> #Exercise 1

- [1] "The number of students is 340823"
- [1] "The number of schools is 640"
- [1] "The number of programs is 32"
- [1] "The number of choices is 5546"
- [1] "The number of missing test score is 179887"
- [1] "The number of Apply to the same school (different programs) is 5546"
- [1] "The number of Apply to less than 6 choices is 18954"

> #Exercise 2

[1] "The answer for Exercise 2 is Choicescore"

> head(Choicescore, 20)

/ 110	ad (Choices)					
	schoolcode	choice	X			male
1	10101	10101Agriculture		288	15	1
7	10101	10101Agriculture		288	14	0
13	10101	10101Agriculture		288	19	1
19	10101	10101Agriculture	230386	289	17	0
25	10101	10101Agriculture	230627	291	16	1
31	10101	10101Agriculture	230893	292	16	0
37	10101	10101Agriculture	230927	293	16	0
43	10101	10101Agriculture	230694	294	16	1
49	10101	10101Agriculture	230578	295	19	1
55	10101	10101Agriculture		295	17	1
61	10101	10101Agriculture		296	15	0
67	10101	10101Agriculture		297	15	0
73	10101	10101Agriculture		298	17	1
79	10101	10101Agriculture		298	16	1
85	10101	10101Agriculture		298	17	1
91	10101	10101Agriculture		299	16	1
97	10101	10101Agriculture		299	16	1
103	10101	10101Agriculture		300	16	1
109	10101	10101Agriculture		302	20	1
115	10101	10101Agriculture		303	19	0
110	choicepgm		strict 1			
1	Agriculture			-ampi	3	288
7	Agriculture				3	288
13	Agriculture	_			3	288
19	Agriculture	-			1	288
25	Agriculture				4	288
31	Agriculture		saman)		3	288
37	Agriculture		Tema		4	288
43					4	288
	Agriculture		saman)			
49	Agriculture				2	288
55	Agriculture					288
61	Agriculture				3	288
67	Agriculture				1	288
73	Agriculture	-			1	288
79	Agriculture		tpond)		2	288
85	Agriculture	-			4	288
91	-		tpond)		2	288
97	Agriculture	-			4	288
103	Agriculture	e Ga West (Ama	saman)		3	288

```
109 Agriculture Ga West (Amasaman)
                                                 288
115 Agriculture
                  Ga West (Amasaman)
                                                  288
     quality size
                                            schoolname
1
    309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
7
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
13
19
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
25
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
31
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
37
43
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
55
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
61
67
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
73
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
79
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
85
91
   309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
97 309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
103 309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
109 309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
115 309.0889 45 EBENEZER SENIOR HIGH. SCHOOL, DANSOMAN
          sssdistrict ssslong
                                   ssslat
   Accra Metropolitan -0.1971153 5.607396
1
7
   Accra Metropolitan -0.1971153 5.607396
13 Accra Metropolitan -0.1971153 5.607396
19 Accra Metropolitan -0.1971153 5.607396
25 Accra Metropolitan -0.1971153 5.607396
31 Accra Metropolitan -0.1971153 5.607396
   Accra Metropolitan -0.1971153 5.607396
43 Accra Metropolitan -0.1971153 5.607396
49 Accra Metropolitan -0.1971153 5.607396
55 Accra Metropolitan -0.1971153 5.607396
61 Accra Metropolitan -0.1971153 5.607396
67 Accra Metropolitan -0.1971153 5.607396
73 Accra Metropolitan -0.1971153 5.607396
79 Accra Metropolitan -0.1971153 5.607396
85 Accra Metropolitan -0.1971153 5.607396
91 Accra Metropolitan -0.1971153 5.607396
97 Accra Metropolitan -0.1971153 5.607396
103 Accra Metropolitan -0.1971153 5.607396
109 Accra Metropolitan -0.1971153 5.607396
115 Accra Metropolitan -0.1971153 5.607396
```

```
> #Exercise 3
```

^{[1] &}quot;The answer for Exercise 3 is the variable Distance in the dataframe Dis "

