## Stratified Analysis

#### Alvin Sheng

```
library(here)
## Warning in readLines(f, n): line 1 appears to contain an embedded nul
## here() starts at /Volumes/ALVINDRIVE/usb_NIEHS_work/flood-risk-health-effects
library(coda)
library(CARBayes)
## Loading required package: MASS
## Loading required package: Rcpp
## Registered S3 method overwritten by 'GGally':
    method from
    +.gg
           ggplot2
library(ggplot2)
library(tidyverse)
## -- Attaching packages --
                                                  ----- tidyverse 1.3.1 --
## v tibble 3.1.6
                     v dplyr
                              1.0.7
## v tidyr 1.1.4
                      v stringr 1.4.0
## v readr
            2.1.1
                      v forcats 0.5.1
## v purrr
           0.3.4
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                   masks stats::lag()
## x dplyr::select() masks MASS::select()
fhs_model_df <- readRDS("intermediary_data/fhs_model_df_all_census_tract_pc.rds")</pre>
```

## CAR model results, Coronary Heart Disease Stratified on Poverty

Inference is based on 3 markov chains, each of which has been run for 110000 samples, the first 10000 of which has been removed for burn-in. The remaining 100000 samples are thinned by 2, resulting in 150000 samples for inference across the 3 Markov chains.

```
load(here("modeling_files/model_stratif_poverty.RData"))
```

#### Beta samples

```
effectiveSize(beta_samples)
##
                    var2
                                var3
                                           var4
                                                       var5
                                                                  var6
         var1
                                                                             var7
## 68447.2046 36382.4841 37761.1319 53281.5366 68914.2531 78405.5864 87890.6361
##
         var8
                    var9
                               var10
                                          var11
                                                     var12
                                                                 var13
                                                                             var14
## 41973.9980 61353.3136 50147.4980 60253.3373 74957.3127 89787.3447 35155.2520
##
        var15
                   var16
                               var17
                                          var18
                                                      var19
                                                                 var20
                                                                             var21
## 63037.1789 62136.1468 70022.6252 73724.5058 32342.7837 88478.5492 57534.7711
##
                                                     var26
        var22
                   var23
                               var24
                                          var25
                                                                 var27
                                                                            var28
##
  10909.7609 6229.8757
                           323.8625 4500.4463 2003.7053 2883.0879
                                                                         996.6574
##
        var29
                   var30
                               var31
                                          var32
                                                     var33
                                                                 var34
                                                                            var35
##
     161.4431
                672.4907 1167.2441 28855.9245 79627.2383 39030.9892 34364.0083
##
                   var37
                               var38
                                          var39
                                                     var40
        var36
                                                                 var41
                                                                             var42
## 52293.7785 66509.7765 69269.6952 76671.2019 56050.2334 50185.4620 50495.6724
##
                                                     var47
                                                                 var48
        var43
                   var44
                               var45
                                          var46
                                                                             var49
  60423.8387 60221.4781 80050.1425 28753.4787 41256.5990 55529.6434 37611.9176
##
                                                     var54
                                                                 var55
                                                                            var56
        var50
                   var51
                               var52
                                          var53
  63008.8724 35946.8002 79938.2627 47002.3867 8686.7542 6769.6085
                                                                         325.5017
##
                                                                 var62
##
                   var58
                               var59
                                          var60
        var57
                                                     var61
                                                                            var63
##
    3937.8319
               2135.7717 2707.4575 1039.3790
                                                  163.8511
                                                              680.0737 1232.0642
##
        var64
## 28006.0742
Examining sigma2, nu2, rho
sigma2_samples <- mcmc.list(chain1$samples$sigma2, chain2$samples$sigma2,
                             chain3$samples$sigma2)
nu2_samples <- mcmc.list(chain1$samples$nu2, chain2$samples$nu2,</pre>
                          chain3$samples$nu2)
effectiveSize(sigma2_samples)
##
       var1
## 6808.768
effectiveSize(nu2_samples)
##
       var1
## 9364.658
Examining a sample of the 3108 phi parameters
phi_samples <- mcmc.list(chain1$samples$phi, chain2$samples$phi, chain3$samples$phi)
set.seed(1157, kind = "Mersenne-Twister", normal.kind = "Inversion", sample.kind = "Rejection")
phi_subset_idx <- sample(1:ncol(phi_samples[[1]]), size = 10)</pre>
phi_samples_subset <- phi_samples[, phi_subset_idx]</pre>
```

effectiveSize(phi\_samples\_subset)

```
## var1 var2 var3 var4 var5 var6 var7 var8
## 37202.660 4572.161 6806.516 20135.793 93307.470 39089.413 33554.743 40535.330
## var9 var10
## 70212.189 4821.368
```

