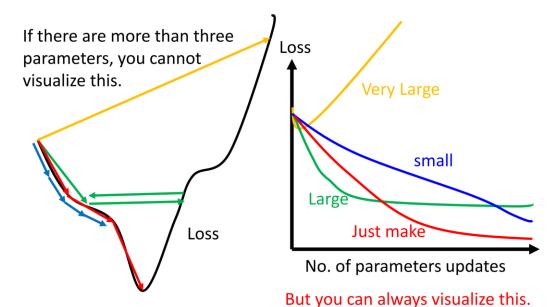
$$\theta^{i} = \theta^{i-1} - \eta \nabla L(\theta^{i-1})$$

Set the learning rate η carefully



$$\eta^t = \frac{\eta}{\sqrt{t+1}}$$
 $g^t = \frac{\partial L(\theta^t)}{\partial w}$

• Divide the learning rate of each parameter by the root mean square of its previous derivatives

Vanilla Gradient descent

$$w^{t+1} \leftarrow w^t - \eta^t g^t$$

w is one parameters

Adagrad

$$w^{t+1} \leftarrow w^t - \frac{\eta^t}{\sigma^t} g^t$$

 σ^t : **root mean square** of the previous derivatives of parameter w

Parameter dependent

Adagrad

 σ^t : **root mean square** of the previous derivatives of parameter w

$$w^{1} \leftarrow w^{0} - \frac{\eta^{0}}{\sigma^{0}} g^{0} \qquad \sigma^{0} = \sqrt{(g^{0})^{2}}$$

$$w^{2} \leftarrow w^{1} - \frac{\eta^{1}}{\sigma^{1}} g^{1} \qquad \sigma^{1} = \sqrt{\frac{1}{2} [(g^{0})^{2} + (g^{1})^{2}]}$$

$$w^{3} \leftarrow w^{2} - \frac{\eta^{2}}{\sigma^{2}} g^{2} \qquad \sigma^{2} = \sqrt{\frac{1}{3} [(g^{0})^{2} + (g^{1})^{2} + (g^{2})^{2}]}$$

$$\vdots$$

$$w^{t+1} \leftarrow w^{t} - \frac{\eta^{t}}{\sigma^{t}} g^{t} \qquad \sigma^{t} = \sqrt{\frac{1}{t+1} \sum_{i=0}^{t} (g^{i})^{2}}$$

Adagrad

 Divide the learning rate of each parameter by the root mean square of its previous derivatives

$$w^{t+1} \leftarrow w^t - \frac{\eta^t}{\sigma^t} g^t$$

$$\sigma^t = \sqrt{\frac{1}{t+1}} \sum_{i=0}^t (g^i)^2$$

$$w^{t+1} \leftarrow w^t - \frac{\eta}{\sqrt{\sum_{i=0}^t (g^i)^2}} g^t$$

Second Derivative

