)):
0.0327 / 0.0269
[15/30] [200/1583]
                        Loss_D: 0.0865
                                         Loss_G: 4.5829
                                                         D(x): 0.9771
                                                                          D(G(z)):
0.0574 / 0.0175
[15/30] [250/1583]
                        Loss_D: 0.3495
                                        Loss_G: 2.8303
                                                         D(x): 0.8211
                                                                          D(G(z)):
0.1032 / 0.0885
[15/30] [300/1583]
                        Loss_D: 0.1052
                                         Loss_G: 3.4138
                                                         D(x): 0.9295
                                                                          D(G(z)):
0.0254 / 0.0555
[15/30] [350/1583]
                        Loss_D: 2.7824
                                         Loss_G: 4.1681
                                                         D(x): 0.9493
                                                                          D(G(z)):
0.8531 / 0.0310
[15/30] [400/1583]
                        Loss_D: 0.4234
                                         Loss_G: 3.2829
                                                         D(x): 0.8300
                                                                          D(G(z)):
0.1567 / 0.0554
[15/30] [450/1583]
                        Loss_D: 1.7269
                                         Loss_G: 6.1527
                                                         D(x): 0.9986
                                                                          D(G(z)):
0.7356 / 0.0047
[15/30] [500/1583]
                        Loss_D: 0.2870
                                         Loss_G: 3.3562
                                                         D(x): 0.8951
                                                                          D(G(z)):
0.1407 / 0.0556
[15/30] [550/1583]
                        Loss_D: 1.2119
                                         Loss_G: 2.3396
                                                         D(x): 0.3747
                                                                          D(G(z)):
0.0088 / 0.1602
[15/30] [600/1583]
                        Loss_D: 0.2934
                                        Loss_G: 6.4083
                                                         D(x): 0.9695
                                                                          D(G(z)):
0.2065 / 0.0027
[15/30] [650/1583]
                        Loss_D: 0.5858
                                         Loss_G: 7.5852
                                                         D(x): 0.9905
                                                                          D(G(z)):
0.3664 / 0.0008
[15/30] [700/1583]
                        Loss_D: 0.1908
                                         Loss_G: 3.1200
                                                         D(x): 0.9208
                                                                          D(G(z)):
0.0864 / 0.0682
[15/30] [750/1583]
                        Loss_D: 0.0901 Loss_G: 4.9398 D(x): 0.9704
                                                                          D(G(z)):
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0.0519 / 0.0126
[15/30] [800/1583]
                        Loss_D: 0.1061 Loss_G: 4.2115 D(x): 0.9481
                                                                         D(G(z)):
0.0466 / 0.0243
[15/30] [850/1583]
                        Loss_D: 0.0963
                                        Loss_G: 4.3794
                                                        D(x): 0.9704
                                                                         D(G(z)):
0.0610 / 0.0192
[15/30] [900/1583]
                        Loss_D: 2.1027
                                        Loss_G: 4.6633
                                                         D(x): 0.9430
                                                                         D(G(z)):
0.7890 / 0.0175
[15/30] [950/1583]
                        Loss_D: 0.1769
                                        Loss_G: 4.3382
                                                        D(x): 0.9285
                                                                         D(G(z)):
0.0830 / 0.0223
[15/30] [1000/1583]
                        Loss D: 0.2747
                                        Loss_G: 5.0431
                                                         D(x): 0.9777
                                                                         D(G(z)):
0.1998 / 0.0092
[15/30] [1050/1583]
                        Loss_D: 0.2945
                                        Loss_G: 3.2323
                                                         D(x): 0.8717
                                                                         D(G(z)):
0.1166 / 0.0768
[15/30] [1100/1583]
                        Loss_D: 0.1816
                                        Loss_G: 3.7839
                                                         D(x): 0.9314
                                                                         D(G(z)):
0.0925 / 0.0374
                                                         D(x): 0.6486
[15/30] [1150/1583]
                        Loss_D: 0.5320
                                        Loss_G: 1.8594
                                                                         D(G(z)):
0.0083 / 0.2238
[15/30] [1200/1583]
                        Loss_D: 0.4725
                                        Loss_G: 5.9297
                                                                         D(G(z)):
                                                         D(x): 0.9717
0.3170 / 0.0052
[15/30] [1250/1583]
                        Loss D: 0.4873
                                        Loss G: 2.9971 D(x): 0.7248
                                                                         D(G(z)):
0.1134 / 0.0828
[15/30] [1300/1583]
                        Loss D: 0.1866
                                        Loss G: 5.3723 D(x): 0.9798
                                                                         D(G(z)):
0.1422 / 0.0076
[15/30] [1350/1583]
                        Loss D: 0.0726
                                        Loss_G: 4.4875
                                                         D(x): 0.9735
                                                                         D(G(z)):
0.0420 / 0.0193
[15/30] [1400/1583]
                        Loss_D: 0.0618
                                        Loss_G: 5.0606
                                                         D(x): 0.9872
                                                                         D(G(z)):
0.0458 / 0.0107
[15/30] [1450/1583]
                        Loss_D: 0.1590 Loss_G: 2.8646
                                                        D(x): 0.9086
                                                                         D(G(z)):
0.0507 / 0.0824
[15/30] [1500/1583]
                        Loss_D: 0.2643
                                        Loss_G: 2.4109
                                                         D(x): 0.8283
                                                                         D(G(z)):
0.0469 / 0.1336
[15/30] [1550/1583]
                        Loss_D: 0.1410 Loss_G: 3.8791 D(x): 0.9334
                                                                         D(G(z)):
0.0618 / 0.0346
[16/30][0/1583] Loss_D: 2.5562 Loss_G: 0.6347 D(x): 0.1354
                                                                 D(G(z)): 0.0049
/ 0.5961
[16/30] [50/1583]
                        Loss_D: 0.1554 Loss_G: 5.6500 D(x): 0.9876
                                                                         D(G(z)):
0.1184 / 0.0060
[16/30] [100/1583]
                        Loss_D: 0.1192 Loss_G: 4.2274 D(x): 0.9246
                                                                         D(G(z)):
0.0355 / 0.0258
[16/30] [150/1583]
                        Loss_D: 0.7639
                                        Loss_G: 8.4642 D(x): 0.9918
                                                                         D(G(z)):
0.4683 / 0.0004
[16/30] [200/1583]
                        Loss_D: 0.5811 Loss_G: 1.7112 D(x): 0.6925
                                                                         D(G(z)):
0.1179 / 0.2587
[16/30] [250/1583]
                        Loss_D: 0.1430
                                        Loss_G: 4.0892
                                                         D(x): 0.9392
                                                                         D(G(z)):
0.0700 / 0.0264
[16/30] [300/1583]
                        Loss_D: 0.1210
                                        Loss_G: 3.9538
                                                         D(x): 0.9242
                                                                         D(G(z)):
0.0360 / 0.0323
[16/30] [350/1583]
                        Loss_D: 0.2219 Loss_G: 4.2149 D(x): 0.9442
                                                                         D(G(z)):
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0.1371 / 0.0251
[16/30] [400/1583]
                        Loss_D: 0.1108 Loss_G: 3.8792 D(x): 0.9468
                                                                          D(G(z)):
0.0490 / 0.0353
[16/30] [450/1583]
                        Loss_D: 0.0763
                                         Loss_G: 4.5190
                                                         D(x): 0.9664
                                                                          D(G(z)):
0.0389 / 0.0204
[16/30] [500/1583]
                        Loss_D: 0.1367
                                         Loss_G: 4.0296
                                                         D(x): 0.9432
                                                                          D(G(z)):
0.0656 / 0.0323
[16/30] [550/1583]
                        Loss_D: 0.1112
                                         Loss_G: 3.6743 D(x): 0.9378
                                                                          D(G(z)):
0.0395 / 0.0449
[16/30] [600/1583]
                        Loss D: 0.0728
                                         Loss_G: 4.2226
                                                         D(x): 0.9630
                                                                          D(G(z)):
0.0326 / 0.0220
[16/30] [650/1583]
                        Loss_D: 0.0495
                                         Loss_G: 4.4040
                                                         D(x): 0.9806
                                                                          D(G(z)):
0.0286 / 0.0212
[16/30] [700/1583]
                        Loss_D: 0.0457
                                         Loss_G: 5.1374 D(x): 0.9747
                                                                          D(G(z)):
0.0190 / 0.0105
[16/30] [750/1583]
                        Loss_D: 0.2385
                                         Loss_G: 2.4762 D(x): 0.8353
                                                                          D(G(z)):
0.0250 / 0.1314
[16/30] [800/1583]
                        Loss_D: 0.4975
                                         Loss_G: 4.1157
                                                                          D(G(z)):
                                                         D(x): 0.8629
0.2447 / 0.0284
[16/30] [850/1583]
                        Loss D: 0.2086
                                         Loss G: 4.9552
                                                         D(x): 0.9786
                                                                          D(G(z)):
0.1500 / 0.0111
[16/30] [900/1583]
                        Loss D: 0.2917
                                         Loss G: 3.2505
                                                         D(x): 0.7932
                                                                          D(G(z)):
0.0140 / 0.0749
                                         Loss_G: 4.5020
[16/30] [950/1583]
                        Loss_D: 0.1104
                                                         D(x): 0.9690
                                                                          D(G(z)):
0.0686 / 0.0192
[16/30] [1000/1583]
                        Loss_D: 0.0922
                                         Loss_G: 3.4859
                                                         D(x): 0.9415
                                                                          D(G(z)):
0.0266 / 0.0488
[16/30] [1050/1583]
                        Loss_D: 0.2341
                                         Loss_G: 3.6761
                                                         D(x): 0.9057
                                                                          D(G(z)):
0.1010 / 0.0427
[16/30] [1100/1583]
                        Loss_D: 0.1454
                                         Loss_G: 4.8087
                                                         D(x): 0.9545
                                                                          D(G(z)):
0.0804 / 0.0155
[16/30] [1150/1583]
                        Loss_D: 0.2641
                                         Loss_G: 3.7464
                                                         D(x): 0.8096
                                                                          D(G(z)):
0.0197 / 0.0531
[16/30] [1200/1583]
                                         Loss_G: 4.2203
                        Loss_D: 0.1193
                                                         D(x): 0.9683
                                                                          D(G(z)):
0.0774 / 0.0237
[16/30] [1250/1583]
                        Loss_D: 0.3027
                                         Loss_G: 6.6293
                                                         D(x): 0.9910
                                                                          D(G(z)):
0.2189 / 0.0023
[16/30] [1300/1583]
                        Loss_D: 0.1165
                                         Loss_G: 3.8110
                                                         D(x): 0.9309
                                                                          D(G(z)):
0.0375 / 0.0386
[16/30] [1350/1583]
                        Loss_D: 0.1018
                                         Loss_G: 4.0529
                                                         D(x): 0.9536
                                                                          D(G(z)):
0.0478 / 0.0282
[16/30] [1400/1583]
                        Loss_D: 0.1303
                                         Loss_G: 3.6275
                                                         D(x): 0.8952
                                                                          D(G(z)):
0.0110 / 0.0509
[16/30] [1450/1583]
                        Loss_D: 0.0735
                                         Loss_G: 4.4133
                                                         D(x): 0.9625
