

# Wedge Impedance Analysis Program Documentation

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November 26, 2024

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## 1 Overview

This documentation describes a MATLAB-based program designed for calculating acoustic impedance and wave fields around a wedge structure. The

program implements various mathematical functions to compute scattered and direct wave fields using complex acoustic calculations.

## 2 Key Components

### 2.1 Main Control Script (testscript.m)

The main script initializes and controls the program execution with the following components:

- Global parameters initialization including:
  - Geometric parameters ( $r, \phi, r', \phi'$ )
  - Wave parameters ( $\theta_n, \theta_0$ )
  - Physical constants ( $c = 340$  m/s for speed of sound)
- Frequency range setup (20 Hz to 10 kHz)
- Wave field calculations and normalization
- Results visualization

### 2.2 Wave Field Components

The program consists of several specialized functions for different aspects of the wave field calculations:

#### 2.2.1 Direct Field Calculations

- `u_d.m`: Direct wave field calculator
- `u_ss.m`: Source-source interaction computation
- `u_sd.m`: Source-diffraction interaction handler
- `u_ds.m`: Diffraction-source interaction computation
- `u_dsw.m`: Diffraction-source-wedge interaction calculator

### **2.2.2 Mathematical Support Functions**

- `A_n.m`, `M_n.m`: Coefficient calculations
- `P_l.m`: Legendre polynomial implementations
- `omega_n.m`: Angular frequency calculations
- `epsy_n.m`, `epsy_cap.m`: Phase calculations
- `g_small.m`, `h_small.m`: Field calculation helper functions

## **3 Program Flow**

The program follows a systematic approach to compute acoustic fields:

### **3.1 Initialization Phase**

1. Global parameter setup
2. Geometric configuration definition
3. Material properties initialization

### **3.2 Computation Phase**

1. Frequency range iteration (20 Hz - 10 kHz)
2. Wave number calculation per frequency
3. Field computations:
  - Normal incidence field
  - Direct field
  - Scattered field components
  - Field combination

### **3.3 Output Phase**

1. Results normalization
2. Frequency response plotting

## 4 Mathematical Foundation

The program implements complex acoustic theory including:

### 4.1 Wave Propagation

The wave equation in cylindrical coordinates:

$$\nabla^2\Phi + k^2\Phi = 0 \quad (1)$$

where  $k$  is the wave number and  $\Phi$  is the velocity potential.

### 4.2 Scattered Field

The total field is composed of incident and scattered components:

$$\Phi_{\text{total}} = \Phi_{\text{incident}} + \Phi_{\text{scattered}} \quad (2)$$

### 4.3 Impedance Boundary Conditions

At the wedge surface:

$$\frac{\partial\Phi}{\partial n} + \beta\Phi = 0 \quad (3)$$

where  $\beta$  is the surface admittance and  $n$  is the normal direction.

## 5 Usage Instructions

To use the program:

1. Ensure all MATLAB files are in the same directory
2. Execute `testscript.m`
3. Review the generated plots showing field ratio vs. frequency

## 6 Conclusion

This implementation provides a comprehensive solution for analyzing acoustic behavior around wedge-shaped structures. It combines theoretical acoustic models with numerical methods to provide accurate simulations of wave propagation and interaction phenomena.