## Chapter12 Semi-Supervised Learning

- 1. Introduction
  - a) Transductive Learning: Unlabeled data is the testing data
  - b) Inductive Learning: Unlabeled data is not the testing data
  - c) Collecting data is easy, but collecting 'labeled' data is expensive
  - d) We do semi-supervised learning in our lives
  - e) The distribution of the unlabeled data tells us something
- 2. Generative Model
  - a) Supervised Generative model
    - i) Prior Probability:  $P(C_i)$  Class-Dependent Probability:  $P(x|C_i)$
    - ii)  $P(x|C_i)$  is a Gaussian distribution parameterized by  $\mu_i$  and  $\Sigma$

iii) 
$$P(C_1|x) = \frac{P(x|C_1)P(C_1)}{P(x|C_1)P(C_1) + P(x|C_2)P(C_2)}$$

- a) Semi-Supervised Generative Model
  - i) The unlabeled data  $x^u$  help re-estimate  $P(C_1), P(C_2), \mu_1, \mu_2, \Sigma$
  - ii) E-M Algorithm

Step1: Compute the posterior probability of unlabeled data Step2: Update Model

- 3. Low-density Separation Assumption: Black or white
  - a) Self-Training
    - i) Train model  $f^*$  from labeled data set
    - ii) Apply  $f^*$  to the unlabeled data, obtain  $\{(x^u, y^u)\}_{u=R}^{R+U}$  (Pseudo Label)
    - iii) Remove a set of data from unlabeled set, and add them into labeled set
    - iv) Self-training uses hard label, and generative model uses soft label
  - b) Entropy-based Regularization
    - i) Entropy of  $y^u$ : evaluate how concentrate the distribution  $y^u$  is
    - ii)  $E(y^u) = -\sum_{m=1}^5 y_m^u \ln(y_m^u)$  should be as small as possible
    - iii)  $L = \sum_{x^r} C(y^r, \hat{y}^r) + \lambda \sum_{x^u} E(y^u)$
  - c) Semi-supervised SVM
    - i) Enumerate all possible labels for the unlabeled data
    - ii) Find a boundary that can provide the largest margin and least error
- 4. Smoothness Assumption: You are known by the company you keep
  - a) Smoothness Assumption
    - i) Assumption: "similar" x has the same  $\hat{y}$
    - ii) More precisely:

x is not uniform

If  $x^1$  and  $x^2$  are close in a high-density region,  $\hat{y}^1$  and  $\hat{y}^2$  are same

- b) Cluster and then label
- c) Graph-based Approach
  - Represent the data points as a graph
  - ii) Graph representation is nature sometimes

Hyperlink of webpages

Citation of papers

iii) Sometimes you have to construct the graph yourself

- iv) Define the similarity  $s(x^i, x^j)$  between  $x^i$  and  $x^j$ 
  - K Nearest Neighbor
  - e-Neighborhood
- v) Labeled data influence their neighbors, propagate through the graph
- vi) Define the smoothness of labels on the graph

$$S = \frac{1}{2} \sum_{i,j} w_{i,j} (y^i - y^j)^2 = y^T L y$$

Smaller means smoother

$$L = \sum_{x^r} C(y^r, \hat{y}^r) + \lambda S$$

- 5. Better Representation
  - a) Find the latent factors behind the observation
  - b) the latent factors are better representations

## Chapter13 Deep Auto-Encoder

- 1. Auto-Encoder
  - a) Compact representation of the input object
  - b) Reconstruct the original object
- 2. PCA
  - a) Bottleneck layer
  - b) Decoding matrix is the transpose of the encoding matrix
- 3. Deep Auto-Encoder
  - a) De-noising auto-encoder
  - b) Text-Retrieval
    - i) Vector Space Model
    - ii) The documents talking about the same thing will have close code
  - c) Similar Image Search
- 4. Auto-Encoder for CNN
  - a) Unpooling
    - i) Alternative: simply repeat the values
  - b) Deconvolution
    - i) Actually, deconvolution is convolution
- 5. Pre-train DNN