                                                                          D(G(z)):
0.0306 / 0.0227
[16/30] [1500/1583]
                        Loss_D: 0.7567
                                         Loss_G: 0.8946
                                                         D(x): 0.5487
                                                                          D(G(z)):
0.0225 / 0.5167
[16/30] [1550/1583]
                        Loss_D: 0.3891 Loss_G: 3.7005 D(x): 0.7898
                                                                          D(G(z)):
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0.0927 / 0.0454
[17/30][0/1583] Loss_D: 0.0820 Loss_G: 4.4065 D(x): 0.9565
                                                                 D(G(z)): 0.0341
/ 0.0231
[17/30] [50/1583]
                        Loss_D: 0.4868 Loss_G: 2.6087 D(x): 0.7517
                                                                          D(G(z)):
0.1282 / 0.1276
[17/30] [100/1583]
                        Loss_D: 0.3304
                                        Loss_G: 3.3167
                                                         D(x): 0.8545
                                                                          D(G(z)):
0.1114 / 0.0630
[17/30] [150/1583]
                        Loss_D: 0.2851 Loss_G: 3.8000 D(x): 0.8765
                                                                          D(G(z)):
0.1121 / 0.0366
[17/30] [200/1583]
                        Loss D: 0.4941
                                        Loss_G: 2.8908
                                                         D(x): 0.7873
                                                                          D(G(z)):
0.1744 / 0.0806
[17/30] [250/1583]
                        Loss_D: 0.5490
                                        Loss_G: 8.8095
                                                         D(x): 0.9951
                                                                          D(G(z)):
0.3530 / 0.0002
[17/30] [300/1583]
                        Loss_D: 1.1378
                                        Loss_G: 1.5516
                                                         D(x): 0.4435
                                                                          D(G(z)):
0.0830 / 0.2746
[17/30] [350/1583]
                        Loss_D: 0.2843
                                        Loss_G: 6.1783
                                                                          D(G(z)):
                                                         D(x): 0.9634
0.1859 / 0.0036
[17/30] [400/1583]
                        Loss_D: 0.5245
                                        Loss_G: 2.6074 D(x): 0.7611
                                                                          D(G(z)):
0.1728 / 0.1021
[17/30] [450/1583]
                        Loss D: 0.1551
                                        Loss G: 2.8391 D(x): 0.8808
                                                                          D(G(z)):
0.0167 / 0.0929
[17/30] [500/1583]
                        Loss D: 0.2219
                                        Loss G: 4.6521 D(x): 0.8374
                                                                          D(G(z)):
0.0187 / 0.0203
                                        Loss_G: 5.0533
[17/30] [550/1583]
                        Loss D: 0.0831
                                                        D(x): 0.9432
                                                                          D(G(z)):
0.0202 / 0.0122
[17/30] [600/1583]
                        Loss_D: 0.0847
                                        Loss_G: 4.1042 D(x): 0.9633
                                                                          D(G(z)):
0.0432 / 0.0276
[17/30] [650/1583]
                        Loss_D: 0.0741
                                        Loss_G: 4.5136
                                                        D(x): 0.9570
                                                                          D(G(z)):
0.0280 / 0.0197
[17/30] [700/1583]
                        Loss_D: 0.0862
                                        Loss_G: 4.2054
                                                         D(x): 0.9387
                                                                          D(G(z)):
0.0179 / 0.0291
[17/30] [750/1583]
                        Loss_D: 0.0508
                                        Loss_G: 5.0692
                                                         D(x): 0.9872
                                                                          D(G(z)):
0.0359 / 0.0105
[17/30] [800/1583]
                        Loss_D: 0.0554
                                        Loss_G: 4.8164
                                                        D(x): 0.9802
                                                                          D(G(z)):
0.0333 / 0.0148
[17/30] [850/1583]
                        Loss_D: 0.0963
                                        Loss_G: 3.4095
                                                         D(x): 0.9272
                                                                          D(G(z)):
0.0139 / 0.0668
[17/30] [900/1583]
                        Loss D: 0.6370
                                        Loss_G: 2.9603
                                                         D(x): 0.8411
                                                                          D(G(z)):
0.3074 / 0.0733
[17/30] [950/1583]
                        Loss_D: 0.1430
                                        Loss_G: 4.3604 D(x): 0.9476
                                                                          D(G(z)):
0.0725 / 0.0239
[17/30] [1000/1583]
                        Loss_D: 0.2689
                                        Loss_G: 4.3476
                                                        D(x): 0.8043
                                                                          D(G(z)):
0.0100 / 0.0315
[17/30] [1050/1583]
                        Loss_D: 0.2997
                                         Loss_G: 3.2393
                                                         D(x): 0.7852
                                                                          D(G(z)):
0.0132 / 0.0783
[17/30] [1100/1583]
                        Loss_D: 0.1734
                                        Loss_G: 3.9904
                                                         D(x): 0.8706
                                                                          D(G(z)):
0.0193 / 0.0384
[17/30] [1150/1583]
                        Loss_D: 0.1602 Loss_G: 4.5899 D(x): 0.9894
                                                                          D(G(z)):
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0.1266 / 0.0158
[17/30] [1200/1583]
                        Loss_D: 0.1127 Loss_G: 3.4512 D(x): 0.9318
                                                                         D(G(z)):
0.0321 / 0.0548
[17/30] [1250/1583]
                                        Loss_G: 0.7138
                        Loss_D: 1.8546
                                                        D(x): 0.2665
                                                                         D(G(z)):
0.0071 / 0.5553
[17/30] [1300/1583]
                        Loss_D: 0.1658
                                        Loss_G: 3.4971
                                                         D(x): 0.8707
                                                                         D(G(z)):
0.0102 / 0.0594
[17/30] [1350/1583]
                        Loss_D: 0.2915
                                        Loss_G: 4.7850 D(x): 0.9765
                                                                         D(G(z)):
0.1966 / 0.0156
[17/30] [1400/1583]
                        Loss D: 0.1570
                                        Loss_G: 5.4237
                                                         D(x): 0.9684
                                                                         D(G(z)):
0.1054 / 0.0081
[17/30] [1450/1583]
                        Loss_D: 0.3852
                                        Loss_G: 7.4126
                                                         D(x): 0.9876
                                                                         D(G(z)):
0.2729 / 0.0012
[17/30] [1500/1583]
                        Loss_D: 0.1949
                                        Loss_G: 2.2943
                                                        D(x): 0.8695
                                                                         D(G(z)):
0.0307 / 0.1503
[17/30] [1550/1583]
                        Loss_D: 0.0983 Loss_G: 4.7620 D(x): 0.9681
                                                                         D(G(z)):
0.0596 / 0.0157
[18/30][0/1583] Loss_D: 0.0825 Loss_G: 4.4848 D(x): 0.9686
                                                                 D(G(z)): 0.0460
/ 0.0196
[18/30] [50/1583]
                        Loss_D: 0.7841 Loss_G: 1.5794 D(x): 0.7097
                                                                         D(G(z)):
0.2817 / 0.2673
[18/30] [100/1583]
                        Loss D: 0.1797 Loss G: 4.6923 D(x): 0.9513
                                                                         D(G(z)):
0.1056 / 0.0164
                                        Loss_G: 3.5530
[18/30] [150/1583]
                        Loss D: 0.1049
                                                         D(x): 0.9160
                                                                         D(G(z)):
0.0130 / 0.0516
[18/30] [200/1583]
                        Loss_D: 0.6017
                                        Loss_G: 1.8990
                                                         D(x): 0.6783
                                                                         D(G(z)):
0.1346 / 0.2073
[18/30] [250/1583]
                        Loss_D: 0.0940
                                        Loss_G: 3.6887
                                                         D(x): 0.9435
                                                                         D(G(z)):
0.0308 / 0.0492
[18/30] [300/1583]
                        Loss_D: 0.1079
                                        Loss_G: 4.4993
                                                         D(x): 0.9664
                                                                         D(G(z)):
0.0655 / 0.0195
[18/30] [350/1583]
                        Loss_D: 0.1508
                                        Loss_G: 3.9044
                                                         D(x): 0.9346
                                                                         D(G(z)):
0.0672 / 0.0404
[18/30] [400/1583]
                                        Loss_G: 6.0711 D(x): 0.9713
                        Loss_D: 0.2566
                                                                         D(G(z)):
0.1764 / 0.0042
[18/30] [450/1583]
                        Loss_D: 1.4850
                                        Loss_G: 5.9779 D(x): 0.9913
                                                                         D(G(z)):
0.6740 / 0.0045
[18/30] [500/1583]
                        Loss D: 0.0831
                                        Loss_G: 3.8387
                                                                         D(G(z)):
                                                         D(x): 0.9483
0.0228 / 0.0377
[18/30] [550/1583]
                        Loss D: 0.1211
                                        Loss_G: 5.6405 D(x): 0.9894
                                                                         D(G(z)):
0.0980 / 0.0057
[18/30] [600/1583]
                        Loss_D: 0.0693
                                        Loss_G: 4.7632
                                                        D(x): 0.9537
                                                                         D(G(z)):
0.0198 / 0.0170
[18/30] [650/1583]
                        Loss_D: 0.0723
                                        Loss_G: 4.5687
                                                         D(x): 0.9617
                                                                         D(G(z)):
0.0291 / 0.0198
[18/30] [700/1583]
                        Loss_D: 0.0595
                                        Loss_G: 4.4199
                                                         D(x): 0.9683
                                                                         D(G(z)):
0.0253 / 0.0232
[18/30] [750/1583]
                        Loss_D: 0.0788 Loss_G: 4.3915 D(x): 0.9557
                                                                         D(G(z)):
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0.0288 / 0.0252
[18/30] [800/1583]
                        Loss_D: 0.3808 Loss_G: 4.9723 D(x): 0.9618
                                                                         D(G(z)):
0.2363 / 0.0160
[18/30] [850/1583]
                        Loss_D: 0.6532
                                        Loss_G: 2.5454
                                                        D(x): 0.6017
                                                                         D(G(z)):
0.0169 / 0.1358
[18/30] [900/1583]
                        Loss_D: 0.0645
                                        Loss_G: 5.1007
                                                         D(x): 0.9692
                                                                         D(G(z)):
0.0304 / 0.0124
[18/30] [950/1583]
                        Loss_D: 0.0970
                                        Loss_G: 4.3983
                                                        D(x): 0.9351
                                                                         D(G(z)):
0.0220 / 0.0211
[18/30] [1000/1583]
                        Loss D: 0.2013
                                        Loss_G: 6.0688
                                                        D(x): 0.9918
                                                                         D(G(z)):
0.1569 / 0.0041
[18/30] [1050/1583]
                        Loss_D: 0.0938
                                        Loss_G: 3.7722 D(x): 0.9412
                                                                         D(G(z)):
0.0241 / 0.0442
[18/30] [1100/1583]
                        Loss_D: 0.0329
                                        Loss_G: 5.2791
                                                         D(x): 0.9844
                                                                         D(G(z)):
0.0165 / 0.0110
[18/30] [1150/1583]
                                        Loss_G: 2.9099
                                                                         D(G(z)):
                        Loss_D: 0.9216
                                                         D(x): 0.8726
0.4378 / 0.0935
[18/30] [1200/1583]
                        Loss_D: 0.1893
                                        Loss_G: 4.5255
                                                                         D(G(z)):
                                                        D(x): 0.8775
0.0241 / 0.0236
[18/30] [1250/1583]
                        Loss D: 0.1254
                                       Loss G: 5.5214 D(x): 0.9924
