



# Cornell Bowers CIS

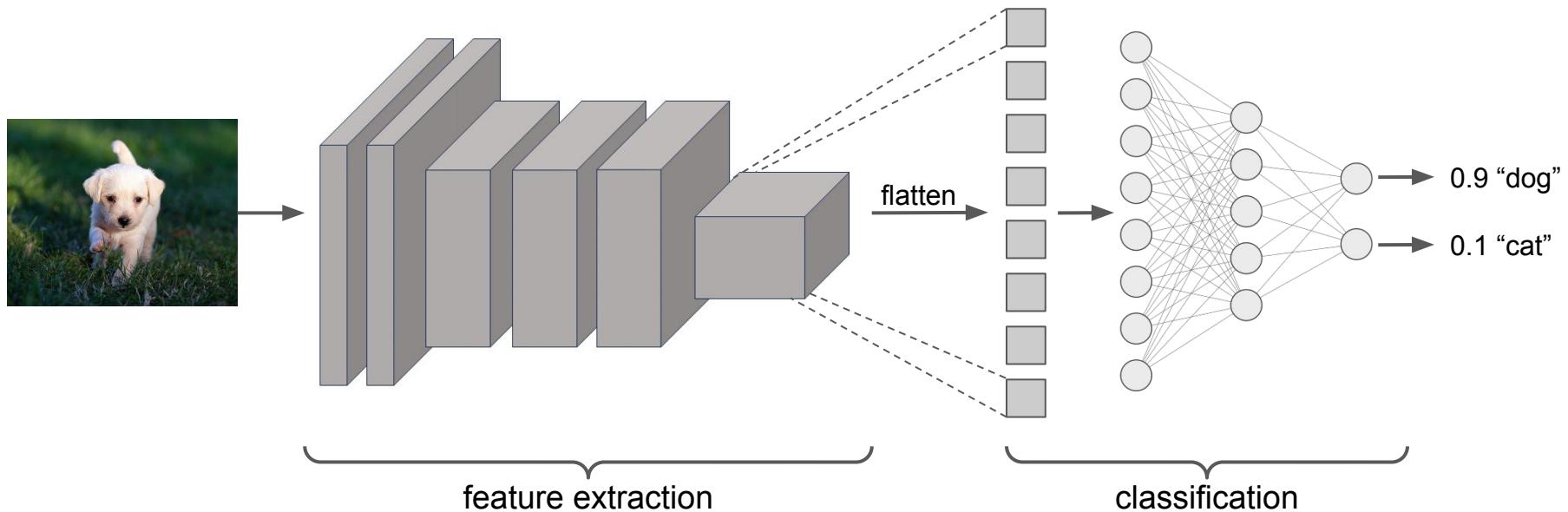
## College of Computing and Information Science

# Modern Convolutional Neural Networks 2

CS4782: Intro to Deep Learning

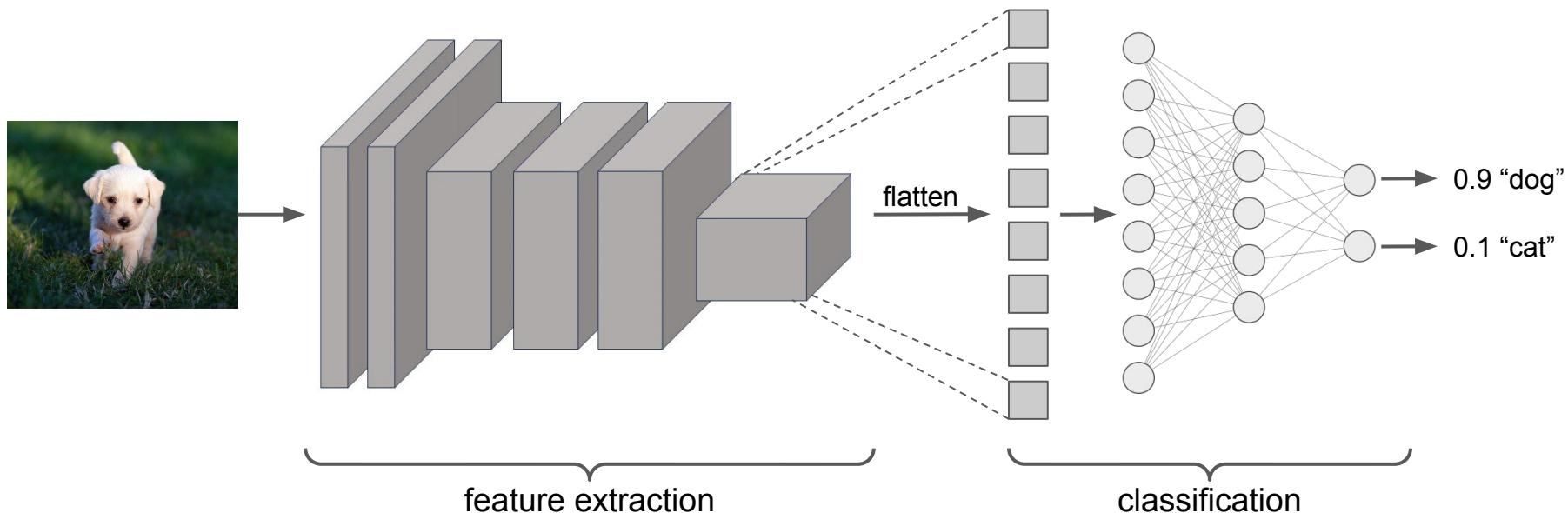
Varsha Kishore, Justin Lovelace, Anissa Dallmann, Stephanie Ginting

# Review: Image Classification

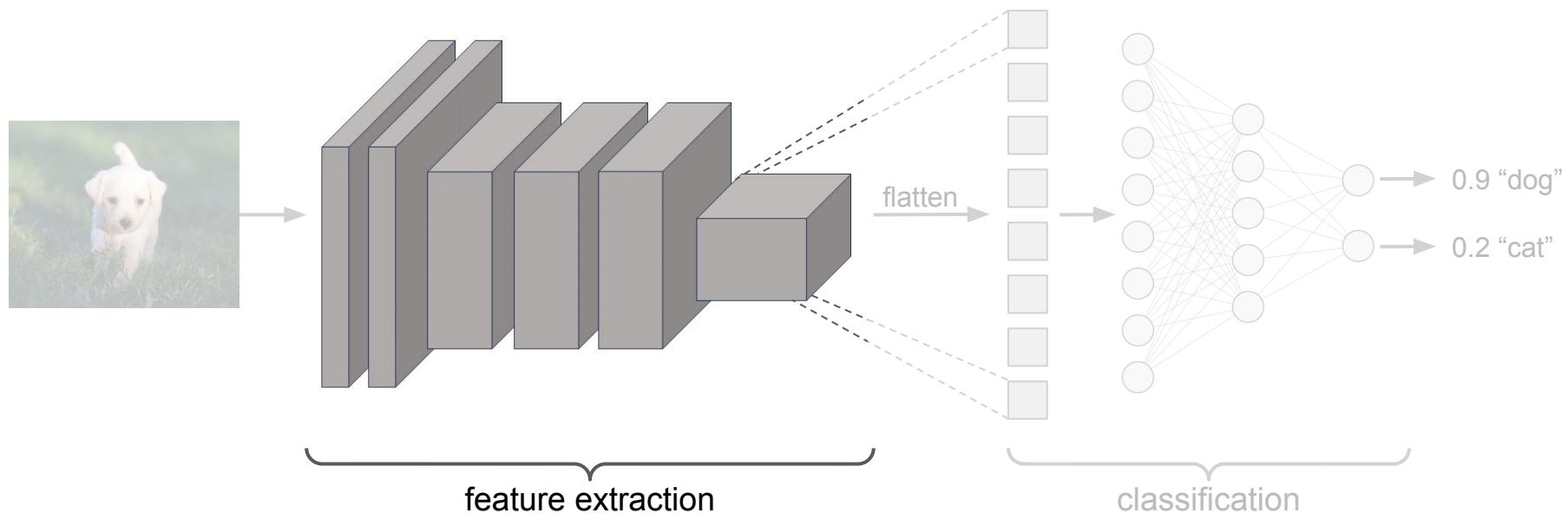


# Image Classification

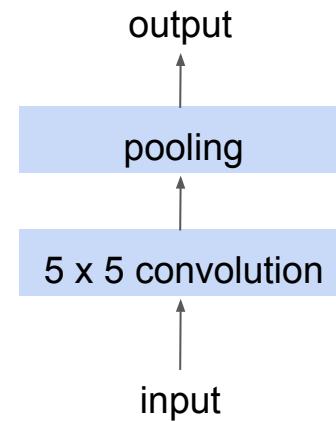
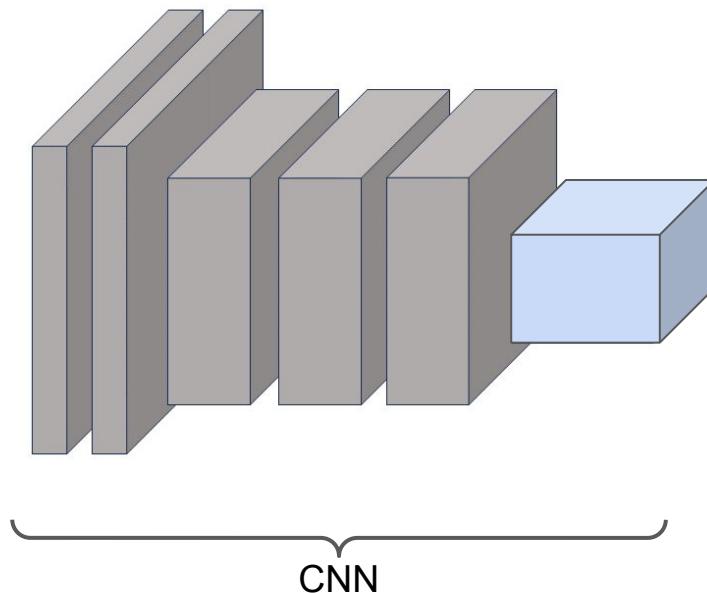
- Important: Everything is differentiable!
- Can calculate gradient of the loss with backpropagation
  - Train with SGD/Adam/etc.
  - Learn convolutional filters and classification head end-to-end!



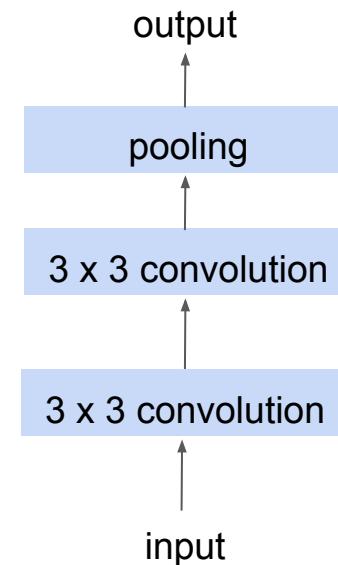
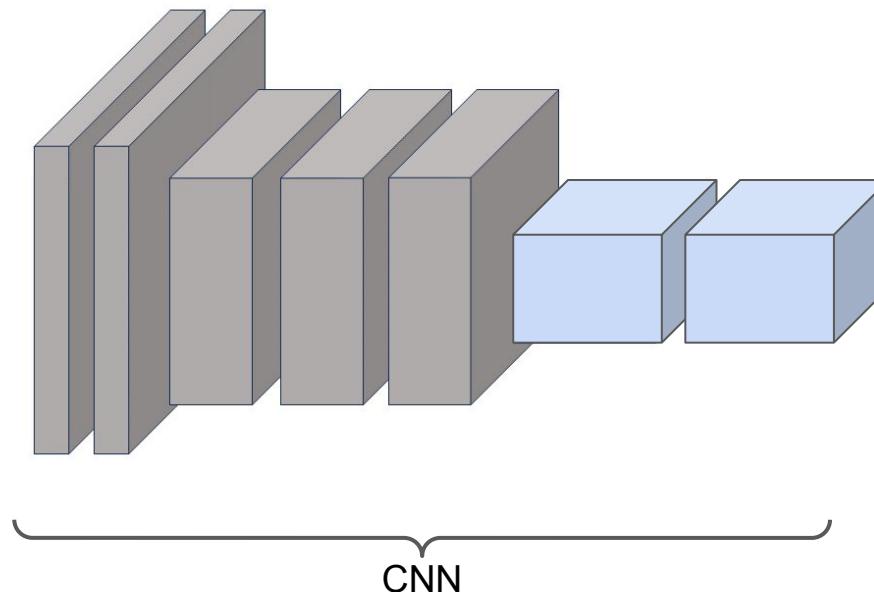
# Deeper CNN Architectures



