# Project2

# Group-11

```
library(tidyverse)
library(moderndive)
library(gapminder)
library(sjPlot)
library(jtools)
library(GGally)
library(gt)
library(gridExtra)
library(knitr)
library(patchwork)
library(broom)
```

### 1 Data Visulization

Preprocessing the data and conducting summary statistics, while also generating visualizations to better understand the data.

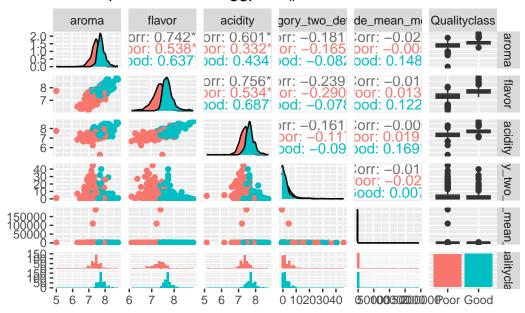
```
# Read the dataset
data <- read.csv("dataset11.csv")
data <- na.omit(data)
data$Qualityclass <- factor(data$Qualityclass, levels = c("Poor", "Good"))
str(data)

'data.frame': 894 obs. of 8 variables:
$ country_of_origin : chr "Guatemala" "Taiwan" "Brazil" "Colombia" ...
$ aroma : num 7.58 7.92 7.83 7.5 7.33 7.83 7.83 7.5 7.08 7.08 ...
$ flavor : num 7.5 7.75 7.83 7.75 7.17 8.33 7.75 7.58 6.92 6.92 ...
$ acidity : num 7.58 7.67 7.67 7.75 7.08 8.25 7.58 7.75 7 7.25 ...
$ category_two_defects: int 1 0 3 0 1 9 2 2 15 2 ...</pre>
```

```
$ altitude_mean_meters: num 1901 1000 1250 1450 1450 ...
$ harvested : int 2017 2016 2012 2011 2013 2012 2015 2014 2013 2015 ...
$ Qualityclass : Factor w/ 2 levels "Poor", "Good": 1 2 2 2 1 2 2 2 1 1 ...
- attr(*, "na.action") = 'omit' Named int [1:200] 5 13 16 23 27 28 33 42 45 46 ...
..- attr(*, "names") = chr [1:200] "5" "13" "16" "23" ...

# Scatterplot matrix with ggpairs()
scatterplot = data %>%
select(aroma, flavor, acidity, category_two_defects, altitude_mean_meters, Qualityclass)
ggpairs(scatterplot, aes(color = Qualityclass), title="Scatterplot matrix with ggpairs()")
```

### Scatterplot matrix with ggpairs()



# Summary Statistics for 'aroma', 'flavor', and 'acidity' across different quality classes
data |>

```
'ac.Sd' = sd(acidity),
          'ac.Min' = min(acidity),
          'ac.Max' = max(acidity),
             .by = Qualityclass) |>
gt() |>
  fmt_number(decimals = 2) |>
 tab_spanner(
    label = "aroma",
    columns = c(ar.Mean, ar.Sd, ar.Min, ar.Max)
  ) |>
 tab_spanner(
    label = "flavor",
    columns = c(fl.Mean, fl.Sd, fl.Min, fl.Max)
  ) |>
 tab_spanner(
   label = "acidity",
    columns = c(ac.Mean, ac.Sd, ac.Min, ac.Max)
# Summary statistics for 'category_two_defects' and 'altitude_mean_meters' across differen
data |>
  summarize('C.Mean' = mean(category_two_defects),
          'C.Sd' = sd(category_two_defects),
          'C.Min' = min(category_two_defects),
          'C.Max' = max(category_two_defects),
          'A.Mean' = mean(log(altitude_mean_meters)),
          'A.Sd' = sd(log(altitude_mean_meters)),
          'A.Min' = min(log(altitude_mean_meters)),
          'A.Max' = max(log(altitude_mean_meters)),
             .by = Qualityclass) |>
gt() |>
 fmt_number(decimals = 2) |>
 tab_spanner(
    label = "Defects",
    columns = c(C.Mean, C.Sd, C.Min, C.Max)
  ) |>
 tab_spanner(
    label = "log_Altitude",
    columns = c(A.Mean, A.Sd, A.Min, A.Max)
  )
```

Table 1: Summary statistics

(a)

Qualityclass         ar.Mean         ar.Sd         ar.Min         ar.Max         fl.Mean         fl.Sd         fl.Min         fl.Max         ac.Mean         ac.Sd           Poor         7.38         0.28         5.08         8.25         7.31         0.27         6.17         8.08         7.35         0.26		aroma					flavor				acidity			
Poor 7 38 0 28 5 08 8 25 7 31 0 27 6 17 8 08 7 35 0 26	Qualityclass	ar.Mean	ar.Sd	ar.Min	ar.Max	fl.Mean	fl.Sd	fl.Min	fl.Max	ac.Mean	ac.Sd	ac.M		
1.001 1.00 0.20 0.20 1.01 0.21 0.11 0.00 1.00 0.20	Poor	7.38	0.28	5.08	8.25	7.31	0.27	6.17	8.08	7.35	0.26	5.5		
Good $7.76 \ 0.23 \ 7.17 \ 8.75 \ 7.74 \ 0.23 \ 7.25 \ 8.83 \ 7.72 \ 0.24$	$\operatorname{Good}$	7.76	0.23	7.17	8.75	7.74	0.23	7.25	8.83	7.72	0.24	7.0		