                                                                         D(G(z)):
0.1029 / 0.0067
[18/30] [1300/1583]
                        Loss D: 0.0813 Loss G: 4.5697 D(x): 0.9499
                                                                         D(G(z)):
0.0237 / 0.0185
                                        Loss_G: 5.0560
[18/30] [1350/1583]
                        Loss_D: 0.1653
                                                        D(x): 0.8678
                                                                         D(G(z)):
0.0029 / 0.0138
[18/30] [1400/1583]
                        Loss_D: 0.3222 Loss_G: 7.4699
                                                         D(x): 0.9926
                                                                         D(G(z)):
0.2451 / 0.0008
[18/30] [1450/1583]
                        Loss_D: 0.1176 Loss_G: 4.1764 D(x): 0.9656
                                                                         D(G(z)):
0.0728 / 0.0262
[18/30] [1500/1583]
                        Loss_D: 0.0574 Loss_G: 4.1657
                                                        D(x): 0.9810
                                                                         D(G(z)):
0.0362 / 0.0268
[18/30] [1550/1583]
                        Loss_D: 0.0481 Loss_G: 4.4394 D(x): 0.9748
                                                                         D(G(z)):
0.0209 / 0.0242
[19/30][0/1583] Loss_D: 0.5531 Loss_G: 3.2212 D(x): 0.8347
                                                                 D(G(z)): 0.2579
/ 0.0587
[19/30] [50/1583]
                        Loss_D: 0.1028 Loss_G: 5.9111 D(x): 0.9797
                                                                         D(G(z)):
0.0645 / 0.0069
[19/30] [100/1583]
                        Loss_D: 1.1290
                                        Loss_G: 2.8971 D(x): 0.4496
                                                                         D(G(z)):
0.0132 / 0.1175
[19/30] [150/1583]
                        Loss D: 0.8319
                                        Loss_G: 3.6964 D(x): 0.9315
                                                                         D(G(z)):
0.4567 / 0.0413
[19/30] [200/1583]
                        Loss_D: 0.6267 Loss_G: 2.9204 D(x): 0.6235
                                                                         D(G(z)):
0.0271 / 0.0961
[19/30] [250/1583]
                        Loss_D: 0.4341
                                        Loss_G: 7.8842
                                                         D(x): 0.9987
                                                                         D(G(z)):
0.3085 / 0.0007
[19/30] [300/1583]
                        Loss_D: 0.2323
                                        Loss_G: 4.2646
                                                        D(x): 0.8245
                                                                         D(G(z)):
0.0074 / 0.0271
[19/30] [350/1583]
                        Loss_D: 0.1429 Loss_G: 5.1749 D(x): 0.9847
                                                                         D(G(z)):
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0.1093 / 0.0091
[19/30] [400/1583]
                        Loss_D: 0.0888 Loss_G: 4.2390 D(x): 0.9557
                                                                          D(G(z)):
0.0378 / 0.0271
[19/30] [450/1583]
                        Loss_D: 0.0658
                                         Loss_G: 3.9788
                                                          D(x): 0.9724
                                                                          D(G(z)):
0.0354 / 0.0291
[19/30] [500/1583]
                        Loss_D: 0.4089
                                         Loss_G: 3.5396
                                                          D(x): 0.8459
                                                                          D(G(z)):
0.1766 / 0.0444
[19/30] [550/1583]
                        Loss_D: 0.1131
                                         Loss_G: 3.7268
                                                         D(x): 0.9305
                                                                          D(G(z)):
0.0330 / 0.0440
[19/30] [600/1583]
                        Loss D: 0.0550
                                         Loss_G: 4.5006
                                                          D(x): 0.9656
                                                                          D(G(z)):
0.0180 / 0.0229
[19/30] [650/1583]
                        Loss_D: 0.0474
                                         Loss_G: 5.0889
                                                          D(x): 0.9641
                                                                          D(G(z)):
0.0101 / 0.0116
[19/30] [700/1583]
                        Loss_D: 0.1213
                                         Loss_G: 5.9167 D(x): 0.9828
                                                                          D(G(z)):
0.0906 / 0.0044
[19/30] [750/1583]
                        Loss_D: 1.2977
                                         Loss_G: 10.2171 D(x): 0.9989
                                                                          D(G(z)):
0.6160 / 0.0001
[19/30] [800/1583]
                        Loss_D: 0.0966
                                         Loss_G: 5.3962 D(x): 0.9792
                                                                          D(G(z)):
0.0641 / 0.0092
[19/30] [850/1583]
                        Loss D: 0.6236
                                         Loss G: 5.3830
                                                         D(x): 0.9453
                                                                          D(G(z)):
0.3611 / 0.0095
[19/30] [900/1583]
                        Loss D: 0.6587
                                         Loss G: 1.8850
                                                         D(x): 0.6454
                                                                          D(G(z)):
0.0848 / 0.2387
[19/30] [950/1583]
                        Loss D: 0.2194
                                         Loss G: 4.2464
                                                         D(x): 0.8887
                                                                          D(G(z)):
0.0652 / 0.0281
[19/30] [1000/1583]
                        Loss_D: 0.1902
                                         Loss_G: 3.8589
                                                          D(x): 0.9125
                                                                          D(G(z)):
0.0795 / 0.0370
[19/30] [1050/1583]
                        Loss_D: 0.1202
                                         Loss_G: 3.9328
                                                          D(x): 0.9222
                                                                          D(G(z)):
0.0280 / 0.0405
[19/30] [1100/1583]
                        Loss_D: 0.1234
                                         Loss_G: 3.4380
                                                          D(x): 0.9258
                                                                          D(G(z)):
0.0411 / 0.0526
[19/30] [1150/1583]
                        Loss_D: 0.1151
                                         Loss_G: 3.6068
                                                          D(x): 0.9292
                                                                          D(G(z)):
0.0341 / 0.0476
[19/30] [1200/1583]
                                         Loss_G: 4.0961
                        Loss_D: 0.0782
                                                          D(x): 0.9418
                                                                          D(G(z)):
0.0144 / 0.0349
[19/30] [1250/1583]
                        Loss_D: 0.0701
                                         Loss_G: 4.8587
                                                          D(x): 0.9596
                                                                          D(G(z)):
0.0251 / 0.0167
[19/30] [1300/1583]
                        Loss_D: 0.0941
                                         Loss_G: 6.2296
                                                          D(x): 0.9174
                                                                          D(G(z)):
0.0028 / 0.0039
[19/30] [1350/1583]
                        Loss D: 0.0443
                                         Loss_G: 4.6317
                                                         D(x): 0.9778
                                                                          D(G(z)):
0.0208 / 0.0186
[19/30] [1400/1583]
                        Loss_D: 0.0828
                                         Loss_G: 4.2426
                                                         D(x): 0.9754
                                                                          D(G(z)):
0.0529 / 0.0237
[19/30] [1450/1583]
                        Loss_D: 0.0498
                                         Loss_G: 4.8216
                                                          D(x): 0.9890
                                                                          D(G(z)):
0.0368 / 0.0147
[19/30] [1500/1583]
                        Loss_D: 1.2735
                                         Loss_G: 1.7896
                                                          D(x): 0.6357
                                                                          D(G(z)):
0.3540 / 0.2320
[19/30] [1550/1583]
                        Loss_D: 0.3289
                                         Loss_G: 3.4676 D(x): 0.8424
                                                                          D(G(z)):
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0.1053 / 0.0577
[20/30][0/1583] Loss_D: 0.1979 Loss_G: 4.6176 D(x): 0.9282
                                                                 D(G(z)): 0.1002
/ 0.0164
[20/30] [50/1583]
                        Loss_D: 0.3797 Loss_G: 3.4430 D(x): 0.8949
                                                                         D(G(z)):
0.1867 / 0.0591
[20/30] [100/1583]
                        Loss_D: 0.3862
                                        Loss_G: 2.8429
                                                         D(x): 0.7242
                                                                         D(G(z)):
0.0065 / 0.1312
[20/30] [150/1583]
                        Loss_D: 0.6217 Loss_G: 2.8501 D(x): 0.8542
                                                                         D(G(z)):
0.3194 / 0.0878
[20/30] [200/1583]
                        Loss D: 0.2350
                                        Loss_G: 6.4236
                                                        D(x): 0.9679
                                                                         D(G(z)):
0.1520 / 0.0030
[20/30] [250/1583]
                        Loss_D: 3.3301
                                        Loss_G: 0.4812 D(x): 0.0702
                                                                         D(G(z)):
0.0007 / 0.7078
[20/30] [300/1583]
                        Loss_D: 0.1092
                                        Loss_G: 4.5133 D(x): 0.9761
                                                                         D(G(z)):
0.0730 / 0.0211
[20/30] [350/1583]
                                        Loss_G: 4.0548
                                                                         D(G(z)):
                        Loss_D: 1.1752
                                                        D(x): 0.8842
0.5592 / 0.0314
[20/30] [400/1583]
                        Loss_D: 0.5210
                                        Loss_G: 2.5100 D(x): 0.6831
                                                                         D(G(z)):
0.0484 / 0.1382
[20/30] [450/1583]
                        Loss D: 0.1880
                                        Loss G: 6.2592 D(x): 0.9756
                                                                         D(G(z)):
0.1370 / 0.0031
[20/30] [500/1583]
                        Loss D: 0.0903
                                        Loss G: 4.3513 D(x): 0.9503
                                                                         D(G(z)):
0.0338 / 0.0223
                        Loss_D: 0.1238
                                        Loss_G: 3.6562 D(x): 0.9147
                                                                         D(G(z)):
[20/30] [550/1583]
0.0236 / 0.0529
[20/30] [600/1583]
                        Loss_D: 0.3501
                                        Loss_G: 3.0629
                                                         D(x): 0.8570
                                                                         D(G(z)):
0.1510 / 0.0724
[20/30] [650/1583]
                        Loss_D: 0.1182 Loss_G: 4.5413
                                                        D(x): 0.9398
                                                                         D(G(z)):
0.0484 / 0.0209
[20/30] [700/1583]
                        Loss_D: 0.1305
                                        Loss_G: 2.7298
                                                         D(x): 0.9031
                                                                         D(G(z)):
0.0166 / 0.1155
[20/30] [750/1583]
                        Loss_D: 0.4052
                                        Loss_G: 2.9392
                                                         D(x): 0.8340
                                                                         D(G(z)):
0.1636 / 0.0847
[20/30] [800/1583]
                        Loss_D: 0.1013 Loss_G: 4.3564
                                                        D(x): 0.9482
                                                                         D(G(z)):
0.0411 / 0.0228
[20/30] [850/1583]
                        Loss_D: 0.6184
                                        Loss_G: 2.1547
                                                         D(x): 0.7541
                                                                         D(G(z)):
0.2051 / 0.1664
[20/30] [900/1583]
                        Loss D: 0.6036
                                        Loss_G: 1.2603
                                                        D(x): 0.7090
                                                                         D(G(z)):
0.1310 / 0.3777
[20/30] [950/1583]
                        Loss D: 0.2719
                                        Loss_G: 4.9214 D(x): 0.9886
                                                                         D(G(z)):
0.1960 / 0.0121
[20/30] [1000/1583]
                        Loss_D: 0.5443 Loss_G: 7.0925
                                                        D(x): 0.9892
                                                                         D(G(z)):
0.3341 / 0.0016
[20/30] [1050/1583]
                        Loss_D: 0.1210
                                        Loss_G: 5.2534
                                                         D(x): 0.9883
                                                                         D(G(z)):
0.0945 / 0.0086
[20/30] [1100/1583]
                        Loss_D: 0.0451
