Analysis before fitting the CAR model

Alvin Sheng

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```
library(here)
## Warning in readLines(f, n): line 1 appears to contain an embedded nul
## Warning in readLines(f, n): incomplete final line found on '/Volumes/
## ALVINDRIVE2/flood-risk-health-effects/._flood-risk-health-effects.Rproj'
## here() starts at /Volumes/ALVINDRIVE2/flood-risk-health-effects
library(ape)
library(GGally)
## Loading required package: ggplot2
## Registered S3 method overwritten by 'GGally':
##
    method from
    +.gg
           ggplot2
library(usdm)
## Loading required package: sp
## Loading required package: raster
library(spdep)
## Loading required package: spData
## To access larger datasets in this package, install the spDataLarge
## package with: `install.packages('spDataLarge',
## repos='https://nowosad.github.io/drat/', type='source')`
## Loading required package: sf
## Linking to GEOS 3.8.1, GDAL 3.2.1, PROJ 7.2.1
## Registered S3 method overwritten by 'spdep':
    method
             from
    plot.mst ape
##
library(factoextra)
## Welcome! Want to learn more? See two factoextra-related books at https://goo.gl/ve3WBa
library(tidyverse)
## -- Attaching packages -----
                                                  ----- tidyverse 1.3.1 --
## v tibble 3.1.6
                     v dplyr
                               1.0.7
## v tidyr 1.1.4 v stringr 1.4.0
## v readr 2.1.1 v forcats 0.5.1
```

Summary Statistics for Table 1 of paper

```
first_var <- 19
summ_stats <- round(t(apply(fhs_model_df[, first_var:ncol(fhs_model_df)], 2, function(vec) {</pre>
  c(mean(vec, na.rm = T), sd(vec, na.rm = T), range(vec, na.rm = T))
})),2)
colnames(summ_stats) <- c("mean", "sd", "min", "max")</pre>
summ_stats
                              mean
                                         sd
                                               min
                                                          max
                                              0.00
## pct_fs_risk_2020_5
                              0.03
                                       0.08
                                                         1.00
## pct_fs_risk_2050_5
                              0.04
                                       0.10
                                              0.00
                                                         1.00
## pct_fs_risk_2020_100
                              0.11
                                       0.15
                                              0.00
                                                         1.00
## pct_fs_risk_2050_100
                              0.12
                                       0.18
                                              0.00
                                                         1.00
## pct_fs_risk_2020_500
                              0.17
                                       0.21
                                              0.00
                                                         1.00
## pct_fs_risk_2050_500
                              0.19
                                       0.22
                                              0.00
                                                         1.00
                                       1.14
                                              1.00
                                                        10.00
## avg_risk_score_all
                              1.86
## sd_risk_score_all
                              1.53
                                       0.77
                                              0.00
                                                         6.36
## cv_risk_score_all
                              0.86
                                       0.32
                                              0.00
                                                         1.50
## avg_risk_score_2_10
                              5.64
                                       1.35
                                              2.00
                                                        10.00
## avg_risk_fsf_2020_100
                              6.76