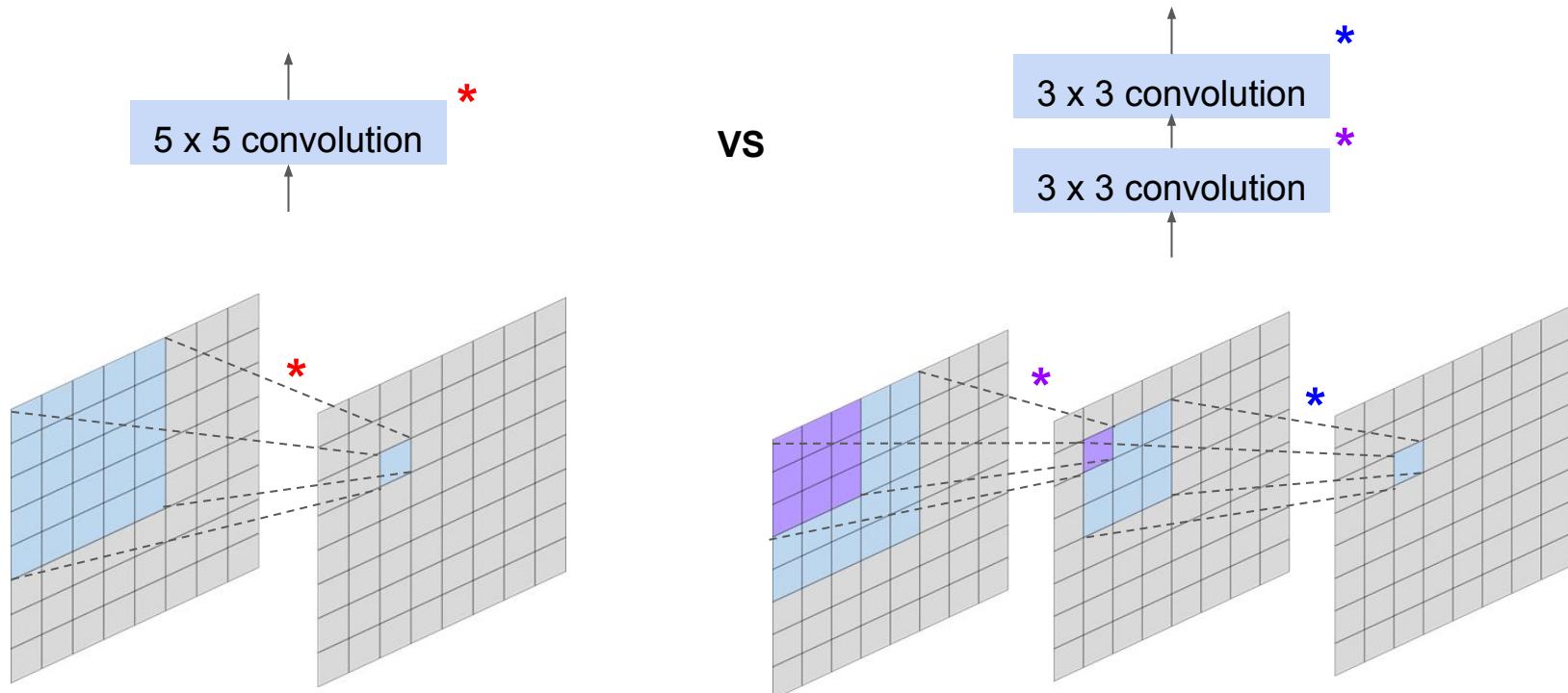
# Deeper CNN Architectures



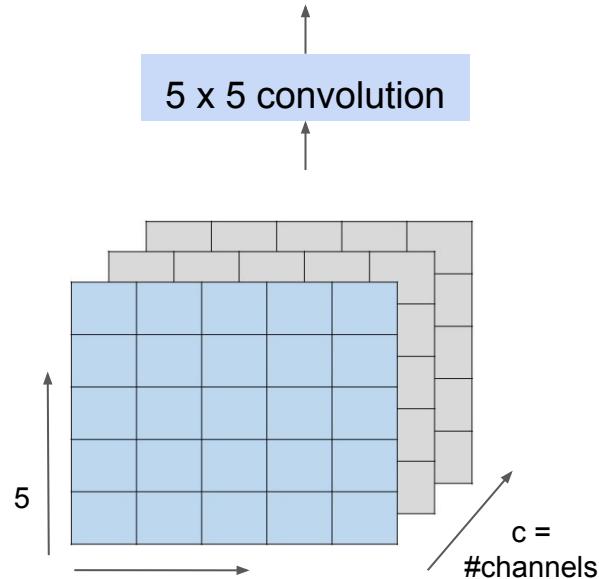
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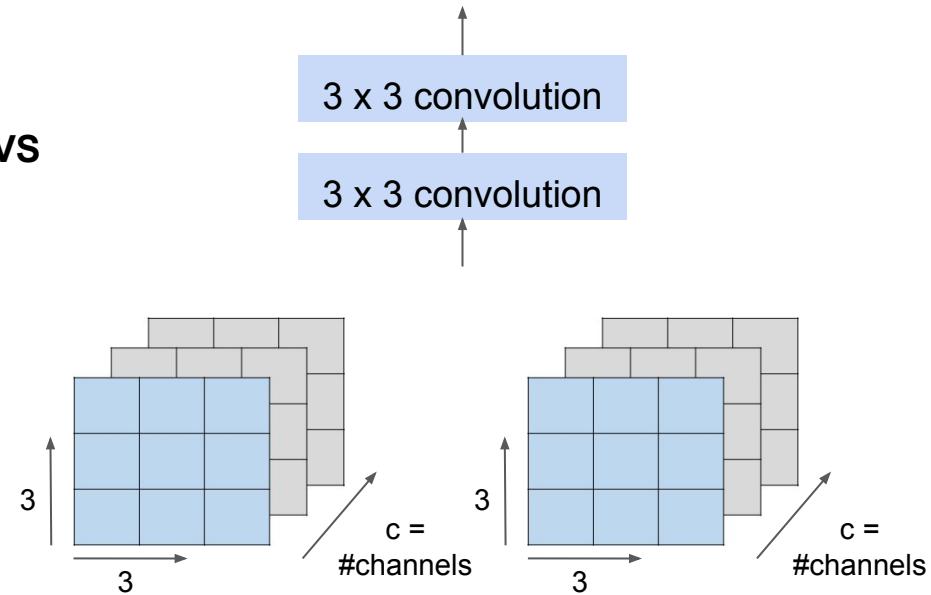


# Deeper CNN Architectures



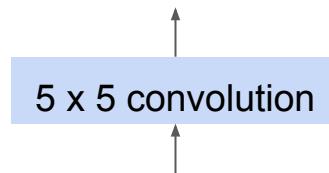
$$5 * 5 * c^2  
= 25c^2 \text{ parameters}$$

vs

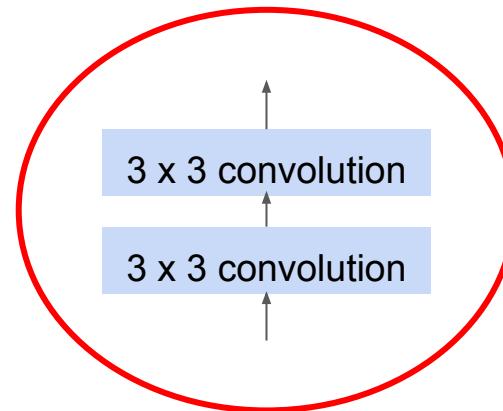


$$2 * 3 * 3 * c^2  
= 18c^2 \text{ parameters}$$

# Deeper CNN Architectures

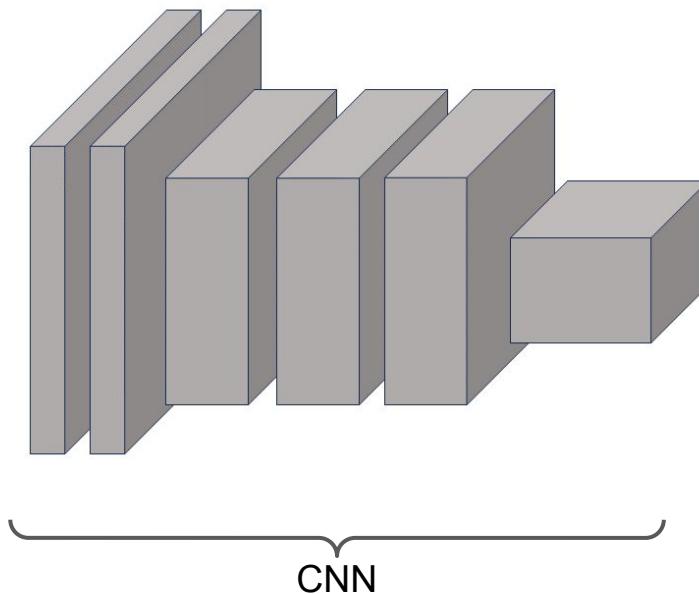


vs

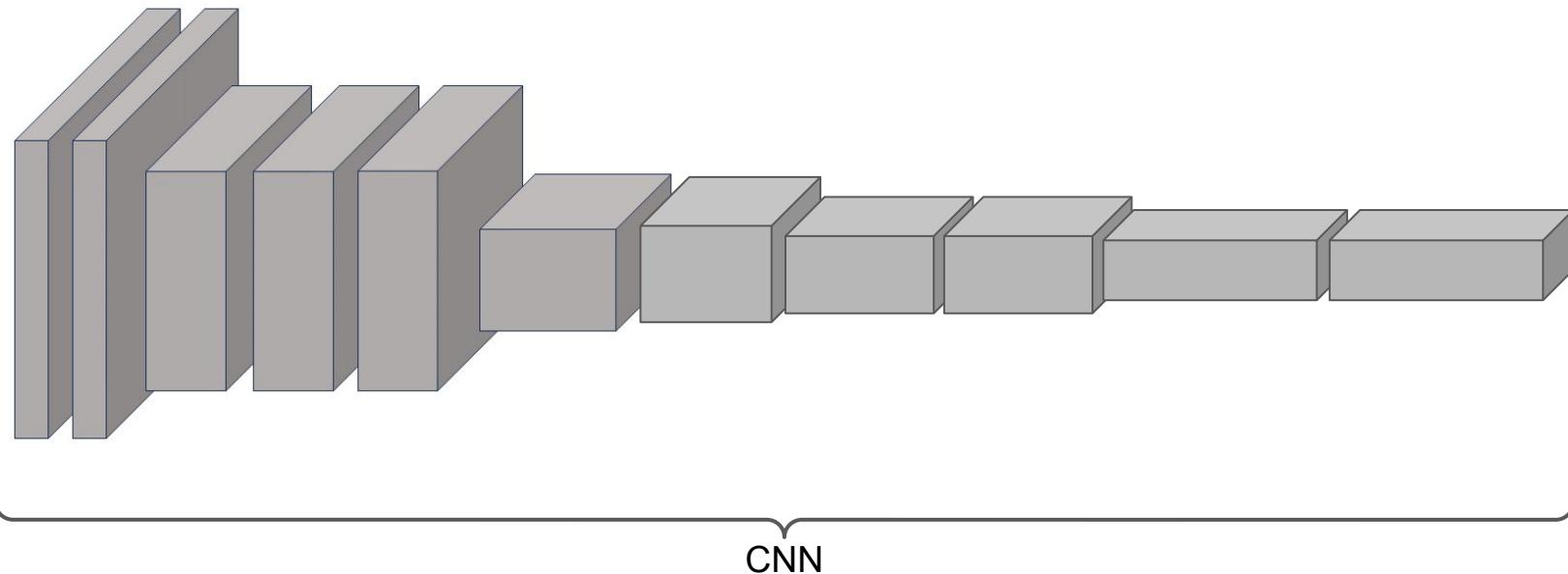


**Performed better!**

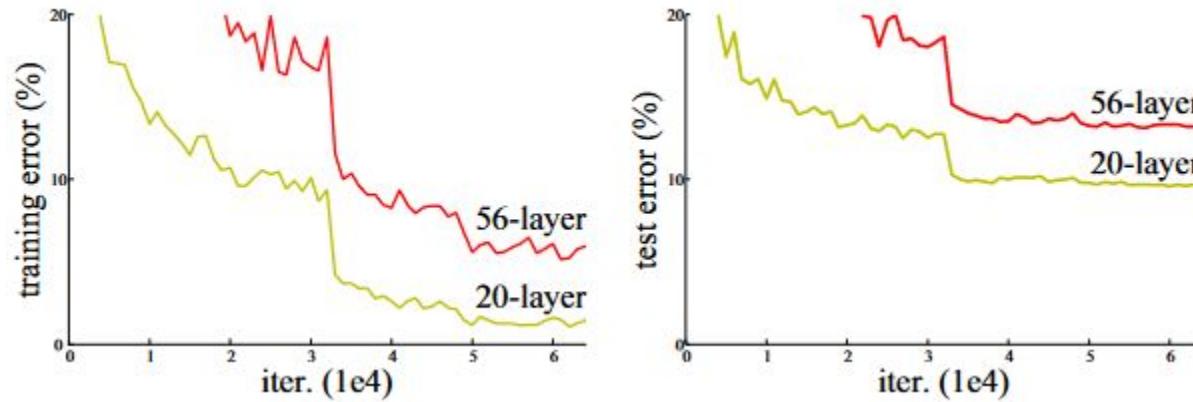
Deeper == better



Deeper == better



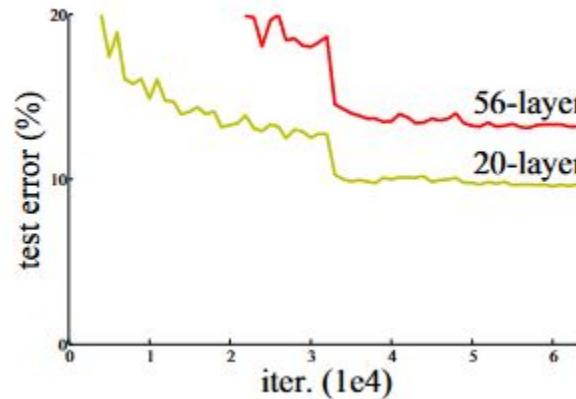
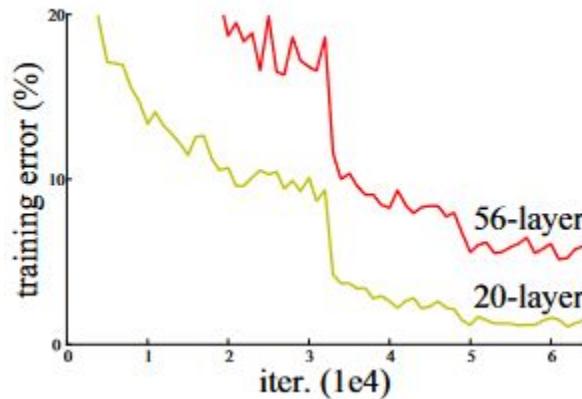
# Deeper == better?