                                        Loss_G: 4.8267
                                                         D(x): 0.9797
                                                                         D(G(z)):
0.0227 / 0.0133
[20/30] [1150/1583]
                        Loss_D: 2.2066 Loss_G: 8.6236 D(x): 0.9896
                                                                         D(G(z)):
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0.8059 / 0.0006
[20/30] [1200/1583]
                        Loss_D: 0.0431 Loss_G: 5.3366 D(x): 0.9864
                                                                          D(G(z)):
0.0279 / 0.0095
[20/30] [1250/1583]
                        Loss_D: 0.0937
                                         Loss_G: 4.1801
                                                         D(x): 0.9479
                                                                          D(G(z)):
0.0278 / 0.0311
[20/30] [1300/1583]
                                         Loss_G: 4.9440
                        Loss_D: 0.0574
                                                         D(x): 0.9759
                                                                          D(G(z)):
0.0304 / 0.0129
[20/30] [1350/1583]
                        Loss_D: 0.0796
                                         Loss_G: 4.9909
                                                        D(x): 0.9669
                                                                          D(G(z)):
0.0417 / 0.0144
[20/30] [1400/1583]
                        Loss D: 0.0595
                                         Loss_G: 4.4127
                                                         D(x): 0.9665
                                                                          D(G(z)):
0.0218 / 0.0250
[20/30] [1450/1583]
                        Loss_D: 0.1059
                                         Loss_G: 5.0015
                                                         D(x): 0.9589
                                                                          D(G(z)):
0.0555 / 0.0125
[20/30] [1500/1583]
                        Loss_D: 0.7678 Loss_G: 2.8266
                                                         D(x): 0.6213
                                                                          D(G(z)):
0.0849 / 0.1469
[20/30] [1550/1583]
                        Loss_D: 0.1448 Loss_G: 4.4900 D(x): 0.8920
                                                                          D(G(z)):
0.0075 / 0.0273
[21/30][0/1583] Loss_D: 0.1411 Loss_G: 5.0671 D(x): 0.9718
                                                                 D(G(z)): 0.0955
/ 0.0114
[21/30] [50/1583]
                        Loss D: 0.6569 Loss G: 2.5870 D(x): 0.5954
                                                                          D(G(z)):
0.0097 / 0.1411
[21/30] [100/1583]
                        Loss D: 0.1848 Loss G: 3.5763 D(x): 0.8614
                                                                          D(G(z)):
0.0116 / 0.0595
                        Loss_D: 0.0792 Loss_G: 5.0063
                                                                          D(G(z)):
[21/30] [150/1583]
                                                         D(x): 0.9679
0.0405 / 0.0126
[21/30] [200/1583]
                        Loss_D: 0.0819
                                         Loss_G: 3.6486
                                                         D(x): 0.9517
                                                                          D(G(z)):
0.0282 / 0.0510
[21/30] [250/1583]
                        Loss_D: 0.0598 Loss_G: 5.1799
                                                         D(x): 0.9511
                                                                          D(G(z)):
0.0076 / 0.0111
[21/30] [300/1583]
                        Loss_D: 0.0446
                                         Loss_G: 4.7156
                                                         D(x): 0.9908
                                                                          D(G(z)):
0.0335 / 0.0162
[21/30] [350/1583]
                        Loss_D: 0.0327
                                         Loss_G: 4.8541
                                                         D(x): 0.9829
                                                                          D(G(z)):
0.0145 / 0.0168
[21/30] [400/1583]
                        Loss_D: 0.5237
                                         Loss_G: 2.6928
                                                         D(x): 0.7246
                                                                          D(G(z)):
0.1194 / 0.1102
[21/30] [450/1583]
                        Loss_D: 0.2135
                                         Loss_G: 4.2244 D(x): 0.9016
                                                                          D(G(z)):
0.0850 / 0.0291
[21/30] [500/1583]
                        Loss D: 0.7091
                                         Loss_G: 3.0457
                                                         D(x): 0.6058
                                                                          D(G(z)):
0.0445 / 0.0953
[21/30] [550/1583]
                        Loss D: 0.6536
                                         Loss_G: 7.4863
                                                        D(x): 0.9924
                                                                          D(G(z)):
0.3809 / 0.0010
[21/30] [600/1583]
                        Loss_D: 0.1416
                                        Loss_G: 4.6040
                                                         D(x): 0.9224
                                                                          D(G(z)):
0.0474 / 0.0228
[21/30] [650/1583]
                        Loss_D: 3.7572
                                         Loss_G: 1.3610
                                                         D(x): 0.0506
                                                                          D(G(z)):
0.0006 / 0.3739
[21/30] [700/1583]
                        Loss_D: 0.2589
                                         Loss_G: 3.2951
                                                         D(x): 0.8525
                                                                          D(G(z)):
0.0651 / 0.0705
[21/30] [750/1583]
                        Loss_D: 2.8843 Loss_G: 0.5690 D(x): 0.1056
                                                                          D(G(z)):
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0.0007 / 0.6295
[21/30] [800/1583]
                        Loss_D: 0.2649 Loss_G: 2.6509 D(x): 0.7944
                                                                         D(G(z)):
0.0099 / 0.1210
[21/30] [850/1583]
                        Loss_D: 0.3261
                                        Loss_G: 4.3262 D(x): 0.8740
                                                                         D(G(z)):
0.1437 / 0.0233
[21/30] [900/1583]
                                        Loss_G: 5.2822
                        Loss D: 0.1262
                                                         D(x): 0.9857
                                                                         D(G(z)):
0.0940 / 0.0090
[21/30] [950/1583]
                        Loss_D: 0.1032 Loss_G: 3.3382 D(x): 0.9262
                                                                         D(G(z)):
0.0210 / 0.0662
[21/30] [1000/1583]
                        Loss D: 0.0682
                                        Loss_G: 4.2910
                                                        D(x): 0.9709
                                                                         D(G(z)):
0.0359 / 0.0248
[21/30] [1050/1583]
                        Loss_D: 0.2989
                                        Loss_G: 3.1525
                                                        D(x): 0.8861
                                                                         D(G(z)):
0.1314 / 0.0785
[21/30] [1100/1583]
                        Loss_D: 0.4046
                                        Loss_G: 2.8704 D(x): 0.7427
                                                                         D(G(z)):
0.0306 / 0.1190
[21/30] [1150/1583]
                                        Loss_G: 3.8117 D(x): 0.8894
                                                                         D(G(z)):
                        Loss_D: 0.2474
0.0956 / 0.0403
[21/30] [1200/1583]
                        Loss_D: 0.1496
                                        Loss_G: 4.8153 D(x): 0.9665
                                                                         D(G(z)):
0.0973 / 0.0147
[21/30] [1250/1583]
                        Loss D: 0.0495
                                        Loss G: 4.0597
                                                         D(x): 0.9767
                                                                         D(G(z)):
0.0248 / 0.0280
[21/30] [1300/1583]
                        Loss D: 0.0734 Loss G: 5.8039 D(x): 0.9896
                                                                         D(G(z)):
0.0568 / 0.0050
                                        Loss_G: 4.9799
                                                                         D(G(z)):
[21/30] [1350/1583]
                        Loss D: 0.0587
                                                        D(x): 0.9696
0.0255 / 0.0137
[21/30] [1400/1583]
                        Loss_D: 0.0375
                                        Loss_G: 4.8032 D(x): 0.9870
                                                                         D(G(z)):
0.0234 / 0.0155
[21/30] [1450/1583]
                        Loss_D: 0.0692 Loss_G: 4.6305
                                                        D(x): 0.9479
                                                                         D(G(z)):
0.0135 / 0.0201
[21/30] [1500/1583]
                        Loss_D: 0.0243
                                        Loss_G: 4.9887
                                                         D(x): 0.9915
                                                                         D(G(z)):
0.0153 / 0.0131
[21/30] [1550/1583]
                        Loss_D: 0.0503 Loss_G: 4.6102 D(x): 0.9713
                                                                         D(G(z)):
0.0190 / 0.0209
[22/30][0/1583] Loss_D: 0.0530 Loss_G: 4.5232 D(x): 0.9648
                                                                 D(G(z)): 0.0157
/ 0.0238
[22/30] [50/1583]
                        Loss_D: 0.0382 Loss_G: 4.7982 D(x): 0.9828
                                                                         D(G(z)):
0.0199 / 0.0166
[22/30] [100/1583]
                        Loss D: 0.8676
                                        Loss_G: 2.8096
                                                                         D(G(z)):
                                                        D(x): 0.7998
0.4004 / 0.0963
[22/30] [150/1583]
                        Loss D: 0.3917
                                        Loss_G: 5.4280 D(x): 0.9385
                                                                         D(G(z)):
0.2357 / 0.0088
[22/30] [200/1583]
                        Loss_D: 0.0794 Loss_G: 4.5790
                                                        D(x): 0.9561
                                                                         D(G(z)):
0.0292 / 0.0223
[22/30] [250/1583]
                        Loss_D: 0.4698
                                        Loss_G: 4.7256
                                                         D(x): 0.8799
                                                                         D(G(z)):
0.2270 / 0.0221
[22/30] [300/1583]
                        Loss_D: 0.2179
                                        Loss_G: 3.3802
                                                        D(x): 0.9047
                                                                         D(G(z)):
0.0870 / 0.0707
[22/30] [350/1583]
                        Loss_D: 0.6413 Loss_G: 7.1738 D(x): 0.9922
                                                                         D(G(z)):
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0.3885 / 0.0016
[22/30] [400/1583]
                        Loss_D: 0.1103 Loss_G: 4.3472 D(x): 0.9716
                                                                          D(G(z)):
0.0694 / 0.0245
[22/30] [450/1583]
                        Loss_D: 0.1265
                                         Loss_G: 5.6422 D(x): 0.9696
                                                                          D(G(z)):
0.0834 / 0.0068
[22/30] [500/1583]
                        Loss_D: 0.0957
                                         Loss_G: 4.2757
                                                         D(x): 0.9478
                                                                          D(G(z)):
0.0305 / 0.0280
[22/30] [550/1583]
                        Loss_D: 0.0993
                                         Loss_G: 5.4364
                                                         D(x): 0.9662
                                                                          D(G(z)):
0.0576 / 0.0090
[22/30] [600/1583]
                        Loss D: 0.2049
                                         Loss_G: 3.4368
                                                         D(x): 0.8746
                                                                          D(G(z)):
0.0437 / 0.0667
[22/30] [650/1583]
                        Loss_D: 0.0970
                                         Loss_G: 3.5614 D(x): 0.9287
                                                                          D(G(z)):
0.0158 / 0.0545
[22/30] [700/1583]
                        Loss_D: 0.4995
                                         Loss_G: 7.9128
                                                         D(x): 0.9960
                                                                          D(G(z)):
0.3302 / 0.0008
[22/30] [750/1583]
                        Loss_D: 0.2197
                                         Loss_G: 6.0515
                                                                          D(G(z)):
                                                         D(x): 0.9871
0.1696 / 0.0036
[22/30] [800/1583]
                        Loss_D: 0.7785
                                         Loss_G: 2.6450
                                                                          D(G(z)):
                                                         D(x): 0.8018
0.3552 / 0.0972
[22/30] [850/1583]
                        Loss D: 0.1908
                                         Loss G: 3.7118 D(x): 0.8922
                                                                          D(G(z)):
0.0574 / 0.0476
[22/30] [900/1583]
                        Loss D: 0.0981
                                         Loss G: 4.3919 D(x): 0.9332
                                                                          D(G(z)):
0.0203 / 0.0242
                        Loss_D: 0.1545
                                         Loss_G: 5.4475
[22/30] [950/1583]
                                                         D(x): 0.9638
