Attaque réseaux BHP

20 déc. 2017

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set.seed(11715490)

Pour lire fichiers en format .arff

```
## install.packages("foreign")
library(foreign)

setwd("C:/Users/ellie/Documents/R/OpticalBurstSwitching")
OBS <- read.arff("OBS-Network-DataSet_2_Aug27.arff")
head(OBS)</pre>
```

##		Node Ut	ilised	Bandwith	Rate	Packet	Drop	Rate	Full_E	Bandwi	dth	
##	1	3		0.8	22038		0.19	90381		1	.000	
##	2						0.72	0.729111 100				
##	3							0.090383 900				
##	4							0.637710 100				
##	5							800				
##	6	9 0.514687 0.494142 100										
##		Average_Delay_Time_Per_Sec Percentage_Of_Lost_Pcaket_Rate										
##								19.	.03148	37		
##	2	2 0.004815							72.	. 88903	36	
##	3	3 0.000633							9.	. 03583	34	
##	4	4 0.000552							63.	.73784	.3	
##							10.864208					
##	6			0.00						. 39213		
##		Percent	age_Of_	Lost_Byt	e_Rate	e Packe	et Rece	eived	Rate	of Us	ed_B	andwidth
##	1				038129				309619		8	22.03750
##	2				91114:			0.2	270889			27.55125
##	-				038339		0.909617 831.336					
##					770999		0.362290 36.8775					
##					86697		0.891330 724.1737					
##	6				41423				505858			51.46875
##				Packet		-	acket_	Transn		Packe	et_Re	
##			7.96250			1440			90324			73128
##			2.44875			1440			9048			2451
##			8.66400			1440	81276 73930				73930	
##			3.12250			1440			9048			3278
##	5	7	5.82625	, ,	:	1440			72228			64379

```
9048
## 6
           48.53125
                                1440
   Packet_lost Transmitted_Byte Received_Byte 10-Run-AVG-Drop-Rate
                                      105304320
           17196
                   130066560
                                                             0.146594
## 2
            6598
                         13029120
                                                             0.517669
                                        3529440
## 3
            7346
                        117037440
                                      106459200
                                                             0.058749
## 4
            5770
                         13029120
                                        4720320
                                                             0.522922
## 5
            7849
                        104008320
                                       92705760
                                                             0.076069
            4471
## 6
                         13029120
                                        6590880
                                                             0.405197
    10-Run-AVG-Bandwith-Use 10-Run-Delay Node Status Flood Status
## 1
                    0.780936
                                 0.001838
                                                   В
                                                          0.023455
## 2
                    0.242451
                                 0.002236
                                                   NB
                                                           0.460725
## 3
                    0.886758
                                 0.001751
                                                    В
                                                           0.000000
## 4
                    0.324522
                                 0.001776
                                                   NB
                                                           0.439255
## 5
                    0.869009
                                 0.001767
                                                          0.000000
                                                   В
## 6
                    0.442631
                                 0.002250
                                                   NB
                                                           0.291742
##
           Class
## 1 NB-No Block
## 2
           Block
## 3
       No Block
## 4
           Block
## 5
       No Block
## 6 NB-No Block
```

dim(OBS)