                                       1.11
                                              3.00
                                                        10.00
## avg_risk_fsf_2020_500
                              5.84
                                       1.32
                                              2.00
                                                        10.00
## pct floodfactor1
                              0.81
                                       0.22
                                              0.00
                                                         1.00
                              0.01
                                       0.04
                                              0.00
## pct_floodfactor2
                                                         1.00
## pct_floodfactor3
                              0.03
                                       0.06
                                              0.00
                                                         1.00
## pct_floodfactor4
                              0.04
                                       0.09
                                              0.00
                                                         1.00
## pct_floodfactor5
                              0.01
                                       0.03
                                              0.00
                                                         1.00
## pct_floodfactor6
                              0.05
                                       0.08
                                              0.00
                                                         1.00
## pct_floodfactor7
                              0.02
                                       0.03
                                              0.00
                                                         1.00
## pct_floodfactor8
                              0.00
                                       0.01
                                              0.00
                                                         1.00
## pct_floodfactor9
                              0.02
                                       0.05
                                              0.00
                                                         1.00
                                              0.00
## pct_floodfactor10
                              0.02
                                       0.06
                                                         1.00
## EP_POV
                             15.28
                                      11.93
                                              0.00
                                                       100.00
## EP_UNEMP
                                       4.67
                              6.38
                                              0.00
                                                       100.00
## EP PCI
                         32258.07 16848.70 42.00 227064.00
## EP_NOHSDP
                             13.03
                                      10.56
                                              0.00
                                                       100.00
## EP_AGE65
                            15.98
                                       8.02
                                              0.00
                                                       100.00
## EP_AGE17
                                       6.83
                                              0.00
                             21.97
                                                        87.60
```

EP_DISABL	13.37	5.88	0.00	100.00
EP_SNGPNT	9.18	6.44	0.00	100.00
EP_MINRTY	37.96	30.03	0.00	100.00
EP_LIMENG	4.13	6.81	0.00	100.00
EP_MUNIT	12.25	18.45	0.00	100.00
EP_MOBILE	6.06	10.76	0.00	100.00
EP_CROWD	3.52	5.18	0.00	100.00
EP_NOVEH	9.39	12.24	0.00	100.00
EP_GROUPQ	2.66	9.53	0.00	100.00
EP_UNINSUR	9.37	7.09	0.00	100.00
со	0.36	0.09	0.21	1.93
no2	10.20	5.66	1.09	33.08
03	47.32	5.17	29.37	60.51
pm10	20.25	5.42	3.88	49.35
pm25	10.46	2.32	2.43	18.69
so2	2.19	0.98	0.58	9.01
summer_tmmx	303.09	3.36	289.37	316.04
winter_tmmx	283.48	7.17	265.42	299.36
