

# Sensitivity Analysis: Non-Spatial Models

Alvin Sheng

## Contents

<b>Modeling Set-up</b>	<b>2</b>
Helper Functions . . . . .	3
<b>CAR model results, Coronary Heart Disease Stratified on RPL_THEMES</b>	<b>3</b>
Credible Interval plots for the coefficients, in ggplot . . . . .	5
<b>CAR model results, High Blood Pressure Stratified on RPL_THEMES</b>	<b>7</b>
Credible Interval plots for the coefficients, in ggplot . . . . .	8
<b>CAR model results, Asthma Stratified on RPL_THEMES</b>	<b>11</b>
Credible Interval plots for the coefficients, in ggplot . . . . .	12
<b>CAR model results, Poor Mental Health Stratified on RPL_THEMES</b>	<b>15</b>
Credible Interval plots for the coefficients, in ggplot . . . . .	16

## Modeling Set-up

```
library(here)

## Warning in readLines(f, n): line 1 appears to contain an embedded nul
## here() starts at /Volumes/ALVINDRIVE2/flood-risk-health-effects

library(coda)
library(CARBayes)

## Loading required package: MASS
## Loading required package: Rcpp
## Registered S3 method overwritten by 'GGally':
##   method from
##   +.gg      ggplot2

library(ggplot2)
library(tidyverse)

## -- Attaching packages ----- tidyverse 1.3.1 --
## v tibble  3.1.8      v dplyr   1.0.10
## v tidyr   1.2.1      v stringr 1.4.0
## v readr   2.1.1      v forcats 0.5.1
## v purrr   0.3.4

## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()     masks stats::lag()
## x dplyr::select() masks MASS::select()

fhs_model_df <- readRDS("intermediary_data/fhs_model_df_fr_and_pollute_pc.rds")

var_names <- c("Intercept", "flood_risk_pc1", "flood_risk_pc2",
               "flood_risk_pc3", "flood_risk_pc4", "flood_risk_pc5",
               "EP_UNINSUR", "pollute_conc_pc1", "pollute_conc_pc2",
               "pollute_conc_pc3", "tmmx", "rmax", "Data_Value_CSMOKING")

names_non_spat_strat <- c(paste("strat0", var_names, sep = ":"),
                           paste("strat1", var_names, sep = ":"))

# extract the four response variables
responses <- fhs_model_df[, (ncol(fhs_model_df) - 3):ncol(fhs_model_df)]
# extract the other covariates, except the SVI variables
covariates <- select(fhs_model_df[, -((ncol(fhs_model_df) - 3):ncol(fhs_model_df))], -EP_POV,
                    -EP_UNEMP, -EP_PCI, -EP_NOHSDP,
                    -EP_AGE17, -EP_DISABL, -EP_SNGPNT,
                    -EP_MINRTY, -EP_LIMENG,
                    -EP_MUNIT, -EP_MOBILE, -EP_CROWD, -EP_NOVEH, -EP_GROUPQ)

first_var <- which(names(covariates) == "flood_risk_pc1")

strat_covariate <- fhs_model_df$RPL_THEMES

# CHD
covariates_CHD <- data.frame(covariates, Data_Value_CHD = responses$Data_Value_CHD)
```

```
# BPHIGH
covariates_BPHIGH <- data.frame(covariates, Data_Value_BPHIGH = responses$Data_Value_BPHIGH)
# CASTHMA
covariates_CASTHMA <- data.frame(covariates, Data_Value_CASTHMA = responses$Data_Value_CASTHMA)
# MHLTH
covariates_MHLTH <- data.frame(covariates, Data_Value_MHLTH = responses$Data_Value_MHLTH)
```

## Helper Functions

Function to run the stratified non-spatial model

```
source(here("scripts/sensitivity_analysis/non_spatial_strat_model.R"))
```

Function for post-processing the inference

```
pc2flip <- c(-1, 1, -1, -1, -1,
            -1, 1, -1, -1, -1)
```

```
post_flip <- function(beta_inf_subset, pc2flip) {
  names_temp <- colnames(beta_inf_subset)
  beta_inf_subset[pc2flip == -1, ] <- beta_inf_subset[pc2flip == -1, c(1, 3, 2)]
  colnames(beta_inf_subset) <- names_temp
  return(sweep(beta_inf_subset, 1, pc2flip, FUN = "*"))
}
```

```
# extract the flood risk PC coefficients
# pc_idx is the vector of indices of the flood risk PC coefficients, after splitting data frame by strata
beta_data_frames_extract <- function(beta_inference_df, pc_idx) {

  beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]

  beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df)]

  beta_pcs_strat0 <- beta_inference_df_strat0[pc_idx, ]

  beta_pcs_strat1 <- beta_inference_df_strat1[pc_idx, ]

  beta_pcs_strat0 <- mutate(beta_pcs_strat0, var_idx = factor(1:nrow(beta_pcs_strat0)))
  beta_pcs_strat1 <- mutate(beta_pcs_strat1, var_idx = factor(1:nrow(beta_pcs_strat1)))

  return(list(beta_pcs_strat0 = beta_pcs_strat0, beta_pcs_strat1 = beta_pcs_strat1))
}
```

## CAR model results, Coronary Heart Disease Stratified on RPL\_THEMES

```
chd_res <- non_spatial_strat_model(covariates_CHD, first_var, strat_covariate, strat_fn = median)
```

```

beta_results <- summary(chd_res$lm_obj)$coefficients

row.names(beta_results) <- names_non_spat_strat

beta_inference <- cbind(beta_results[, 1],
                        beta_results[, 1] - 2 * beta_results[, 2],
                        beta_results[, 1] + 2 * beta_results[, 2])

colnames(beta_inference) <- c("pt_est", "lb", "ub")

beta_inference <- round(beta_inference, 5)

pc_idx <- c(2:6,
           nrow(beta_inference)/2 + 2:6)

# flipping the inference results according to the flipped PCs
beta_inference[pc_idx, ] <- post_flip(beta_inference[pc_idx, ], pc2flip)

```

```
beta_inference
```

##	pt_est	lb	ub
## strat0:Intercept	6.20734	6.18203	6.23266
## strat0:flood_risk_pc1	0.29900	0.27898	0.31901
## strat0:flood_risk_pc2	0.12765	0.10411	0.15120
## strat0:flood_risk_pc3	0.00772	-0.01139	0.02683
## strat0:flood_risk_pc4	-0.05570	-0.07576	-0.03564
## strat0:flood_risk_pc5	0.04084	0.02105	0.06063
## strat0:EP_UNINSUR	-0.14258	-0.17638	-0.10879
## strat0:pollute_conc_pc1	-0.50207	-0.52805	-0.47609
## strat0:pollute_conc_pc2	-0.14877	-0.17189	-0.12566
## strat0:pollute_conc_pc3	-0.11643	-0.13951	-0.09334
## strat0:tmmx	0.27562	0.25326	0.29798
## strat0:rmax	0.01957	-0.00301	0.04216
## strat0:Data_Value_CSMOKING	0.90161	0.87311	0.93010
## strat1:Intercept	6.96475	6.94253	6.98696
## strat1:flood_risk_pc1	0.16400	0.14415	0.18384
## strat1:flood_risk_pc2	0.18791	0.16728	0.20854
## strat1:flood_risk_pc3	-0.00212	-0.02170	0.01746
## strat1:flood_risk_pc4	-0.08027	-0.09786	-0.06268
## strat1:flood_risk_pc5	-0.03117	-0.04901	-0.01333
## strat1:EP_UNINSUR	-0.21052	-0.22967	-0.19138
## strat1:pollute_conc_pc1	-0.37572	-0.39552	-0.35592
## strat1:pollute_conc_pc2	-0.07416	-0.09699	-0.05133
## strat1:pollute_conc_pc3	-0.12533	-0.14516	-0.10550
## strat1:tmmx	0.42498	0.40214	0.44783
## strat1:rmax	0.02574	0.00535	0.04614
## strat1:Data_Value_CSMOKING	1.19944	1.17728	1.22161