[1] 1075 22

summary(OBS) # On voit que la variable `Packet Size_Byte` est complètement inutile car elle ne change ja

```
Utilised Bandwith Rate Packet Drop Rate Full_Bandwidth
        Node
                                                        Min. : 100.0
##
  Min. :3.000 Min. :0.2356
                                   Min. :0.08613
   1st Qu.:3.000 1st Qu.:0.4469
                                       1st Qu.:0.24754
                                                        1st Qu.: 300.0
  Median :9.000
                Median :0.5772
                                       Median :0.43799
                                                        Median : 500.0
  Mean :6.014
                Mean :0.5979
                                       Mean :0.41136
                                                        Mean : 540.5
##
   3rd Qu.:9.000
                                                        3rd Qu.: 800.0
                  3rd Qu.:0.7645
                                       3rd Qu.:0.55658
## Max. :9.000
                        :0.9280
                                             :0.76794
                 Max.
                                       Max.
                                                        Max.
                                                             :1000.0
##
  Average_Delay_Time_Per_Sec Percentage_Of_Lost_Pcaket_Rate
                            Min. : 8.61
## Min.
         :0.0004060
  1st Qu.:0.0004510
                            1st Qu.:24.75
## Median :0.0006110
                            Median :43.80
                            Mean :41.16
## Mean :0.0009619
##
   3rd Qu.:0.0009530
                            3rd Qu.:56.67
##
  Max. :0.0052370
                            Max. :76.79
##
##
  Percentage_Of_Lost_Byte_Rate Packet Received Rate of Used_Bandwidth
  Min. : 8.613
                              Min. :0.2321
                                                  Min. : 27.55
##
  1st Qu.:24.754
                              1st Qu.:0.4333
                                                   1st Qu.:138.41
## Median:43.799
                              Median: 0.5620
                                                  Median: 291.59
## Mean :41.192
                              Mean :0.5881
                                                   Mean :340.78
##
   3rd Qu.:56.672
                              3rd Qu.:0.7525
                                                   3rd Qu.:515.18
## Max. :76.794
                              Max. :0.9139
                                                   Max.
                                                         :867.04
##
```

```
Lost Bandwidth
                     Packet Size_Byte Packet_Transmitted Packet_Received
##
   Min. : 34.16
                     Min.
                            :1440
                                      Min.
                                             : 9048
                                                                : 2451
                                                          Min.
                     1st Qu.:1440
   1st Qu.: 81.20
                                       1st Qu.:27092
                                                          1st Qu.:12491
  Median :159.51
                     Median:1440
                                                          Median :26847
##
                                      Median :45188
##
   Mean
          :199.68
                     Mean
                            :1440
                                      Mean
                                             :48826
                                                          Mean
                                                                 :30593
##
   3rd Qu.:279.27
                     3rd Qu.:1440
                                      3rd Qu.:72228
                                                          3rd Qu.:46588
   Max.
           :687.93
                     Max.
                            :1440
                                      Max.
                                             :90324
                                                          Max.
##
                                                                 :77131
##
##
    Packet lost
                    Transmitted Byte
                                         Received Byte
##
   Min. : 3913
                    Min. : 13029120
                                        Min.
                                               : 3529440
                    1st Qu.: 39012480
   1st Qu.: 7984
                                         1st Qu.: 17736480
                    Median : 65070720
                                         Median: 37357920
##
   Median :14944
   Mean
           :18590
                    Mean
                           : 70308837
                                         Mean
                                               : 49873429
                    3rd Qu.:104008320
##
   3rd Qu.:25962
                                         3rd Qu.: 67086720
##
  Max.
           :62415
                    Max.
                           :130066560
                                        Max.
                                                :980066560
##
   NA's
           :15
##
   10-Run-AVG-Drop-Rate 10-Run-AVG-Bandwith-Use 10-Run-Delay
           :0.05875
                         Min.
                                :0.2074
                                                  Min.
                                                         :0.0004050
   1st Qu.:0.18993
                         1st Qu.:0.3799
                                                  1st Qu.:0.0006560
##
##
   Median :0.30702
                         Median :0.5089
                                                  Median :0.0007650
##
   Mean
           :0.30760
                         Mean
                                :0.5532
                                                  Mean
                                                         :0.0009336
   3rd Qu.:0.40600
                         3rd Qu.:0.7341
                                                  3rd Qu.:0.0009840
##
   Max.
           :0.63371
                         Max.
                                :0.8909
                                                  Max.
                                                         :0.0049040
##
   Node Status Flood Status
##
                                           Class
        :475
                Min.
                       :0.00000
                                  Block
                                              :120
##
   NB :285
                1st Qu.:0.02305
                                  NB-No Block:500
   P NB:315
                Median :0.07933
##
                                  NB-Wait
                                              :300
                                              :155
##
                Mean
                       :0.13194
                                  No Block
##
                3rd Qu.:0.23054
##
                Max.
                       :0.56674
##
```