56 layer CNN has higher training and test error than 20 layer CNN  
on CIFAR-10 dataset for image classification

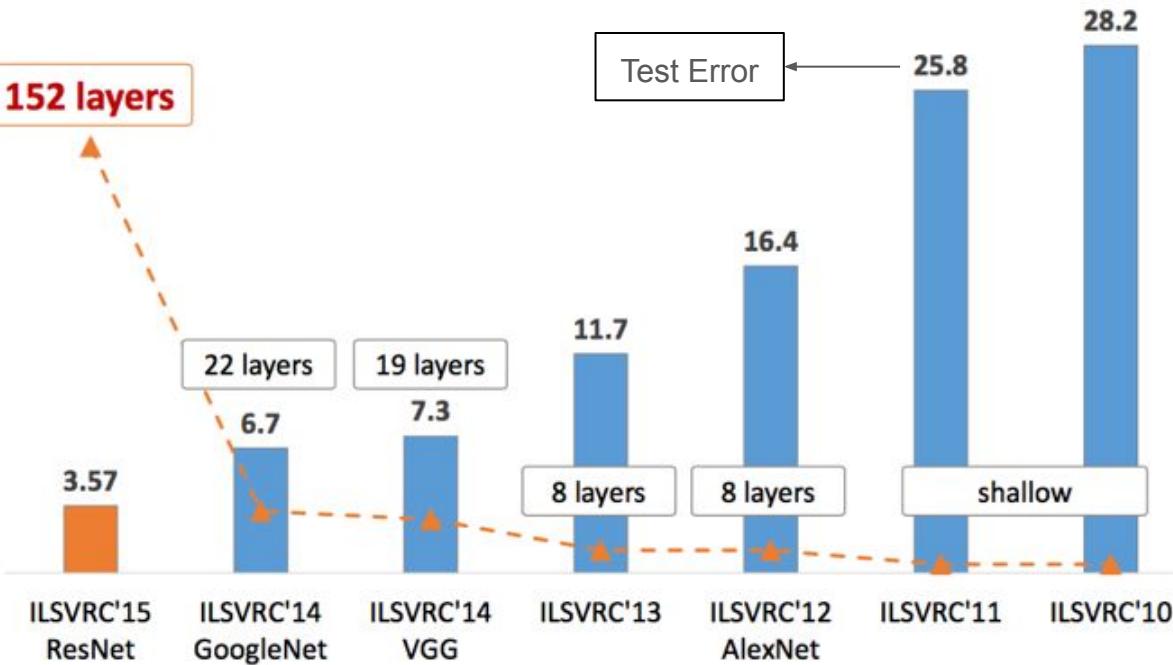
[He, Kaiming, et al. "Deep residual learning for image recognition." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016.]

Discuss: How can a larger network achieve a higher training error?



56 layer CNN has higher training and test error than 20 layer CNN  
on CIFAR-10 dataset for image classification

# ImageNet Classification Challenge: Deeper == better



[Nguyen, Kien & Fookes, Clinton & Ross, Arun & Sridharan, Sridha. (2017). Iris Recognition with Off-the-Shelf CNN Features: A Deep Learning Perspective. IEEE Access. PP. 1-1. 10.1109/ACCESS.2017.2784352. ]

# GoogLeNet/Inception Net

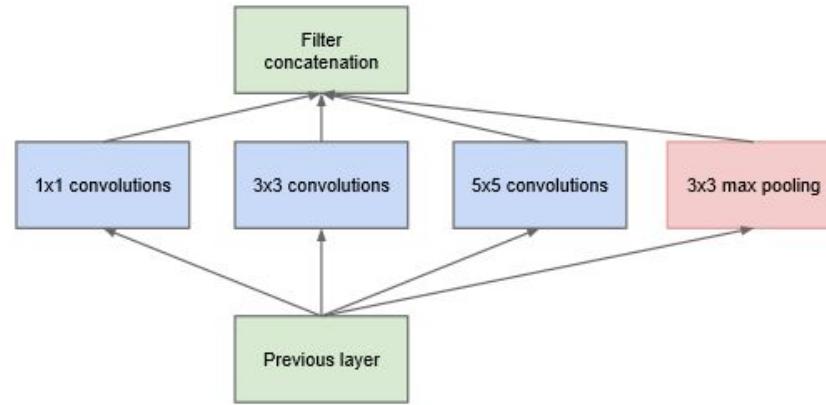
Goal: given a fixed computational budget, build a deeper network

=> Deeper networks with computational budget



In this paper, we will focus on an efficient deep neural network architecture for computer vision, codenamed Inception, which derives its name from the Network in network paper by Lin et al [12] in conjunction with the famous “we need to go deeper” internet meme [1]. In our case, the word

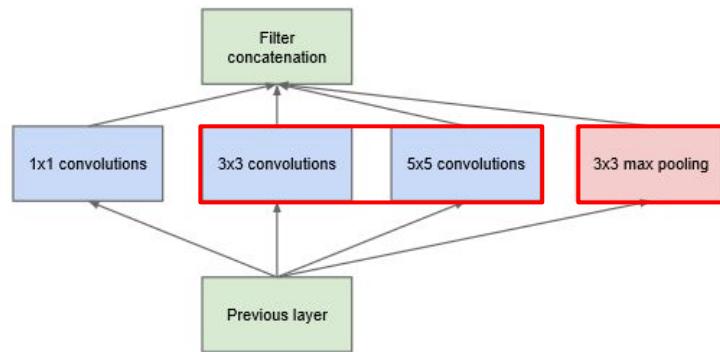
# Inception Module



Inception module = main  
building blocks

# Inception Module

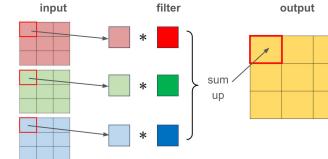
Still expensive!



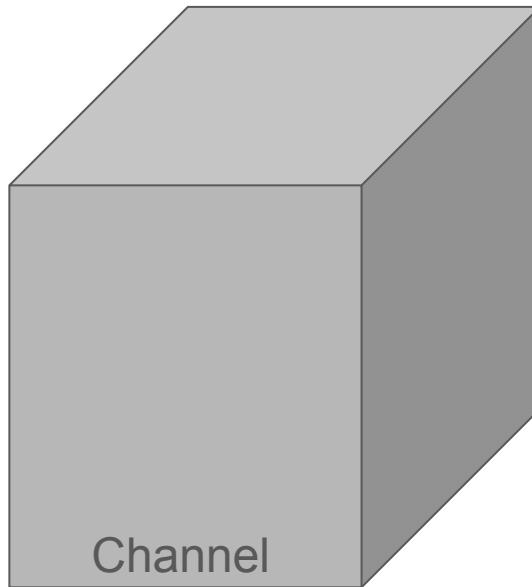
- 3x3 and 5x5 convolutions have large number of operations
- Output of pooling layer increases the output channel dimension when concatenated

# Remember: 1x1 convolutions

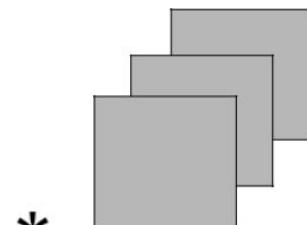
Cornell Bowers CIS  
Slight Detour: 1x1 convolutions



input

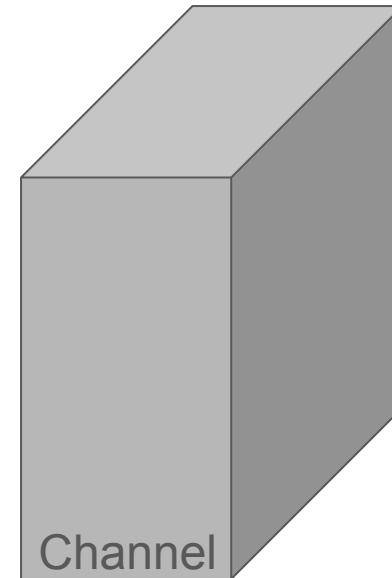


filters



\* 32 filters

output



56x56x64

56x56x32

## Discuss: Impact of Dimension Reduction

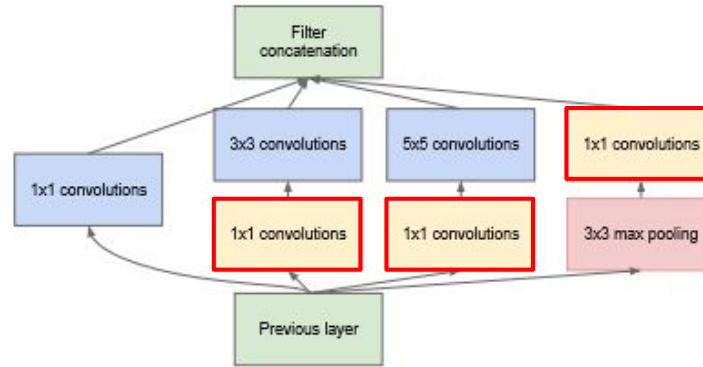
Assume you have an input feature map with 256 channels/features.

Compare the parameter counts from:

1. 3x3 conv with 256 filters
  
2. 1x1 conv with 64 filters → 3x3 conv with 64 filters → 1x1 conv with 256 filters

# Inception Module

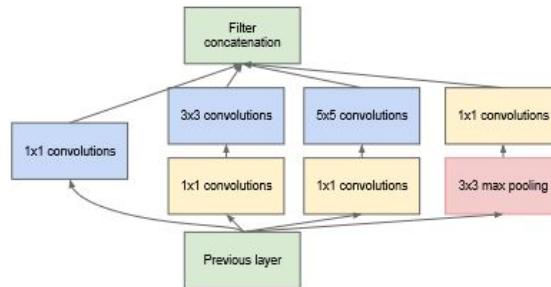
Solution: Inception module with dimension reduction



- “Bottleneck” with  $1 \times 1$  convolutions to reduce dimensions

# GoogLeNet Architecture

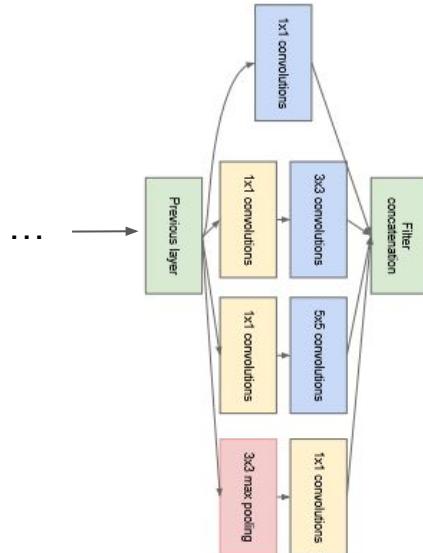
Key idea: stack inception modules together



[Szegedy, Christian, et al. "Going deeper with convolutions." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2015.]