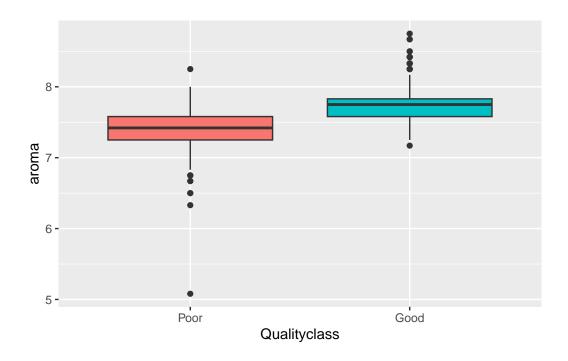
(b)

		ects			log_A	ltitude		
Qualityclass	C.Mean	C.Sd	C.Min	C.Max	A.Mean	A.Sd	A.Min	A.Max
Poor	4.16	5.91	0.00	45.00	6.94	1.10	0.00	12.16
$\operatorname{Good}$	2.85	4.32	0.00	40.00	7.13	0.77	0.00	8.10

# 2 Predictor Modeling and Evaluation

Modeling each predictor separately with the response variable to observe the individual impact of each feature on the quality of coffee.

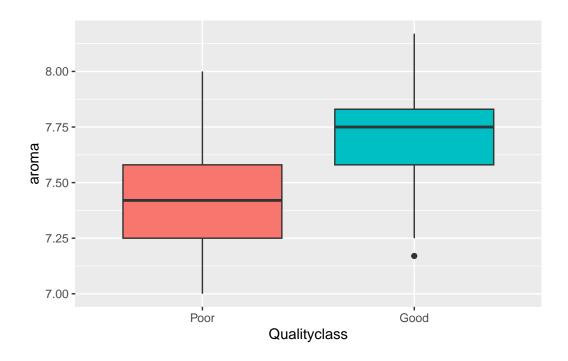
### 2.1 Aroma and Qualityclass



```
# Calculate quartiles and determine lower and upper bounds
q1_aroma <- quantile(data_aroma$aroma, 0.25)
q3_aroma <- quantile(data_aroma$aroma, 0.75)
iqr_aroma <- q3_aroma - q1_aroma
lower_bound_aroma <- q1_aroma - 1.5 * iqr_aroma
upper_bound_aroma <- q3_aroma + 1.5 * iqr_aroma

# Filter 'aroma' within the calculated bounds
data_aroma_filtered <- data_aroma %>%
    filter(aroma >= lower_bound_aroma & aroma <= upper_bound_aroma)

# Create a boxplot of 'aroma'
p2 <- ggplot(data = data_aroma_filtered, aes(x = Qualityclass, y = aroma, fill = Qualityclass(x = "Qualityclass", y = "aroma")+
    theme(legend.position = "none")
p2</pre>
```



### Call:

```
glm(formula = Qualityclass ~ aroma, family = binomial(link = "logit"),
    data = data_aroma_filtered)
```

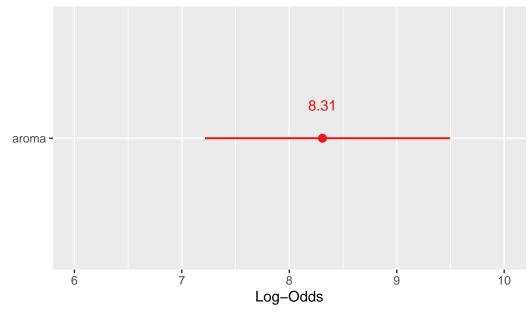
#### Coefficients:

Null deviance: 1171 on 844 degrees of freedom Residual deviance: 762 on 843 degrees of freedom

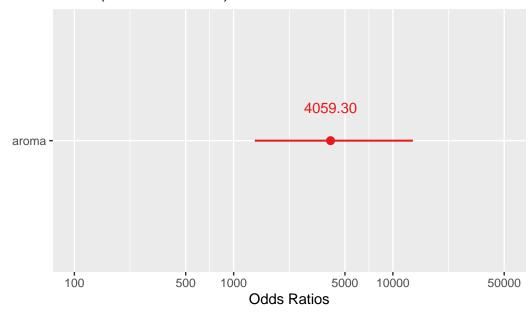
#### AIC: 766

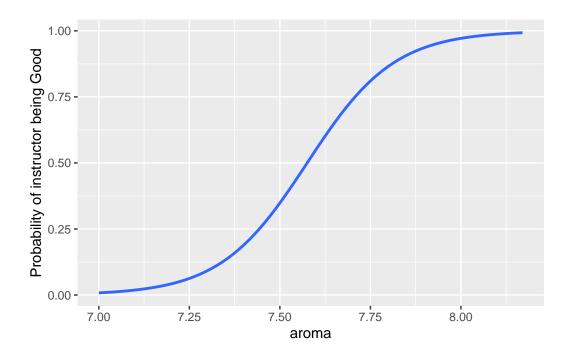
### Number of Fisher Scoring iterations: 5