#### Inference

```
beta_samples_matrix <- rbind(chain1$samples$beta, chain2$samples$beta, chain3$samples$beta)
# TODO: change to var_names later
colnames(beta_samples_matrix) <- c("strat0",</pre>
"strat0:flood_risk_pc1",
"strat0:flood_risk_pc2",
"strat0:flood_risk_pc3",
"strat0:flood_risk_pc4",
"strat0:flood_risk_pc5",
"strat0:EP_UNEMP",
"strat0:EP_PCI",
"strat0:EP_NOHSDP",
"strat0:EP_AGE65",
"strat0:EP AGE17",
"strat0:EP_DISABL",
"strat0:EP SNGPNT",
"strat0:EP_MINRTY",
"strat0:EP_LIMENG",
"strat0:EP MUNIT",
"strat0:EP MOBILE",
"strat0:EP_CROWD",
"strat0:EP_NOVEH",
"strat0:EP_GROUPQ",
"strat0:EP_UNINSUR",
"strat0:co",
"strat0:no2",
"strat0:o3",
"strat0:pm10",
"strat0:pm25",
"strat0:so2",
"strat0:summer tmmx",
"strat0:winter_tmmx",
"strat0:summer_rmax",
"strat0:winter_rmax",
"strat0:Data_Value_CSMOKING",
"strat1",
"strat1:flood_risk_pc1",
"strat1:flood_risk_pc2",
"strat1:flood_risk_pc3",
"strat1:flood_risk_pc4",
"strat1:flood_risk_pc5",
"strat1:EP_UNEMP",
"strat1:EP_PCI",
"strat1:EP_NOHSDP",
"strat1:EP_AGE65",
```

```
"strat1:EP_AGE17",
"strat1:EP_DISABL",
"strat1:EP SNGPNT",
"strat1:EP MINRTY",
"strat1:EP LIMENG",
"strat1:EP_MUNIT",
"strat1:EP_MOBILE",
"strat1:EP_CROWD",
"strat1:EP NOVEH",
"strat1:EP_GROUPQ",
"strat1:EP_UNINSUR",
"strat1:co",
"strat1:no2",
"strat1:03",
"strat1:pm10"
"strat1:pm25",
"strat1:so2",
"strat1:summer tmmx",
"strat1:winter_tmmx",
"strat1:summer_rmax",
"strat1:winter rmax",
"strat1:Data_Value_CSMOKING") # var_names
(beta_inference <- round(t(apply(beta_samples_matrix, 2, quantile, c(0.5, 0.025, 0.975))),5))
##
                                  50%
                                          2.5%
                                                  97.5%
## strat0
                              6.43057 6.41684 6.44428
## strat0:flood_risk_pc1
                             -0.01479 -0.02603 -0.00362
## strat0:flood_risk_pc2
## strat0:flood_risk_pc3
                              0.00961 -0.00341 0.02245
                             -0.00201 -0.01169 0.00766
                            0.00792 -0.00135 0.01719
## strat0:flood_risk_pc4
## strat0:flood risk pc5
                             0.00190 -0.00692 0.01075
## strat0:EP_UNEMP
                             0.05020 0.03500 0.06527
## strat0:EP PCI
                            -0.04941 -0.06333 -0.03545
## strat0:EP_NOHSDP
                             0.23345 0.20579 0.26097
## strat0:EP_AGE65
                              1.23105 1.21750 1.24458
## strat0:EP_AGE17
                             0.15970 0.14417 0.17523
## strat0:EP_DISABL
                             0.22445 0.20776 0.24128
## strat0:EP_SNGPNT
                             0.01504 -0.00063 0.03067
## strat0:EP_MINRTY
                             -0.17432 -0.19679 -0.15201
## strat0:EP_LIMENG
                            -0.02997 -0.05533 -0.00480
## strat0:EP_MUNIT
                            -0.05975 -0.07265 -0.04682
## strat0:EP_MOBILE
                             0.07762 0.06456 0.09065
## strat0:EP_CROWD
                             0.01336 -0.00717 0.03394
## strat0:EP_NOVEH
                             0.08992 0.06770 0.11209
## strat0:EP_GROUPQ
                             -0.09386 -0.10680 -0.08081
                             0.13585 0.11884 0.15277
## strat0:EP_UNINSUR
## strat0:co
                             -0.11942 -0.15848 -0.07998
## strat0:no2
                             0.01534 -0.03633 0.06636
## strat0:o3
                            -0.14595 -0.21856 -0.07619
## strat0:pm10
                            -0.19961 -0.23314 -0.16712
## strat0:pm25
                             0.43798 0.39060 0.48763
## strat0:so2
                             0.05621 0.02290 0.09022
                         0.13280 0.08339 0.18615
## strat0:summer_tmmx
```

```
-0.31593 -0.47846 -0.18847
## strat0:winter_tmmx
## strat0:summer_rmax
                              0.00254 -0.06569 0.07049
## strat0:winter_rmax
                              0.05320 0.00389 0.10322
## strat0:Data_Value_CSMOKING 0.70817 0.67899 0.73708
## strat1
                              0.31696 0.29857 0.33528
## strat1:flood risk pc1
                             -0.01268 -0.02315 -0.00227
## strat1:flood_risk_pc2
                              0.00658 -0.00523 0.01846
## strat1:flood_risk_pc3
                              0.00569 -0.00365 0.01504
## strat1:flood_risk_pc4
                             -0.00259 -0.01103 0.00583
## strat1:flood_risk_pc5
                              0.00154 -0.00691 0.00993
## strat1:EP_UNEMP
                              0.05283 0.04390 0.06177
## strat1:EP_PCI
                             -0.08201 -0.10645 -0.05750
## strat1:EP_NOHSDP
                              0.14347 0.12630 0.16066
                              1.63400 1.61986
## strat1:EP_AGE65
                                               1.64827
## strat1:EP_AGE17
                              0.30099 0.28704 0.31510
## strat1:EP_DISABL
                              0.22420 0.21232 0.23611
## strat1:EP_SNGPNT
                             -0.05794 -0.06914 -0.04666
## strat1:EP MINRTY
                              0.01348 -0.00424 0.03122
## strat1:EP_LIMENG
                             -0.04214 -0.05721 -0.02698
## strat1:EP_MUNIT
                             -0.00647 -0.01763 0.00469
## strat1:EP_MOBILE
                             0.05158 0.04197 0.06119
## strat1:EP_CROWD
                             -0.02294 -0.03467 -0.01119
## strat1:EP_NOVEH
                             0.19940 0.18479 0.21408
## strat1:EP_GROUPQ
                             -0.05314 -0.06171 -0.04457
## strat1:EP_UNINSUR
                              0.08819 0.07621 0.10005
## strat1:co
                             -0.14840 -0.19083 -0.10638
## strat1:no2
                             -0.02954 -0.08115 0.02160
## strat1:o3
                             -0.15649 -0.22953 -0.08649
## strat1:pm10
                             -0.14592 -0.18058 -0.11255
                              0.45173 0.40449 0.50151
## strat1:pm25
## strat1:so2
                              0.01675 -0.01555 0.04973
## strat1:summer_tmmx
                              0.04595 -0.00426 0.09936
## strat1:winter_tmmx
                             -0.16618 -0.32870 -0.03905
## strat1:summer_rmax
                             -0.07471 -0.14382 -0.00705
## strat1:winter rmax
                              0.04073 -0.00820 0.09070
## strat1:Data_Value_CSMOKING 1.03745 1.01707 1.05807
```