OBS <- OBS[names(OBS) != "Packet Size_Byte"] names(OBS)</pre>

```
[1] "Node"
                                          "Utilised Bandwith Rate"
##
##
    [3] "Packet Drop Rate"
                                          "Full_Bandwidth"
##
       "Average_Delay_Time_Per_Sec"
                                          "Percentage_Of_Lost_Pcaket_Rate"
       "Percentage_Of_Lost_Byte_Rate"
                                          "Packet Received Rate"
   [9] "of Used Bandwidth"
##
                                          "Lost Bandwidth"
## [11] "Packet_Transmitted"
                                          "Packet Received"
## [13] "Packet_lost"
                                          "Transmitted_Byte"
## [15] "Received_Byte"
                                          "10-Run-AVG-Drop-Rate"
## [17] "10-Run-AVG-Bandwith-Use"
                                          "10-Run-Delay"
## [19] "Node Status"
                                          "Flood Status"
## [21] "Class"
```

names(OBS) <- make.names(names(OBS), unique = TRUE)</pre>

Traitement des valeurs manquantes

```
valMan <- which(is.na(OBS), arr.ind = TRUE, useNames = TRUE)
dim(valMan) # Only 15 * 2 so we don't have to draw it.</pre>
```

[1] 15 2

```
library(mice)
mdp <- md.pattern(OBS)
mdp</pre>
```

```
Node Utilised.Bandwith.Rate Packet.Drop.Rate Full_Bandwidth
## 1060
##
    15
          1
                                                  1
##
##
       Average_Delay_Time_Per_Sec Percentage_Of_Lost_Pcaket_Rate
## 1060
##
    15
                                                               1
##
       Percentage_Of_Lost_Byte_Rate Packet.Received..Rate of.Used_Bandwidth
##
## 1060
##
    15
                                                                          1
##
##
       Lost_Bandwidth Packet_Transmitted Packet_Received Transmitted_Byte
## 1060
##
##
                    0
##
       Received_Byte X10.Run.AVG.Drop.Rate X10.Run.AVG.Bandwith.Use
                   1
## 1060
##
    15
##
       X10.Run.Delay Node.Status Flood.Status Class Packet_lost
## 1060
                   1
                               1
                                            1 1 1 0
##
    15
                   1
                                                              0 1
##
                   0
                                            0
                                                             15 15
```

```
library(ipred)
# preproc <- preProcess(OBS, method = "bagImpute")

# mice(OBS, m=5, maxit=50, meth='pmm', seed=500)

# OBScomplet <- mice(OBS)

# aggr(mdp, prop = FALSE, numbers = TRUE)

# install.packages("DMwR")
library(DMwR)</pre>
```

```
## Warning: package 'DMwR' was built under R version 3.4.3
## Loading required package: lattice
## Loading required package: grid
```

OBScomplet <- knnImputation(OBS[! names(OBS) %in% c("Node.Status", "Class")]) OBScomplet[valMan]

```
## [1] 20480.07 12191.96 11870.21 20480.07 12191.96 11870.21 20480.07
## [8] 12191.96 11870.21 20480.07 12191.96 11870.21 20480.07 12191.96
## [15] 11870.21
```

head(OBScomplet)