# Log-Odds (Good instructor)



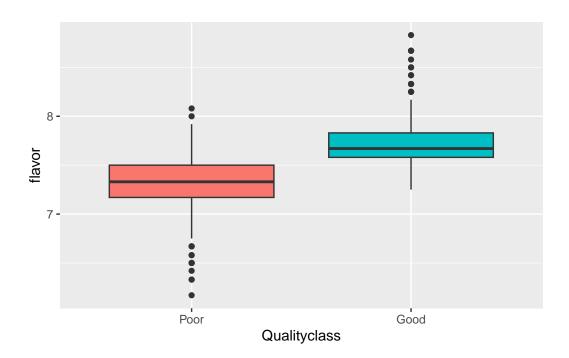
# Odds (Good instructor)





### 2.2 Flavor and Qualityclass

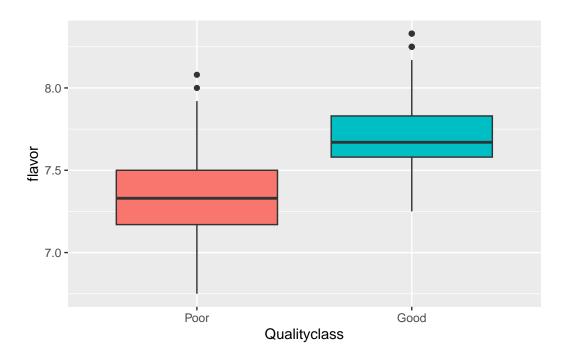
```
geom_boxplot() +
labs(x = "Qualityclass", y = "flavor")+
theme(legend.position = "none")
p3
```



```
# Calculate quartiles and determine lower and upper bounds
q1_flavor <- quantile(data_flavor$flavor, 0.25)
q3_flavor <- quantile(data_flavor$flavor, 0.75)
iqr_flavor <- q3_flavor - q1_flavor
lower_bound_flavor <- q1_flavor - 1.5 * iqr_flavor
upper_bound_flavor <- q3_flavor + 1.5 * iqr_flavor

# Filter 'flavor' within the calculated bounds
data_flavor_filtered <- data_flavor %>%
    filter(flavor >= lower_bound_flavor & flavor <= upper_bound_flavor)

# Create a boxplot of 'flavor'
p4 <- ggplot(data = data_flavor_filtered, aes(x = Qualityclass, y = flavor, fill = Quality geom_boxplot() +
    labs(x = "Qualityclass", y = "flavor")+
    theme(legend.position = "none")</pre>
```



#### Call:

```
glm(formula = Qualityclass ~ flavor, family = binomial(link = "logit"),
    data = data_flavor_filtered)
```

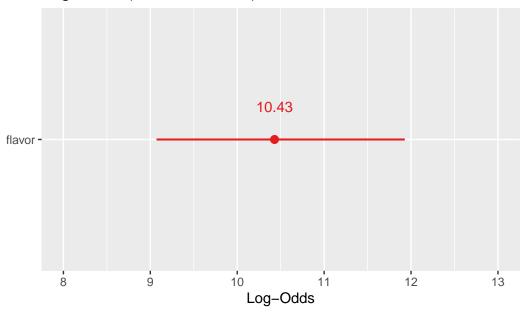
### Coefficients:

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 1207.32 on 870 degrees of freedom
Residual deviance: 648.91 on 869 degrees of freedom
AIC: 652.91
Number of Fisher Scoring iterations: 6
  # Calculate lower and upper bounds for 'flavor' log-odds
  mod2.coef.logodds <- model2 %>%
                         summary() %>%
                         coef()
  flavor.logodds.lower <- mod2.coef.logodds["flavor", "Estimate"] -</pre>
                         1.96 * mod2.coef.logodds["flavor", "Std. Error"]
  flavor.logodds.upper <- mod2.coef.logodds["flavor", "Estimate"] +</pre>
                         1.96 * mod2.coef.logodds["flavor", "Std. Error"]
  # Display the confidence interval
  paste("(", flavor.logodds.lower, ",", flavor.logodds.upper, ")")
[1] "( 9.00535216215199 , 11.8527408569355 )"
  # Plot log-odds of being a good instructor
  plot_model(model2, show.values = TRUE, transform = NULL,
```

title = "Log-Odds (Good instructor)", show.p = FALSE)

# Log-Odds (Good instructor)



