

## Graph algorithms

Given a transport network of  $n$  cities ( $1 \leq n \leq 1000000$ ) and roads between them write algorithms that solve problems:

- 1) Finding path between given two cities that passes through least number of other cities.
- 2) Finding path between given two cities that has the shortest total distance (standard algorithm)
- 3) Finding path between given two cities that has the shortest total distance (use geographical heuristic)

Compare algorithms execution time for given data.

### Input:

In the first line there are two integers  $n$  and  $m$  ( $1 \leq n \leq 1000$ ,  $1 \leq m \leq 100000$ ) meaning number of cities and number of roads between them. In the next  $n$  lines there are coords of cities (numbered from 1 to  $n$ ): latitude and longitude. In the next  $m$  lines road descriptions are given: in each line three numbers:  $v1$ ,  $v2$  and  $w$ . They mean there is a road between cities  $v1$  and  $v2$  (undirected graph, both directions) and its distance is  $w$ . In the last line starting and ending cities ( $s$  and  $e$ ) are given.

### Output:

In the first line a path length for algorithm variant 1) is given. In the second line vertices on the path are given (separated by spaces). In the third line a path length for variant 2) is given and in the fourth line its vertices (separated by spaces)

### Example: (graph illustrated below)

Input:

```
6 9 // 6 vertices, 9 edges
55 16 // exemplary coords of 6 cities
54.30 18.20
53.70 17
54.5 18
53 15.50
53.50 19.3
1 4 4 // road between city 1 and city 4 has distance of 4
1 5 2 // road between city 1 and 5 has distance of 2
2 3 2 //etc
2 4 4
2 6 1
3 4 1
3 5 4
4 5 1
4 6 6
1 6 // path from 1 to 6
```

Output:

```
1 // the path from 1 to 6 that passes through least other cities has only one city on path.
1 4 6 // the path
7 // the shortest path from 1 to 6 (in terms of distances sum) has length of 7
1 5 4 3 2 6 // the path
```