List of significant beta coefficients:

```
row.names(beta_inference)[sign(beta_inference[, 2]) == sign(beta_inference[, 3])]
```

```
## [1] "strat0:Intercept"          "strat0:flood_risk_pc1"
```

```
## [3] "strat0:flood_risk_pc2"      "strat0:flood_risk_pc4"
## [5] "strat0:flood_risk_pc5"      "strat0:EP_UNINSUR"
## [7] "strat0:pollute_conc_pc1"     "strat0:pollute_conc_pc2"
## [9] "strat0:pollute_conc_pc3"     "strat0:tmmx"
## [11] "strat0:Data_Value_CSMOKING" "strat1:Intercept"
## [13] "strat1:flood_risk_pc1"       "strat1:flood_risk_pc2"
## [15] "strat1:flood_risk_pc4"       "strat1:flood_risk_pc5"
## [17] "strat1:EP_UNINSUR"           "strat1:pollute_conc_pc1"
## [19] "strat1:pollute_conc_pc2"     "strat1:pollute_conc_pc3"
## [21] "strat1:tmmx"                 "strat1:rmax"
## [23] "strat1:Data_Value_CSMOKING"
```

## Credible Interval plots for the coefficients, in ggplot

```
# first, process the beta_inference matrix in a form ggplot can understand
beta_inference_df <- as.data.frame(beta_inference)
beta_inference_df <- mutate(beta_inference_df, var_name = row.names(beta_inference_df))
beta_inference_df$var_name <- substring(beta_inference_df$var_name, first = 8)
beta_inference_df$var_name <- factor(beta_inference_df$var_name,
                                     levels = unique(beta_inference_df$var_name))
beta_inference_df$strat <- factor(c(rep("Low SV", (nrow(beta_inference_df)/2)),
                                   rep("High SV", (nrow(beta_inference_df)/2))), levels = c("Low SV",
```

Splitting up the beta coefficients for each strata

```
beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]

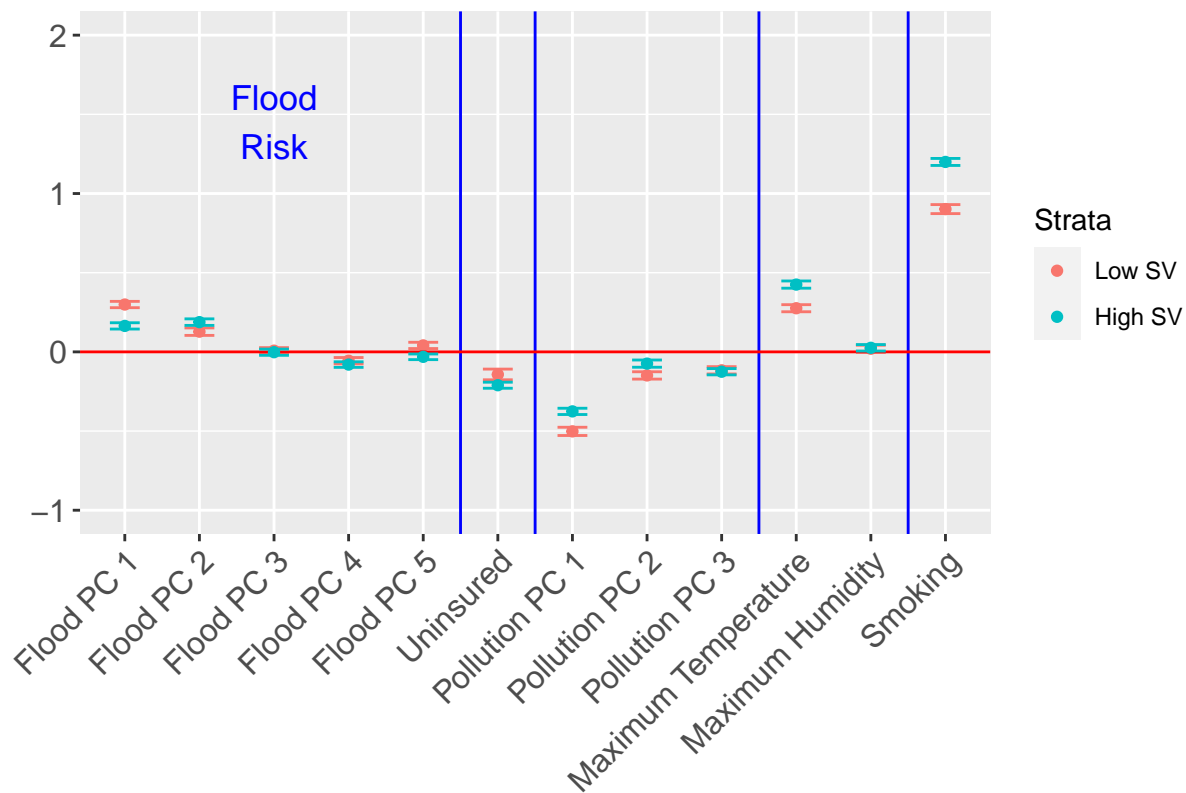
beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df),]
```

Note: The intercept for both strata is not included.

```
p <- ggplot(beta_inference_df_strat0[-1, ], aes(x = var_name, y = pt_est, color = strat)) +
  geom_point() +
  ylim(c(-1, 2)) +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis.
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_vline(xintercept = c(5.5, 6.5, 9.5, 11.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3, y = 1.45, label = "Flood\nRisk",
          col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("Flood PC 1", "Flood PC 2", "Flood PC 3", "Flood PC 4", "Flood PC 5",
                              "Uninsured",
                              "Pollution PC 1", "Pollution PC 2", "Pollution PC 3",
                              "Maximum Temperature", "Maximum Humidity",
                              "Smoking")) + ggtitle("95% Credible Intervals, CHD, Stratified on All RPL")
p <- p +
  geom_point(data = beta_inference_df_strat1[-1, ], col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_inference_df_strat1[-1, ], aes(ymin = lb, ymax = ub, width = 0.4), col = "#00BFC4") +
  scale_color_manual(name = "Strata",
                    values = c("#F8766D", "#00BFC4"),
                    drop = FALSE)
```

p

## 95% Credible Intervals, CHD, Stratified on All RPL Themes, Non-Spatial



```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/CHD_CI_rpls.pdf"),
       plot = p, device = "pdf",
       width = 8, height = 6, units = "in")
```