summer_rmax	86.38	11.60	27.90	99.77
winter_rmax	82.51	7.57	48.82	98.03
Data_Value_CSMOKING	18.28	5.87	3.20	51.70
Data_Value_CHD	6.67	2.21	0.50	36.00
Data_Value_CASTHMA	9.90	1.58	5.40	20.60
Data_Value_BPHIGH	32.35	7.30	4.90	70.30
Data_Value_MHLTH	14.26	3.41	5.20	35.50
	EP_DISABL EP_SNGPNT EP_MINRTY EP_LIMENG EP_MUNIT EP_MOBILE EP_CROWD EP_NOVEH EP_GROUPQ EP_UNINSUR co no2 o3 pm10 pm25 so2 summer_tmmx winter_tmmx summer_rmax winter_rmax Data_Value_CSMOKING Data_Value_CHD Data_Value_BPHIGH Data_Value_MHLTH	EP_SNGPNT 9.18 EP_MINRTY 37.96 EP_LIMENG 4.13 EP_MUNIT 12.25 EP_MOBILE 6.06 EP_CROWD 3.52 EP_NOVEH 9.39 EP_GROUPQ 2.66 EP_UNINSUR 9.37 co 0.36 no2 10.20 o3 47.32 pm10 20.25 pm25 10.46 so2 2.19 summer_tmmx 303.09 winter_tmmx 283.48 summer_rmax 86.38 winter_rmax 82.51 Data_Value_CSMOKING 18.28 Data_Value_CHD 6.67 Data_Value_CASTHMA 9.90 Data_Value_BPHIGH 32.35	EP_SNGPNT 9.18 6.44 EP_MINRTY 37.96 30.03 EP_LIMENG 4.13 6.81 EP_MUNIT 12.25 18.45 EP_MOBILE 6.06 10.76 EP_CROWD 3.52 5.18 EP_NOVEH 9.39 12.24 EP_GROUPQ 2.66 9.53 EP_UNINSUR 9.37 7.09 co 0.36 0.09 no2 10.20 5.66 o3 47.32 5.17 pm10 20.25 5.42 pm25 10.46 2.32 so2 2.19 0.98 summer_tmmx 303.09 3.36 winter_tmmx 283.48 7.17 summer_rmax 86.38 11.60 winter_rmax 82.51 7.57 Data_Value_CSMOKING 18.28 5.87 Data_Value_CASTHMA 9.90 1.58 Data_Value_BPHIGH 32.35 7.30	EP_SNGPNT 9.18 6.44 0.00 EP_MINRTY 37.96 30.03 0.00 EP_LIMENG 4.13 6.81 0.00 EP_MUNIT 12.25 18.45 0.00 EP_MOBILE 6.06 10.76 0.00 EP_CROWD 3.52 5.18 0.00 EP_NOVEH 9.39 12.24 0.00 EP_GROUPQ 2.66 9.53 0.00 EP_UNINSUR 9.37 7.09 0.00 co 0.36 0.09 0.21 no2 10.20 5.66 1.09 o3 47.32 5.17 29.37 pm10 20.25 5.42 3.88 pm25 10.46 2.32 2.43 so2 2.19 0.98 0.58 summer_tmmx 303.09 3.36 289.37 winter_tmmx 283.48 7.17 265.42 summer_rmax 86.38 11.60 27.90 winter_rmax 82.51 7.57 48.82 Data_Value_CSMOKING 18.28

Checking for multicollinearity among the covariates

S.CARleroux() automatically puts a fixed ridge penalty on the beta coefficients. Therefore, the large number of covariates and multicollinearity would be accounted for.

Actually no, because the penalty is negligible.

Flood risk variables

```
fr_index <- 19:40
apply(fhs_model_df[fr_index], 2, function(vec) sd(vec, na.rm = T))
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                 pct_fs_risk_2020_100
##
              0.07588759
                                     0.09713802
                                                            0.15288601
##
    pct_fs_risk_2050_100
                          pct_fs_risk_2020_500
                                                 pct_fs_risk_2050_500
##
              0.17630796
                                     0.20712713
                                                            0.22417139
##
                              sd_risk_score_all
      avg_risk_score_all
                                                     cv_risk_score_all
##
              1.13805698
                                     0.76598522
                                                            0.31550045
##
     avg_risk_score_2_10 avg_risk_fsf_2020_100 avg_risk_fsf_2020_500
              1.35167833
                                     1.10638589
                                                            1.32059843
##
        pct_floodfactor1
                               pct_floodfactor2
##
                                                      pct_floodfactor3
##
              0.22422161
                                     0.03629972
                                                            0.06143963
                                                      pct_floodfactor6
##
        pct_floodfactor4
                               pct_floodfactor5
              0.09444138
                                     0.03121215
                                                            0.08487768
##
##
        pct_floodfactor7
                               pct_floodfactor8
                                                      pct_floodfactor9
```

```
##
              0.02575375
                                     0.01092882
                                                             0.04667818