# GoogLeNet Architecture

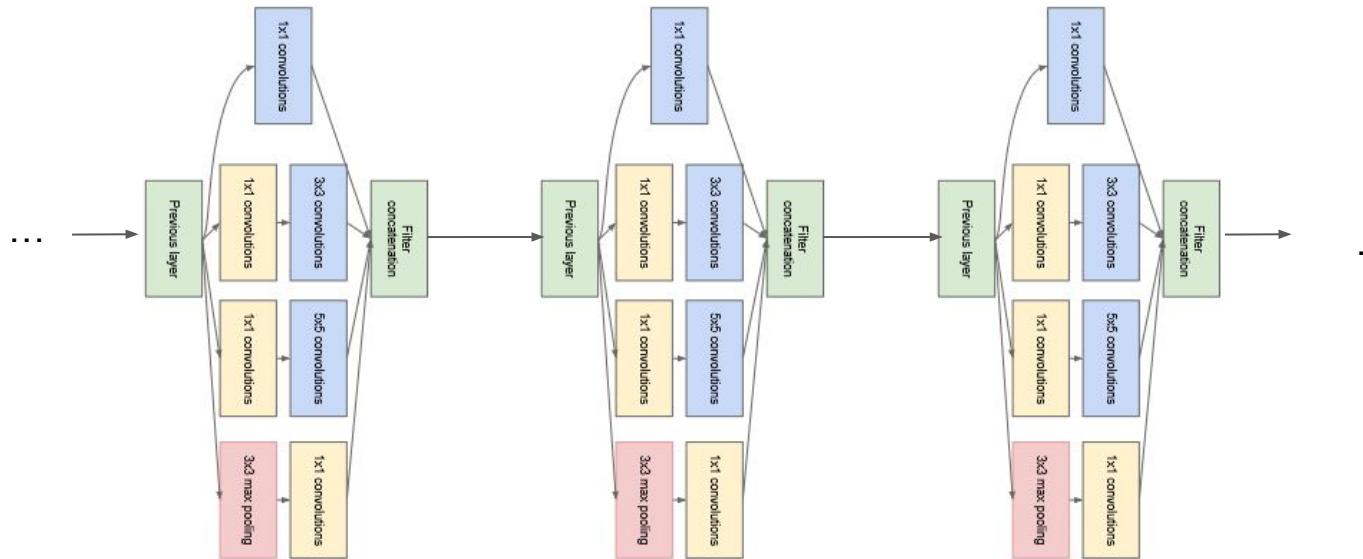
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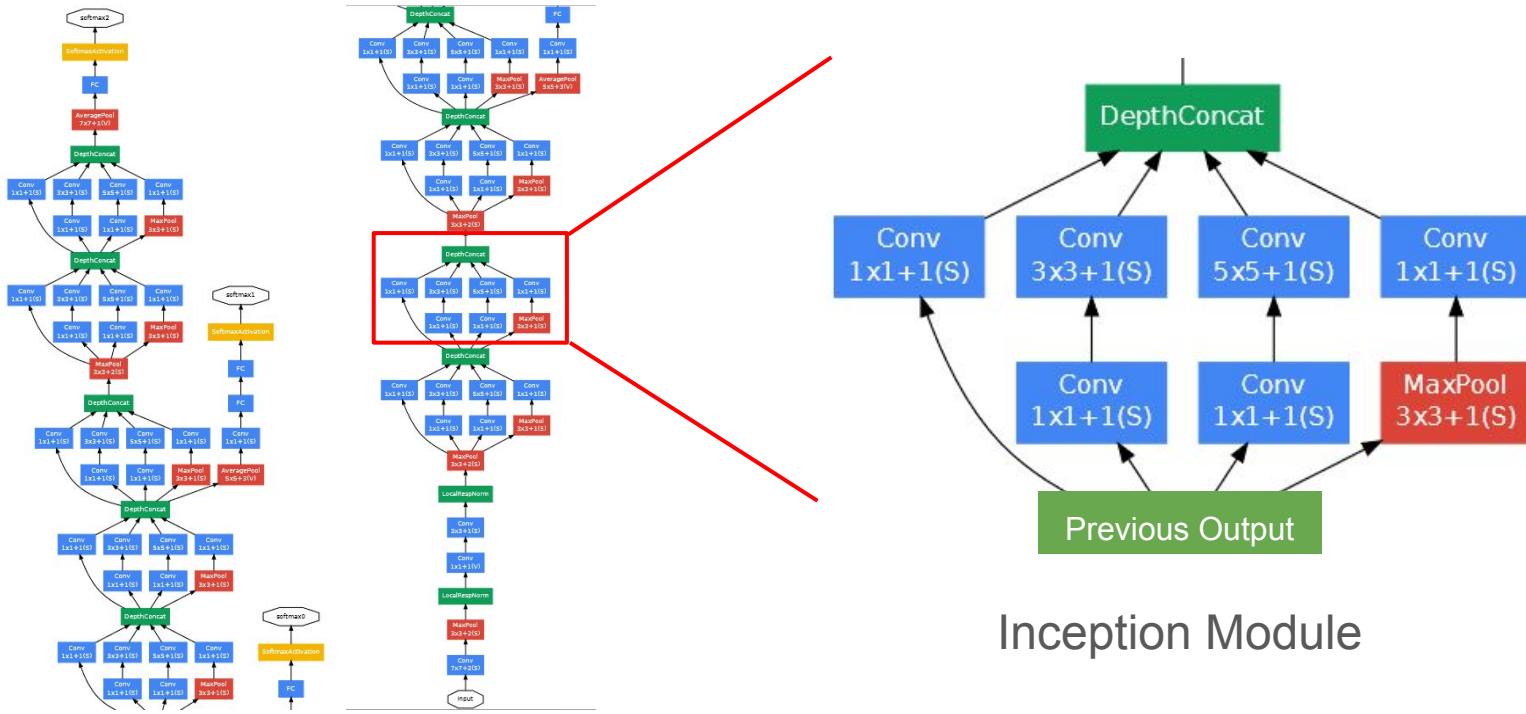
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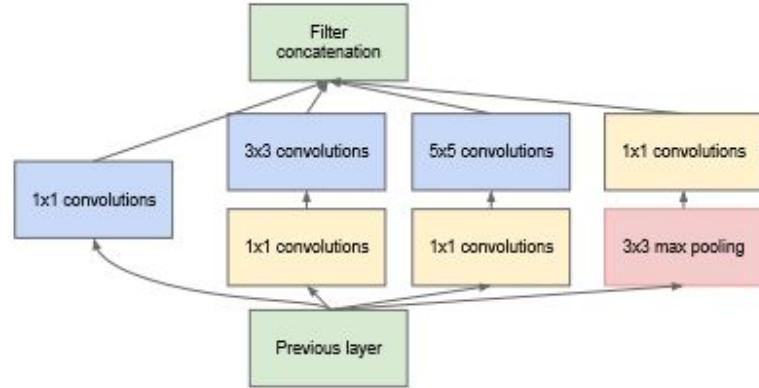
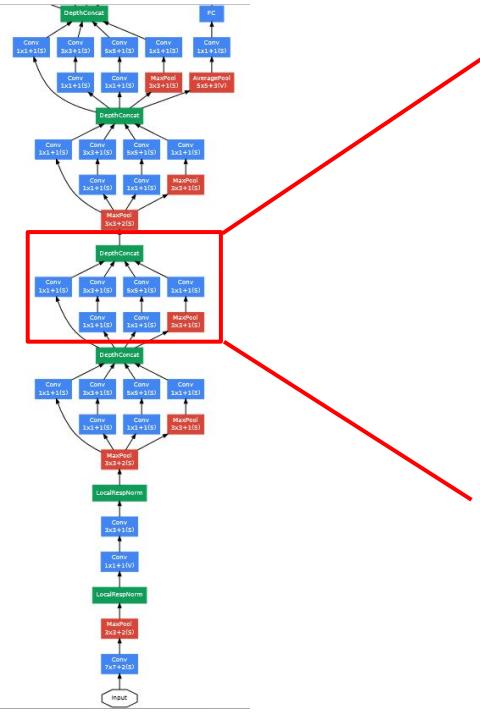
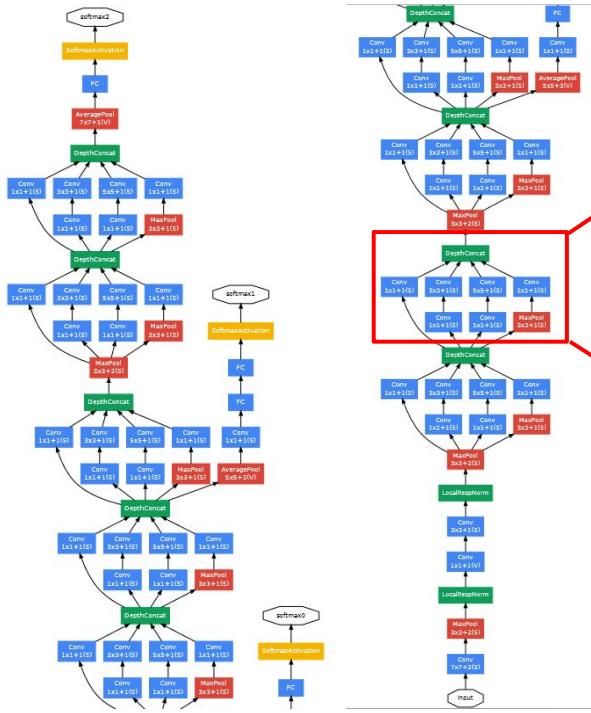
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# The Entire GoogLeNet Architecture



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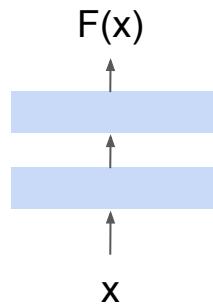
Inception Module

[Szegedy, Christian, et al. "Going deeper with convolutions." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2015.]

# CNN Architectures

## “Plain” CNN

Simple connection  
from previous to next  
layer



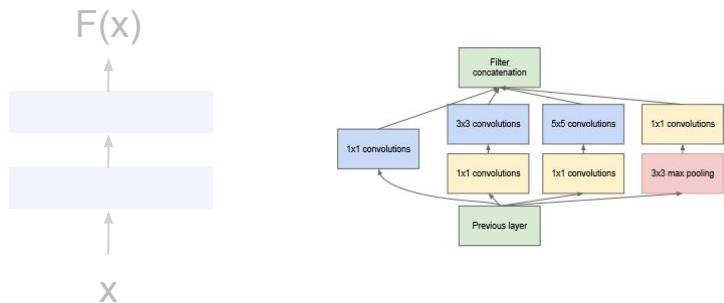
# CNN Architectures

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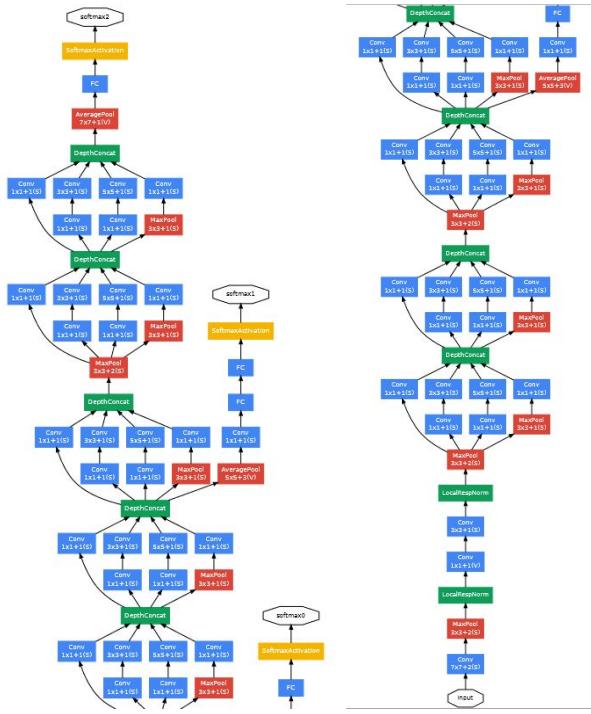
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## GoogLeNet

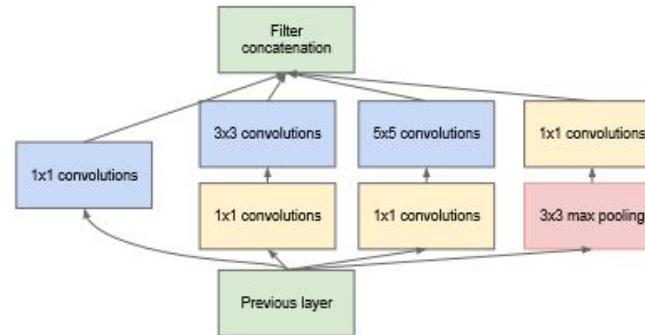
1x1, 3x3, 5x5  
convolutions and  
pooling between each  
layer



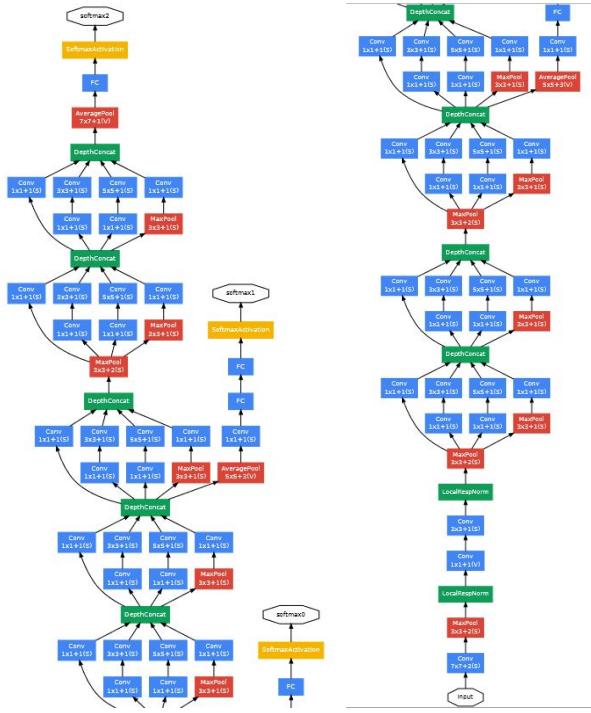
# The Entire GoogleNet Architecture



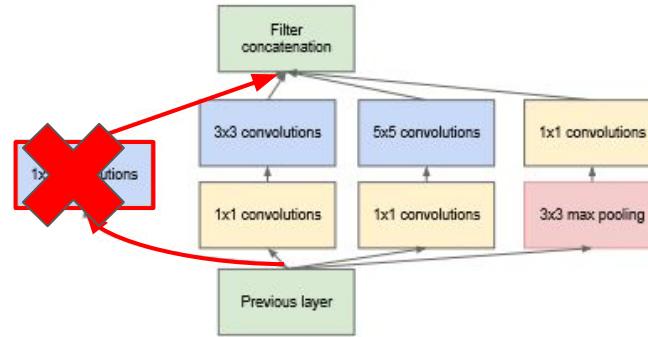
Very complicated - how exactly did this architecture solve the problem?



