

参考数列

$$x_0 = \{x_0(k) \mid k=1, 2, \dots, n\} = (x_0(1), x_0(2), \dots, x_0(n))$$

有 m 个比较数列

$$x_i = \{x_i(k) \mid \underbrace{k=1, 2, \dots, n}_{\text{时刻}}\} = (x_i(1), \dots, x_i(n)) \quad i=1, \dots, m$$

关联系数: $\varepsilon_k = \frac{\min_s \min_t |x_0(t) - x_s(t)| + \rho \max_s \max_t |x_0(t) - x_s(t)|}{|x_0(k) - x_i(k)| + \rho \max_s \max_t |x_0(t) - x_s(t)|}$

关联系数 $\in [0, 1]$

两两取差

两两最大差

$$x_i \text{ 对 } x_0 \text{ 的关联度: } r_i = \frac{1}{n} \sum_{k=1}^n \varepsilon_i(k)$$

实例

① 计算关联度前, 要对数据进行初始化处理 $x = (x(1), x(2), \dots, x(n))$

1) 初始化数列 $\bar{x} = [1, \frac{x(2)}{x(1)}, \dots, \frac{x(n)}{x(1)}]$

└ 数

对列序的数列 (数越小越好)

$$x_i = [1, \frac{x_i(1)}{x_i(2)}, \dots, \frac{x_i(1)}{x_i(n)}]$$

r 越大, 相关性越大.

但要判断正负关联, 要用

$$\sigma = \sum_{k=1}^n k x_i(k) - \sum_{k=1}^n x_i(k) \sum_{k=1}^n \frac{k}{n}$$

$$i=1, 2, \dots, n$$

$\text{sign}(\sigma_i) = \text{sign}(\sigma_j)$ 为正关联