                                                                          D(G(z)):
0.0927 / 0.0079
[22/30] [1000/1583]
                        Loss_D: 0.0780
                                         Loss_G: 4.9008
                                                         D(x): 0.9783
                                                                          D(G(z)):
0.0513 / 0.0145
[22/30] [1050/1583]
                        Loss_D: 0.0517
                                         Loss_G: 5.2115
                                                         D(x): 0.9851
                                                                          D(G(z)):
0.0342 / 0.0111
[22/30] [1100/1583]
                        Loss_D: 0.3693
                                         Loss_G: 5.1912
                                                         D(x): 0.9690
                                                                          D(G(z)):
0.2508 / 0.0101
[22/30] [1150/1583]
                        Loss_D: 0.1082
                                         Loss_G: 5.8789
                                                         D(x): 0.9923
                                                                          D(G(z)):
0.0848 / 0.0052
[22/30] [1200/1583]
                                         Loss_G: 3.3706
                        Loss_D: 0.1611
                                                         D(x): 0.9202
                                                                          D(G(z)):
0.0672 / 0.0611
[22/30] [1250/1583]
                        Loss_D: 0.4809
                                         Loss_G: 4.4242
                                                         D(x): 0.9658
                                                                          D(G(z)):
0.2969 / 0.0201
[22/30] [1300/1583]
                        Loss_D: 0.6220
                                         Loss_G: 2.8276
                                                                          D(G(z)):
                                                         D(x): 0.8264
0.2745 / 0.0889
[22/30] [1350/1583]
                        Loss D: 0.8091
                                         Loss_G: 9.0249 D(x): 0.9968
                                                                          D(G(z)):
0.4535 / 0.0003
[22/30] [1400/1583]
                        Loss_D: 0.4775
                                         Loss_G: 4.1937
                                                         D(x): 0.8909
                                                                          D(G(z)):
0.2546 / 0.0246
[22/30] [1450/1583]
                        Loss_D: 0.5300
                                         Loss_G: 1.6278
                                                         D(x): 0.6453
                                                                          D(G(z)):
0.0026 / 0.2844
[22/30] [1500/1583]
                        Loss_D: 0.0544
                                         Loss_G: 5.4477
                                                         D(x): 0.9930
                                                                          D(G(z)):
0.0419 / 0.0084
[22/30] [1550/1583]
                        Loss_D: 0.0772 Loss_G: 4.5795 D(x): 0.9546
                                                                          D(G(z)):
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0.0267 / 0.0241
[23/30][0/1583] Loss_D: 0.1011 Loss_G: 3.5312 D(x): 0.9436
                                                                 D(G(z)): 0.0385
/ 0.0504
[23/30] [50/1583]
                        Loss_D: 0.0620 Loss_G: 3.9903 D(x): 0.9686
                                                                         D(G(z)):
0.0278 / 0.0337
[23/30] [100/1583]
                        Loss_D: 0.0741 Loss_G: 3.6422
                                                        D(x): 0.9530
                                                                         D(G(z)):
0.0227 / 0.0486
[23/30] [150/1583]
                        Loss_D: 0.0473 Loss_G: 4.6498 D(x): 0.9681
                                                                         D(G(z)):
0.0138 / 0.0198
[23/30] [200/1583]
                        Loss D: 0.0530
                                        Loss_G: 5.9248
                                                        D(x): 0.9949
                                                                         D(G(z)):
0.0431 / 0.0057
[23/30] [250/1583]
                        Loss_D: 0.0307
                                        Loss_G: 5.3870 D(x): 0.9827
                                                                         D(G(z)):
0.0127 / 0.0099
[23/30] [300/1583]
                        Loss_D: 0.0313
                                        Loss_G: 5.8107 D(x): 0.9756
                                                                         D(G(z)):
0.0057 / 0.0065
[23/30] [350/1583]
                        Loss_D: 0.3307
                                        Loss_G: 2.9067
                                                                         D(G(z)):
                                                        D(x): 0.8308
0.0944 / 0.0856
[23/30] [400/1583]
                        Loss_D: 0.3478
                                        Loss_G: 4.2496 D(x): 0.8834
                                                                         D(G(z)):
0.1585 / 0.0230
[23/30] [450/1583]
                        Loss D: 2.8041
                                        Loss G: 5.7384 D(x): 0.9827
                                                                         D(G(z)):
0.8648 / 0.0122
[23/30] [500/1583]
                        Loss D: 0.2855
                                        Loss G: 2.7421 D(x): 0.8750
                                                                         D(G(z)):
0.1055 / 0.0969
                        Loss_D: 0.2276
                                        Loss G: 3.5979
                                                                         D(G(z)):
[23/30] [550/1583]
                                                        D(x): 0.8783
0.0669 / 0.0474
[23/30] [600/1583]
                        Loss_D: 0.1558
                                        Loss_G: 3.8308
                                                        D(x): 0.9224
                                                                         D(G(z)):
0.0602 / 0.0404
[23/30] [650/1583]
                        Loss_D: 0.7598 Loss_G: 2.7012 D(x): 0.8456
                                                                         D(G(z)):
0.3798 / 0.1028
[23/30] [700/1583]
                        Loss_D: 0.1101
                                        Loss_G: 4.8130
                                                        D(x): 0.9313
                                                                         D(G(z)):
0.0199 / 0.0230
[23/30] [750/1583]
                        Loss_D: 1.7444
                                        Loss_G: 1.6933
                                                        D(x): 0.2647
                                                                         D(G(z)):
0.0064 / 0.2829
[23/30] [800/1583]
                        Loss_D: 0.5314 Loss_G: 1.8158
                                                        D(x): 0.6711
                                                                         D(G(z)):
0.0281 / 0.2520
                        Loss_D: 0.0805
[23/30] [850/1583]
                                        Loss_G: 4.1678 D(x): 0.9731
                                                                         D(G(z)):
0.0476 / 0.0284
[23/30] [900/1583]
                        Loss D: 0.3848
                                        Loss_G: 1.0217
                                                         D(x): 0.7262
                                                                         D(G(z)):
0.0062 / 0.4684
[23/30] [950/1583]
                        Loss D: 0.1117
                                        Loss_G: 4.4391 D(x): 0.9277
                                                                         D(G(z)):
0.0199 / 0.0329
[23/30] [1000/1583]
                        Loss_D: 0.4121
                                       Loss_G: 2.8351
                                                         D(x): 0.8352
                                                                         D(G(z)):
0.1700 / 0.0924
[23/30] [1050/1583]
                        Loss_D: 0.0955
                                        Loss_G: 4.7129
                                                         D(x): 0.9622
                                                                         D(G(z)):
0.0367 / 0.0191
[23/30] [1100/1583]
                        Loss_D: 0.0496
                                        Loss_G: 4.8009
                                                        D(x): 0.9783
                                                                         D(G(z)):
0.0250 / 0.0160
[23/30] [1150/1583]
                        Loss_D: 0.0424 Loss_G: 5.2242 D(x): 0.9931
                                                                         D(G(z)):
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0.0332 / 0.0107
[23/30] [1200/1583]
                        Loss_D: 0.0502 Loss_G: 4.7103 D(x): 0.9734
                                                                          D(G(z)):
0.0217 / 0.0165
[23/30] [1250/1583]
                        Loss_D: 0.0826
                                        Loss_G: 5.6856
                                                         D(x): 0.9899
                                                                          D(G(z)):
0.0658 / 0.0060
[23/30] [1300/1583]
                        Loss_D: 0.0526
                                        Loss_G: 4.8807
                                                         D(x): 0.9800
                                                                          D(G(z)):
0.0296 / 0.0153
[23/30] [1350/1583]
                        Loss_D: 0.2572
                                        Loss_G: 3.4046 D(x): 0.8953
                                                                          D(G(z)):
0.1193 / 0.0535
[23/30] [1400/1583]
                        Loss D: 0.9129
                                        Loss_G: 0.8920
                                                         D(x): 0.5060
                                                                          D(G(z)):
0.0074 / 0.5001
[23/30] [1450/1583]
                        Loss_D: 0.0836
                                        Loss_G: 5.5183
                                                         D(x): 0.9937
                                                                          D(G(z)):
0.0704 / 0.0068
[23/30] [1500/1583]
                        Loss_D: 0.3555
                                        Loss_G: 3.1837
                                                         D(x): 0.8553
                                                                          D(G(z)):
0.1271 / 0.0775
[23/30] [1550/1583]
                                        Loss_G: 5.0947 D(x): 0.9814
                                                                          D(G(z)):
                        Loss_D: 0.0634
0.0407 / 0.0135
[24/30][0/1583] Loss_D: 0.7052 Loss_G: 2.4630 D(x): 0.6529
                                                                 D(G(z)): 0.1283
/ 0.1327
[24/30] [50/1583]
                        Loss D: 1.2463 Loss G: 3.1129 D(x): 0.9115
                                                                          D(G(z)):
0.5723 / 0.0814
[24/30] [100/1583]
                        Loss D: 0.4313 Loss G: 2.6870 D(x): 0.7282
                                                                          D(G(z)):
0.0320 / 0.1258
                        Loss_D: 0.2512 Loss_G: 6.5124 D(x): 0.9880
[24/30] [150/1583]
                                                                          D(G(z)):
0.1728 / 0.0031
[24/30] [200/1583]
                        Loss_D: 0.1007
                                        Loss_G: 4.9255
                                                        D(x): 0.9912
                                                                          D(G(z)):
0.0835 / 0.0113
[24/30] [250/1583]
                        Loss_D: 0.0603 Loss_G: 5.0184
                                                        D(x): 0.9690
                                                                          D(G(z)):
0.0264 / 0.0133
[24/30] [300/1583]
                        Loss_D: 0.1228
                                        Loss_G: 3.5576
                                                        D(x): 0.9216
                                                                          D(G(z)):
0.0189 / 0.0536
[24/30] [350/1583]
                        Loss_D: 0.0787
                                        Loss_G: 5.1447
                                                         D(x): 0.9899
                                                                          D(G(z)):
0.0622 / 0.0109
[24/30] [400/1583]
                        Loss_D: 0.4258
                                        Loss_G: 2.5127
                                                         D(x): 0.7957
                                                                          D(G(z)):
0.1332 / 0.1293
[24/30] [450/1583]
                        Loss_D: 0.1088
                                        Loss_G: 4.2633
                                                         D(x): 0.9564
                                                                          D(G(z)):
0.0535 / 0.0261
[24/30] [500/1583]
                        Loss D: 0.0676
                                        Loss_G: 5.2089
                                                         D(x): 0.9862
                                                                          D(G(z)):
0.0497 / 0.0102
[24/30] [550/1583]
                        Loss D: 0.0881
                                        Loss_G: 4.0980
                                                         D(x): 0.9356
                                                                          D(G(z)):
0.0166 / 0.0383
[24/30] [600/1583]
                        Loss_D: 0.0320
                                        Loss_G: 5.6339
                                                         D(x): 0.9880
                                                                          D(G(z)):
0.0190 / 0.0090
[24/30] [650/1583]
                        Loss_D: 0.1759
                                         Loss_G: 3.1008
                                                         D(x): 0.8622
                                                                          D(G(z)):
0.0095 / 0.0883
[24/30] [700/1583]
                        Loss_D: 0.0804
                                        Loss_G: 4.5763
                                                         D(x): 0.9488
                                                                          D(G(z)):
0.0238 / 0.0227
[24/30] [750/1583]
                        Loss_D: 0.0382 Loss_G: 6.2334 D(x): 0.9710