##	Node Utilise	ed.Bandwith.Ra	ate Packet.Dro	p.Rate Full	_Bandwidth			
## 1	. 3	0.8220	0.038	. 190381 1000				
## 2	9	0.275	513 0.	.729111 100				
## 3	3	0.9237	707 0.	0.090383 900				
## 4	. 9	0.3687	775 0.	0.637710 100				
## 5	3	0.9052	217 0.	0.108670 800				
## 6				100				
##	Average_Dela	ay_Time_Per_Se	ec Percentage_	ge_Of_Lost_Pcaket_Rate				
## 1				19.031487				
## 2				72.889036				
## 3				9.035834				
## 4	0.000552			6	3.737843			
## 5	0.000497			1	0.864208			
## 6	6 0.003098				9.392131			
##	Percentage_0	Of_Lost_Byte_H	Rate Packet.Re		e of.Used_Bandwidth			
## 1		19.038	8129	0.80961	9 822.03750			
## 2		72.91	1141	0.27088	9 27.55125			
## 3	1	9.038	8339	0.90961	7 831.33600			
## 4	:	63.770	0999	0.36229	0 36.87750			
## 5	5 10.866977			0.89133	0 724.17375			
## 6	6 49.414235			0.505858 51.46875				
##	_	_	ansmitted Pack	_	-			
## 1	177.962	250	90324	73128	17196			
## 1 ## 2	177.962 72.448	250 375	90324 9048	73128 2451	17196 6598			
## 1 ## 2 ## 3	177.962 72.448 68.664	250 375 400	90324 9048 81276	73128 2451 73930	17196 6598 7346			
## 1 ## 2 ## 3 ## 4	177.962 72.448 68.664 63.122	250 375 400 250	90324 9048 81276 9048	73128 2451 73930 3278	17196 6598 7346 5770			
## 1 ## 2 ## 3 ## 4 ## 5	177.962 72.448 68.664 63.122 75.826	250 375 400 250 325	90324 9048 81276 9048 72228	73128 2451 73930 3278 64379	17196 6598 7346 5770 7849			
## 1 ## 2 ## 3 ## 4	177.962 72.448 68.664 63.122 75.826 48.533	250 375 400 250 325 125	90324 9048 81276 9048 72228 9048	73128 2451 73930 3278 64379 4577	17196 6598 7346 5770 7849 4471			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted	250 375 400 250 325 125 _Byte Received	90324 9048 81276 9048 72228 9048 d_Byte X10.Rur	73128 2451 73930 3278 64379 4577 1. AVG. Drop. R	17196 6598 7346 5770 7849 4471			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted	250 375 400 250 325 125 Byte Received	90324 9048 81276 9048 72228 9048 d_Byte X10.Run	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146	17196 6598 7346 5770 7849 4471 ate			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 1	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006	250 375 400 250 525 125 _Byte Received 56560 1053	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517	17196 6598 7346 5770 7849 4471 ate 594			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302	250 375 400 250 525 125 _Byte Received 56560 1053 29120 38 37440 1064	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200	73128 2451 73930 3278 64379 4577 1. AVG. Drop. R 0.146 0.517 0.058	17196 6598 7346 5770 7849 4471 ate 594 669			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3 ## 4	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47	90324 9048 81276 9048 72228 9048 d_Byte X10.Rur 304320 529440 459200 720320	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522	17196 6598 7346 5770 7849 4471 ate 594 669 749			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3 ## 4 ## 5	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47 28320 927	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076	17196 6598 7346 5770 7849 4471 ate 594 669 749 922			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3 ## 4 ## 5	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10400 1302	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47 29120 927 29120 68	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3 ## 4 ## 5 ## 6	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 10400 1302 X10.Run.AVG	250 375 400 250 525 125 Byte Received 66560 1053 29120 39 37440 1064 29120 47 08320 927 08320 927 08320 68	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069			
## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1 ## 2 ## 3 ## 4 ## 5 ## 6 ## 1	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10400 1302 X10.Run.AVG	250 375 400 250 325 125 _Byte Received 36560 1053 29120 39 29120 47 29120 47 29120 69 29120 69 29120 69 29120 69 29120 69 29120 69 29120 69	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay 0.001838	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405 7 Flood.Stat	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069 197			
## 1 ## 2 ## 3 ## 4 ## 5 ## 1 ## 2 ## 3 ## 4 ## 5 ## 1 ## 2	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10400 1302 X10.Run.AVG	250 375 400 250 525 125 Byte Received 56560 1053 29120 38 37440 1064 29120 47 29120 47 29120 68 29120 68 29120 68 29120 68 29120 68 29120 68 29120 68 29120 68 29120 68	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay 0.001838 0.002236	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405 7.Flood.Stat 8.0.0234 6.0.4607	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069 197 us 55			
## 1	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10400 1302 X10.Run.AVG	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47 08320 927 29120 68 .Bandwith.Use 0.780936 0.242451 0.886758	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay 0.001838 0.002236 0.001751	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405 7.Flood.Stat 8.0.0234 6.0.4607 0.0000	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069 197 us 55 25			
## 1 2 ## 3 4 ## 5 6 ## 1 2 2 ## 4 4 ## 4 5 6 ## 4 4 ## 4 ## 4 4 ##	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10406 1302 X10.Run.AVG	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47 08320 927 29120 68 0.780936 0.242451 0.886758 0.324522	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay 0.001838 0.002236 0.001751 0.001776	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405 7 Flood.Stat 8 0.0234 6 0.4607 0.0000 6 0.4392	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069 197 us 55 25			
## 1	177.962 72.448 68.664 63.122 75.826 48.533 Transmitted 13006 1302 11703 1302 10400 1302 X10.Run.AVG	250 375 400 250 325 125 Byte Received 36560 1053 29120 38 37440 1064 29120 47 08320 927 29120 68 .Bandwith.Use 0.780936 0.242451 0.886758	90324 9048 81276 9048 72228 9048 d_Byte X10.Run 304320 529440 459200 720320 705760 590880 X10.Run.Delay 0.001838 0.002236 0.001751	73128 2451 73930 3278 64379 4577 1.AVG.Drop.R 0.146 0.517 0.058 0.522 0.076 0.405 7.Flood.Stat 3.0.234 0.0000 0.4392 0.0000	17196 6598 7346 5770 7849 4471 ate 594 669 749 922 069 197 us 55 25 00 55			

```
# install.packages("Amelia")
# library(Amelia)
# missmap(OBS)
```