```
# Calculate lower and upper bounds for 'flavor' odds
exp(mod2.coef.logodds)
```

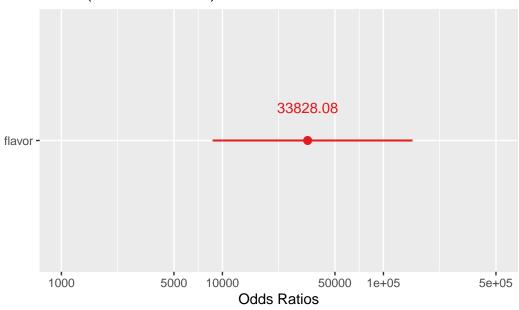
```
Estimate Std. Error z value Pr(>|z|) (Intercept) 7.392437e-35 240.035635 5.923404e-07 1 flavor 3.382808e+04 2.067571 1.719714e+06 1
```

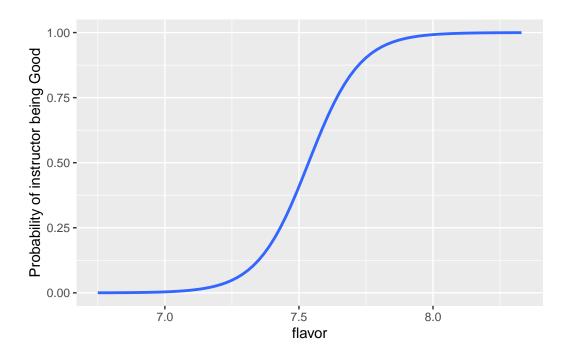
```
flavor.odds.lower <- exp(flavor.logodds.lower)
flavor.odds.upper <- exp(flavor.logodds.upper)

# Display the confidence interval
paste("(", flavor.odds.lower, ",", flavor.odds.upper, ")")</pre>
```

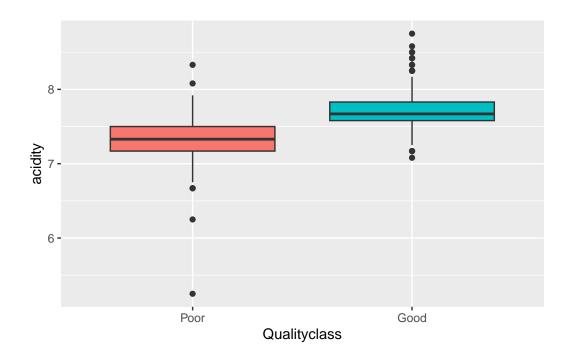
### [1] "( 8146.56921303119 , 140468.824988887 )"

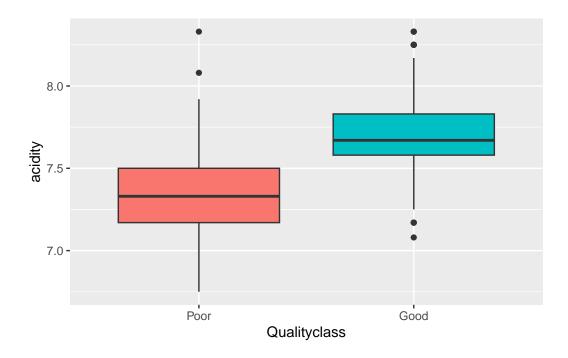
# Odds (Good instructor)





# 2.3 Acidity and Qualityclass





### Call:

```
glm(formula = Qualityclass ~ acidity, family = binomial(link = "logit"),
    data = data_acidity_filtered)
```

### Coefficients:

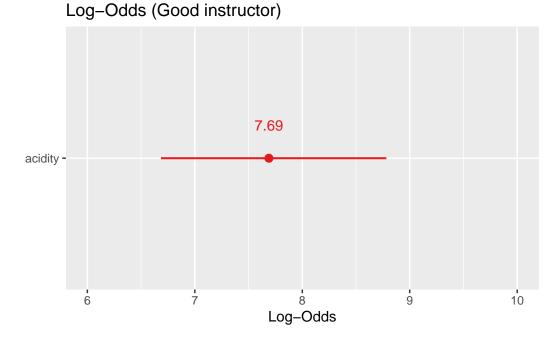
Null deviance: 1219.92 on 879 degrees of freedom Residual deviance: 790.64 on 878 degrees of freedom

#### AIC: 794.64

### Number of Fisher Scoring iterations: 5

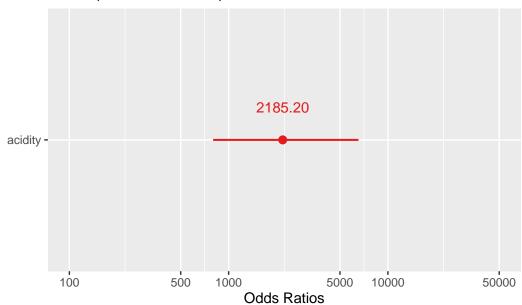
# Plot log-odds of being a good instructor

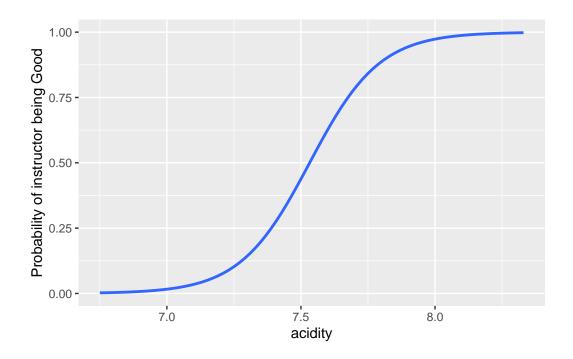
plot\_model(model3, show.values = TRUE, transform = NULL,



title = "Log-Odds (Good instructor)", show.p = FALSE)

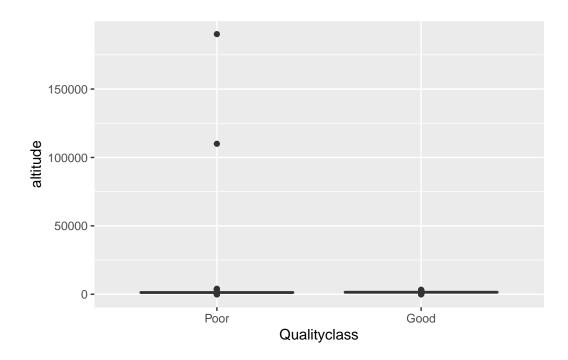
# Odds (Good instructor)





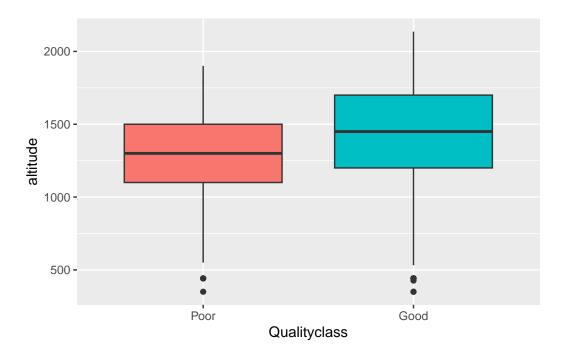
### 2.4 Altitude mean meters and Qualityclass

