

## Key Concepts and Terminology

Chi-Square Analysis: Non-parametric analysis method used in analyzing categorical data with no continuous dependent variable. It is very sensitive to large sample sizes thus increasing power but also prone to Type I errors.

Counts: A measure used in counting within each category. Just a simple count of say 10 Orange M&Ms in a 1.74 Oz bag made up of 56 M&Ms.

Proportions: The ratio of counts relative the sample size (n). It can be expressed as a percentage.

Chi-Square Test: One tailed test reported as a two tailed test.

Goodness of Fit Test: Compare the observed distribution to the expected distribution (equal vs unequal proportions).

Test of Association: A test to determine association between two variables or categories (OR sample (my bag) vs population (class bag)). A comparison of observed responses to expected responses in a truly independent scenario for the variables involved (odds ratio == 1).

Chi-Square Statistic:

$$\chi^2 = \sum \frac{(\text{Observed Freq} - \text{Expected Freq})^2}{\text{Expected Frequency}}$$

$$\chi^2 = \sum_{i=0}^{\infty} \frac{(O - E)^2}{E}$$

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Chi-Square Distribution: Positive or right skewed non-normal distribution with increasing symmetry as the degrees of freedom increase (DF++); unique because it begins at zero. The PDF is dependent on the Chi-square value and DF (constant).

$$\chi^2 = \sum_{i=1}^r Y_i^2, \text{ mean}=0, \text{ variance}=I, r = \text{DF}$$

$$P_r(x) = \frac{x^{\frac{r}{2}-1} e^{-\frac{x}{2}}}{\Gamma\left(\frac{1}{2}r\right) 2^{\frac{r}{2}}}$$

$$D_r(\chi^2) = \int_0^{\chi^2} \frac{t^{\frac{r}{2}-1} e^{-\frac{t}{2}}}{\Gamma\left(\frac{1}{2}r\right) 2^{\frac{r}{2}}} dt$$

$$P\left(\frac{1}{2}r, \frac{1}{2}\chi^2\right) = 1 - \int_0^{\chi^2} \frac{t^{\frac{r}{2}-1} e^{-\frac{t}{2}}}{\Gamma\left(\frac{1}{2}r\right) 2^{\frac{r}{2}}} dt$$

Goodness of Fit DF: # of Categories - 1

Test of Association DF: (Nrow-1) \* (Ncol-1)

Phi-stat: A measure of the strength of association following a Chi-sq test of association analysis.

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Fisher's exact p: Used as an alternative to the Chi-sq test of association if one or more of the cell counts in the contingency table is <5.

$$\text{Fisher's exact } p = \frac{((a + b)! (c + d)! (a + c)! (b + d)!)}{a! b! c! d! N!}$$

Yate's correction (1934): Subtraction of 0.5 from the absolute value difference of O-E frequencies. The outcome reduces the calculated Chi-sq stat.

Contingency table: A table used to represent a Chi-square test of association and also used when dealing with treatment-control setups like in clinical trials.

		Color		
		Orange	Not orange	Total
Bags	Mybag	2	54	56
	Class	440	1581	2021
	Total	442	1635	2077

Odds Ratio: a ratio of odds\_var1\_with\_condition to odds\_var2\_with\_condition. Unlike the risk ratio, calculations here are dependent on outcomes.

$$\text{Odds Ratio} = \frac{\frac{a = 64}{b = 166}}{\frac{c = 178}{d = 277}} = .5999$$

Risk ratio: a ratio of risk\_var1\_with\_condition to risk\_var2\_with\_condition. Calculations dependent on the sample size and risk factor.

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OR confidence interval: If 1 falls outside the OR CI then the OR is significantly different from 1 (using alpha = 0.05).

$$OR_{CI} = e^{ln(OR) \pm 1.96 * \sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}}$$

Fisher's test in R: Use of a matrix is needed to accomplish this endeavor.

[Vassar Stats](#): A tool used to perform contingency table analysis.