                                                                          D(G(z)):
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0.0081 / 0.0046
[24/30] [800/1583]
                        Loss_D: 4.4322 Loss_G: 0.3204 D(x): 0.0596
                                                                         D(G(z)):
0.0169 / 0.7679
[24/30] [850/1583]
                        Loss_D: 0.3048
                                        Loss_G: 3.5062 D(x): 0.8181
                                                                         D(G(z)):
0.0536 / 0.0589
[24/30] [900/1583]
                        Loss_D: 0.2815
                                        Loss_G: 3.7480
                                                         D(x): 0.8593
                                                                         D(G(z)):
0.0974 / 0.0467
[24/30] [950/1583]
                        Loss_D: 0.2126
                                        Loss_G: 3.1697
                                                         D(x): 0.8553
                                                                         D(G(z)):
0.0303 / 0.0867
[24/30] [1000/1583]
                        Loss D: 0.0617
                                        Loss_G: 4.6704 D(x): 0.9754
                                                                         D(G(z)):
0.0335 / 0.0249
[24/30] [1050/1583]
                        Loss_D: 0.3831
                                        Loss_G: 3.0472 D(x): 0.7795
                                                                         D(G(z)):
0.0747 / 0.0762
[24/30] [1100/1583]
                        Loss_D: 0.0595
                                        Loss_G: 4.9938
                                                         D(x): 0.9718
                                                                         D(G(z)):
0.0288 / 0.0147
[24/30] [1150/1583]
                        Loss_D: 0.1028
                                        Loss_G: 4.8767
                                                                         D(G(z)):
                                                         D(x): 0.9515
0.0447 / 0.0196
[24/30] [1200/1583]
                        Loss_D: 0.5528
                                        Loss_G: 2.2989
                                                                         D(G(z)):
                                                         D(x): 0.7354
0.1361 / 0.1536
[24/30] [1250/1583]
                        Loss D: 0.0735
                                        Loss G: 4.8616 D(x): 0.9519
                                                                         D(G(z)):
0.0147 / 0.0179
[24/30] [1300/1583]
                        Loss D: 1.1233
                                        Loss G: 3.0238 D(x): 0.9025
                                                                         D(G(z)):
0.5258 / 0.0854
                        Loss_D: 0.2180
                                        Loss G: 6.9813 D(x): 0.9973
[24/30] [1350/1583]
                                                                         D(G(z)):
0.1708 / 0.0017
[24/30] [1400/1583]
                        Loss_D: 0.1224
                                        Loss_G: 5.4097
                                                         D(x): 0.9711
                                                                         D(G(z)):
0.0789 / 0.0093
[24/30] [1450/1583]
                        Loss_D: 0.1705 Loss_G: 5.5160
                                                         D(x): 0.9618
                                                                         D(G(z)):
0.1084 / 0.0087
[24/30] [1500/1583]
                        Loss_D: 0.1907
                                        Loss_G: 5.3189
                                                         D(x): 0.9738
                                                                         D(G(z)):
0.1332 / 0.0101
[24/30] [1550/1583]
                        Loss_D: 0.1441 Loss_G: 4.8331 D(x): 0.9500
                                                                         D(G(z)):
0.0758 / 0.0172
[25/30][0/1583] Loss_D: 0.1247 Loss_G: 4.1697 D(x): 0.9052
                                                                 D(G(z)): 0.0066
/ 0.0338
[25/30] [50/1583]
                        Loss_D: 0.2811 Loss_G: 2.3668 D(x): 0.8313
                                                                         D(G(z)):
0.0520 / 0.1478
[25/30] [100/1583]
                        Loss_D: 0.0521 Loss_G: 5.2032 D(x): 0.9704
                                                                         D(G(z)):
0.0201 / 0.0113
[25/30] [150/1583]
                        Loss_D: 1.0048 Loss_G: 4.1383 D(x): 0.9279
                                                                         D(G(z)):
0.5068 / 0.0297
[25/30] [200/1583]
                        Loss_D: 0.1868 Loss_G: 5.2473
                                                        D(x): 0.9530
                                                                         D(G(z)):
0.1166 / 0.0093
[25/30] [250/1583]
                        Loss_D: 0.0741
                                        Loss_G: 4.5161
                                                         D(x): 0.9700
                                                                         D(G(z)):
0.0386 / 0.0222
[25/30] [300/1583]
                        Loss_D: 0.1286
                                        Loss_G: 5.7262
                                                         D(x): 0.9735
                                                                         D(G(z)):
0.0899 / 0.0059
[25/30] [350/1583]
                        Loss_D: 0.0547 Loss_G: 4.7509 D(x): 0.9597
                                                                         D(G(z)):
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0.0117 / 0.0189
[25/30] [400/1583]
                        Loss_D: 0.1049
                                         Loss_G: 4.9505 D(x): 0.9866
                                                                          D(G(z)):
0.0659 / 0.0126
[25/30] [450/1583]
                        Loss_D: 0.0363
                                         Loss_G: 5.2222 D(x): 0.9862
                                                                          D(G(z)):
0.0215 / 0.0102
[25/30] [500/1583]
                        Loss_D: 0.0599
                                         Loss_G: 4.3482
                                                         D(x): 0.9640
                                                                          D(G(z)):
0.0180 / 0.0253
[25/30] [550/1583]
                        Loss_D: 0.0382
                                         Loss_G: 5.8324
                                                         D(x): 0.9764
                                                                          D(G(z)):
0.0125 / 0.0064
[25/30] [600/1583]
                        Loss_D: 0.0455
                                         Loss_G: 5.6248
                                                         D(x): 0.9943
                                                                          D(G(z)):
0.0373 / 0.0068
[25/30] [650/1583]
                        Loss_D: 0.2111
                                         Loss_G: 2.6176
                                                         D(x): 0.8315
                                                                          D(G(z)):
0.0030 / 0.1634
[25/30] [700/1583]
                        Loss_D: 0.0280
                                         Loss_G: 5.4339
                                                         D(x): 0.9868
                                                                          D(G(z)):
0.0141 / 0.0103
[25/30] [750/1583]
                        Loss_D: 0.0541
                                         Loss_G: 6.1515
                                                                          D(G(z)):
                                                         D(x): 0.9915
0.0423 / 0.0043
[25/30] [800/1583]
                        Loss_D: 1.4315
                                         Loss_G: 0.6496
                                                                          D(G(z)):
                                                         D(x): 0.3463
0.0427 / 0.6214
[25/30] [850/1583]
                        Loss D: 0.6171
                                         Loss G: 1.7169
                                                         D(x): 0.7066
                                                                          D(G(z)):
0.1404 / 0.2396
[25/30] [900/1583]
                        Loss D: 0.1269
                                         Loss G: 4.3210 D(x): 0.9232
                                                                          D(G(z)):
0.0299 / 0.0274
                                         Loss_G: 6.1100
[25/30] [950/1583]
                        Loss D: 0.0822
                                                         D(x): 0.9399
                                                                          D(G(z)):
0.0147 / 0.0051
[25/30] [1000/1583]
                        Loss_D: 0.2170
                                         Loss_G: 4.2131
                                                         D(x): 0.9628
                                                                          D(G(z)):
0.1306 / 0.0304
[25/30] [1050/1583]
                        Loss_D: 0.0906
                                         Loss_G: 6.0388
                                                         D(x): 0.9916
                                                                          D(G(z)):
0.0695 / 0.0048
[25/30] [1100/1583]
                        Loss_D: 0.1103
                                         Loss_G: 3.9956
                                                         D(x): 0.9328
                                                                          D(G(z)):
0.0336 / 0.0350
[25/30] [1150/1583]
                        Loss_D: 0.0470
                                         Loss_G: 4.4248
                                                         D(x): 0.9809
                                                                          D(G(z)):
0.0262 / 0.0278
[25/30] [1200/1583]
                                         Loss_G: 4.0546
                        Loss_D: 0.0625
                                                         D(x): 0.9535
                                                                          D(G(z)):
0.0117 / 0.0442
[25/30] [1250/1583]
                        Loss_D: 0.8635
                                         Loss_G: 3.8264
                                                         D(x): 0.9322
                                                                          D(G(z)):
0.4681 / 0.0371
[25/30] [1300/1583]
                        Loss_D: 0.1932
                                         Loss_G: 4.5203
                                                                          D(G(z)):
                                                         D(x): 0.9267
0.0893 / 0.0204
[25/30] [1350/1583]
                        Loss_D: 0.3776
                                         Loss_G: 4.5052 D(x): 0.9595
                                                                          D(G(z)):
0.2456 / 0.0175
[25/30] [1400/1583]
                        Loss_D: 0.0447
                                         Loss_G: 5.5156
                                                         D(x): 0.9848
                                                                          D(G(z)):
0.0277 / 0.0086
[25/30] [1450/1583]
                        Loss_D: 0.0652
                                         Loss_G: 5.2166
                                                         D(x): 0.9790
                                                                          D(G(z)):
0.0368 / 0.0135
[25/30] [1500/1583]
                        Loss_D: 0.4905
                                         Loss_G: 2.8427
                                                         D(x): 0.7207
                                                                          D(G(z)):
0.0652 / 0.1185
[25/30] [1550/1583]
                        Loss_D: 0.1206 Loss_G: 4.4111 D(x): 0.9255
                                                                          D(G(z)):
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0.0270 / 0.0302
[26/30][0/1583] Loss_D: 2.3661 Loss_G: 6.6980 D(x): 0.9852
                                                                 D(G(z)): 0.8205
/ 0.0034
[26/30] [50/1583]
                        Loss_D: 0.2332 Loss_G: 3.8076 D(x): 0.8857
                                                                          D(G(z)):
0.0829 / 0.0468
[26/30] [100/1583]
                        Loss_D: 0.2583 Loss_G: 3.4882
                                                         D(x): 0.8999
                                                                          D(G(z)):
0.1185 / 0.0522
[26/30] [150/1583]
                        Loss_D: 0.0910 Loss_G: 4.8078 D(x): 0.9538
                                                                          D(G(z)):
0.0362 / 0.0188
[26/30] [200/1583]
                        Loss D: 0.0945
                                         Loss_G: 5.2893
                                                         D(x): 0.9765
                                                                          D(G(z)):
0.0607 / 0.0097
[26/30] [250/1583]
                        Loss_D: 0.0832
                                         Loss_G: 4.8488
                                                         D(x): 0.9332
                                                                          D(G(z)):
0.0084 / 0.0183
[26/30] [300/1583]
                        Loss_D: 0.0448
                                         Loss_G: 5.6622
                                                         D(x): 0.9637
                                                                          D(G(z)):
0.0065 / 0.0074
[26/30] [350/1583]
                        Loss_D: 0.0714
                                         Loss_G: 4.4106
                                                                          D(G(z)):
                                                         D(x): 0.9535
0.0202 / 0.0230
[26/30] [400/1583]
                        Loss_D: 0.0726
                                         Loss_G: 4.4266
                                                                          D(G(z)):
                                                         D(x): 0.9553
0.0206 / 0.0245
[26/30] [450/1583]
                        Loss D: 0.0298
                                        Loss G: 5.4795
                                                         D(x): 0.9802
                                                                          D(G(z)):
0.0092 / 0.0086
[26/30] [500/1583]
                        Loss D: 0.0435
                                         Loss G: 4.9472 D(x): 0.9726
                                                                          D(G(z)):
0.0143 / 0.0157
                        Loss_D: 0.0386
                                         Loss G: 5.4983