```
geom_boxplot() +
labs(x = "Qualityclass", y = "altitude")+
theme(legend.position = "none")
p7
```



```
# Calculate quartiles and determine lower and upper bounds
q1_altitude <- quantile(data_altitude$altitude_mean_meters, 0.25)
q3_altitude <- quantile(data_altitude$altitude_mean_meters, 0.75)
iqr_altitude <- q3_altitude - q1_altitude
lower_bound_altitude <- q1_altitude - 1.5 * iqr_altitude
upper_bound_altitude <- q3_altitude + 1.5 * iqr_altitude

# Filter 'altitude_mean_meters' within the calculated bounds
data_altitude_filtered <- data_altitude %>%
    filter(altitude_mean_meters >= lower_bound_altitude & altitude_mean_meters <= upper_bound
# Create a boxplot of 'altitude_mean_meters'
p8 <- ggplot(data = data_altitude_filtered, aes(x = Qualityclass, y = altitude_mean_meters
    geom_boxplot() +
labs(x = "Qualityclass", y = "altitude")+
theme(legend.position = "none")</pre>
```



#### Call:

### Coefficients:

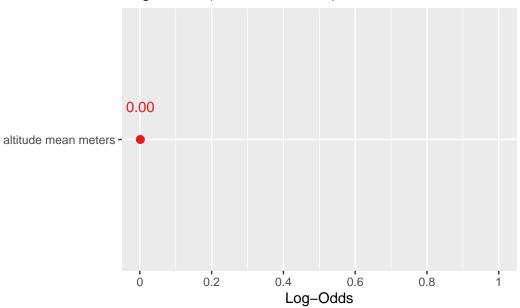
```
Estimate Std. Error z value Pr(>|z|)

(Intercept) -1.6483638 0.3003784 -5.488 4.07e-08 ***
altitude_mean_meters 0.0012630 0.0002167 5.829 5.58e-09 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 1169.5 on 843 degrees of freedom
Residual deviance: 1133.4 on 842 degrees of freedom
AIC: 1137.4
Number of Fisher Scoring iterations: 4
  # Calculate lower and upper bounds for 'altitude_mean_meters' log-odds
  mod4.coef.logodds <- model4 %>%
                        summary() %>%
                        coef()
  altitude.logodds.lower <- mod4.coef.logodds["altitude_mean_meters", "Estimate"] -</pre>
                         1.96 * mod4.coef.logodds["altitude_mean_meters", "Std. Error"]
  altitude.logodds.upper <- mod4.coef.logodds["altitude_mean_meters", "Estimate"] +
                        1.96 * mod4.coef.logodds["altitude_mean_meters", "Std. Error"]
  # Display the confidence interval
  paste("(", altitude.logodds.lower, ",", altitude.logodds.upper, ")")
[1] "( 0.00083832899657146 , 0.00168775443306841 )"
  # Plot log-odds of being a good instructor
  plot_model(model4, show.values = TRUE, transform = NULL,
             title = "Log-Odds (Good instructor)", show.p = FALSE)
```