> head(Dis, 20)

```
19679
                                                      30403
                                  Agona Swedru
20031
                                  Agona Swedru
                                                      30403
428
                                                      30403
       Abura/Asebu/Kwamankese (Abura Dunkwa)
461
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
15
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
161
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
17
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
33
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
21640
               Ajumako/Enyan/Essiam (Ajumako)
                                                      30403
21848
               Ajumako/Enyan/Essiam (Ajumako)
                                                      30403
128201
                   Twifo Hemang (Twifo Praso)
                                                      30403
128284
                   Twifo Hemang (Twifo Praso)
                                                      30403
37302
                  Awutu/Efutu/Senya (Winneba)
                                                      30403
37395
                  Awutu/Efutu/Senya (Winneba)
                                                      30403
                        Mfantsiman (Saltpond)
96339
                                                      30403
96639
                        Mfantsiman (Saltpond)
                                                      30403
60
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
141
       Abura/Asebu/Kwamankese (Abura Dunkwa)
                                                      30403
96923
                        Mfantsiman (Saltpond)
                                                      30403
97032
                        Mfantsiman (Saltpond)
                                                      30403
                                  X score agey male
                     choice
19679
         30403General Arts 179888
                                       249
                                             16
                                                    0
20031
         30403General Arts 179888
                                       249
                                             16
428
           30403Agriculture 179890
                                       254
                                             19
                                                    1
461
          30403Agriculture 179890
                                       254
                                             19
                                                    1
15
       30403Home Economics 179891
                                       277
                                             17
                                                    0
       30403Home Economics 179891
                                       277
                                             17
                                                    0
161
17
         30403General Arts 179892
                                       236
                                             16
                                                    0
         30403General Arts 179892
33
                                       236
                                             16
                                                    0
21640
         30403General Arts 179893
                                       237
                                             18
                                                    1
21848
         30403General Arts 179893
                                       237
                                             18
                                                    1
          30403Agriculture 179894
128201
                                       262
                                             16
                                                    0
          30403Agriculture 179894
                                       262
                                             16
                                                    0
128284
         30403General Arts 179895
                                       249
                                             15
37302
                                                    1
         30403General Arts 179895
                                       249
37395
                                             15
                                                    1
                                       229
                                             17
                                                    0
96339
         30403General Arts 179896
96639
         30403General Arts 179896
                                       229
                                             17
                                                    0
         30403General Arts 179897
                                       219
60
                                             18
                                                    1
                                                    1
141
         30403General Arts 179897
                                       219
                                             18
          30403Agriculture 179898
96923
                                       227
                                             17
                                                    0
                                       227
                                             17
97032
          30403Agriculture 179898
                                                    0
             choicepgm rankplace cutoff
                                         quality size
19679
         General Arts
                                5
                                     208 242.0857
20031
                                5
                                     208 242.0857
         General Arts
                                2
428
          Agriculture
                                     219 241.9333
                                                      15
461
                                2
          Agriculture
                                     219 241.9333
                                                      15
15
       Home Economics
                                4
                                     215 248.3750
                                                       8
161
       Home Economics
                                4
                                     215 248.3750
                                                       8
17
                                3
                                     208 242.0857
                                                      35
         General Arts
                                3
33
         General Arts
                                     208 242.0857
                                                      35
                                1
21640
                                     208 242.0857
                                                      35
         General Arts
                                1
21848
         General Arts
                                     208 242.0857
                                                      3.5
128201
          Agriculture
                                6
                                     219 241.9333
                                                      15
128284
          Agriculture
                                6
                                     219 241.9333
                                                      15
```

```
37302
         General Arts
                              5
                                   208 242.0857
                                                   35
37395
         General Arts
                              5
                                   208 242.0857
                                                   35
96339
                              1
                                   208 242.0857
                                                   35
         General Arts
96639
         General Arts
                              1
                                   208 242.0857
                                                   35
60
         General Arts
                              6
                                   208 242.0857
                                                   35
                                   208 242.0857
141
         General Arts
                              6
                                                   35
96923
                              3
                                   219 241.9333
                                                   1.5
         Agriculture
97032
         Agriculture
                              3
                                   219 241.9333
                                                   15
                                 schoolname
19679
            ABAKRAMPA SENIOR HIGH TECHNICAL
20031
      <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
428
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
            ABAKRAMPA SENIOR HIGH TECHNICAL
461
15
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
161
            ABAKRAMPA SENIOR HIGH TECHNICAL
17
            ABAKRAMPA SENIOR HIGH TECHNICAL
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
33
21640
            ABAKRAMPA SENIOR HIGH TECHNICAL
21848
      <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
            ABAKRAMPA SENIOR HIGH TECHNICAL
128201
128284 <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
37302
            ABAKRAMPA SENIOR HIGH TECHNICAL
37395
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
96339
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
            ABAKRAMPA SENIOR HIGH TECHNICAL
96639
60
            ABAKRAMPA SENIOR HIGH TECHNICAL
       <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
141
96923
            ABAKRAMPA SENIOR HIGH TECHNICAL
97032
      <d8>?ABAKRAMPA SENIOR HIGH TECHNICAL
                                 sssdistrict
                                               ssslong
19679
      Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
20031 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
428
461
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
15
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
161
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
17
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
33
      Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
21640
21848 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
128201 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
128284 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
37302 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
37395 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
96339 Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
96639
      Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
60
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
141
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
96923
      Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
97032
       Abura/Asebu/Kwamankese (Abura Dunkwa) -1.197088
                  point x point y Distance
         ssslat
       5.130001 -0.7552425 5.617353 45.40499
19679
      5.130001 -0.7552425 5.617353 45.40499
20031
428
       5.130001 -1.1970884 5.130001 0.00000
```

```
5.130001 -1.1970884 5.130001
                                    0.00000
15
       5.130001 -1.1970884 5.130001
                                    0.00000
      5.130001 -1.1970884 5.130001 0.00000
161
17
      5.130001 -1.1970884 5.130001 0.00000
33
       5.130001 -1.1970884 5.130001 0.00000
21640 5.130001 -1.0053846 5.401725 22.96873
21848 5.130001 -1.0053846 5.401725 22.96873
128201 5.130001 -1.5597034 5.572999 39.52487
128284 5.130001 -1.5597034 5.572999 39.52487
37302 5.130001 -0.5086389 5.544896 55.41003
37395 5.130001 -0.5086389 5.544896 55.41003
96339 5.130001 -1.0064534 5.201528 14.03343
96639 5.130001 -1.0064534 5.201528 14.03343
      5.130001 -1.1970884 5.130001 0.00000
60
141
      5.130001 -1.1970884 5.130001 0.00000
96923 5.130001 -1.0064534 5.201528 14.03343
97032 5.130001 -1.0064534 5.201528 14.03343
```