                                                                          D(G(z)):
[26/30] [550/1583]
                                                         D(x): 0.9772
0.0141 / 0.0098
[26/30] [600/1583]
                        Loss_D: 0.0646
                                         Loss_G: 3.7464
                                                         D(x): 0.9503
                                                                          D(G(z)):
0.0104 / 0.0480
[26/30] [650/1583]
                        Loss_D: 0.0207
                                         Loss_G: 5.8038
                                                         D(x): 0.9927
                                                                          D(G(z)):
0.0131 / 0.0071
[26/30] [700/1583]
                        Loss_D: 0.7007
                                         Loss_G: 2.8453
                                                         D(x): 0.7836
                                                                          D(G(z)):
0.2969 / 0.0957
[26/30] [750/1583]
                        Loss_D: 0.1062
                                        Loss_G: 3.7792
                                                         D(x): 0.9513
                                                                          D(G(z)):
0.0463 / 0.0460
[26/30] [800/1583]
                        Loss_D: 0.9127
                                         Loss_G: 9.8329
                                                         D(x): 0.9886
                                                                          D(G(z)):
0.5137 / 0.0002
[26/30] [850/1583]
                        Loss_D: 0.1408
                                        Loss_G: 7.2212 D(x): 0.9863
                                                                          D(G(z)):
0.1085 / 0.0013
[26/30] [900/1583]
                        Loss D: 0.0623
                                         Loss_G: 5.0211
                                                        D(x): 0.9565
                                                                          D(G(z)):
0.0152 / 0.0153
[26/30] [950/1583]
                        Loss D: 0.0460
                                         Loss_G: 4.7860 D(x): 0.9670
                                                                          D(G(z)):
0.0103 / 0.0203
[26/30] [1000/1583]
                        Loss_D: 0.2311
                                        Loss_G: 3.2815
                                                         D(x): 0.8767
                                                                          D(G(z)):
0.0604 / 0.0661
[26/30] [1050/1583]
                        Loss_D: 0.2798
                                         Loss_G: 3.6894
                                                         D(x): 0.8060
                                                                          D(G(z)):
0.0137 / 0.0529
[26/30] [1100/1583]
                        Loss_D: 0.0715
                                         Loss_G: 4.8308
                                                         D(x): 0.9666
                                                                          D(G(z)):
0.0334 / 0.0163
[26/30] [1150/1583]
                        Loss_D: 0.1742 Loss_G: 5.4404 D(x): 0.8749
                                                                          D(G(z)):
```

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0.0037 / 0.0139
[26/30] [1200/1583]
                        Loss_D: 0.0476 Loss_G: 4.8422 D(x): 0.9711
                                                                         D(G(z)):
0.0166 / 0.0157
[26/30] [1250/1583]
                        Loss_D: 0.0254
                                        Loss_G: 5.9726
                                                        D(x): 0.9884
                                                                         D(G(z)):
0.0132 / 0.0062
[26/30] [1300/1583]
                        Loss_D: 0.0956
                                        Loss_G: 3.5899
                                                         D(x): 0.9361
                                                                         D(G(z)):
0.0194 / 0.0608
[26/30] [1350/1583]
                        Loss_D: 0.7914 Loss_G: 1.4780 D(x): 0.7345
                                                                         D(G(z)):
0.2759 / 0.3363
[26/30] [1400/1583]
                        Loss D: 0.1458
                                        Loss_G: 3.7518
                                                        D(x): 0.9245
                                                                         D(G(z)):
0.0562 / 0.0459
[26/30] [1450/1583]
                        Loss_D: 0.6081
                                        Loss_G: 3.5397
                                                         D(x): 0.8294
                                                                         D(G(z)):
0.2730 / 0.0541
[26/30] [1500/1583]
                        Loss_D: 0.6770 Loss_G: 5.0084
                                                        D(x): 0.9381
                                                                         D(G(z)):
0.3902 / 0.0103
[26/30] [1550/1583]
                        Loss_D: 0.3181 Loss_G: 4.2035 D(x): 0.8926
                                                                         D(G(z)):
0.1550 / 0.0250
[27/30][0/1583] Loss_D: 1.6587 Loss_G: 0.6531 D(x): 0.3008
                                                                 D(G(z)): 0.0503
/ 0.6203
[27/30] [50/1583]
                        Loss D: 0.2153 Loss G: 1.5499 D(x): 0.8368
                                                                         D(G(z)):
0.0126 / 0.3304
[27/30] [100/1583]
                        Loss D: 0.1616 Loss G: 2.8692 D(x): 0.9050
                                                                         D(G(z)):
0.0425 / 0.1093
                        Loss_D: 0.2544 Loss_G: 3.8927
                                                                         D(G(z)):
[27/30] [150/1583]
                                                         D(x): 0.8897
0.1044 / 0.0399
[27/30] [200/1583]
                        Loss_D: 0.4975
                                        Loss_G: 2.5848
                                                         D(x): 0.8128
                                                                         D(G(z)):
0.1901 / 0.1192
[27/30] [250/1583]
                        Loss_D: 0.1263 Loss_G: 3.6980
                                                         D(x): 0.9242
                                                                         D(G(z)):
0.0385 / 0.0512
[27/30] [300/1583]
                        Loss_D: 0.0840
                                         Loss_G: 5.0980
                                                         D(x): 0.9810
                                                                         D(G(z)):
0.0568 / 0.0141
[27/30] [350/1583]
                        Loss_D: 0.0465
                                        Loss_G: 4.9254
                                                         D(x): 0.9776
                                                                         D(G(z)):
0.0221 / 0.0151
[27/30] [400/1583]
                        Loss_D: 0.3465
                                        Loss_G: 2.7391
                                                         D(x): 0.8153
                                                                         D(G(z)):
0.0965 / 0.1051
[27/30] [450/1583]
                        Loss_D: 0.0630
                                        Loss_G: 4.6327
                                                         D(x): 0.9627
                                                                         D(G(z)):
0.0186 / 0.0209
[27/30] [500/1583]
                        Loss D: 0.6302
                                        Loss_G: 2.5159
                                                         D(x): 0.7042
                                                                         D(G(z)):
0.1577 / 0.1352
[27/30] [550/1583]
                        Loss D: 0.0894
                                        Loss_G: 4.9951 D(x): 0.9404
                                                                         D(G(z)):
0.0174 / 0.0159
[27/30] [600/1583]
                        Loss_D: 0.1260
                                        Loss_G: 5.0246
                                                        D(x): 0.9748
                                                                         D(G(z)):
0.0852 / 0.0124
[27/30] [650/1583]
                        Loss_D: 0.1348
                                         Loss_G: 3.9339
                                                         D(x): 0.9200
                                                                         D(G(z)):
0.0352 / 0.0359
[27/30] [700/1583]
                        Loss_D: 0.1375
                                        Loss_G: 5.4936
                                                         D(x): 0.8861
                                                                         D(G(z)):
0.0021 / 0.0084
[27/30] [750/1583]
                        Loss_D: 0.3453 Loss_G: 2.7739 D(x): 0.8113
                                                                         D(G(z)):
```

```
0.0850 / 0.1098
[27/30] [800/1583]
                        Loss_D: 0.0753 Loss_G: 4.7702 D(x): 0.9517
                                                                         D(G(z)):
0.0214 / 0.0176
[27/30] [850/1583]
                        Loss_D: 0.0380
                                        Loss_G: 4.8801 D(x): 0.9800
                                                                         D(G(z)):
0.0165 / 0.0158
[27/30] [900/1583]
                                        Loss_G: 5.1310
                        Loss_D: 0.0612
                                                         D(x): 0.9759
                                                                         D(G(z)):
0.0295 / 0.0134
[27/30] [950/1583]
                        Loss_D: 0.0488
                                        Loss_G: 4.9938
                                                        D(x): 0.9823
                                                                         D(G(z)):
0.0269 / 0.0149
[27/30] [1000/1583]
                        Loss D: 0.1035
                                        Loss_G: 5.3265
                                                        D(x): 0.9671
                                                                         D(G(z)):
0.0605 / 0.0098
[27/30] [1050/1583]
                        Loss_D: 0.0443
                                        Loss_G: 5.3222 D(x): 0.9867
                                                                         D(G(z)):
0.0293 / 0.0093
[27/30] [1100/1583]
                        Loss_D: 0.0461
                                        Loss_G: 6.2075
                                                        D(x): 0.9899
                                                                         D(G(z)):
0.0330 / 0.0052
[27/30] [1150/1583]
                        Loss_D: 0.0483
                                        Loss_G: 5.0769
                                                                         D(G(z)):
                                                         D(x): 0.9882
0.0340 / 0.0126
[27/30] [1200/1583]
                        Loss_D: 0.0367
                                        Loss_G: 5.2016 D(x): 0.9822
                                                                         D(G(z)):
0.0178 / 0.0115
[27/30] [1250/1583]
                        Loss D: 0.2454
                                        Loss G: 3.5602 D(x): 0.8535
                                                                         D(G(z)):
0.0519 / 0.0491
[27/30] [1300/1583]
                        Loss D: 0.2981 Loss G: 2.5775 D(x): 0.8554
                                                                         D(G(z)):
0.1028 / 0.1287
                        Loss_D: 0.8119
                                        Loss G: 2.8906
[27/30] [1350/1583]
                                                        D(x): 0.5528
                                                                         D(G(z)):
0.0084 / 0.1278
[27/30] [1400/1583]
                        Loss_D: 0.1799
                                        Loss_G: 3.8418 D(x): 0.9044
                                                                         D(G(z)):
0.0454 / 0.0416
[27/30] [1450/1583]
                        Loss_D: 0.0630 Loss_G: 4.6687
                                                         D(x): 0.9636
                                                                         D(G(z)):
0.0180 / 0.0211
[27/30] [1500/1583]
                        Loss_D: 0.1247
                                        Loss_G: 3.8215
                                                        D(x): 0.8970
                                                                         D(G(z)):
0.0078 / 0.0440
[27/30] [1550/1583]
                        Loss_D: 0.0858 Loss_G: 5.2630 D(x): 0.9719
                                                                         D(G(z)):
0.0466 / 0.0120
[28/30][0/1583] Loss_D: 0.0477 Loss_G: 5.4592 D(x): 0.9871
                                                                 D(G(z)): 0.0323
/ 0.0098
[28/30] [50/1583]
                        Loss_D: 0.0907 Loss_G: 3.9657 D(x): 0.9282
                                                                         D(G(z)):
0.0099 / 0.0423
[28/30] [100/1583]
                        Loss D: 1.4942
                                       Loss_G: 3.8786
                                                                         D(G(z)):
                                                        D(x): 0.9532
0.6490 / 0.0411
[28/30] [150/1583]
                        Loss_D: 0.3282 Loss_G: 6.8815 D(x): 0.9915
                                                                         D(G(z)):
0.2147 / 0.0023
[28/30] [200/1583]
                        Loss_D: 2.2833 Loss_G: 7.9774 D(x): 0.9999
                                                                         D(G(z)):
0.8181 / 0.0017
[28/30] [250/1583]
                        Loss_D: 0.3784
                                        Loss_G: 2.8322
                                                        D(x): 0.8195
                                                                         D(G(z)):
0.1201 / 0.1008
[28/30] [300/1583]
                        Loss_D: 0.0970
                                        Loss_G: 4.4016 D(x): 0.9571
                                                                         D(G(z)):
0.0269 / 0.0274
[28/30] [350/1583]
                        Loss_D: 0.1902 Loss_G: 3.5635 D(x): 0.9054
                                                                         D(G(z)):
```

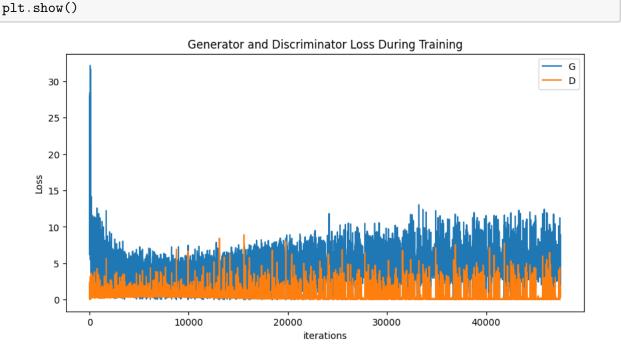
```
0.0664 / 0.0564
[28/30] [400/1583]
                        Loss_D: 0.0618 Loss_G: 5.4655 D(x): 0.9908
                                                                          D(G(z)):
0.0445 / 0.0085
[28/30] [450/1583]
                        Loss_D: 0.1070
                                         Loss_G: 5.4384
