

Chapter04 Gradient Descent

1. Learning Rate

Vanilla Gradient Descent: $\theta^i = \theta^{i-1} - \eta \nabla L(\theta^{i-1})$

2. Adagrad

- a) Divide the learning rate of each parameter by the root mean square of its previous derivatives

$$b) w^{t+1} = w^t - \frac{\eta^t}{\sigma^t} g^t \quad \eta^t = \frac{\eta}{\sqrt{t+1}} \quad \sigma^t = \sqrt{\frac{1}{t+1} \sum_{i=0}^t (g^i)^2}$$

$$c) w^{t+1} = w^t - \frac{\eta}{\sqrt{\sum_{i=0}^t (g^i)^2}} g^t$$

$$d) \text{ The best step is: } \frac{|First\ Derivative|}{|Second\ Derivative|}$$

3. Stochastic Gradient Descent

- a) Make the training faster
b) Loss for only one example

4. Feature Scaling

- a) $y = b + w_1 x_1 + w_2 x_2$ make different features have the same scaling
b) $x_r^i = \frac{x_r^i - m_i}{\sigma_i}$

Chapter05 Classification

1. Classification as Regression: Penalize to the examples that are "too correct"

$$2. P(C_1|x) = \frac{P(x|C_1)P(C_1)}{P(x|C_1)P(C_1) + P(x|C_2)P(C_2)}$$

3. Using maximum likelihood to get $P(x|C_1)$ and $P(x|C_2)$: The Gaussian with mean μ and covariance matrix Σ can generate all the points, likelihood function is written as: $L(\mu, \Sigma) = \prod f_{\mu, \Sigma}(x_i)$ $\mu^*, \Sigma^* = \argmax L(\mu, \Sigma)$
 $\mu^* = \text{average}(x_i)$ $\Sigma^* = \text{average}(x_i - \mu^*)(x_i - \mu^*)^T$

4. To get better performance, we usually use the same covariance matrix

- a) $\Sigma = \text{weighted_average}(\Sigma_1, \Sigma_2)$
b) The modified model's boundary line is linear

5. Posterior Probability

$$a) P(C_1|x) = \frac{P(x|C_1)P(C_1)}{P(x|C_1)P(C_1) + P(x|C_2)P(C_2)} = \frac{1}{1 + \exp(-z)} = \sigma(z) = \sigma(w \cdot x + b)$$

$$b) z = \ln \frac{P(x|C_1)P(C_1)}{P(x|C_2)P(C_2)} = w^T x + b$$

$$w^T = (\mu^1 - \mu^2)^T \Sigma^{-1} \quad b = \ln \frac{N_1}{N_2} + \frac{1}{2} ((\mu^2)^T \Sigma^{-1} \mu^2 - (\mu^1)^T \Sigma^{-1} \mu^1)$$