# The Entire GoogleNet Architecture

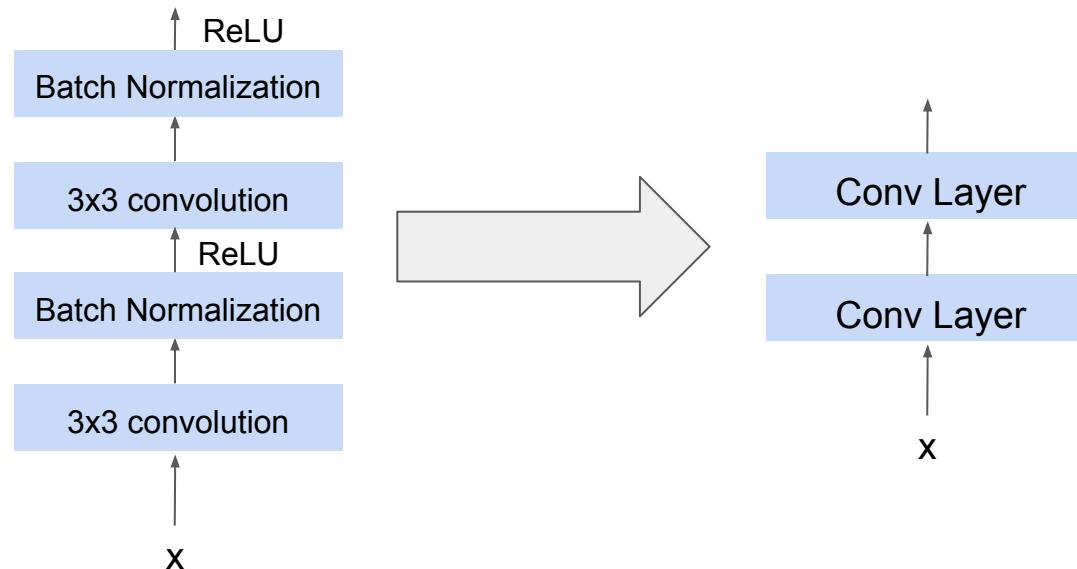


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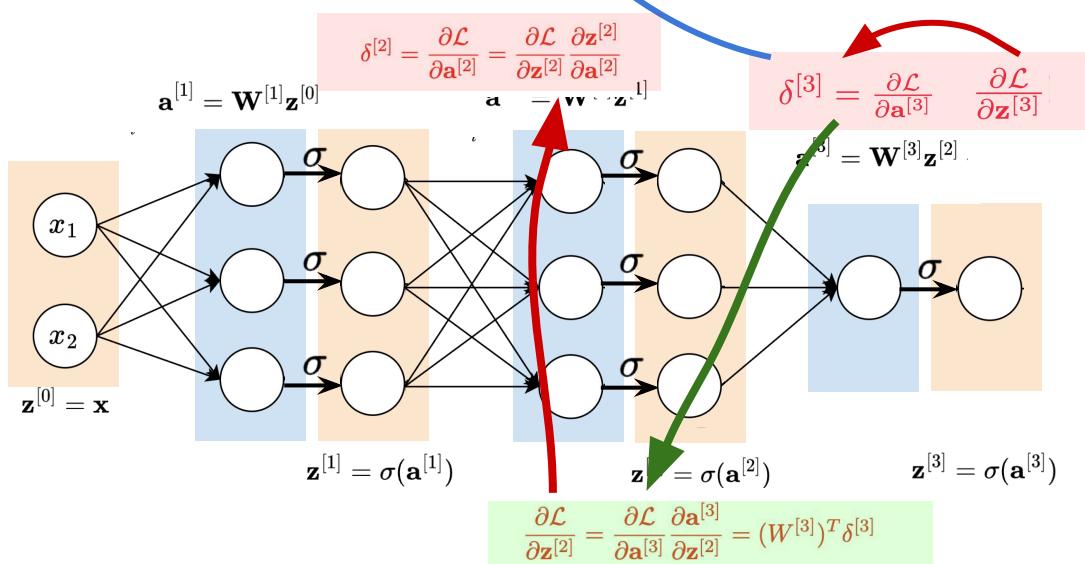
Residual connections: connect layers directly

# Aside: Conv Layer Abstraction



# Backpropagation

$$\begin{aligned}\frac{\partial \mathcal{L}}{\partial \mathbf{W}^{[3]}} &= \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[3]}} \frac{\partial \mathbf{a}^{[3]}}{\partial \mathbf{W}^{[3]}} \\ &= \delta^{[3]} (\mathbf{z}^{[2]})^T\end{aligned}$$



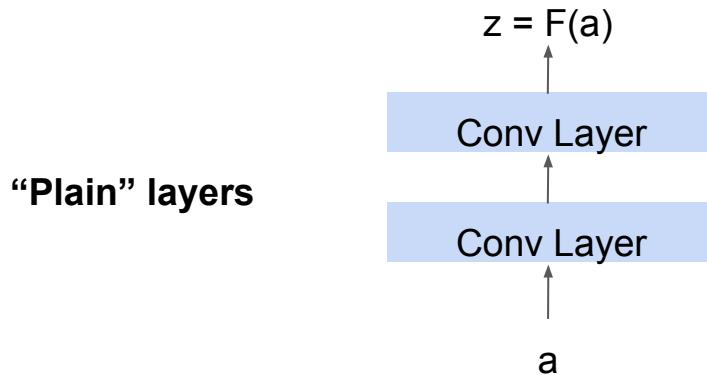
## Algorithm Backward Pass through MLP (Detailed)

- 
- 1: **Input:**  $\{\mathbf{z}^{[1]}, \dots, \mathbf{z}^{[L]}\}$ ,  $\{\mathbf{a}^{[1]}, \dots, \mathbf{a}^{[L]}\}$ , loss gradient  $\frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[L]}}$
  - 2:  $\delta^{[L]} = \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[L]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[L]}} \frac{\partial \mathbf{z}^{[L]}}{\partial \mathbf{a}^{[L]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[L]}} \odot \sigma^{[L]}'(\mathbf{a}^{[L]})$  ▷ Error term
  - 3: **for**  $l = L$  **to** 1 **do**
  - 4:  $\frac{\partial \mathcal{L}}{\partial \mathbf{W}^{[l]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[l]}} \frac{\partial \mathbf{a}^{[l]}}{\partial \mathbf{W}^{[l]}} = \delta^{[l]} (\mathbf{z}^{[l-1]})^T$  ▷ Gradient of weights
  - 5:  $\frac{\partial \mathcal{L}}{\partial \mathbf{b}^{[l]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[l]}} \frac{\partial \mathbf{a}^{[l]}}{\partial \mathbf{b}^{[l]}} = \delta^{[l]}$  ▷ Gradient of biases
  - 6:  $\frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[l-1]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[l]}} \frac{\partial \mathbf{a}^{[l]}}{\partial \mathbf{z}^{[l-1]}} = (\mathbf{W}^{[l]})^T \delta^{[l]}$
  - 7:  $\delta^{[l-1]} = \frac{\partial \mathcal{L}}{\partial \mathbf{a}^{[l-1]}} = \frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[l-1]}} \frac{\partial \mathbf{z}^{[l-1]}}{\partial \mathbf{a}^{[l-1]}} = ((\mathbf{W}^{[l]})^T \delta^{[l]}) \odot \sigma^{[l-1]}'(\mathbf{a}^{[l-1]})$
  - 8: **end for**
  - 9: **Output:**  $\frac{\partial \mathcal{L}}{\partial \mathbf{W}^{[1:L]}}$ ,  $\frac{\partial \mathcal{L}}{\partial \mathbf{b}^{[1:L]}}$
- 

$$\mathcal{L}(\mathbf{z}^{[3]}, \mathbf{y})$$

We can directly compute  $\frac{\partial \mathcal{L}}{\partial \mathbf{z}^{[3]}}!$

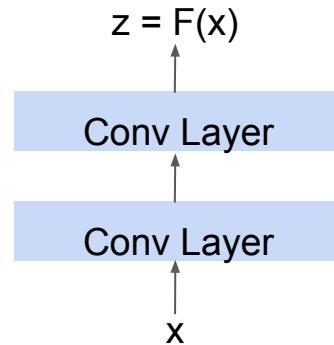
# Backpropagation through “plain” conv layers



$$\frac{\partial L}{\partial a} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial a} = \frac{\partial L}{\partial z} \boxed{F'(a)}$$

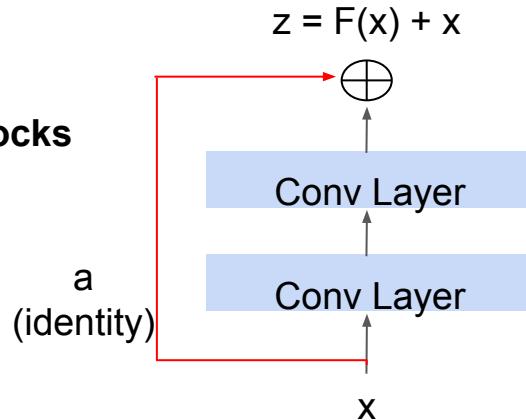
# Backpropagation through Residual blocks

“Plain” layers



$$\frac{\partial L}{\partial x} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial x} = \frac{\partial L}{\partial z} F'(x)$$

Residual Blocks

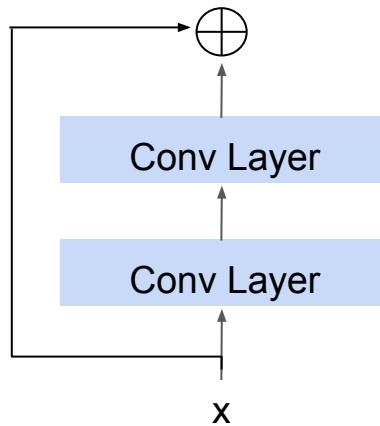


$$\frac{\partial L}{\partial x} =$$

A dashed rectangular box with a dashed border, representing the gradient flow through the residual connection. It spans the width of the residual block and has a height corresponding to the depth of the layers.

# ResNet

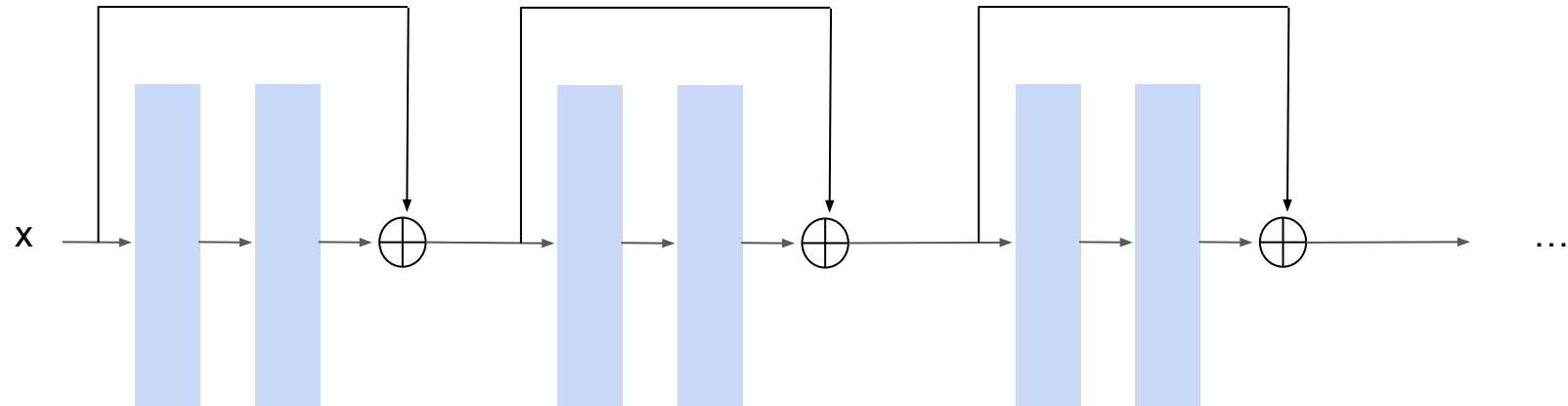
Stack residual blocks together!



[He, Kaiming, et al. "Deep residual learning for image recognition." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016.]