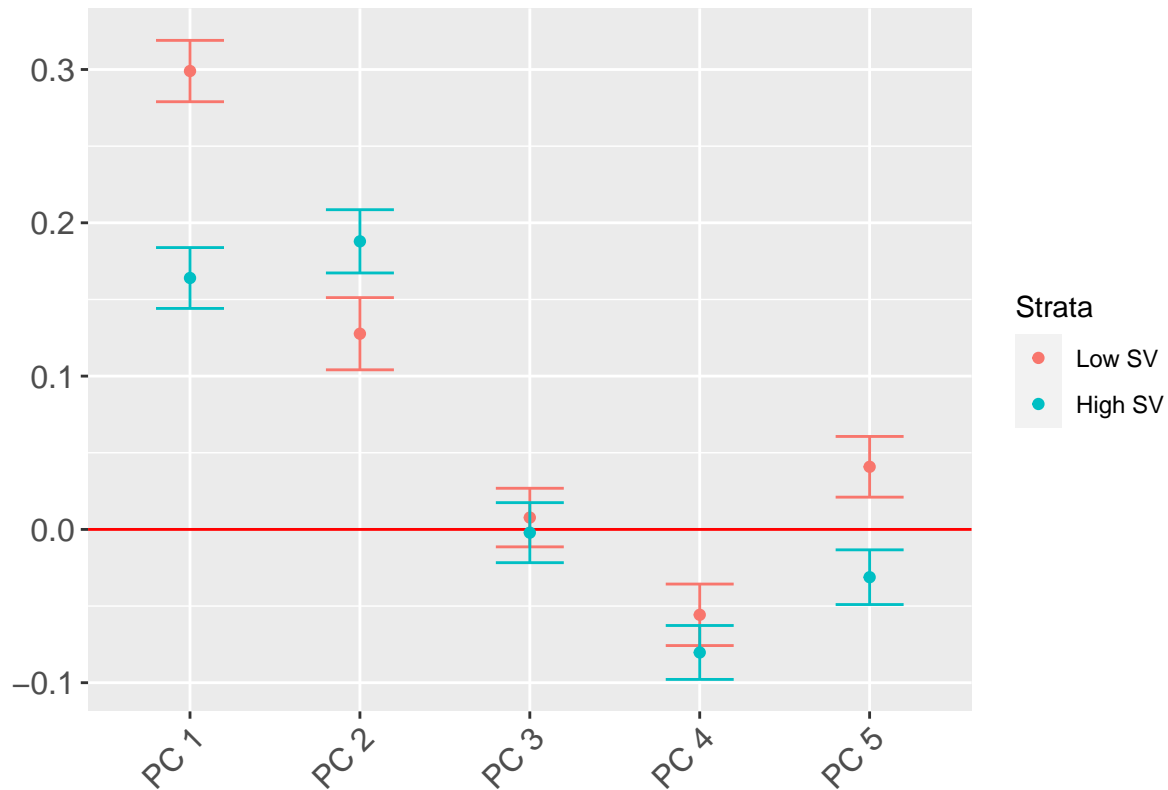
```
pc_extract_idx <- 2:6
```

```
beta_CHD_pcs <- beta_data_frames_extract(beta_inference_df, pc_extract_idx)
```

```
p <- ggplot(beta_CHD_pcs$beta_pcs_strat0, aes(x = var_idx, y = pt_est, color = strat)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis.title.y = element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_hline(yintercept = 0, col = "red") +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5"), 6) + ggtitle("95% Credible Intervals, CHD, Stratified on All RPL Themes, Non-Spatial")
  geom_point(data = beta_CHD_pcs$beta_pcs_strat1, col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_CHD_pcs$beta_pcs_strat1, aes(ymin = lb, ymax = ub, width = 0.4), col = "#00BFC4") +
  scale_color_manual(name = "Strata",
                    values = c("#F8766D", "#00BFC4"),
                    drop = FALSE)
```

p

## 95% Credible Intervals for Flood Risk PCs, Coronary Heart Disease



```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/CHD_cred_intervals_fr_only.pdf"),
       plot = p, device = "pdf",
       width = 8, height = 6, units = "in")
```

## CAR model results, High Blood Pressure Stratified on RPL\_THEMES

```
bphigh_res <- non_spatial_strat_model(covariates_BPHIGH, first_var, strat_covariate, strat_fn = median)

beta_results <- summary(bphigh_res$lm_obj)$coefficients

row.names(beta_results) <- names_non_spat_strat

beta_inference <- cbind(beta_results[, 1],
                        beta_results[, 1] - 2 * beta_results[, 2],
                        beta_results[, 1] + 2 * beta_results[, 2])

colnames(beta_inference) <- c("pt_est", "lb", "ub")

beta_inference <- round(beta_inference, 5)

pc_idx <- c(2:6,
            nrow(beta_inference)/2 + 2:6)
```

```
# flipping the inference results according to the flipped PCs
beta_inference[pc_idx, ] <- post_flip(beta_inference[pc_idx, ], pc2flip)
```

```
beta_inference
```

##	pt_est	lb	ub
## strat0:Intercept	30.73013	30.64740	30.81285
## strat0:flood_risk_pc1	0.70636	0.64096	0.77175
## strat0:flood_risk_pc2	0.30457	0.22762	0.38151
## strat0:flood_risk_pc3	0.08334	0.02089	0.14578
## strat0:flood_risk_pc4	-0.13820	-0.20375	-0.07265
## strat0:flood_risk_pc5	0.07678	0.01212	0.14145
## strat0:EP_UNINSUR	-0.42172	-0.53215	-0.31128
## strat0:pollute_conc_pc1	-1.59672	-1.68161	-1.51183
## strat0:pollute_conc_pc2	-1.17673	-1.25226	-1.10119
## strat0:pollute_conc_pc3	0.12649	0.05105	0.20193
## strat0:tmmx	1.49213	1.41908	1.56519
## strat0:rmax	0.71100	0.63720	0.78481
## strat0:Data_Value_CSMOKING	2.45027	2.35716	2.54339
## strat1:Intercept	33.13258	33.06000	33.20517
## strat1:flood_risk_pc1	-0.01265	-0.07750	0.05220
## strat1:flood_risk_pc2	0.07606	0.00864	0.14347
## strat1:flood_risk_pc3	0.13166	0.06767	0.19566
## strat1:flood_risk_pc4	0.03108	-0.02639	0.08855
## strat1:flood_risk_pc5	-0.00335	-0.06166	0.05496
## strat1:EP_UNINSUR	-0.85655	-0.91912	-0.79399
## strat1:pollute_conc_pc1	-0.62788	-0.69259	-0.56317
## strat1:pollute_conc_pc2	-1.54546	-1.62005	-1.47086
## strat1:pollute_conc_pc3	-0.66607	-0.73087	-0.60127
## strat1:tmmx	2.36678	2.29213	2.44143
## strat1:rmax	0.79117	0.72453	0.85782
## strat1:Data_Value_CSMOKING	3.88775	3.81533	3.96018

List of significant beta coefficients:

```
row.names(beta_inference)[sign(beta_inference[, 2]) == sign(beta_inference[, 3])]
```

```
## [1] "strat0:Intercept"      "strat0:flood_risk_pc1"
## [3] "strat0:flood_risk_pc2" "strat0:flood_risk_pc3"
## [5] "strat0:flood_risk_pc4" "strat0:flood_risk_pc5"
## [7] "strat0:EP_UNINSUR"    "strat0:pollute_conc_pc1"
## [9] "strat0:pollute_conc_pc2" "strat0:pollute_conc_pc3"
## [11] "strat0:tmmx"          "strat0:rmax"
## [13] "strat0:Data_Value_CSMOKING" "strat1:Intercept"
## [15] "strat1:flood_risk_pc2" "strat1:flood_risk_pc3"
## [17] "strat1:EP_UNINSUR"    "strat1:pollute_conc_pc1"
## [19] "strat1:pollute_conc_pc2" "strat1:pollute_conc_pc3"
## [21] "strat1:tmmx"          "strat1:rmax"
## [23] "strat1:Data_Value_CSMOKING"
```