##
       pct floodfactor10
##
              0.06209557
ggcorr(data = fhs_model_df[, c(fr_index, ncol(fhs_model_df))])
                                                   Data Value
                                                  pct floodfacto
                                                pct floodfactors
                                             pct floodfactor8
                                          pct floodfactor7
                                        pct floodfactor6
                                     pct_floodfactor5
                                  pct floodfactor4
                               pct_floodfactor3
                                                                      1.0
                             pct floodfactor2
                                                                      0.5
                          pct floodfactor1
                    avg risk fsf 2020 500
                                                                      0.0
                 avg_risk_fsf_2020_100
               avg_risk_score_2_10
                                                                       -0.5
              cv_risk_score_all
                                                                       -1.0
            sd_risk_score_all
        avg_risk_score_all
    pct_fs_risk_2050_500
 pct fs risk 2020 500
ct_fs_risk_2050_100
fs risk 2020 100
3_risk_2050_5
isk 2020 5
flood_cor <- cor(fhs_model_df[complete.cases(fhs_model_df[, c(fr_index, ncol(fhs_model_df))]), c(fr_ind</pre>
flood_cor[nrow(flood_cor), ] # correlation with dependent variable
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
             0.028703467
                                    0.013699636
                                                           0.053585772
##
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
                                     0.072378089
##
             0.060164340
                                                           0.066051913
##
      avg_risk_score_all
                              sd_risk_score_all
                                                     cv_risk_score_all
             0.052739411
                                    0.088976754
                                                           0.006287786
##
##
     avg_risk_score_2_10 avg_risk_fsf_2020_100 avg_risk_fsf_2020_500
            -0.000661695
##
                                   -0.011451127
                                                           -0.003586298
##
        pct_floodfactor1
                               pct_floodfactor2
                                                      pct_floodfactor3
##
            -0.066084071
                                    0.035628588
                                                           0.022041402
##
        pct_floodfactor4
                               pct_floodfactor5
                                                      pct_floodfactor6
##
             0.062106455
                                    0.032507082
                                                           0.040710421
##
        pct floodfactor7
                               pct floodfactor8
                                                      pct floodfactor9
##
             0.028293267
                                   -0.004997891
                                                           -0.011414654
##
       pct_floodfactor10
                               Data_Value_MHLTH
##
             0.033368238
                                     1.00000000
```

For each variable, I take the summary of its correlations with other variables, not including itself.