# ResNet

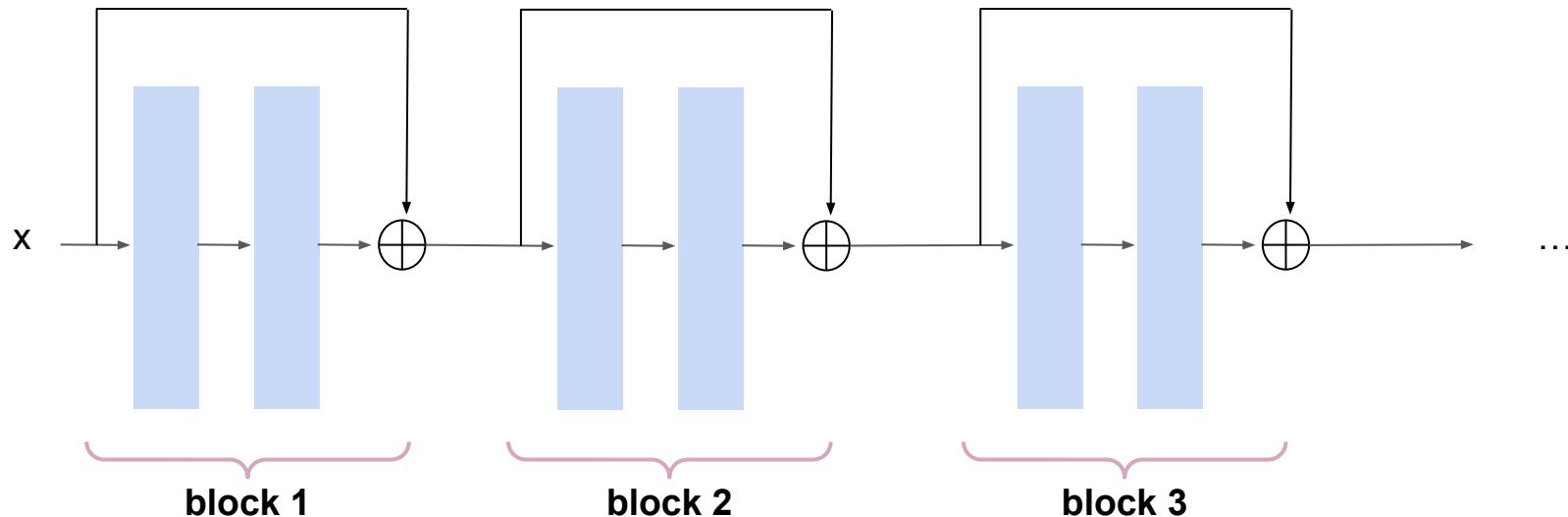
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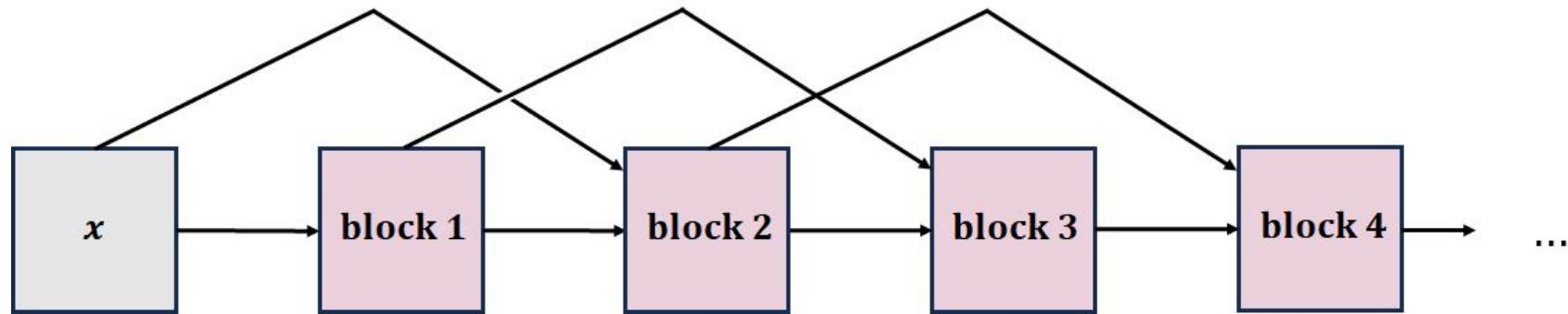
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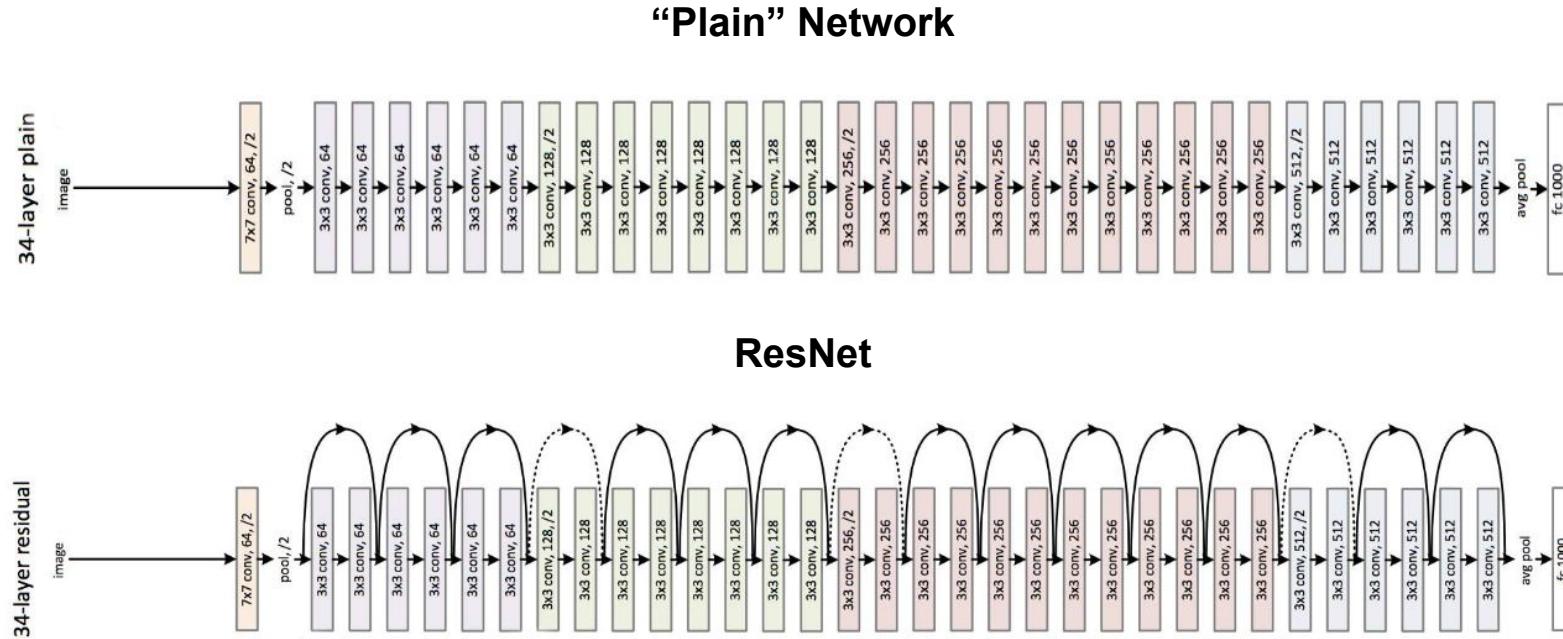
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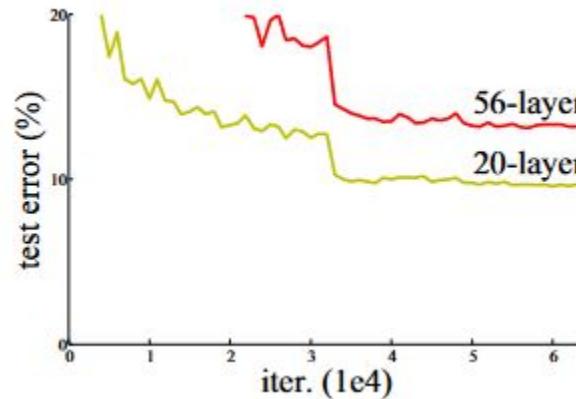
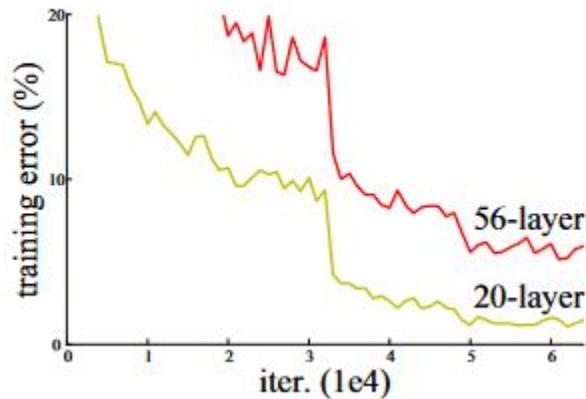
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# Full ResNet Architecture



[He, Kaiming, et al. "Deep residual learning for image recognition." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2016.]

Recall: How can a larger network achieve a higher training error?



56 layer CNN has higher training and test error than 20 layer CNN  
on CIFAR-10 dataset for image classification

# Deeper == better

Can train deeper models!

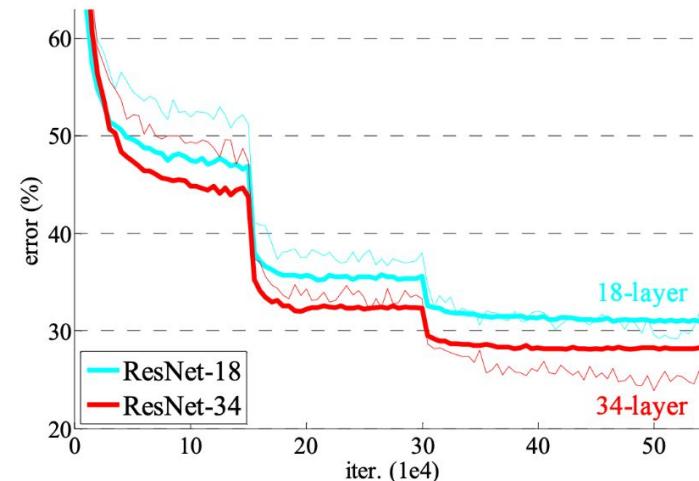
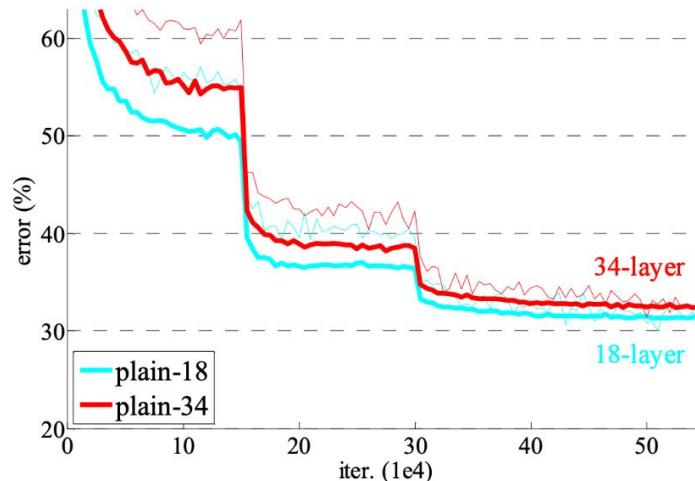


Figure 4. Training on **ImageNet**. Thin curves denote training error, and bold curves denote validation error of the center crops. Left: plain networks of 18 and 34 layers. Right: ResNets of 18 and 34 layers. In this plot, the residual networks have no extra parameter compared to their plain counterparts.

# Visualizing the Effect of Skip Connections

Makes optimization easier!

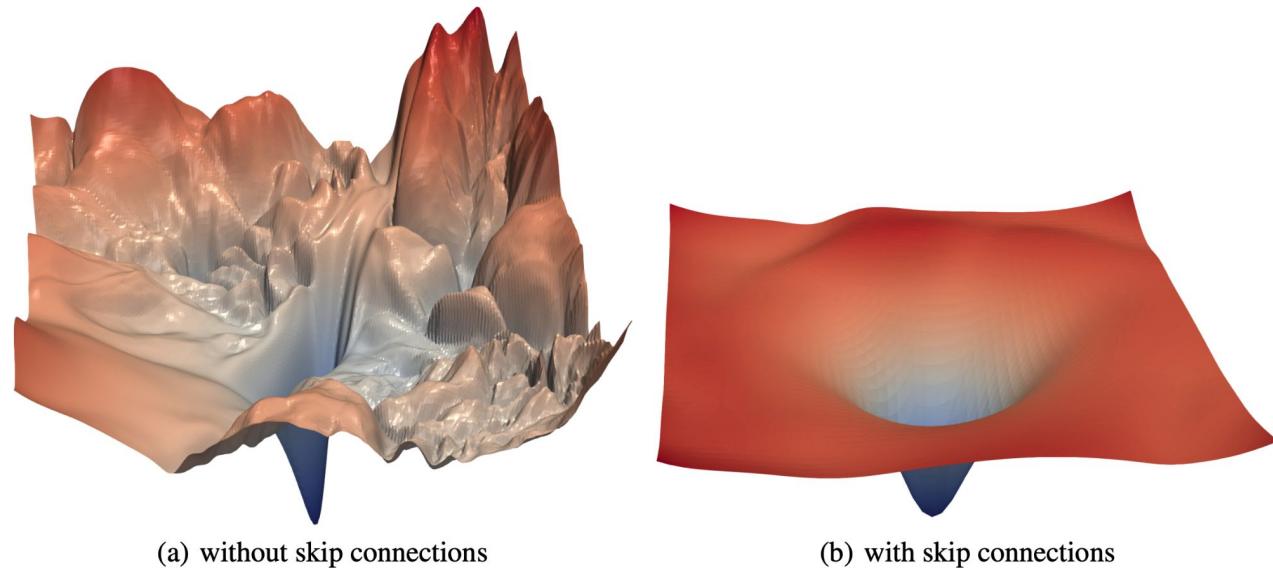


Figure 1: The loss surfaces of ResNet-56 with/without skip connections. The proposed filter normalization scheme is used to enable comparisons of sharpness/flatness between the two figures.