List of significant beta coefficients:

```
colnames(beta_samples_matrix)[sign(beta_inference[, 2]) == sign(beta_inference[, 3])]
```

```
##
    [1] "strat0"
                                      "strat0:flood_risk_pc1"
##
   [3] "strat0:EP_UNEMP"
                                      "strat0:EP_PCI"
  [5] "strat0:EP_NOHSDP"
                                      "strat0:EP_AGE65"
  [7] "strat0:EP AGE17"
                                      "strat0:EP_DISABL"
##
## [9] "strat0:EP_MINRTY"
                                      "strat0:EP_LIMENG"
## [11] "strat0:EP_MUNIT"
                                      "strat0:EP_MOBILE"
## [13] "strat0:EP_NOVEH"
                                      "strat0:EP_GROUPQ"
## [15] "strat0:EP_UNINSUR"
                                      "strat0:co"
## [17] "strat0:o3"
                                      "strat0:pm10"
## [19] "strat0:pm25"
                                      "strat0:so2"
## [21] "strat0:summer_tmmx"
                                      "strat0:winter_tmmx"
## [23] "strat0:winter_rmax"
                                      "strat0:Data_Value_CSMOKING"
## [25] "strat1"
                                      "strat1:flood_risk_pc1"
## [27] "strat1:EP_UNEMP"
                                      "strat1:EP_PCI"
```

```
## [29] "strat1:EP_NOHSDP"
                                      "strat1:EP_AGE65"
                                     "strat1:EP_DISABL"
## [31] "strat1:EP_AGE17"
                                     "strat1:EP LIMENG"
## [33] "strat1:EP_SNGPNT"
## [35] "strat1:EP_MOBILE"
                                     "strat1:EP_CROWD"
## [37] "strat1:EP_NOVEH"
                                     "strat1:EP GROUPQ"
## [39] "strat1:EP UNINSUR"
                                     "strat1:co"
## [41] "strat1:o3"
                                      "strat1:pm10"
## [43] "strat1:pm25"
                                      "strat1:winter tmmx"
## [45] "strat1:summer_rmax"
                                     "strat1:Data_Value_CSMOKING"
```