## Credible Interval plots for the coefficients, in ggplot

```
# first, process the beta_inference matrix in a form ggplot can understand
beta_inference_df <- as.data.frame(beta_inference)
```



```

beta_inference_df <- mutate(beta_inference_df, var_name = row.names(beta_inference_df))
beta_inference_df$var_name <- substring(beta_inference_df$var_name, first = 8)
beta_inference_df$var_name <- factor(beta_inference_df$var_name,
                                     levels = unique(beta_inference_df$var_name))
beta_inference_df$strat <- factor(c(rep("Low SV", (nrow(beta_inference_df)/2)),
                                   rep("High SV", (nrow(beta_inference_df)/2))), levels = c("Low SV",

```

Splitting up the beta coefficients for each strata

```

beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]

beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df),]

```

Note: The intercept for both strata is not included.

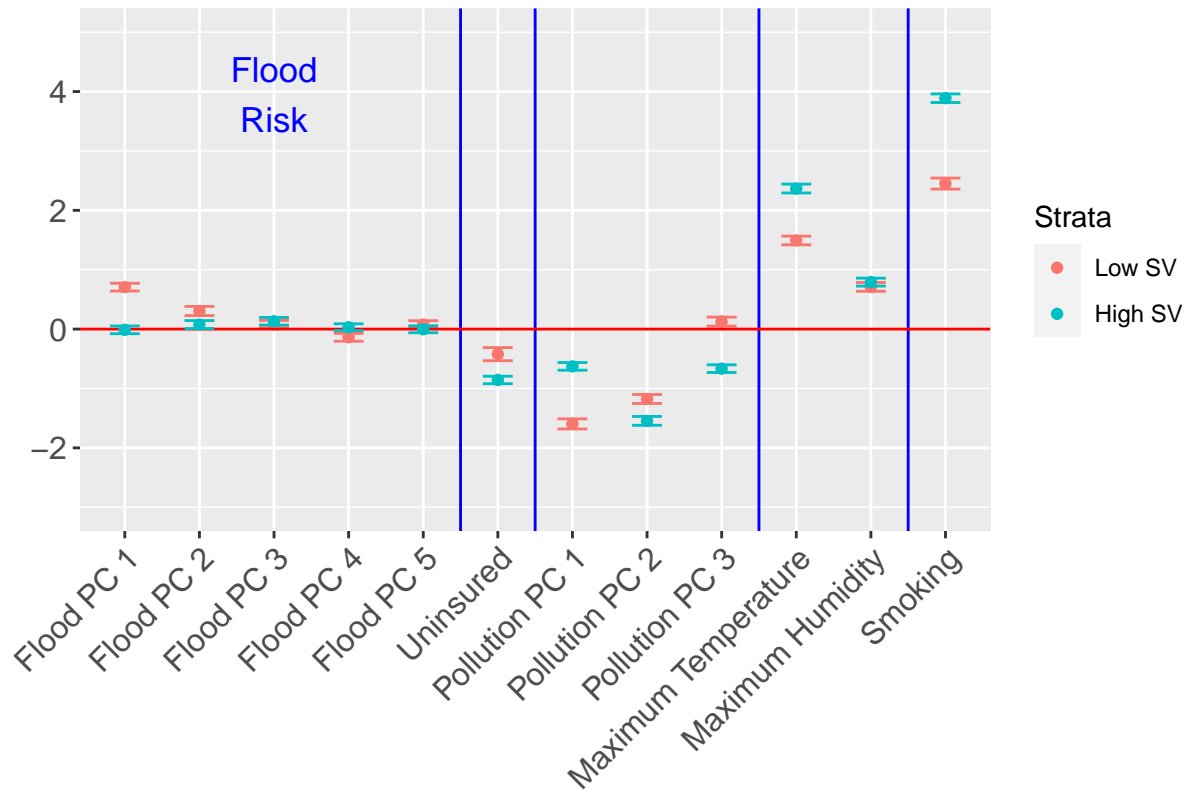
```

p <- ggplot(beta_inference_df_strat0[-1, ], aes(x = var_name, y = pt_est, color = strat)) +
  geom_point() +
  ylim(c(-3, 5)) +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_vline(xintercept = c(5.5, 6.5, 9.5, 11.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3, y = 3.95, label = "Flood\nRisk",
          col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("Flood PC 1", "Flood PC 2", "Flood PC 3", "Flood PC 4", "Flood PC 5",
                             "Uninsured",
                             "Pollution PC 1", "Pollution PC 2", "Pollution PC 3",
                             "Maximum Temperature", "Maximum Humidity",
                             "Smoking")) + ggtitle("95% Credible Intervals, BPHIGH, Stratified on All I
  geom_point(data = beta_inference_df_strat1[-1, ], col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_inference_df_strat1[-1, ], aes(ymin = lb, ymax = ub, width = 0.4), col = "#
  scale_color_manual(name = "Strata",
                    values = c("#F8766D", "#00BFC4"),
                    drop = FALSE)

