### **Graph algorithms**

Given a transport network of n cities (1 <= n <=1000000) and roads between them write algorithms that solve problems:

- 1) Finding path between given two cities that passes through least number of other cities.
- 2) Finding path between given two cities that has the shortest total distance (standard algorithm)
- 3) Finding path between given two cities that has the shortest total distance (use geographical heuristic)

Compare algorithms execution time for given data.

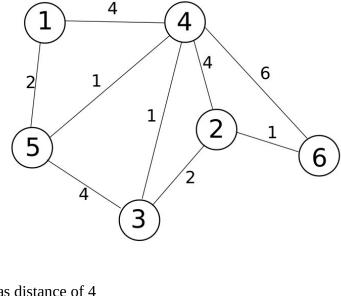
## Input:

In the first line there are two integers n and m (1<=n<=1000, 1<=m<=100000) meaning number of cities and number of roads between them. In the next n lines there are coords of cities (numbered from 1 to *n*): latitude and longitude. In the next *m* lines road descriptions are given: in each line three numbers: v1, v2 and w. They mean there is a road between cities v1 and v2 (undirected graph, both directions) and its distance is w. In the last line starting and ending cities (s and e) are given.

#### **Output:**

In the first line a path length for algorithm variant 1) is given. In the second line vertices on the path are given (separated by spaces). In the third line a path length for variant 2) is given and in the

fourth line its vertices (separated by spaces)



# **Example:** (graph illustrated below)

```
Input:
69
       // 6 vertices, 9 edges
55 16 // exemplary coords of 6 cities
54.30 18.20
53.70 17
54.5 18
53 15.50
```

144 // road between city 1 and city 4 has distance of 4 152 // road between city 1 and 5 has distance of 2 232 //etc 244 261 341 354 451

466 // path from 1 to 6 16

### Output:

53.50 19.3

// the path from 1 to 6 that passes through least other cities has only one city on path. 1 146 // the path // the shortest path from 1 to 6 (in terms of distances sum) has length of 7

7

// the path 154326