

Instructions to run the code:

Compile c++ code in GNU G++17 7.3.0 or similar

Input must be named "input.def" and it will be generated an "out.txt" text file, you can change this part of the code.

Algorithm:

- (1) Read the input and keep coordinates, name and out/in drivers in a vector
- (2) Generate the cluster (k-mean optimized) $O(n)$.:
 - (2.1) We get 16 random centers for the 16 clusters.
 - (2.2) We connect every point with its nearest cluster center in $O(n)$ (Voronoi Diagrams).
 - (2.3) We get the mean of every set of points with an amortized quick search in $O(n)$.
 - (2.4) Repete (2.2) and (2.3) until clusters get stable (30 times).
- (3) For every cluster, we will find an optimal path with Square Root Decomposition $O(n \log^2(n))$:
 - (3.1) Sort point by x/y (two iterations, keep the best).
 - (3.2) Sort point as in MO's algorithm but in 2D in $O(n \log n)$ (blocks by y , sort by x).
 - (3.3) Notice that blocks are not Square Root decomposition, to get the size of the blocks, we multiply \sqrt{n} by x , where we do golden ratio ternary search to get optimal x in optimal time (do not have time to implement, but the solution is quite improved).
 - (3.4) We connect every point in the order of the vector.
- (4) Connect drivers and clusters in $O(1)$:
 - (4.1) Sort points and divers by y and connect them in order.
- (5) Give the output.

The total time complexity of the algorithm is $O(n)$ *amortized* and the space complexity is $O(n)$