> #Exercise 4

- [1] "For 1st Rankplace"
- [1] "The average of the cutoff is 281.666696851018"
- [1] "The sd of the cutoff is 58.8290705689274"
- [1] "The average of the Quality is 308.362561581667"
- [1] "The sd of the Quality is 52.1712365763513"
- [1] "The average of the Distance is 35.1811012348586"
- [1] "The sd of the Distance is 52.8207408451784"
- [1] "For 2nd Rankplace"
- [1] "The average of the cutoff is 275.943484190162"
- [1] "The sd of the cutoff is 51.1390749676321"
- [1] "The average of the Quality is 301.936452507742"
- [1] "The sd of the Quality is 44.5486524805607"
- [1] "The average of the Distance is 34.0217710653266"
- [1] "The sd of the Distance is 48.4151155841386"
- [1] "For 3rd Rankplace"
- [1] "The average of the cutoff is 261.26926286509"
- [1] "The sd of the cutoff is 43.8014658133546"
- [1] "The average of the Quality is 288.566888990669"
- [1] "The sd of the Quality is 37.492231591051"
- [1] "The average of the Distance is 28.6654303706568"
- [1] "The sd of the Distance is 43.3276802542669"
- [1] "For 4th Rankplace"
- [1] "The average of the cutoff is 247.957375629723"
- [1] "The sd of the cutoff is 37.6479586381162"
- [1] "The average of the Quality is 276.922107837596"
- [1] "The sd of the Quality is 31.7422473327192"
- [1] "The average of the Distance is 22.8660114943869"
- [1] "The sd of the Distance is 38.671561364868"
- [1] "For 5th Rankplace"
- [1] "The average of the cutoff is 211.090909090909"

```
[1] "The sd of the cutoff is 8.18112838937557"
[1] "The average of the Quality is 251.778416288314"
[1] "The sd of the Quality is 12.7789805612124"
[1] "The average of the Distance is 32.3881553859471"
[1] "The sd of the Distance is 30.5839074535372"
[1] "For 6th Rankplace"
[1] "The average of the cutoff is 211.181939353549"
[1] "The sd of the cutoff is 8.20046057879195"
[1] "The average of the Quality is 249.449253381274"
[1] "The sd of the Quality is 11.2054957202403"
[1] "The average of the Distance is 31.9538100119105"
[1] "The sd of the Distance is 29.7359428251178"
> Quantiles<- Dis[order(Dis$score, Dis$X),]</pre>
[1] "For 1st quantile"
[1] "The average of the cutoff is 216.727445079747"
[1] "The sd of the cutoff is 13.7504012401409"
[1] "The average of the Quality is 250.98769286784"
[1] "The sd of the Quality is 12.2768746968854"
[1] "The average of the Distance is 25.97192694149"
[1] "The sd of the Distance is 42.6813644020342"
[1] "For 2nd quantile"
[1] "The average of the cutoff is 228.874516582679"
[1] "The sd of the cutoff is 22.3503980789819"
[1] "The average of the Quality is 261.097918819516"
[1] "The sd of the Quality is 17.9526811040484"
[1] "The average of the Distance is 27.4219464315344"
[1] "The sd of the Distance is 45.9810011218846"
[1] "For 3rd quantile"
[1] "The average of the cutoff is 243.377261994572"
[1] "The sd of the cutoff is 32.1635880454268"
[1] "The average of the Quality is 273.609336668229"
[1] "The sd of the Quality is 26.5693976879494"
[1] "The average of the Distance is 28.7161280998983"
[1] "The sd of the Distance is 46.5872322494831"
[1] "For 4th quantile"
[1] "The average of the cutoff is 266.199677056391"
[1] "The sd of the cutoff is 52.0582572606955"
[1] "The average of the Quality is 293.943176433258"
[1] "The sd of the Quality is 45.4150688237614"
[1] "The average of the Distance is 31.1064247813155"
[1] "The sd of the Distance is 46.6952354382574"
> #Exercise 5
> head(Y, 20)
     1.9032843 -3.1350882 3.8277599 1.5970899 1.9943875
 [1]
     4.5373519 -4.1700785 -4.7640866 -0.3120093 -2.4801004
```

```
> head(ydum, 20)
[1] 1 0 1 1 1 1 0 0 1 0 0 1 1 1 1 1 0 0 0 0
```