```

p

## 95% Credible Intervals, BPHIGH, Stratified on All RPL Themes, Non-Spatial



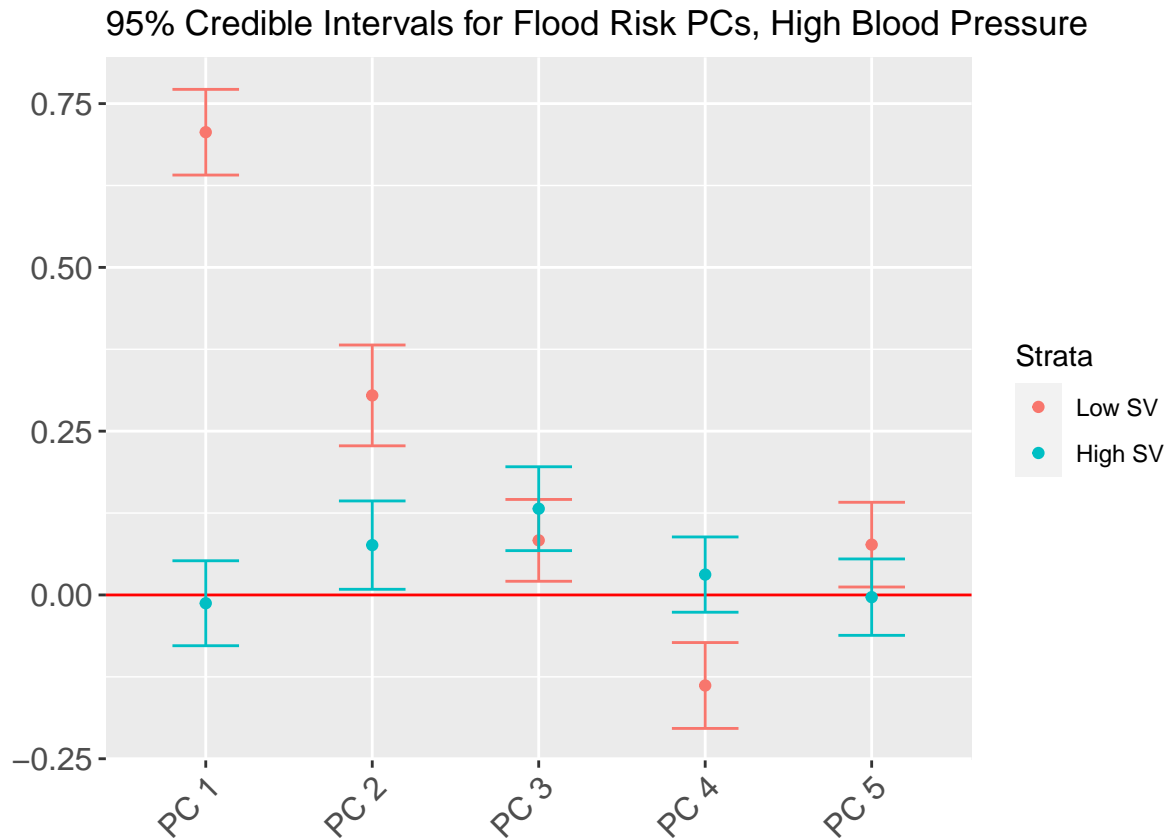
```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/BPHIGH_CI_rpls.pdf"),
  plot = p, device = "pdf",
  width = 8, height = 6, units = "in")
```

```
pc_extract_idx <- 2:6
```

```
beta_BPHIGH_pcs <- beta_data_frames_extract(beta_inference_df, pc_extract_idx)
```

```
p <- ggplot(beta_BPHIGH_pcs$beta_pcs_strat0, aes(x = var_idx, y = pt_est, color = strat)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis.title.y = element_text(size=12),
    plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_hline(yintercept = 0, col = "red") +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5"), 6) + ggtitle("95% Credible Intervals")
  geom_point(data = beta_BPHIGH_pcs$beta_pcs_strat1, col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_BPHIGH_pcs$beta_pcs_strat1, aes(ymin = lb, ymax = ub, width = 0.4), col = "#00BFC4") +
  scale_color_manual(name = "Strata",
    values = c("#F8766D", "#00BFC4"),
    drop = FALSE)
```

p



```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/BPHIGH_cred_intervals_fr_only.pdf"),
       plot = p, device = "pdf",
       width = 8, height = 6, units = "in")
```

## CAR model results, Asthma Stratified on RPL\_THEMES

```
casthma_res <- non_spatial_strat_model(covariates_CASTHMA, first_var, strat_covariate, strat_fn = median)

beta_results <- summary(casthma_res$lm_obj)$coefficients

row.names(beta_results) <- names_non_spat_strat

beta_inference <- cbind(beta_results[, 1],
                        beta_results[, 1] - 2 * beta_results[, 2],
                        beta_results[, 1] + 2 * beta_results[, 2])

colnames(beta_inference) <- c("pt_est", "lb", "ub")

beta_inference <- round(beta_inference, 5)

pc_idx <- c(2:6,
           nrow(beta_inference)/2 + 2:6)
```

```
# flipping the inference results according to the flipped PCs
beta_inference[pc_idx, ] <- post_flip(beta_inference[pc_idx, ], pc2flip)
```

```
beta_inference
```

##	pt_est	lb	ub
## strat0:Intercept	9.51735	9.50353	9.53117
## strat0:flood_risk_pc1	-0.04812	-0.05905	-0.03720
## strat0:flood_risk_pc2	0.04318	0.03033	0.05603
## strat0:flood_risk_pc3	-0.03481	-0.04524	-0.02438
## strat0:flood_risk_pc4	-0.00907	-0.02001	0.00188
## strat0:flood_risk_pc5	-0.02076	-0.03156	-0.00996
## strat0:EP_UNINSUR	-0.03892	-0.05737	-0.02048
## strat0:pollute_conc_pc1	-0.09957	-0.11375	-0.08540
## strat0:pollute_conc_pc2	-0.03182	-0.04444	-0.01920
## strat0:pollute_conc_pc3	-0.20417	-0.21677	-0.19157
## strat0:tmmx	-0.18704	-0.19924	-0.17484
## strat0:rmax	-0.27993	-0.29226	-0.26760
## strat0:Data_Value_CSMOKING	0.85935	0.84380	0.87491
## strat1:Intercept	10.07571	10.06359	10.08784
## strat1:flood_risk_pc1	-0.08182	-0.09265	-0.07098
## strat1:flood_risk_pc2	-0.07783	-0.08909	-0.06657
## strat1:flood_risk_pc3	-0.01080	-0.02149	-0.00011
## strat1:flood_risk_pc4	0.05325	0.04365	0.06285
## strat1:flood_risk_pc5	0.01051	0.00078	0.02025
## strat1:EP_UNINSUR	-0.20966	-0.22011	-0.19921
## strat1:pollute_conc_pc1	0.07572	0.06492	0.08653
## strat1:pollute_conc_pc2	-0.00755	-0.02001	0.00491
## strat1:pollute_conc_pc3	-0.18350	-0.19432	-0.17267
## strat1:tmmx	-0.17869	-0.19116	-0.16622
## strat1:rmax	-0.25626	-0.26739	-0.24512
## strat1:Data_Value_CSMOKING	1.33353	1.32143	1.34563

List of significant beta coefficients:

```
row.names(beta_inference)[sign(beta_inference[, 2]) == sign(beta_inference[, 3])]
```

## [1] "strat0:Intercept"	"strat0:flood_risk_pc1"
## [3] "strat0:flood_risk_pc2"	"strat0:flood_risk_pc3"
## [5] "strat0:flood_risk_pc5"	"strat0:EP_UNINSUR"
## [7] "strat0:pollute_conc_pc1"	"strat0:pollute_conc_pc2"
## [9] "strat0:pollute_conc_pc3"	"strat0:tmmx"
## [11] "strat0:rmax"	"strat0:Data_Value_CSMOKING"
## [13] "strat1:Intercept"	"strat1:flood_risk_pc1"
## [15] "strat1:flood_risk_pc2"	"strat1:flood_risk_pc3"
## [17] "strat1:flood_risk_pc4"	"strat1:flood_risk_pc5"
## [19] "strat1:EP_UNINSUR"	"strat1:pollute_conc_pc1"
## [21] "strat1:pollute_conc_pc3"	"strat1:tmmx"
## [23] "strat1:rmax"	"strat1:Data_Value_CSMOKING"

## Credible Interval plots for the coefficients, in ggplot

```
# first, process the beta_inference matrix in a form ggplot can understand
beta_inference_df <- as.data.frame(beta_inference)
```

```

beta_inference_df <- mutate(beta_inference_df, var_name = row.names(beta_inference_df))
beta_inference_df$var_name <- substring(beta_inference_df$var_name, first = 8)
beta_inference_df$var_name <- factor(beta_inference_df$var_name,
                                     levels = unique(beta_inference_df$var_name))
beta_inference_df$strat <- factor(c(rep("Low SV", (nrow(beta_inference_df)/2)),
                                   rep("High SV", (nrow(beta_inference_df)/2))), levels = c("Low SV",

```

Splitting up the beta coefficients for each strata

```

beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]

beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df),]

```

Note: The intercept for both strata is not included.