Méthode ACP

library(plotly)

Loading required package: ggplot2

```
## Attaching package: 'plotly'
   The following object is masked from 'package:ggplot2':
##
##
##
       last_plot
## The following object is masked from 'package:stats':
##
##
       filter
##
   The following object is masked from 'package:graphics':
##
##
       layout
corOBS <- cor(OBScomplet[! names(OBScomplet) %in% c("Node.Status", "Class")])</pre>
corHmp <- plot_ly(x = names(OBScomplet[! names(OBScomplet) %in% c("Node.Status", "Class")]</pre>
                   y = names(OBScomplet[! names(OBScomplet) %in% c("Node.Status", "Class")]
corHmp
```

In the correlation heatmap we can repeatly spot extremely high pairwise correlation close or even equal to 1 or -1. Highly to perfectly correlated variables could bias the PCA result in a way that PCA will overemphasize the common contribution of the (nearly) redundant variables. Therefore, it might make sense to find out and remove such variables before doing a PCA, Especially when they describe actually (nearly) the same aspect of an issue. For instance, Tansmitted_Byte and Packet_Transmitted have a correlation of 1, because they reflect the same quantity up to a ratio Packet Size_Byte, which, as being mentioned here above, never changes. Thus, we will remove one of both. Which one to remove is of our free choice. Here, we consider that quantitative variables in packets may be more reader friendly than those in bytes in terms of unit, so that we keep the variable Packet_Transmitted and drop the other one. But what about the high correlation between other variables (e.g. higher than 97%)? Shall we remove the nearly redundant variables too before doing our PCA? The statistical community doesn't have a straightforward anwer to it. As a matter of fact, it hugely depends on the nature of data and the purpose to do the PCA. On one hand, like we said, highly correlated variables would be possible to strongly influence the result of the PCA and, as a result, the real contributions to the principal components of the underlying variables that are truly meaningful. If our PCA is meant to give such information, then high correlation should better be avoided prior to the PCA. On the other hand, however, a PCA with redundant variables can still faithfully reveal the high correlation between them, though principal components would be probably established otherwise. In that sense, if it is an exploratory PCA that we are doing, which only aims to find a broad outline of the relationships between variables disregarding how principal components are built, then including some redundant ones may be fine. In the light of this, we decide to go an onerous but careful way, in which we do firstly a PCA with almost all the variables. With both the correlation circle of PCA and the correlation heatmap, we then kick out the

redundant variables and do a second PCA with only variables that we consider to be meaningful. Further analysis (variable and individual relationship, quantitative and qualitative variable relationship) shall also be based on the latter PCA. In a rough and rapid preprocessing procedure, we could limit our focus on high pairwise correlations (the reader should know that in a more rigorous treatment, high correlations within a multuple tuple of variables should also be considered) and refer to the heatmap of variable correlations. We may set a threshold, e.g. 0.97, and find out all couples whose absolute value of correlation exceeds this threshold, before we remove one of both variables by verifying that they are indeed telling (nearly) the same story.