```
# Calculate lower and upper bounds for 'altitude_mean_meters' odds
exp(mod4.coef.logodds)
```

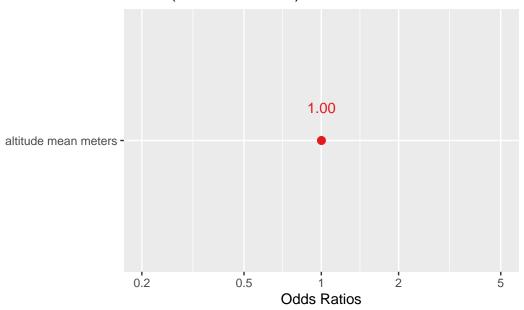
```
Estimate Std. Error z value Pr(>|z|)
(Intercept) 0.1923644 1.350370 4.137664e-03 1
altitude_mean_meters 1.0012638 1.000217 3.399475e+02 1
```

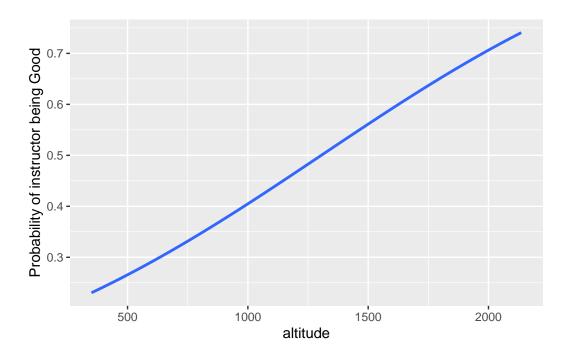
```
altitude.odds.lower <- exp(altitude.logodds.lower)
altitude.odds.upper <- exp(altitude.logodds.upper)

# Display the confidence interval
paste("(", altitude.odds.lower, ",", altitude.odds.upper, ")")</pre>
```

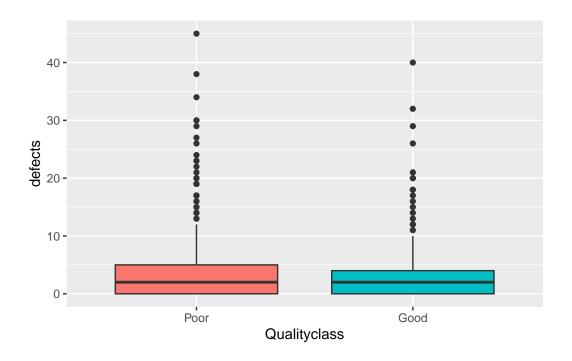
# [1] "( 1.00083868049254 , 1.00168917949219 )"

# Odds (Good instructor)





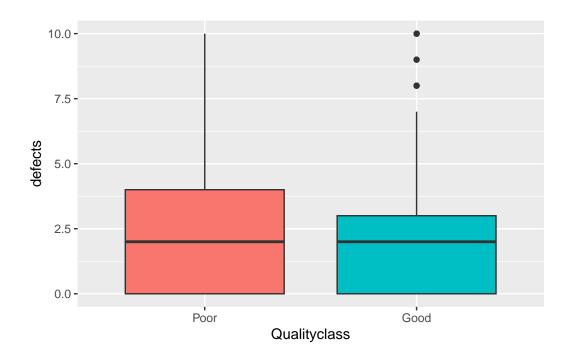
# 2.5 Category 2 type defects and Qualityclass



```
# Calculate quartiles and determine lower and upper bounds
q1_defect <- quantile(data_defects$category_two_defects, 0.25)
q3_defect <- quantile(data_defects$category_two_defects, 0.75)
iqr_defect <- q3_defect - q1_defect
lower_bound_defect <- q1_defect - 1.5 * iqr_defect
upper_bound_defect <- q3_defect + 1.5 * iqr_defect

# Filter 'category_two_defects' within the calculated bounds
data_defects_filtered <- data_defects %>%
    filter(category_two_defects >= lower_bound_defect & category_two_defects <= upper_bound_

# Create a boxplot of 'category_two_defects'
p10 <- ggplot(data = data_defects_filtered, aes(x = Qualityclass, y = category_two_defects
    geom_boxplot() +
    labs(x = "Qualityclass", y = "defects")+
    theme(legend.position = "none")
p10</pre>
```



### Call:

```
glm(formula = Qualityclass ~ category_two_defects, family = binomial(link = "logit"),
    data = data_defects_filtered)
```

### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)

(Intercept) 0.25514 0.09676 2.637 0.00837 **

category_two_defects -0.07499 0.02798 -2.680 0.00736 **
---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)
```

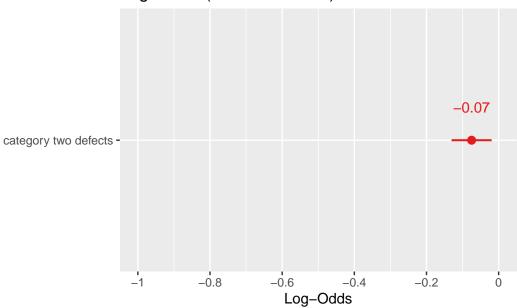
Null deviance: 1159.2 on 836 degrees of freedom Residual deviance: 1151.9 on 835 degrees of freedom