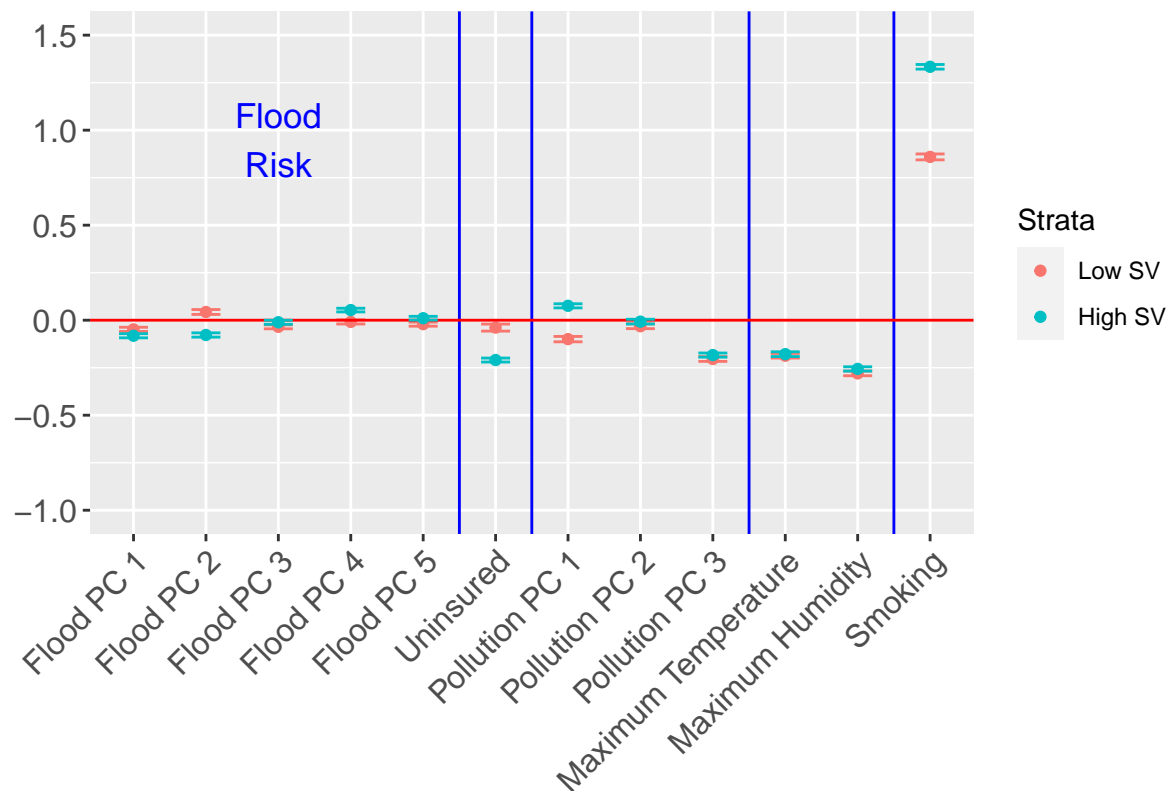
```

p <- ggplot(beta_inference_df_strat0[-1, ], aes(x = var_name, y = pt_est, color = strat)) +
  geom_point() +
  ylim(c(-1, 1.5)) +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_vline(xintercept = c(5.5, 6.5, 9.5, 11.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3, y = 0.95, label = "Flood\nRisk",
          col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("Flood PC 1", "Flood PC 2", "Flood PC 3", "Flood PC 4", "Flood PC 5",
                              "Uninsured",
                              "Pollution PC 1", "Pollution PC 2", "Pollution PC 3",
                              "Maximum Temperature", "Maximum Humidity",
                              "Smoking")) + ggtitle("95% Credible Intervals, Asthma, Stratified on All I
  geom_point(data = beta_inference_df_strat1[-1, ], col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_inference_df_strat1[-1, ], aes(ymin = lb, ymax = ub, width = 0.4), col = "#
  scale_color_manual(name = "Strata",
                    values = c("#F8766D", "#00BFC4"),
                    drop = FALSE)

```

p

## 95% Credible Intervals, Asthma, Stratified on All RPL Themes, Non-Spa



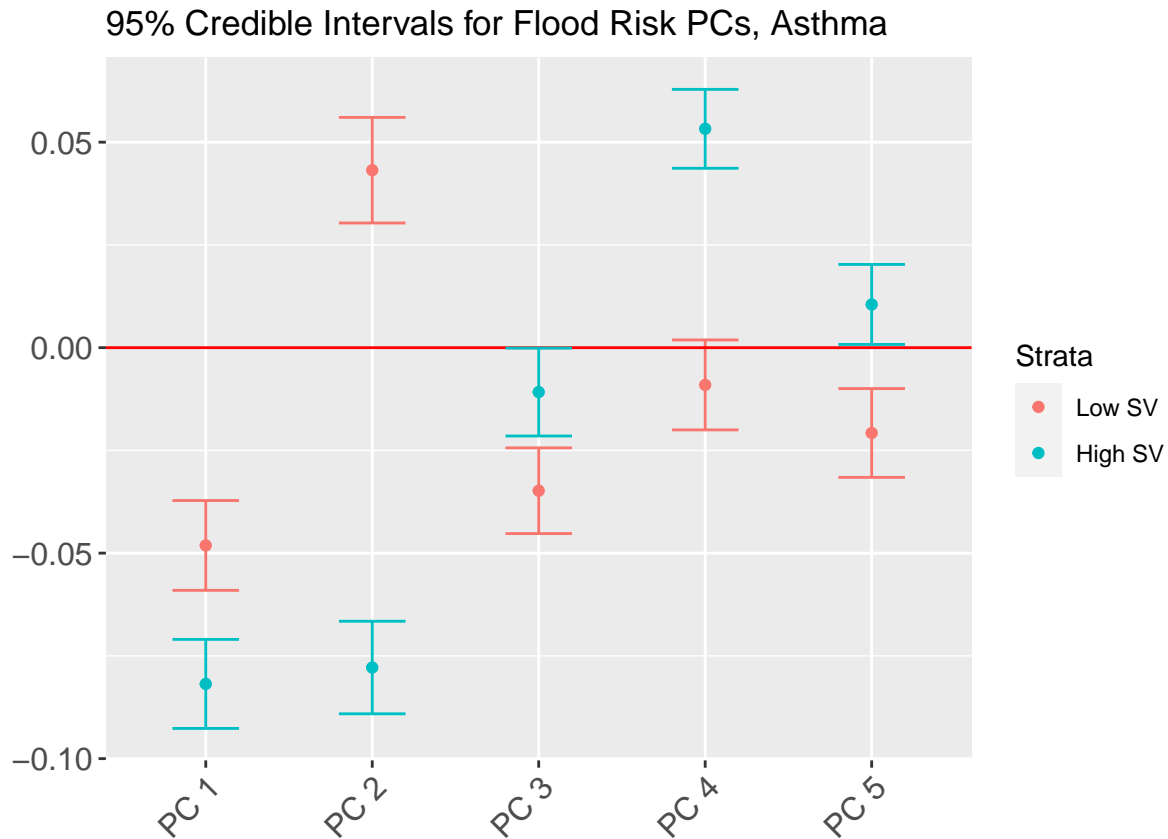
```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/CASTHMA_CI_rpls.pdf"),
  plot = p, device = "pdf",
  width = 8, height = 6, units = "in")
```

```
pc_extract_idx <- 2:6
```

```
beta_CASTHMA_pcs <- beta_data_frames_extract(beta_inference_df, pc_extract_idx)
```

```
p <- ggplot(beta_CASTHMA_pcs$beta_pcs_strat0, aes(x = var_idx, y = pt_est, color = strat)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis.title.y = element_text(size=12),
    plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_hline(yintercept = 0, col = "red") +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5"), 6) + ggtitle("95% Credible Intervals, Asthma, Stratified on All RPL Themes, Non-Spatial")
  geom_point(data = beta_CASTHMA_pcs$beta_pcs_strat1, col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_CASTHMA_pcs$beta_pcs_strat1, aes(ymin = lb, ymax = ub, width = 0.4), col = "#00BFC4") +
  scale_color_manual(name = "Strata",
    values = c("#F8766D", "#00BFC4"),
    drop = FALSE)
```

```
p
```



```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/CASTHMA_cred_intervals_fr_only.pdf"),
       plot = p, device = "pdf",
       width = 8, height = 6, units = "in")
```