# Stochastic Depth

Still have long training times! Solution: stochastic depth

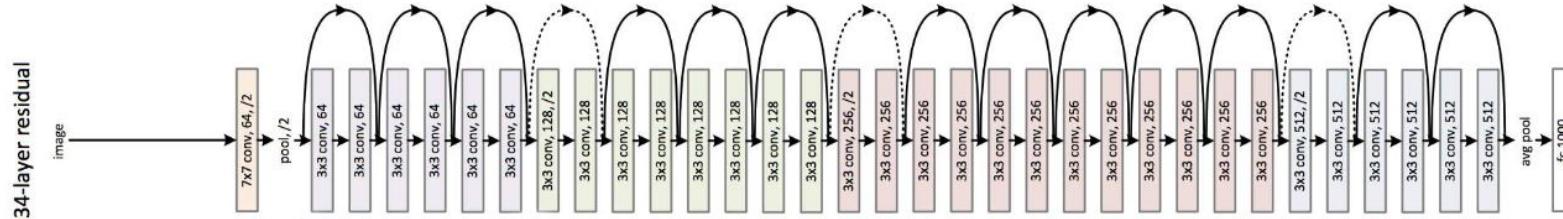
# Stochastic Depth

During training, randomly drop Residual Blocks using skip connections

Like dropout but with residual blocks instead of individual neurons

Another benefit: robustness/mitigating overfitting

$$\text{Drop probability for layer } l \text{ (out of } L\text{)}: \quad p_l = 1 - \frac{l}{L}(1 - p_L)$$



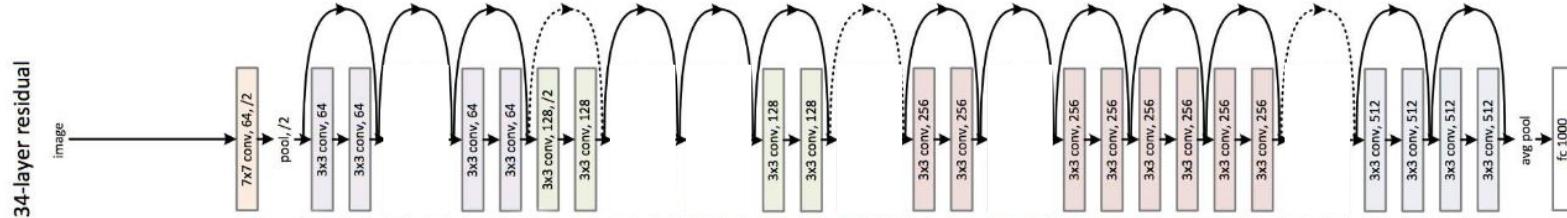
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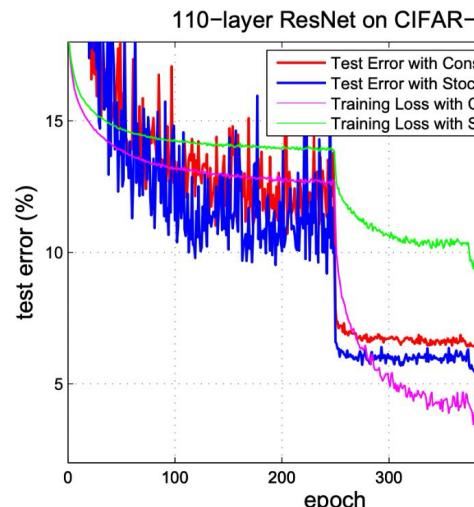
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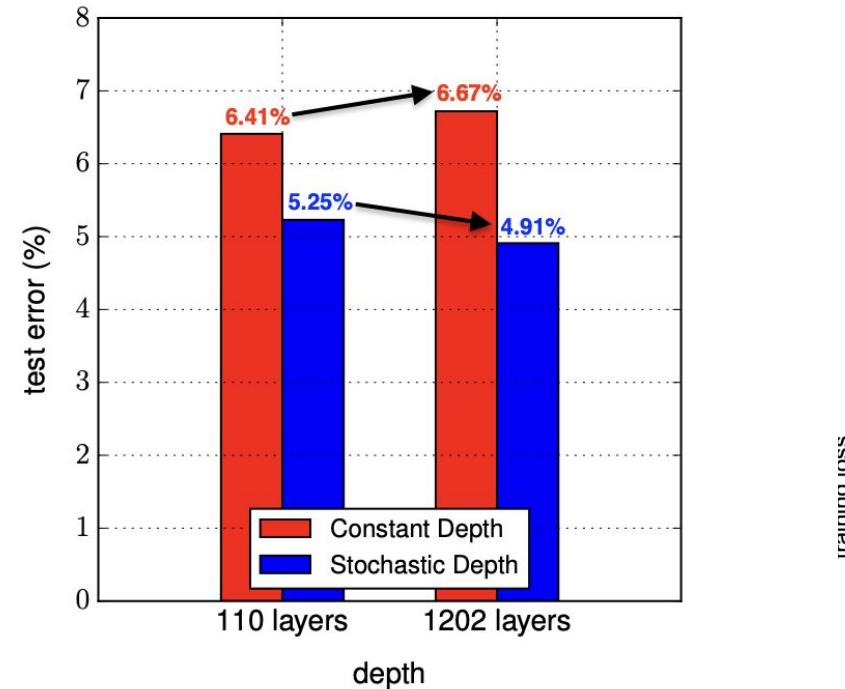


# Stochastic Depth

Increases training loss, but... decreases te



**Fig. 3.** Test error on CIFAR-10 layer ResNet still significantly improves data augmentation, correspond



**Fig. 5.** With stochastic depth, the 1202-layer ResNet still significantly improves over the 110-layer one.

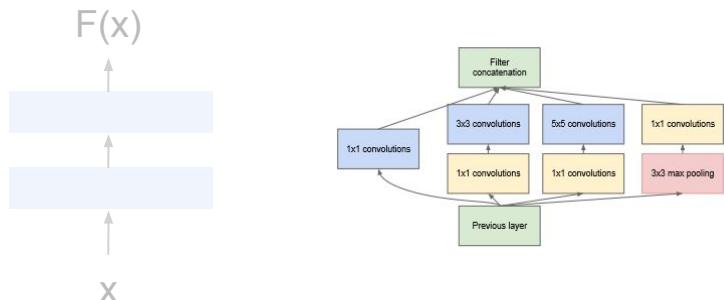
# CNN Architectures

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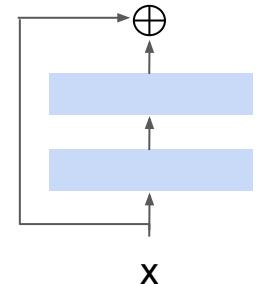
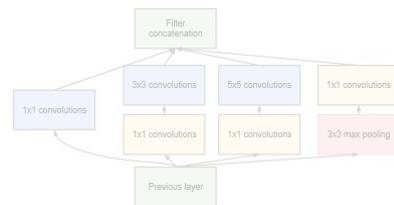
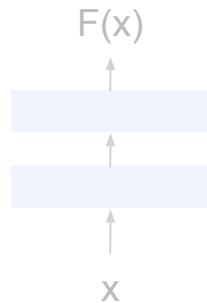
## GoogLeNet

1x1, 3x3, 5x5  
convolutions and  
pooling between each  
layer

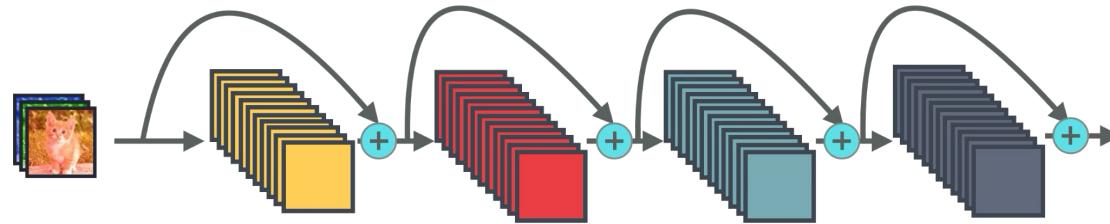


# CNN Architectures

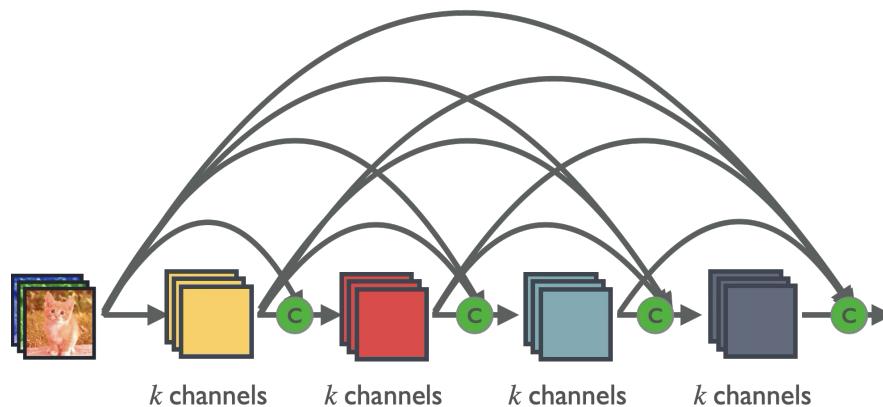
“Plain” CNN	GoogLeNet	ResNet
Simple connection from previous to next layer	1x1, 3x3, 5x5 convolutions and pooling between each layer	Skip connections Add output of previous layer to next layer



# From ResNets to DenseNets

**ResNet**

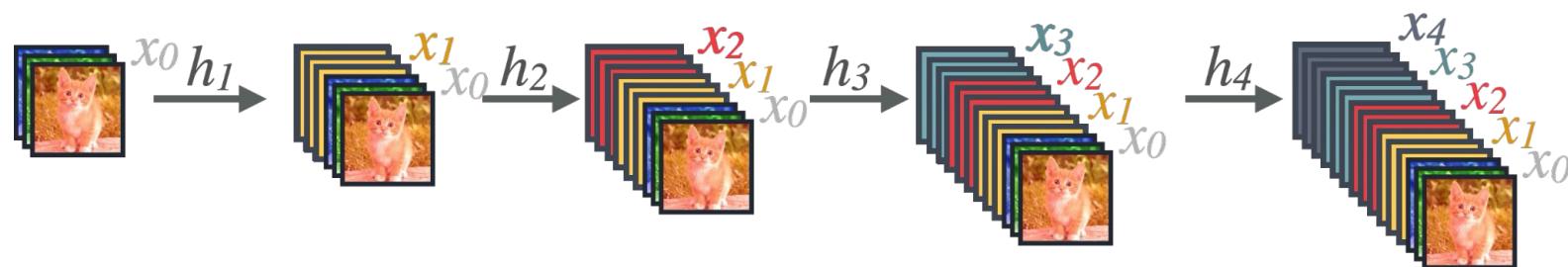
⊕ : Element-wise addition

**DenseNet**

[Huang, Gao, et al. "Densely connected convolutional networks." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2017.]