library("factoextra")

```
pcaOBS <- prcomp(OBScomplet[! names(OBScomplet) %in% c("Node.Status", "Class")], scale. = TRUE, rank.
# fviz_eig(pcaOBS)
summary(pcaOBS)$importance[3, c(1, 2)]
##
       PC1
               PC2
## 0.52732 0.79172
fviz_pca_var(pcaOBS, col.var = "contrib", gradient.cols = c("#0OAFBB",
                                                                        "#E7B800",
                                                                                   "#FC4E07
## Warning in var.loadings * comp.sdev:
```

```
## Warning in var.loadings * comp.sdev:
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-1.pdf
## We see that in the correlation circle there are four subgroups of very closely situated variables wh
## redundant variables (visibly there are five, but the one at the very left is highly negatively corre
## very right). For example, Tansmitted_Byte`, `Packet_Transmitted` and `Full_Bandwidth` are even perfe
## which can be also confirmed by the previous correlation heatmap. No doubt those subgroups consist of
## variables, because they are redundant! We now decide to remove extremely high correlation among vari
## 97) for our next PCA so that only
## one variable of each of the four subgroups should stay in the game. Another reason for doing this, i
## of field knowledge, is that all the variables
## within the same subgroup mean in fact the same thing just in some different way. At the end, we choo
## `Packet.Received..Rate`, `Packet_Received`, `Packet_Transmitted` and `Packet_Lost` as representative
## other well defined variables. In the more balanced coming PCA with uniquely the non redundant variab
## a change in variance contributions.
pca0BS2 <- prcomp(OBScomplet[c("Packet.Received..Rate", "Packet_Received", "Packet_Transmitted", "Packet_
                             "Average_Delay_Time_Per_Sec", "X10.Run.Delay", "Node", "Received_Byte", "F
summary(pcaOBS2)$importance[3, c(1, 2, 3)]
##
       PC1
               PC2
                       PC3
## 0.36840 0.61203 0.75056
fviz_eig(pcaOBS, ncp = 3, addlabels = TRUE, ylim = c(0, 60))
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-2.pdf
fviz_pca_var(pcaOBS2, col.var = "contrib", gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel =
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-3.pdf
## Following information can be extracted from the correlation circle of PCA above:
     `Flood.Status`, `Packet_lost`, `Packet_Transmitted`, `Packet_Received` and `Packet.Received..Rate`
## represented or in other words most contributing variables to the first both principal dimensions.
##
       `Packet_Received` has no contribution to the first dimension while `Node` has no contribution to
##
      `Received_Byte` has little contribution to the first dimension while `Packe_lost` has litte contr
```

`Packet.Received..Rate` and `Flood.Status` are highly negatively correlated.