## CAR model results, Poor Mental Health Stratified on RPL\_THEMES

```
mhlth_res <- non_spatial_strat_model(covariates_MHLTH, first_var, strat_covariate, strat_fn = median)
beta_results <- summary(mhlth_res$lm_obj)$coefficients
row.names(beta_results) <- names_non_spat_strat

beta_inference <- cbind(beta_results[, 1],
                        beta_results[, 1] - 2 * beta_results[, 2],
                        beta_results[, 1] + 2 * beta_results[, 2])

colnames(beta_inference) <- c("pt_est", "lb", "ub")

beta_inference <- round(beta_inference, 5)

pc_idx <- c(2:6,
            nrow(beta_inference)/2 + 2:6)
```

```
# flipping the inference results according to the flipped PCs
beta_inference[pc_idx, ] <- post_flip(beta_inference[pc_idx, ], pc2flip)
```

```
beta_inference
```

	pt_est	lb	ub
## strat0:Intercept	13.82648	13.80507	13.84789
## strat0:flood_risk_pc1	-0.05243	-0.06936	-0.03551
## strat0:flood_risk_pc2	-0.03904	-0.05895	-0.01912
## strat0:flood_risk_pc3	-0.03741	-0.05358	-0.02125
## strat0:flood_risk_pc4	0.00273	-0.01424	0.01969
## strat0:flood_risk_pc5	-0.02932	-0.04605	-0.01258
## strat0:EP_UNINSUR	0.26889	0.24031	0.29748
## strat0:pollute_conc_pc1	0.16126	0.13928	0.18323
## strat0:pollute_conc_pc2	-0.07410	-0.09365	-0.05455
## strat0:pollute_conc_pc3	-0.19632	-0.21585	-0.17679
## strat0:tmx	0.34283	0.32392	0.36174
## strat0:rmax	-0.08611	-0.10521	-0.06701
## strat0:Data_Value_CSMOKING	2.65060	2.62650	2.67470
## strat1:Intercept	14.56535	14.54656	14.58414
## strat1:flood_risk_pc1	-0.00217	-0.01896	0.01461
## strat1:flood_risk_pc2	-0.08990	-0.10735	-0.07245
## strat1:flood_risk_pc3	0.01672	0.00015	0.03328
## strat1:flood_risk_pc4	0.03849	0.02361	0.05337
## strat1:flood_risk_pc5	-0.00266	-0.01775	0.01243
## strat1:EP_UNINSUR	0.07523	0.05903	0.09142
## strat1:pollute_conc_pc1	0.42166	0.40491	0.43841
## strat1:pollute_conc_pc2	0.17542	0.15611	0.19473
## strat1:pollute_conc_pc3	0.00992	-0.00685	0.02669
## strat1:tmx	0.39273	0.37340	0.41205
## strat1:rmax	0.01504	-0.00221	0.03229
## strat1:Data_Value_CSMOKING	2.94687	2.92812	2.96561

List of significant beta coefficients:

```
row.names(beta_inference)[sign(beta_inference[, 2]) == sign(beta_inference[, 3])]
```

```
## [1] "strat0:Intercept"      "strat0:flood_risk_pc1"
## [3] "strat0:flood_risk_pc2" "strat0:flood_risk_pc3"
## [5] "strat0:flood_risk_pc5" "strat0:EP_UNINSUR"
## [7] "strat0:pollute_conc_pc1" "strat0:pollute_conc_pc2"
## [9] "strat0:pollute_conc_pc3" "strat0:tmx"
## [11] "strat0:rmax"          "strat0:Data_Value_CSMOKING"
## [13] "strat1:Intercept"     "strat1:flood_risk_pc2"
## [15] "strat1:flood_risk_pc3" "strat1:flood_risk_pc4"
## [17] "strat1:EP_UNINSUR"    "strat1:pollute_conc_pc1"
## [19] "strat1:pollute_conc_pc2" "strat1:tmx"
## [21] "strat1:Data_Value_CSMOKING"
```

## Credible Interval plots for the coefficients, in ggplot

```
# first, process the beta_inference matrix in a form ggplot can understand
beta_inference_df <- as.data.frame(beta_inference)
beta_inference_df <- mutate(beta_inference_df, var_name = row.names(beta_inference_df))
```



```

beta_inference_df$var_name <- substring(beta_inference_df$var_name, first = 8)
beta_inference_df$var_name <- factor(beta_inference_df$var_name,
                                     levels = unique(beta_inference_df$var_name))
beta_inference_df$strat <- factor(c(rep("Low SV", (nrow(beta_inference_df)/2)),
                                   rep("High SV", (nrow(beta_inference_df)/2))), levels = c("Low SV",

```

Splitting up the beta coefficients for each strata

```

beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]
beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df),]

```

Note: The intercept for both strata is not included.

