# The Vector problems

Coding the Matrix, 2015

For auto-graded problems, edit the file The\_Vector\_problems.py to include your solution.

### Vector Addition Practice

**Problem 1:** For vectors v = [-1, 3] and u = [0, 4], find the vectors v + u, v - u, and 3v - 2u.

**Problem 2:** Given the vectors v = [2, -1, 5] and u = [-1, 1, 1], find the vectors v + u, v - u, 2v - u, and v + 2u.

**Problem 3:** For the vectors v = [0, one, one] and u = [one, one, one] over GF(2), find v + u and v + u + u.

## Expressing one GF(2) vector as a sum of others

**Problem 4:** Here are six 7-vectors over GF(2):

For each of the following vectors u, find a subset of the above vectors whose sum is u, or report that no such subset exists. You should be able to do this without the help of a computer.

- 1. u = 0010010
- 2. u = 0100010

**Problem 5:** Here are six 7-vectors over GF(2):

For each of the following vectors u, find a subset of the above vectors whose sum is u, or report that no such subset exists.

- 1. u = 0010010
- 2. u = 0100010

**Problem 6:** (You should be able to solve this problem without using a computer.) Find a vector  $\mathbf{x} = [x_1, x_2, x_3, x_4]$  over GF(2) satisfying the following linear equations:

$$1100 \cdot \boldsymbol{x} = 1$$

$$1010 \cdot \boldsymbol{x} = 1$$

$$1111 \cdot \boldsymbol{x} = 1$$

Verify for yourself that x + 1111 also satisfies the equations.

#### Problem 7: Consider the equations

Your job is not to solve these equations but to formulate them using dot-product. In particular, come up with three vectors v1, v2, and v3 represented as lists so that the above equations are equivalent to

$$v1 \cdot x = 10$$

$$v2 \cdot x = 35$$

$$v3 \cdot x = 8$$

where x is a 4-vector over  $\mathbb{R}$ .

### Practice with Dot-Product

**Problem 8:** For each of the following pairs of vectors u and v over  $\mathbb{R}$ , evaluate the expression  $u \cdot v$ :

(a) 
$$u = [1, 0], v = [5, 4321]$$

(b) 
$$\mathbf{u} = [0, 1], \mathbf{v} = [12345, 6]$$

(c) 
$$u = [-1, 3], v = [5, 7]$$

(d) 
$$u = [-\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}], v = [\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}]$$