                                                          D(x): 0.9839
                                                                          D(G(z)):
0.0681 / 0.0084
[28/30] [500/1583]
                        Loss_D: 0.7188
                                         Loss_G: 1.5666
                                                          D(x): 0.6324
                                                                          D(G(z)):
0.1309 / 0.2952
[28/30] [550/1583]
                        Loss_D: 1.9842
                                         Loss_G: 0.3653
                                                         D(x): 0.2561
                                                                          D(G(z)):
0.0470 / 0.7443
[28/30] [600/1583]
                        Loss D: 0.0670
                                         Loss_G: 4.6936
                                                          D(x): 0.9669
                                                                          D(G(z)):
0.0304 / 0.0183
[28/30] [650/1583]
                        Loss_D: 0.4727
                                         Loss_G: 3.1150
                                                          D(x): 0.8919
                                                                          D(G(z)):
0.2479 / 0.0703
[28/30] [700/1583]
                        Loss_D: 0.4473
                                         Loss_G: 3.7508
                                                          D(x): 0.8699
                                                                          D(G(z)):
0.2199 / 0.0391
[28/30] [750/1583]
                        Loss_D: 0.0658
                                         Loss_G: 4.4423
                                                                          D(G(z)):
                                                          D(x): 0.9657
0.0274 / 0.0322
[28/30] [800/1583]
                        Loss_D: 0.0598
                                         Loss_G: 4.7320
                                                                          D(G(z)):
                                                          D(x): 0.9752
0.0319 / 0.0195
[28/30] [850/1583]
                        Loss D: 0.0403
                                         Loss G: 5.2227
                                                          D(x): 0.9768
                                                                          D(G(z)):
0.0156 / 0.0136
[28/30] [900/1583]
                        Loss D: 0.0520
                                         Loss G: 4.5310 D(x): 0.9728
                                                                          D(G(z)):
0.0204 / 0.0208
                        Loss_D: 0.0359
[28/30] [950/1583]
                                         Loss_G: 6.0894
                                                         D(x): 0.9942
                                                                          D(G(z)):
0.0284 / 0.0062
[28/30] [1000/1583]
                        Loss_D: 0.0510
                                         Loss_G: 4.9270
                                                          D(x): 0.9630
                                                                          D(G(z)):
0.0110 / 0.0197
[28/30] [1050/1583]
                        Loss_D: 0.0587
                                         Loss_G: 4.4438
                                                         D(x): 0.9584
                                                                          D(G(z)):
0.0132 / 0.0283
[28/30] [1100/1583]
                        Loss_D: 0.0706
                                         Loss_G: 4.1915
                                                          D(x): 0.9580
                                                                          D(G(z)):
0.0247 / 0.0286
[28/30] [1150/1583]
                        Loss_D: 0.0522
                                         Loss_G: 4.4597
                                                          D(x): 0.9638
                                                                          D(G(z)):
0.0130 / 0.0248
[28/30] [1200/1583]
                        Loss_D: 0.0516
                                         Loss_G: 4.1049
                                                          D(x): 0.9650
                                                                          D(G(z)):
0.0128 / 0.0351
[28/30] [1250/1583]
                        Loss_D: 0.1088
                                         Loss_G: 4.4693
                                                          D(x): 0.9090
                                                                          D(G(z)):
0.0043 / 0.0282
[28/30] [1300/1583]
                        Loss_D: 0.0270
                                         Loss_G: 5.9991
                                                          D(x): 0.9847
                                                                          D(G(z)):
0.0111 / 0.0057
[28/30] [1350/1583]
                        Loss_D: 0.0204
                                         Loss_G: 5.9224 D(x): 0.9927
                                                                          D(G(z)):
0.0127 / 0.0062
[28/30] [1400/1583]
                        Loss_D: 0.7079
                                         Loss_G: 2.6875
                                                         D(x): 0.7990
                                                                          D(G(z)):
0.3019 / 0.1142
[28/30] [1450/1583]
                        Loss_D: 0.2486
                                         Loss_G: 5.3467
                                                          D(x): 0.9596
                                                                          D(G(z)):
0.1572 / 0.0097
[28/30] [1500/1583]
                        Loss_D: 0.2560
                                         Loss_G: 3.1879
                                                          D(x): 0.8415
                                                                          D(G(z)):
0.0333 / 0.0909
[28/30] [1550/1583]
                        Loss_D: 0.5527
                                         Loss_G: 5.4930 D(x): 0.9671
                                                                          D(G(z)):
```

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0.3468 / 0.0078
[29/30][0/1583] Loss_D: 0.1211 Loss_G: 6.0344 D(x): 0.9799
                                                                 D(G(z)): 0.0812
/ 0.0047
[29/30] [50/1583]
                        Loss_D: 0.0697 Loss_G: 4.5248 D(x): 0.9501
                                                                         D(G(z)):
0.0141 / 0.0226
[29/30] [100/1583]
                        Loss_D: 0.0491 Loss_G: 5.4165
                                                         D(x): 0.9895
                                                                         D(G(z)):
0.0333 / 0.0079
[29/30] [150/1583]
                        Loss_D: 0.2907 Loss_G: 5.6282 D(x): 0.9880
                                                                         D(G(z)):
0.2085 / 0.0068
[29/30] [200/1583]
                        Loss D: 0.0447
                                        Loss_G: 5.3334 D(x): 0.9812
                                                                         D(G(z)):
0.0236 / 0.0129
[29/30] [250/1583]
                        Loss_D: 0.7521
                                        Loss_G: 5.6170 D(x): 0.9926
                                                                         D(G(z)):
0.4338 / 0.0078
[29/30] [300/1583]
                        Loss_D: 0.1148
                                        Loss_G: 5.6713 D(x): 0.9750
                                                                         D(G(z)):
0.0714 / 0.0082
[29/30] [350/1583]
                        Loss_D: 0.0637
                                        Loss_G: 5.7029
                                                                         D(G(z)):
                                                         D(x): 0.9842
0.0447 / 0.0063
[29/30] [400/1583]
                        Loss_D: 0.8841
                                        Loss_G: 1.1785
                                                                         D(G(z)):
                                                        D(x): 0.5721
0.1222 / 0.3952
[29/30] [450/1583]
                        Loss D: 0.1771 Loss G: 4.9302 D(x): 0.9803
                                                                         D(G(z)):
0.1098 / 0.0153
[29/30] [500/1583]
                        Loss D: 0.8425
                                        Loss G: 1.3948 D(x): 0.5820
                                                                         D(G(z)):
0.1551 / 0.3291
                        Loss_D: 0.0948
                                        Loss_G: 5.1455
                                                                         D(G(z)):
[29/30] [550/1583]
                                                        D(x): 0.9802
0.0656 / 0.0134
[29/30] [600/1583]
                        Loss_D: 0.5203
                                        Loss_G: 2.6846
                                                        D(x): 0.6638
                                                                         D(G(z)):
0.0138 / 0.1457
[29/30] [650/1583]
                        Loss_D: 0.6436
                                       Loss_G: 3.3537
                                                         D(x): 0.9695
                                                                         D(G(z)):
0.3952 / 0.0535
[29/30] [700/1583]
                        Loss_D: 0.1115
                                        Loss_G: 4.5372
                                                         D(x): 0.9288
                                                                         D(G(z)):
0.0252 / 0.0276
[29/30] [750/1583]
                        Loss_D: 0.0896
                                        Loss_G: 4.6360
                                                         D(x): 0.9355
                                                                         D(G(z)):
0.0110 / 0.0200
[29/30] [800/1583]
                        Loss_D: 0.1304
                                        Loss_G: 6.3736
                                                        D(x): 0.9898
                                                                         D(G(z)):
0.1034 / 0.0038
[29/30] [850/1583]
                        Loss_D: 0.0244
                                        Loss_G: 5.6752
                                                         D(x): 0.9893
                                                                         D(G(z)):
0.0130 / 0.0088
[29/30] [900/1583]
                        Loss D: 0.3495
                                        Loss_G: 2.8866
                                                         D(x): 0.8536
                                                                         D(G(z)):
0.1418 / 0.0826
[29/30] [950/1583]
                        Loss_D: 0.7386
                                        Loss_G: 2.4708 D(x): 0.5742
                                                                         D(G(z)):
0.0030 / 0.1587
[29/30] [1000/1583]
                        Loss_D: 1.0021
                                       Loss_G: 1.0212 D(x): 0.4627
                                                                         D(G(z)):
0.0144 / 0.4701
                        Loss_D: 0.0649
[29/30] [1050/1583]
                                        Loss_G: 5.3172 D(x): 0.9612
                                                                         D(G(z)):
0.0210 / 0.0128
[29/30] [1100/1583]
                        Loss_D: 0.0413
                                        Loss_G: 4.9108 D(x): 0.9837
                                                                         D(G(z)):
0.0234 / 0.0161
[29/30] [1150/1583]
                        Loss_D: 0.0453 Loss_G: 5.4224 D(x): 0.9849
                                                                         D(G(z)):
```

```
0.0254 / 0.0098
     [29/30] [1200/1583]
                              Loss_D: 0.0693
                                              Loss_G: 4.7382 D(x): 0.9663
                                                                               D(G(z)):
     0.0313 / 0.0199
     [29/30] [1250/1583]
                              Loss_D: 0.0513
                                              Loss_G: 5.0466
                                                               D(x): 0.9811
                                                                               D(G(z)):
     0.0296 / 0.0152
     [29/30] [1300/1583]
                              Loss_D: 0.0360
                                              Loss_G: 5.4085
                                                               D(x): 0.9947
                                                                               D(G(z)):
     0.0288 / 0.0089
     [29/30] [1350/1583]
                              Loss_D: 0.0583
                                              Loss_G: 5.2304
                                                              D(x): 0.9538
                                                                               D(G(z)):
     0.0058 / 0.0105
     [29/30] [1400/1583]
                              Loss_D: 0.0659
                                              Loss_G: 5.0292
                                                              D(x): 0.9624
                                                                               D(G(z)):
     0.0195 / 0.0187
     [29/30] [1450/1583]
                              Loss_D: 0.3897
                                              Loss_G: 4.6520
                                                               D(x): 0.9479
                                                                               D(G(z)):
     0.2537 / 0.0160
     [29/30] [1500/1583]
                                                               D(x): 0.9824
                              Loss_D: 0.0424
                                              Loss_G: 5.2643
                                                                               D(G(z)):
     0.0221 / 0.0118
     [29/30] [1550/1583]
                              Loss_D: 0.8248
                                              Loss_G: 1.6220
                                                              D(x): 0.5791
                                                                               D(G(z)):
     0.0994 / 0.2814
[25]: # save the model
      torch.save(netG.state_dict(), 'dcgan_generator.pt')
[26]: plt.figure(figsize=(10,5))
      plt.title("Generator and Discriminator Loss During Training")
      plt.plot(G_losses,label="G")
      plt.plot(D_losses,label="D")
      plt.xlabel("iterations")
```

plt.ylabel("Loss")

plt.legend()



Animation size has reached 21077774 bytes, exceeding the limit of 20971520.0. If you're sure you want a larger animation embedded, set the animation.embed_limit rc parameter to a larger value (in MB). This and further frames will be dropped.

[27]: <IPython.core.display.HTML object>





