

# UNIT 3

## 1.Context-Free Grammar (CFG)

### Definition:

A **Context-Free Grammar (CFG)** is a formal system used to describe the syntax of a language. It defines a set of rules that specify how sentences in a language can be formed.

### Components of CFG:

A CFG is defined as a 4-tuple:

$$G = (V, \Sigma, R, S)$$

Component	Description	Example
<b>V (Variables / Non-terminals)</b>	Symbols that can be replaced by other symbols	S (Sentence), NP (Noun Phrase), VP (Verb Phrase)
<b><math>\Sigma</math> (Alphabet / Terminals)</b>	Symbols that appear in actual sentences	"dog", "runs", "barks"
<b>R (Rules / Productions)</b>	Rules that describe how non-terminals can be expanded	$S \rightarrow NP VP$ $NP \rightarrow Det N$ $VP \rightarrow V NP$ $Det \rightarrow "the"$
<b>S (Start Symbol)</b>	The symbol from which sentence generation begins	Typically S

### How CFG Works:

- Sentences are generated by replacing non-terminals step by step using the production rules.

#### Example:

Start: S

$S \rightarrow NP VP \Rightarrow NP VP$

$NP \rightarrow Det N \Rightarrow Det N VP$

$Det \rightarrow "the", N \rightarrow "dog" \Rightarrow "the dog" VP$

$VP \rightarrow V NP \Rightarrow "the dog" V NP$

$V \rightarrow "chases", NP \rightarrow Det N \rightarrow "a cat" \Rightarrow "the dog chases a cat"$

- CFG ensures that generated sentences are **syntactically valid** according to the rules.

### Applications of CFG in NLP:

1. **Parsing:** Produces parse trees representing hierarchical relationships of words.

**Example Parse Tree for "the dog chases":**

```
S
 / \
NP  VP
 |   / \
Det N  V
 |   |   |
the dog chases
```

2. **Syntax Checking:** Validates if a sentence is grammatically correct.
3. **Machine Translation:** Helps map syntactic structures between languages.
4. **Speech Recognition:** Defines valid sentence structures to improve accuracy.
5. **Information Extraction:** Identifies components like noun phrases, verbs, etc.

### Advantages:

- Simple, formal way to describe syntax.
- Can generate parse trees for structured understanding.
- Useful for rule-based NLP applications.

### Limitations:

- Cannot capture all natural language features, especially context-dependent meanings.
- Too rigid for complex languages.
- Modern NLP often uses **Probabilistic CFGs (PCFGs)** or neural networks to handle ambiguity.

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## 2. Grammar Rules for English

### Basic Components:

Phrase Type	Description	Example Rules
<b>Sentence (S)</b>	A complete thought	$S \rightarrow NP VP$
<b>Noun Phrase (NP)</b>	Subject or object	$NP \rightarrow Det N$
		$NP \rightarrow Det Adj N$
		$NP \rightarrow NP PP$ Examples: "the big dog", "a cat on the roof"
<b>Verb Phrase (VP)</b>	Action or predicate	$VP \rightarrow V$
		$VP \rightarrow V NP$
		$VP \rightarrow V NP PP$ Examples: "runs", "chased the cat", "gave a gift to her"
<b>Prepositional Phrase (PP)</b>	Connects nouns, verbs, or sentences	$PP \rightarrow P NP$ Examples: "on the table", "in the park"
<b>Modifiers &amp; Determiners</b>	Words modifying nouns	Determiners: "the", "a", "an" Adjectives: "big", "small", "red"

#### Example Sentence Generation:

- Sentence: "The big dog chased a cat in the park."

##### Parse Steps:

$S \rightarrow NP VP$

$NP \rightarrow Det Adj N \rightarrow$  "The big dog"

$VP \rightarrow V NP PP \rightarrow$  "chased a cat in the park"

$PP \rightarrow P NP \rightarrow$  "in the park"

#### Purpose in NLP:

- Basis for **parsing**, **sentence generation**, and **syntax checking**.
- Essential for creating **parse trees** and **treebanks**.

### 3. Treebanks

#### Definition:

A **Treebank** is a linguistic resource where sentences are annotated with their **syntactic structure**. Each sentence is represented as a **parse tree**.

### Purpose:

- Provides training data for NLP tasks like parsing, syntax analysis, and grammar checking.
- Helps study natural language structure systematically.