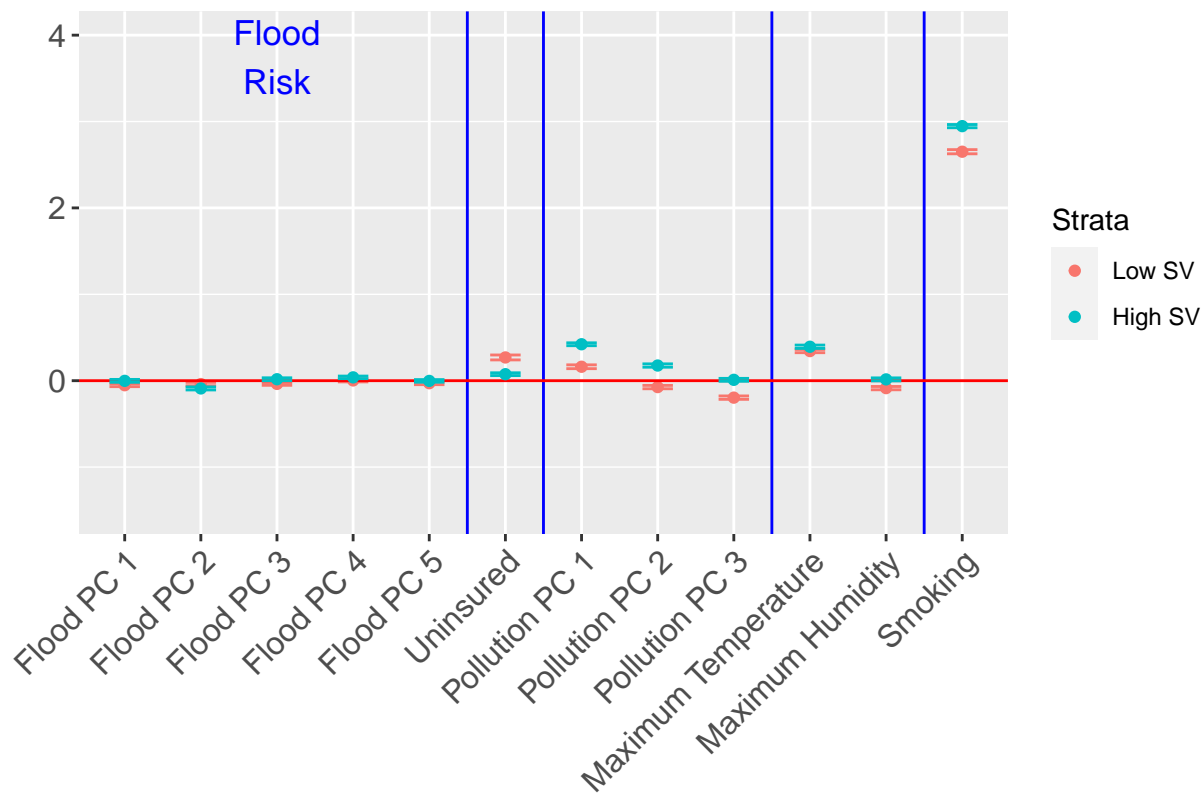
```

p <- ggplot(beta_inference_df_strat0[-1, ], aes(x = var_name, y = pt_est, color = strat)) +
  geom_point() +
  ylim(c(-1.5, 4)) +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_vline(xintercept = c(5.5, 6.5, 9.5, 11.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3, y = 3.75, label = "Flood\nRisk",
          col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("Flood PC 1", "Flood PC 2", "Flood PC 3", "Flood PC 4", "Flood PC 5",
                             "Uninsured",
                             "Pollution PC 1", "Pollution PC 2", "Pollution PC 3",
                             "Maximum Temperature", "Maximum Humidity",
                             "Smoking")) + ggtitle("95% Credible Intervals, MHLTH, Stratified on All R
  geom_point(data = beta_inference_df_strat1[-1, ], col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_inference_df_strat1[-1, ], aes(ymin = lb, ymax = ub, width = 0.4), col = "#
  scale_color_manual(name = "Strata",
                    values = c("#F8766D", "#00BFC4"),
                    drop = FALSE)

```

p

## 95% Credible Intervals, MHLTH, Stratified on All RPL Themes, Non-Spatial



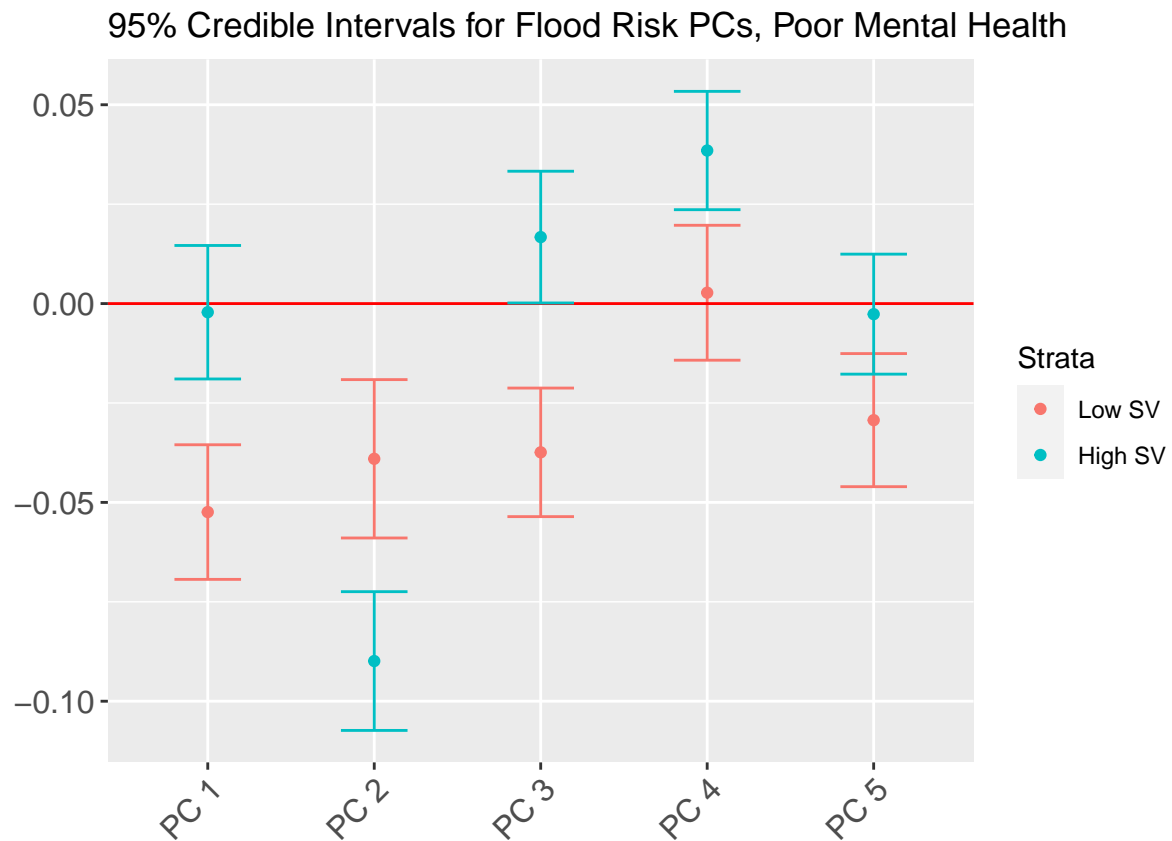
```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/MHLTH_CI_rpls.pdf"),
  plot = p, device = "pdf",
  width = 8, height = 6, units = "in")
```

```
pc_extract_idx <- 2:6
```

```
beta_MHLTH_pcs <- beta_data_frames_extract(beta_inference_df, pc_extract_idx)
```

```
p <- ggplot(beta_MHLTH_pcs$beta_pcs_strat0, aes(x = var_idx, y = pt_est, color = strat)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axis.title.y = element_text(size=12),
    plot.margin = margin(5.5, 5.5, 5.5, 25)) +
  geom_errorbar(aes(ymin = lb, ymax = ub, width = 0.4), col = "#F8766D") +
  geom_hline(yintercept = 0, col = "red") +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5"), 6) + ggtitle("95% Credible Intervals, MHLTH, Stratified on All RPL Themes, Non-Spatial")
  geom_point(data = beta_MHLTH_pcs$beta_pcs_strat1, col = "#00BFC4") + # strat 1
  geom_errorbar(data = beta_MHLTH_pcs$beta_pcs_strat1, aes(ymin = lb, ymax = ub, width = 0.4), col = "#00BFC4") +
  scale_color_manual(name = "Strata",
    values = c("#F8766D", "#00BFC4"),
    drop = FALSE)
```

p



```
ggsave(here("figures/final_figures/sensitivity_analysis/non_spatial/MHLTH_cred_intervals_fr_only.pdf"),  
  plot = p, device = "pdf",  
  width = 8, height = 6, units = "in")
```