

PPGEE2249 - Aprendizagem de Máquina

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$$\textcircled{1} a) \text{ "+1"} \quad f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}(x-2)^2} = p(x|C_{+1})$$

$$\text{"-1"} \quad f(x) = \begin{cases} 1/4 & -2 < x < 2 \\ 0 & \text{otherwise} \end{cases} = p(x|C_{-1})$$

Bayes Rule

$$P(C|x) = \frac{P(C)p(x|C)}{p(x)}$$

Decision

$$\text{choose } C_i \text{ if } P(C_i|x) = \max_k P(C_k|x) = \max_k P(C_k) \cdot p(x|C_k)$$

$$\text{"+1"} \text{ if } 0,6 \cdot \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}(x-2)^2} > 0,4 \cdot \frac{1}{4}$$

$$\text{"-1"} \text{ if } 0,4 \cdot \frac{1}{4} > 0,6 \cdot \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}(x-2)^2}$$

b) Decision rule:

$$p(x|C_{+1}) > \frac{1}{6}$$

$$\frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}(x-2)^2} > \frac{1}{6}$$