#### Credible Interval plots for the coefficients, in ggplot

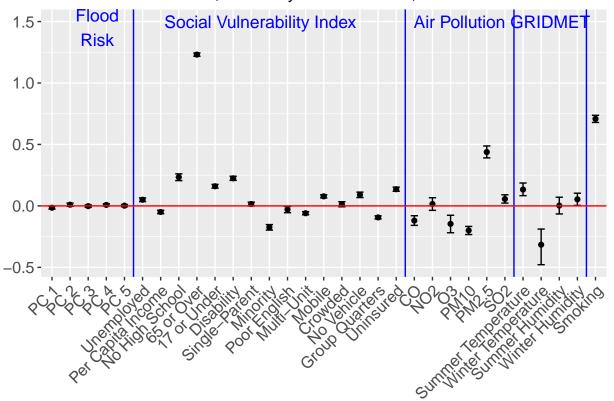
```
# first, process the beta_inference matrix in a form ggplot can understand
beta_inference_df <- as.data.frame(beta_inference)</pre>
beta_inference_df <- mutate(beta_inference_df, var_name = row.names(beta_inference_df))
beta_inference_df <- rename(beta_inference_df,</pre>
                            post_median = `50%`,
                            post_2.5 = 2.5\%
                            post_97.5 = `97.5\%`)
beta_inference_df$var_name <- factor(beta_inference_df$var_name, levels = beta_inference_df$var_name)
Splitting up the beta coefficients for each strata
beta_inference_df_strat0 <- beta_inference_df[1:(nrow(beta_inference_df)/2),]</pre>
beta_inference_df_strat1 <- beta_inference_df[(nrow(beta_inference_df)/2 + 1):nrow(beta_inference_df),]
Note: The intercept for both strata (corresponding to poverty) is not included.
p <- ggplot(beta_inference_df_strat0[-1, ], aes(x = var_name, y = post_median)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axi
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 10)) +
  geom_errorbar(aes(ymin = post_2.5, ymax = post_97.5, width = 0.4)) +
  geom_vline(xintercept = c(5.5, 20.5, 26.5, 30.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3.5, y = 1.45, label = "Flood\nRisk",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 12.5, y = 1.5, label = "Social Vulnerability Index",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 23.5, y = 1.5, label = "Air Pollution",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 28.5, y = 1.5, label = "GRIDMET",
           col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5",
                               "Unemployed", "Per Capita Income", "No High School",
                               "65 or Over", "17 or Under", "Disability",
                               "Single-Parent", "Minority", "Poor English",
                               "Multi-Unit", "Mobile", "Crowded",
```

```
"No Vehicle", "Group Quarters", "Uninsured",

"CO", "NO2", "O3", "PM10", "PM2.5", "SO2",

"Summer Temperature", "Winter Temperature", "Summer Humidity", "Winter Humidity", "Smoking")) + ggtitle("95% Credible Intervals, Coronary Heart Disease, Logical Position of the Cor
```

### 95% Credible Intervals, Coronary Heart Disease, Lower Strata



```
p <- ggplot(beta_inference_df_strat1[-1, ], aes(x = var_name, y = post_median)) +
  geom_point() +
  theme(axis.text.x = element_text(angle = 45, vjust = 1, hjust=1), axis.title.x = element_blank(), axi
        axis.text=element_text(size=12),
        plot.margin = margin(5.5, 5.5, 5.5, 10)) +
  geom_errorbar(aes(ymin = post_2.5, ymax = post_97.5, width = 0.4)) +
  geom_vline(xintercept = c(5.5, 20.5, 26.5, 30.5), col = "blue") +
  geom_hline(yintercept = 0, col = "red") +
  annotate(geom = "text", x = 3.5, y = 1.45, label = "Flood\nRisk",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 12.5, y = 1.5, label = "Social Vulnerability Index",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 23.5, y = 1.5, label = "Air Pollution",
           col = "blue", size = 4.5) +
  annotate(geom = "text", x = 28.5, y = 1.5, label = "GRIDMET",
           col = "blue", size = 4.5) +
  scale_x_discrete(labels = c("PC 1", "PC 2", "PC 3", "PC 4", "PC 5",
                              "Unemployed", "Per Capita Income", "No High School",
                              "65 or Over", "17 or Under", "Disability",
                              "Single-Parent", "Minority", "Poor English",
```

```
"Multi-Unit", "Mobile", "Crowded",

"No Vehicle", "Group Quarters", "Uninsured",

"CO", "NO2", "O3", "PM10", "PM2.5", "SO2",

"Summer Temperature", "Winter Temperature", "Summer Humidity", "Winter Humidity", "Smoking")) + ggtitle("95% Credible Intervals, Coronary Heart Disease, Upper P
```

# 95% Credible Intervals, Coronary Heart Disease, Upper Strata