#### AIC: 1155.9

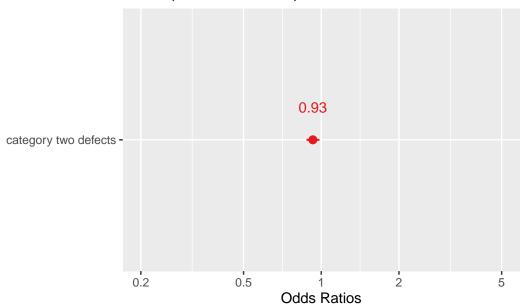
### Number of Fisher Scoring iterations: 3

# Log-Odds (Good instructor)

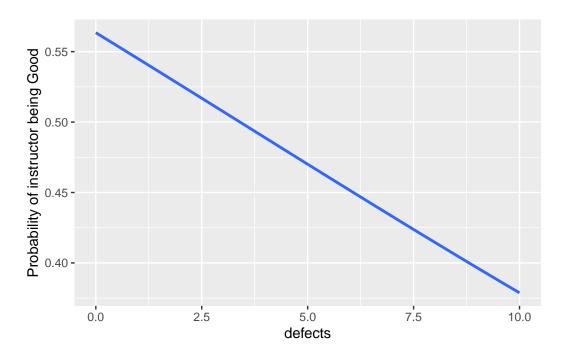
title = "Log-Odds (Good instructor)", show.p = FALSE)



# Odds (Good instructor)

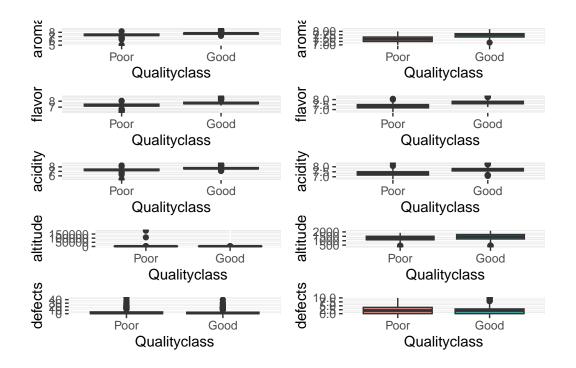


title = "Odds (Good instructor)", show.p = FALSE)



# 3 Stepwise Predictor Reduction in Model Fitting

```
# Arrange multiple plots
grid.arrange(p1, p2, p3, p4, p5, p6, p7, p8, p9, p10, ncol=2)
```



#### Call:

```
glm(formula = Qualityclass ~ aroma + flavor + acidity + category_two_defects +
    altitude_mean_meters, family = binomial(link = "logit"),
    data = data)
```

#### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept)
                     -1.193e+02 8.681e+00 -13.747 < 2e-16 ***
                                            6.994 2.68e-12 ***
                     4.817e+00
                                6.888e-01
aroma
flavor
                     6.913e+00
                                8.469e-01
                                            8.163 3.27e-16 ***
acidity
                     4.071e+00
                                6.820e-01
                                            5.969 2.39e-09 ***
category_two_defects 1.591e-02
                                2.777e-02
                                            0.573
                                                     0.567
altitude_mean_meters -7.169e-06
                                2.579e-05
                                           -0.278
                                                     0.781
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 1239.28 on 893 degrees of freedom Residual deviance: 532.21 on 888 degrees of freedom
```

AIC: 544.21

Number of Fisher Scoring iterations: 7

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
1239.28	893	-266.11	544.21	572.99	532.21	888	894

Due to the non-significant p-values of 'category two defects' and 'altitude mean meters', these two variables are removed.

#### Call:

```
glm(formula = Qualityclass ~ aroma + flavor + acidity, family = binomial(link = "logit"),
    data = data)
```

#### Coefficients:

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1239.28 on 893 degrees of freedom Residual deviance: 532.67 on 890 degrees of freedom

AIC: 540.67

Number of Fisher Scoring iterations: 7

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
1239.28	893	-266.34	540.67	559.85	532.67	890	894

Try reducing one predictor to see if it improves the model.

#### Call:

```
glm(formula = Qualityclass ~ flavor + acidity, family = binomial(link = "logit"),
    data = data)
```

#### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)

(Intercept) -95.7956     6.8135 -14.060 < 2e-16 ***

flavor     8.4212     0.7767     10.842 < 2e-16 ***

acidity     4.2916     0.6352     6.756     1.42e-11 ***

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1239.28 on 893 degrees of freedom Residual deviance: 596.77 on 891 degrees of freedom

AIC: 602.77

Number of Fisher Scoring iterations: 6

_	null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
	1239.28	893	-298.38	602.77	617.15	596.77	891	894

#### Call:

```
glm(formula = Qualityclass ~ aroma + acidity, family = binomial(link = "logit"),
    data = data)
```

### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept) -96.6561 6.7407 -14.34 <2e-16 ***
aroma 6.5855 0.6308 10.44 <2e-16 ***
acidity 6.2039 0.6015 10.31 <2e-16 ***
```