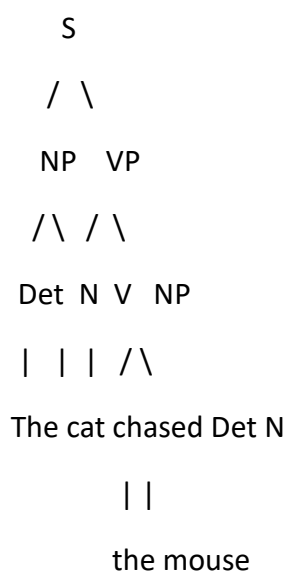
### Structure:

- **Non-terminal nodes:** syntactic categories (e.g., NP, VP)
- **Terminal nodes:** actual words in the sentence

### Types of Treebanks:

1. **Constituency Treebanks:** Show how words group into phrases (CFG-based)  
**Example:** Penn Treebank
2. **Dependency Treebanks:** Show dependencies between words (head-dependent relationships)

### Example Constituency Tree for "The cat chased the mouse":



### Applications in NLP:

- **Syntactic Parsing:** Train parsers to predict structure.
- **Grammar Checking:** Detect grammatical errors.
- **Machine Translation:** Ensure correct sentence structure.
- **Information Extraction:** Identify subject, object, and verb relations.

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## 4. Normal Forms for Grammar

## Normal Forms in NLP

### Definition:

A **Normal Form** is a standardized way of writing grammar rules. It simplifies the structure of rules so that **parsing algorithms** can process them more efficiently and consistently.

- It ensures rules follow a specific pattern.
  - Helps reduce ambiguity and complexity in syntactic analysis.
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### Common Normal Forms:

#### 1. Chomsky Normal Form (CNF):

- Every production rule is in one of the following forms:
  1.  $A \rightarrow BC$  → A non-terminal produces exactly **two non-terminals**
  2.  $A \rightarrow a$  → A non-terminal produces a **single terminal**

### Example:

Original Rules:

$S \rightarrow NP VP$

$NP \rightarrow Det N$

$VP \rightarrow V NP$

$Det \rightarrow \text{"the"}$

$N \rightarrow \text{"dog"}$

$V \rightarrow \text{"chased"}$

CNF Rules (already mostly in CNF):

$S \rightarrow NP VP$

$NP \rightarrow Det N$

$VP \rightarrow V NP$

$Det \rightarrow \text{"the"}$

$N \rightarrow \text{"dog"}$

$V \rightarrow \text{"chased"}$

- **Usage:** Required for the **CYK parsing algorithm**.

- **Benefit:** Ensures parsing can be done in **polynomial time**.
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## 2. Greibach Normal Form (GNF):

- Every production starts with a **terminal symbol**, optionally followed by **non-terminals**.
- **Form:**  $A \rightarrow aB$  (terminal first, then non-terminals)

**Example:**

$A \rightarrow aB$

$B \rightarrow bC$

- **Usage:** Useful for **top-down parsing** (predictive parsers).
  - **Benefit:** Simplifies **predictive parsing** by knowing the first terminal to expect.
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## Applications of Normal Forms in NLP:

1. **Parsing Algorithms:**
    - CNF is essential for **CYK parsing**, which systematically finds all possible parses.
  2. **Automated Grammar Checking:**
    - Standardized rules reduce ambiguity.
  3. **Computational Efficiency:**
    - Simplifies the implementation of syntactic parsers.
    - Reduces the variety of rule types the parser must handle.
  4. **Treebank Processing:**
    - Standardizes tree structures for machine learning models.
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## 5. Dependency Grammar (DG)

**Definition:**

Dependency Grammar analyzes syntactic structure based on **relationships between words** rather than phrase groupings.

**Key Concepts:**

- **Head and Dependent:** Every word (except root) depends on a head word.
- **Dependency Relation:** Grammatical relationship between head and dependent (e.g., nsubj, dobj, det)
- **Root of Sentence:** Main verb often serves as root.

#### Example:

Sentence: "The cat chased the mouse."

#### Word Head Relation

The cat det

cat chased nsubj

chased ROOT root

the mouse det

mouse chased dobj

#### Dependency Tree:

chased

/ \

cat mouse

/ \

The the

#### Advantages:

- Shows **direct relationships** between words.
- Flexible for **free word-order languages**.
- Useful for NLP tasks:
  - Information extraction
  - Machine translation
  - Semantic parsing