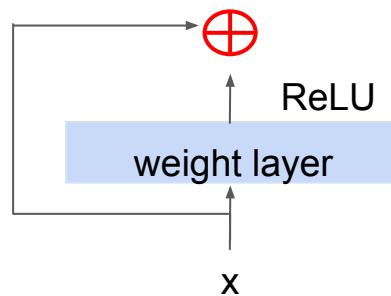
# DenseNets

Feature concatenation

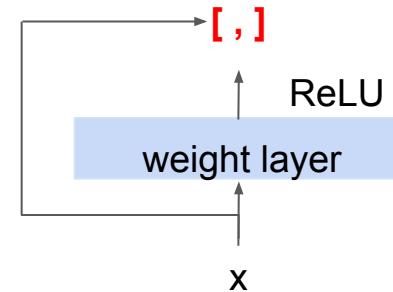


# Dense Blocks

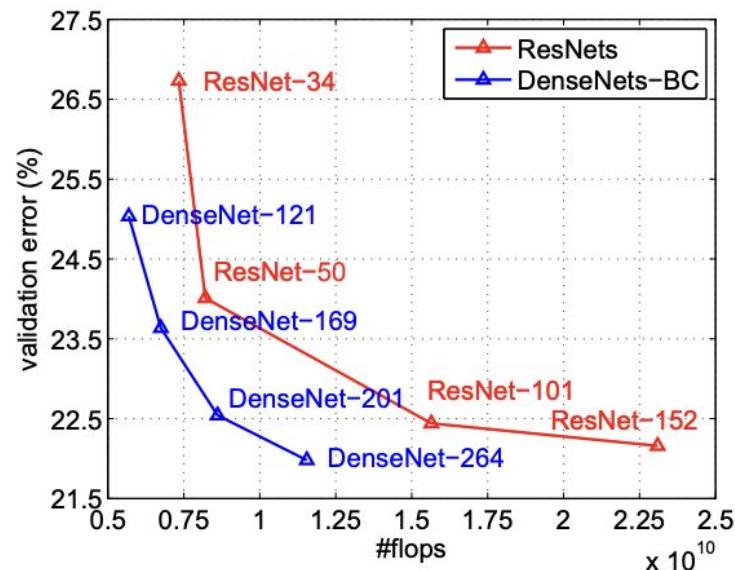
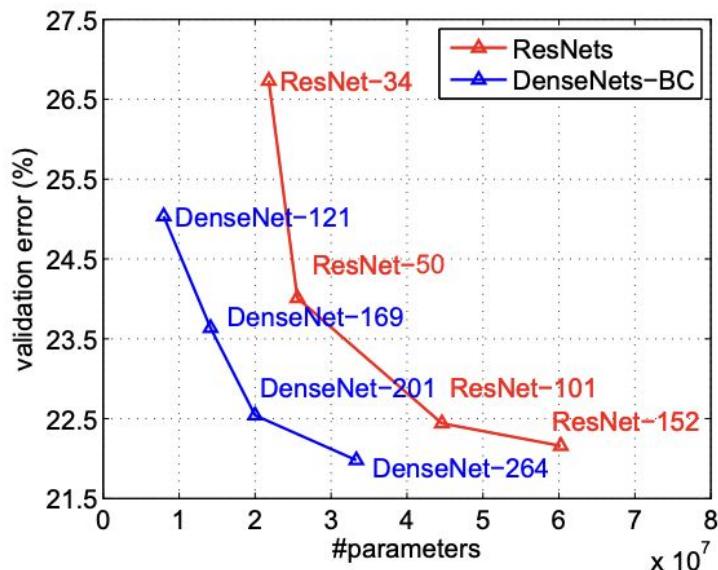
To create dense connections, dense blocks use the same structure as residual blocks, but concatenate (denoted by  $[ , ]$ ) inputs instead of simply adding them



**Residual Blocks**



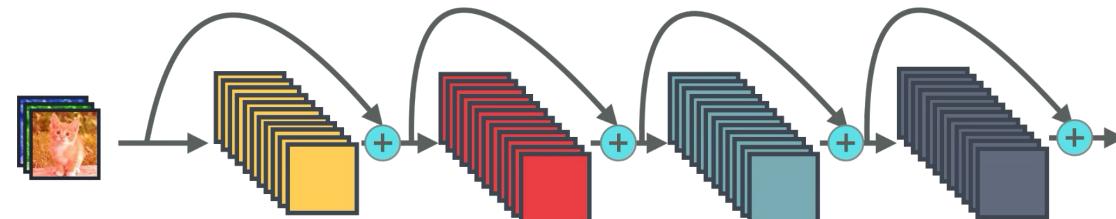
**Dense Blocks**



**Figure 3:** Comparison of the DenseNets and ResNets top-1 error rates (single-crop testing) on the ImageNet validation dataset as a function of learned parameters (*left*) and FLOPs during test-time (*right*).

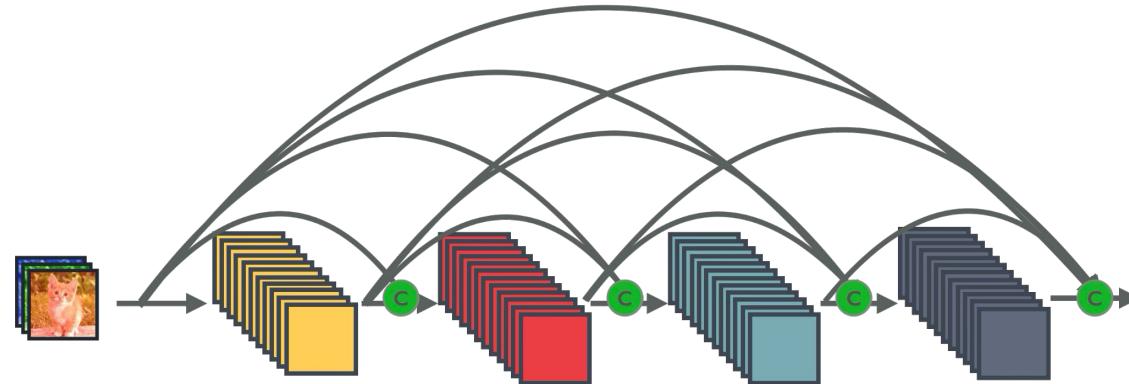
Discussion: What design choices might allow a ~100-layer DenseNet to have fewer parameters than a ~100-layer ResNet?

**ResNet**



+: Element-wise addition

**DenseNet**

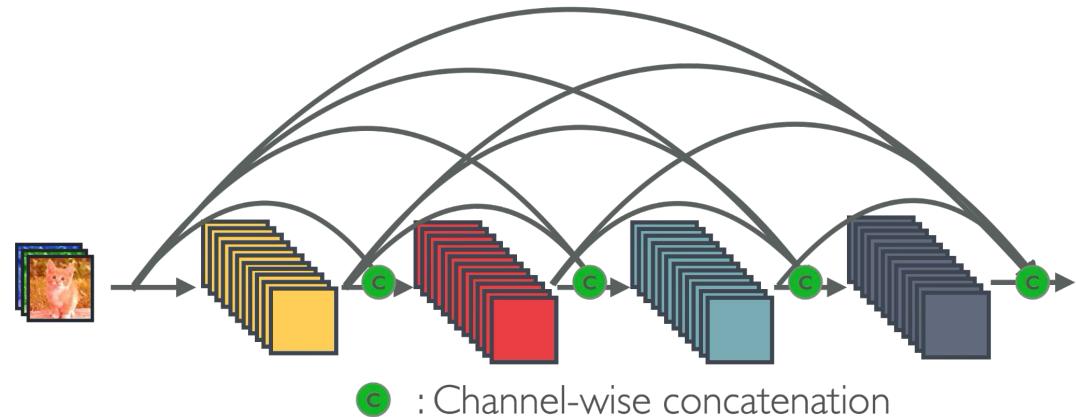


C : Channel-wise concatenation

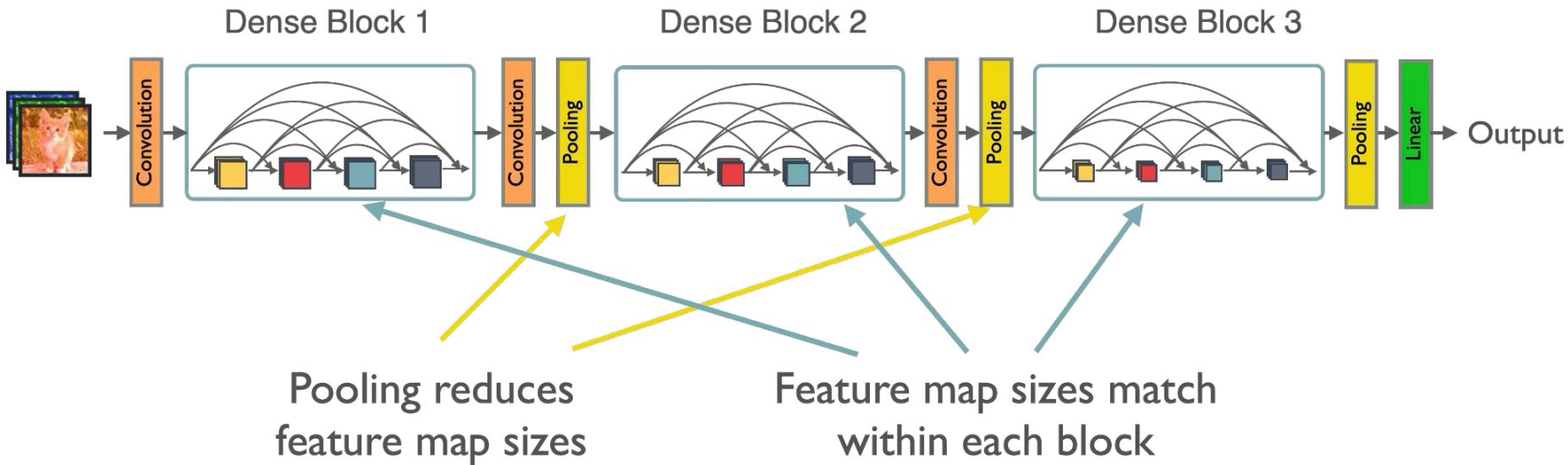
# Dense Connections

Each layer has access to every other layer before it, which:

- maximizes information flow
- allows for feature-map reuse
- less parameters to learn
- alleviates vanishing gradient



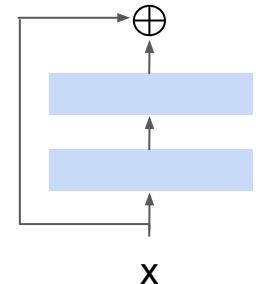
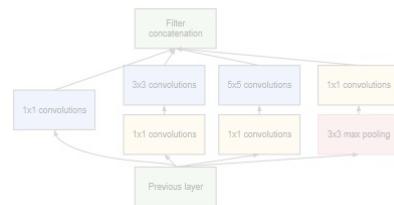
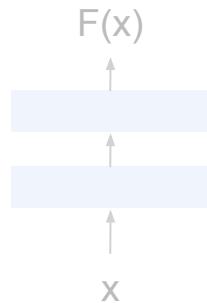
# DenseNets



[Huang, Gao, et al. "Densely connected convolutional networks." *Proceedings of the IEEE conference on computer vision and pattern recognition*. 2017.]

# CNN Architectures

“Plain” CNN	GoogLeNet	ResNet
Simple connection from previous to next layer	1x1, 3x3, 5x5 convolutions and pooling between each layer	Skip connections Add output of previous layer to next layer



# CNN Architectures

“Plain” CNN	GoogLeNet	ResNet	DenseNet
Simple connection from previous to next layer	1x1, 3x3, 5x5 convolutions and pooling between each layer	Skip connections Add output of previous layer to next layer	Dense connections Concatenate output of previous layer to next layer

Diagrams illustrating the four CNN architectures:

- “Plain” CNN:** Shows a simple vertical stack of layers. Input  $x$  is processed by a sequence of layers to produce the final output  $F(x)$ .
- GoogLeNet:** Shows a complex architecture with multiple parallel paths. The “Previous layer” feeds into “1x1 convolutions”, “3x3 convolutions”, “5x5 convolutions”, “1x1 convolutions”, “1x1 convolutions”, and “3x3 max pooling”. These are then combined via “Filter concatenation”.
- ResNet:** Shows skip connections where the input  $x$  is added directly to the output of a residual block before the final output.
- DenseNet:** Shows dense connections where the input  $x$  is concatenated with the outputs of all previous layers before being processed by the current layer.

# Summary of Models

“Plain” CNN	Google Net	ResNet	DenseNet
Simple connection from previous to next layer	1x1, 3x3, 5x5 convolutions and pooling between each layer	Skip connections Add output of previous layer to next layer	Dense connections Concatenate output of previous layer to next layer

Diagrams illustrating the four model architectures:

- “Plain” CNN:** Shows a vertical stack of two blue rectangular layers. An input arrow labeled  $x$  points to the bottom layer, and an output arrow labeled  $F(x)$  points from the top layer.
- Google Net:** Shows a complex network architecture. An input arrow labeled “Previous layer” points to a green box labeled “Filter concatenation”. This box receives inputs from three parallel paths: “1x1 convolutions” (blue), “1x1 convolutions” (orange), and “3x3 max pooling” (pink). The concatenated outputs from these paths then pass through “3x3 convolutions” (blue), “5x5 convolutions” (blue), and “1x1 convolutions” (orange).
- ResNet:** Shows a skip connection. An input arrow labeled  $x$  points to the bottom layer. The output of this layer is then added to its input via a skip connection (indicated by a circle with a plus sign) before exiting as  $F(x)$ .
- DenseNet:** Shows a dense connection. An input arrow labeled  $x$  points to the bottom layer. The output of this layer is concatenated (indicated by brackets [ , ]) with its input before exiting as  $F(x)$ .

# Summary

- Deep CNNs outperform shallow CNNs
- But...
  - Harder optimization problem!
- Residual (and dense) connections make training easier!
  - Can train networks with 100s of layers!
- Stochastic depth let's you train deeper networks faster
  - 1000+ layers!
- In general...
  - Build large networks as stacks of (many!) simple building blocks