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1239.28 on 893 degrees of freedom Residual deviance: 619.97 on 891 degrees of freedom

AIC: 625.97

### Number of Fisher Scoring iterations: 6

null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
1239.28	893	-309.99	625.97	640.36	619.97	891	894

#### Call:

```
glm(formula = Qualityclass ~ aroma + flavor, family = binomial(link = "logit"),
    data = data)
```

#### Coefficients:

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 1239.28 on 893 degrees of freedom Residual deviance: 573.05 on 891 degrees of freedom

AIC: 579.05

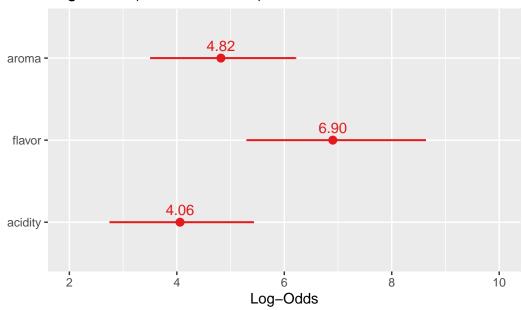
Number of Fisher Scoring iterations: 7

•	null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
	1239.28	893	-286.52	579.05	593.44	573.05	891	894

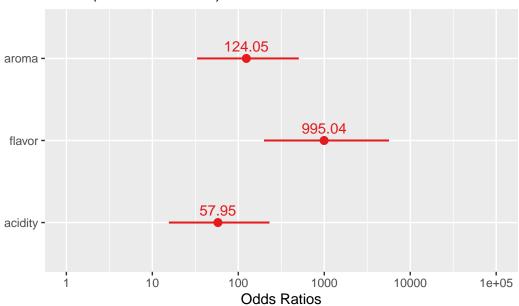
Based on the AIC and BIC values of the above models, it can be concluded that the model with 'aroma', 'flavor', and 'acidity' as predictors is optimal.

Plotting the log-odds and odds of the final model allows for a visual representation of the relationship between the predictors and the response variable.

### Log-Odds (Good instructor)



# Odds (Good instructor)



```
aroma flavor acidity
aroma 1.0000000 0.7423400 0.6005359
flavor 0.7423400 1.0000000 0.7555133
acidity 0.6005359 0.7555133 1.0000000
```

# 4 Principal Component Analysis

Based on the correlation matrix above, it is evident that the predictors exhibit high correlation. Therefore, we adopt principal component analysis (PCA) to help address multicollinearity, thereby enhancing the stability and interpretability of the model.

```
# Perform principal component analysis (PCA)
  data_pca <- data %>%
    select(aroma, flavor, acidity, Qualityclass)
  data_scaled <- scale(data_pca[, -4])</pre>
  pca_result <- prcomp(data_scaled)</pre>
  pca_result
Standard deviations (1, .., p=3):
[1] 1.5495698 0.6322373 0.4462169
Rotation (n \times k) = (3 \times 3):
               PC1
                            PC2
        -0.5620910 0.72400462 0.3998387
aroma
flavor -0.6030176 -0.02787715 -0.7972406
acidity -0.5660595 -0.68923158 0.4522570
  summary(pca_result)
Importance of components:
                           PC1
                                  PC2
                                           PC3
Standard deviation
                        1.5496 0.6322 0.44622
Proportion of Variance 0.8004 0.1332 0.06637
Cumulative Proportion 0.8004 0.9336 1.00000
  # Predict PCA components
  pca_result_selected <- predict(pca_result, newdata = data_scaled)</pre>
  pca_result_selected_df <- as.data.frame(pca_result_selected)</pre>
  # Combine PCA components with Qualityclass
  data_pca_final <- pca_result_selected_df %>%
    mutate(Qualityclass = data_pca$Qualityclass)
  # Fit logistic regression model with PCA components
  pca_model <- glm(Qualityclass ~ ., data = data_pca_final, family = binomial(link = "logit"</pre>
  pca_model_summary <- glance(pca_model)</pre>
  kable(pca_model_summary,digits =2)
```

•	null.deviance	df.null	logLik	AIC	BIC	deviance	df.residual	nobs
	1239.28	893	-266.34	540.67	559.85	532.67	890	894

The cumulative proportion of the three predictor variables adds up to 1, indicating that these three principal components fully explain the variability in the original data without losing information. Therefore, adopting principal component analysis is justified.

Meanwhile, the AIC and BIC values have remained unchanged, and they are still significantly lower than those of other models. This suggests that the three predictors in the original model have already provided the best explanatory power for the response variable. Therefore, the model with three predictors: 'aroma', 'flavor', and 'acidity' is optimal.

Qualityclass = 
$$\beta_0 + \beta_1 \times \text{aroma} + \beta_2 \times \text{flavor} + \beta_3 \times \text{acidity} + \epsilon$$

- Qualityclass is the response variable
- aroma, flavor, and acidity are the predictor variables
- $\beta_0$  to  $\beta_3$  are the coefficients of the model
- $\epsilon$  is the error term