`X10.Run.Delay` and Àverage_Delay_Time_Per_Sec` seem to be correlated in the projected dataset on

```
## To extract all information about the variables, we can do
variables <- get_pca_var(pcaOBS2)</pre>
## What are the coordinates of the variables selected?
# dim(variables$coord) # 9, 9
# head(variables$coord)
variables$coord[, 1:3]
##
                                   Dim.1
                                               Dim.2
                                                          Dim.3
## Packet.Received..Rate
                            -0.7598709053 0.600722370 -0.1033570
## Packet Received
                            -0.9172582980 0.001244397 0.2268809
-0.1315211178 -0.886093952 0.3516166
## Packet_lost
## Average_Delay_Time_Per_Sec   0.5366453995   0.398986327   0.6148888
## X10.Run.Delay
                           0.3971744367 0.532528682 0.5054290
## Node
                            0.0003522424 0.248589468 0.4157637
## Received_Byte
                            -0.5772036435 0.030542401 0.3098019
## Flood.Status
                             0.6851099789 -0.596702315 0.1637975
## What is the quality of representation of the variables by the first two components?
variables$cos2[, 1:2]
##
                                  Dim.1
                                               Dim 2
## Packet.Received..Rate 5.774038e-01 3.608674e-01
## Packet Received
                            8.413628e-01 1.548523e-06
## Packet_Transmitted
                          6.312218e-01 1.850813e-01
## Packet_lost
                            1.729780e-02 7.851625e-01
## Average_Delay_Time_Per_Sec 2.879883e-01 1.591901e-01
## X10.Run.Delay
                          1.577475e-01 2.835868e-01
                            1.240747e-07 6.179672e-02
## Node
## Received_Byte
                            3.331640e-01 9.328383e-04
## Flood.Status
                            4.693757e-01 3.560537e-01
library("corrplot")
## Warning: package 'corrplot' was built under R version 3.4.3
## corrplot 0.84 loaded
corrplot(variables$cos2[, 1:2], is.corr=FALSE)
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-4.pdf
## Total representation quality on dimension 1 and 2
fviz_cos2(pca0BS2, choice = "var", axes = 1:2)
```

```
OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-5.pdf
## How the the contribution of the variables to the first two components?
variables$contrib[, 1:2]
##
                                       Dim.1
                                                     Dim.2
## Packet.Received..Rate 1.741496e+01 1.645788e+01
## Packet_Received 2.537618e+01 7.062263e-05

## Packet_Transmitted 1.903815e+01 8.440901e+00

## Packet lost 5.217156e-01 3.580847e+01
## Average_Delay_Time_Per_Sec 8.685957e+00 7.260093e+00
## X10.Run.Delay
                               4.757792e+00 1.293338e+01
## Node
                               3.742192e-06 2.818328e+00
## Received_Byte
                               1.004849e+01 4.254343e-02
## Flood.Status
                                1.415675e+01 1.623834e+01
corrplot(variables$contrib[, 1:2], is.corr=FALSE)
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-6.pdf
## Contribution of variables to PC1
fviz_contrib(pcaOBS2, choice = "var", axes = 1)
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-7.pdf
## Contribution of variables to PC2
fviz_contrib(pcaOBS2, choice = "var", axes = 2)
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-8.pdf
### Now we would like to plot some individuals. We can see that here, using redundant variables in the
```

10

Firstly a graph of 20 randomly selected individuals drawn in the PCA with redundant variables, colou

lead to a considerable difference.

representation

```
fviz_pca_ind(pcaOBS, col.ind = "cos2", gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRUE
             select.ind = list(name = sample.int(n = nrow(OBS), size = 20)))
 OpticalBurstSwitching files/figure-latex/unnamed-chunk-5-9.pdf
## Their quality of representation is always the best, equal to 1! This is due to the fact that the fir
## consist of a huge amount of redundant information, so that an individual can be easily well represen
## only these variables of him.
## Then we show a graph of 20 randomly selected individuals drawn in the PCA _without_ redundant variab
## representation
fviz_pca_ind(pca0BS2, col.ind = "cos2", gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRU
            select.ind = list(name = sample.int(n = nrow(OBS), size = 20)))
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-10.pdf
## All kinds of quality can be observed this time, which is more meaningful than in the previous case.
## we are going to keep using in the rest of our analysis.
fviz_pca_ind(pca0BS2, col.ind = "cos2", gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"), repel = TRU
             select.ind = list(name = sample.int(n = nrow(OBS), size = 20)))
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-11.pdf
## We now try to involve the categorical information: `Node.Status` and `Class`.
## Firstly a graph of some randomly selected individuals coloured by subgroups of `Node.Status`
fviz_pca_ind(pcaOBS2, geom = "point", habillage = OBS$Node.Status, palette = "jco",
             addEllipses = FALSE, legend.title = "Node Status")
 OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-12.pdf
## Then a graph of randomly selected individuals coloured by subgroups of `Node.Status`
fviz_pca_ind(pcaOBS2, geom = "point", habillage = OBS$Class, palette = "RdBu",
            select.ind = list(name = 1:1075), legend.title = "Class")
```

OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-13.pdf

Now we draw some biplots with randomly selected individuals and variables library(gridExtra)

Warning: package 'gridExtra' was built under R version 3.4.3

plot1 <- fviz pca biplot(pcaQBS2.

OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-14.pdf

OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-15.pdf

cumsum(famdOBS\$eig[, 2])

[1] 32.76325 51.12368 62.28384 71.62478 78.49738

plot(famdOBS, choix = "var")

OpticalBurstSwitching_files/figure-latex/unnamed-chunk-5-16.pdf