[11] -1.9839194 0.9860258 2.1066723 1.9385475 0.8920039 [16] 3.2090729 -3.6149303 -1.3973371 -0.9666107 -3.7247639

- > #Exercise 6
- [1] "The correlation coefficient between Y and X1 is 0.209429106418655"
- [1] "The regression coefficient between Y and X1 is 1.19218588123404"
- [1] "The difference from 1.2 is -0.0078141187659575"

The regression result is $Y=2.550967+1.192186\ X1+-0.9046174\ X2+0.1099006\ X3+e$

The coefficients are $2.550967\ 1.192186\ -0.9046174\ 0.1099006$ The standard errors in this OLS are $0.04093615\ 0.01748154\ 0.002925907\ 0.02176734$

```
> #Exercise 7
'log Lik.' -2161.466 (df=4)
  True parameter R: GLM : est R: own :se R: GLM :se
                2.9654092 0.10011006 0.10011170
      2.5509674
                1.2343270 0.04458552 0.04463045
X1
      1.1921859
X2
               -0.9199287 0.01886599 0.01884960
     -0.9046174
               0.1354812 0.04694495 0.04705767
Х3
      0.1099006
'log Lik.' -2167.151 (df=4)
  True parameter R: GLM : est R: own :se R: GLM :se
      2.5509674 5.3212472 0.18728370 0.10011170
                2.2190576 0.08304348 0.04463045
X1
      1.1921859
               -1.6529784 0.03763265 0.01884960
     -0.9046174
X2
Х3
      0.1099006
               0.2439212 0.08434958 0.04705767
True parameter
                 Probit
                           Logit
                                      LPM
                       5.3212472 0.89111066
      2.5509674 2.9654092
      1.1921859 1.2343270 2.2190576 0.14521037
Х1
     -0.9046174 -0.9199287 -1.6529784 -0.10485191
X2
      0.1099006 0.1354812 0.2439212 0.01078067
Х3
```

- [1] "For the intercept, X1 and X2, all the three models hold 0.001 significant level" $\,$
- [1] "But for X3, the Probit and Logit models hold 0.01 significant level. But for LPM, the X3 is not significant."

```
> #Exercise 8
> # Probit Model
Marginal Effects:
            dF/dx Std. Err. z P>|z|
X1 0.4924149 0.0177859 27.6857 < 2e-16 ***
X2 -0.3669907 0.0075174 -48.8187 < 2e-16 ***
X3 0.0539974 0.0186723 2.8918 0.00383 **
Signif. codes:
0 \ \hat{a} \in ``*** \hat{a} \in \mathsf{TM} \ 0.001 \ \hat{a} \in ``** \hat{a} \in \mathsf{TM} \ 0.01 \ \hat{a} \in ``* \hat{a} \in \mathsf{TM} \ 0.05 \ \hat{a} \in ``. \hat{a} \in \mathsf{TM} \ 0.1 \ \hat{a} \in `` \ \hat{a} \in \mathsf{TM} \ 1
> # Logit Model
Marginal Effects:
            dF/dx Std. Err.
                                           z P>|z|
X1 0.5547272 0.0207585 26.723 < 2e-16 ***
X2 -0.4132169 0.0093871 -44.020 < 2e-16 ***
X3 0.0608904 0.0209894
                                       2.901 0.00372 **
Signif. codes:
0 \ \hat{a} \in ``*** \hat{a} \in \mathsf{TM} \ 0.001 \ \hat{a} \in ``** \hat{a} \in \mathsf{TM} \ 0.01 \ \hat{a} \in ``** \hat{a} \in \mathsf{TM} \ 0.05 \ \hat{a} \in ``. \hat{a} \in \mathsf{TM} \ 0.1 \ \hat{a} \in `` \ \hat{a} \in \mathsf{TM} \ 1
```