### Kyrgyz Republic, Bishkek

# FACULTY OF ENGINEERING AND COMPUTER SCIENCE DEPARTMENT OF APPLIED MATHEMATICS AND INFORMATICS

#### OUTLINE FOR THE DISCRETE MATHEMATICS II

Instructor:	
Dr. Remudin Reshid MEKURIA	
Program:	${\bf Undergraduate}$
Year:	Freshman
Cr. hr.:	$6.0   \mathrm{hrs/week}$
Department taking the course:	Applied Maths and Informatics

# Course Objectives

Students should learn a particular set of mathematical facts and how to apply them; more importantly, such a course should teach students how to think logically and mathematically. To achieve these goals, this course stresses on the mathematical reasoning and the different ways problems are solved. Five important themes are interwoven in this text: mathematical reasoning, combinatorial analysis, discrete structures, algorithmic thinking, and applications and modeling. A successful discrete mathematics course should carefully blend and balance all the five themes.

# Course Descriptions

Mathematical Reasoning: Students must understand mathematical reasoning in order to read, comprehend, and construct mathematical arguments. This text starts with a discussion of mathematical logic, which serves as the foundation for the subsequent discussions of methods of proof. Both the science and the art of constructing proofs are addressed.

## Learning Outcomes

#### The students will be able to

- express a logical sentence in terms of predicates, quantifiers, and logical connectives.
- write an argument using logical notation and determine if the argument is or is not valid.
- prove basic set inequalities.
- apply counting principles to determine probabilities.
- **demonstrate** an understanding of relations and functions and able to determine their properties.
- apply the rules of inference and methods of proof including direct and indirect proof strategies, proof by contradictions, and using the principles of mathematical inductions.

### Structure of the Lectures

#### Week 1:

- Lecture 1: Recursive Algorithms and Program Correctness
- Lecture 2: Solving examples

### Week 2: Counting

- Lecture 1: The Basics of Counting
- Lecture 2: The Pigeonhole Principle

#### Week 3:Counting (cont.)

- Lecture 1: Permutations and Combinations
- Lecture 2: Solved Problems

#### Week 4:

- Lecture 1: Binomial Coefficients, Generalized Permutations and Combinations
- Lecture 2: Generating Permutations and Combinations

#### Week 5: Discrete Probability

• Lecture 1: An Introduction to Discrete Probability, Probability
Theory

• Lecture 2: Bayes' Theorem, Expected Value and Variance

#### Week 6: Advanced Counting Techniques

- Lecture 1: Recurrence Relations, Solving Recurrence Relations
- Lecture 2: Divide-and-Conquer Algorithms and Recurrence Relations, Generating Functions

#### Week 7: Advanced Counting Techniques (cont.)

- Lecture 1: Inclusion-Exclusion, Applications of Inclusion-Exclusion
- Lecture 2: Solved Problems

Week 8: Preparation for the mid term Exam: revision of previous lessons and solving problems.

#### Week 9: Relations

- Lecture 1: Relations and Their Properties
- Lecture 2: n-ary Relations and Their Applications

#### Week 10: Relations (cont.)

- Lecture 1: Representing Relations
- Lecture 2: Closures of Relations

#### Week 11: Relations (cont.)

- Lecture 1: Equivalence Relations
- Lecture 2: Partial Orderings

#### Week 12: Graphs

- Lecture 1: Graphs and Graph Models
- Lecture 2: Graph Terminology

### Week 13: Graphs (cont.)

- Lecture 1: Representing Graphs and Graph Isomorphism
- Lecture 2: Connectivity

#### Week 14: Graphs (cont.)

- Lecture 1: Euler and Hamilton Paths
- Lecture 2: Shortest-Path Problems

### Week 15: Graphs (cont.)

- Lecture 1: Planar Graphs
- Lecture 2: Graph Coloring

Week 16: Preparation for the final term Exam: course revision and solving problems.

# Teaching Materials

**Text Book:** Discrete Mathematics and Its Applications  $7^{th}$  Edition by Kenneth H. Rosen.

#### Reference Books:

- 1. Essentials of Discrete Mathematics  $3^{rd}$  Edition by David J. Hunter
- 2. Journey into Discrete Mathematics by Owen D. Byer, Deirdre L. Smeltzer, and Kenneth L. Wantz
- 3. Discrete Mathematics: A First Course by Alexander Stanoyevitch

### Lecture Videos and Web Pages:

All lectures have been recorded and they are accessible from OCS.

Several web page links are also available on the OCS for the respective

lessons.

# Evaluation and Assessment Types

• Mid Term Exam 15%

• Final Term Exam 25%

• Qu	izzes (continuous assessment)	50%
• Ass	signments	10%