summary(flood_cor) pct_fs_risk_2020_5 pct_fs_risk_2050_5 pct_fs_risk_2020_100 ## Min. :-0.41258Min. :-0.5036 Min. :-0.8052 ## 1st Qu.: 0.03317 1st Qu.: 0.0418 1st Qu.: 0.1848 ## Median : 0.42470 Median : 0.4285 Median : 0.4121 : 0.32982 : 0.3539 : 0.3872 ## Mean Mean Mean ## 3rd Qu.: 0.54557 3rd Qu.: 0.6171 3rd Qu.: 0.6688 ## Max. : 0.88390 Max. : 0.8829 Max. : 0.9373 NA's :1 NA's :1 NA's :1 ## pct_fs_risk_2050_100 pct_fs_risk_2020_500 pct_fs_risk_2050_500 ## Min. :-0.8672 Min. :-0.9656Min. :-1.0000## 1st Qu.: 0.1670 1st Qu.: 0.1012 1st Qu.: 0.1173 Median: 0.4207 Median: 0.4081 Median: 0.3988 ## Mean : 0.3762 Mean : 0.3388 Mean : 0.3366 3rd Qu.: 0.6291 3rd Qu.: 0.5681 3rd Qu.: 0.5650 ## ## Max. : 0.9373 Max. : 0.9656 Max. : 0.9656 ## NA's :1 NA's :1 NA's :1 ## avg_risk_score_all sd_risk_score_all cv_risk_score_all avg_risk_score_2_10 ## Min. :-0.9013 Min. :-0.3256 Min. :-0.45146 Min. :-0.36560 ## 1st Qu.: 0.2599 1st Qu.: 0.1610 1st Qu.:-0.01594 1st Qu.:-0.31476 Median: 0.4296 Median : 0.3352 Median :-0.11407 Median: 0.25807 ## Mean : 0.4103 Mean : 0.3021 Mean :-0.03583 Mean : 0.23244 ## 3rd Qu.: 0.6805 3rd Qu.: 0.4341 3rd Qu.: 0.04764 3rd Qu.: 0.47516 ## Max. : 0.9332 Max. : 0.6054 Max. : 0.57772 Max. : 0.96516 NA's NA's ## :1 :1 NA's :1 NA's :1 ## avg risk fsf 2020 100 avg risk fsf 2020 500 pct floodfactor1 ## Min. :-0.35635 Min. :-0.308819 Min. :-1.0000 1st Qu.:-0.05283 1st Qu.:-0.003222 1st Qu.:-0.6554 Median : 0.255205 ## Median: 0.18534 Median :-0.4204 ## Mean : 0.20935 : 0.243471 Mean :-0.4274 Mean ## 3rd Qu.: 0.45731 3rd Qu.: 0.489202 3rd Qu.:-0.2847 Max. : 0.965161 : 0.91241 Max. Max. : 0.4514 NA's NA's ## :1 NA's :1 :1 pct_floodfactor5 ## pct_floodfactor2 pct_floodfactor3 pct_floodfactor4 ## :-0.33290 Min. :-0.52073:-0.57504 Min. Min. Min. :-0.534991st Qu.:-0.01982 1st Qu.:-0.03180 1st Qu.:-0.04915 1st Qu.: 0.02091 ## Median: 0.03029 Median : 0.01718 Median :-0.01931 Median: 0.11932 ## Mean : 0.02048 Mean : 0.03583 Mean : 0.03601 Mean : 0.13565 3rd Qu.: 0.12165 3rd Qu.: 0.23844 3rd Qu.: 0.21566 3rd Qu.: 0.34498 ## ## Max. : 0.33275 Max. : 0.52045 Max. : 0.58485 Max. : 0.53506 NA's NA's ## :1 NA's :1 :1 NA's :1 ## pct floodfactor6 pct_floodfactor7 pct_floodfactor8 pct_floodfactor9 :-0.68214 Min. :-0.3593 Min. :-0.27107 Min. :-0.42826 1st Qu.: 0.04623 1st Qu.: 0.0763 1st Qu.: 0.04401 1st Qu.: 0.01582 ## Median : 0.16419 Median : 0.2623 Median : 0.25821 Median: 0.38830 ## Mean : 0.19445 Mean : 0.2218 Mean : 0.19782 Mean : 0.29026 ## 3rd Qu.: 0.41876 3rd Qu.: 0.3772 3rd Qu.: 0.34150 3rd Qu.: 0.44108 ## Max. : 0.69827 Max. : 0.5021 : 0.46059 : 0.78917 Max. Max. NA's NA's :1 NA's :1 NA's ## :1 :1 pct_floodfactor10 Data_Value_MHLTH Min. :-0.38505Min. :-0.066084

diag(flood_cor) <- NA</pre>

```
1st Qu.: 0.02112
                       1st Qu.: 0.001076
   Median : 0.36135
                       Median: 0.030605
                               : 0.027229
    Mean
           : 0.28196
                       Mean
                        3rd Qu.: 0.053374
    3rd Qu.: 0.45601
    Max.
           : 0.88390
                       Max.
                               : 0.088977
##
    NA's
                       NA's
           :1
                               :1
```

Many of the flood risk variables are very correlated.

Using VIF to exclude variables

```
fhs model df <- readRDS(here("intermediary data/fhs model df all census tract reorg.rds"))
X <- fhs_model_df[, 19:(ncol(fhs_model_df) - 4)]</pre>
X <- X[, names(X) != "pct floodfactor1"]</pre>
             <- scale(X) # Scale covariates</pre>
Х
X <- data.frame(X)</pre>
vif(X)
##
                   Variables
                                        VIF
## 1
         pct_fs_risk_2020_5
                                 11.465666
         pct_fs_risk_2050_5
                                 21.182886
       pct_fs_risk_2020_100
## 3
                                 21.459315
## 4
       pct_fs_risk_2050_100
                                 23.869460
## 5
       pct_fs_risk_2020_500
                                 48.104435
       pct_fs_risk_2050_500 42324.109965
## 6
## 7
         avg_risk_score_all
                                        Inf
## 8
          sd_risk_score_all
                                  5.911560
## 9
          cv_risk_score_all
                                  6.803326
## 10
        avg_risk_score_2_10
                                 29.820665
## 11 avg_risk_fsf_2020_100
                                  7.989054
## 12 avg_risk_fsf_2020_500
                                 34.691647
## 13
           pct floodfactor2
                                        Inf
## 14
                                        Inf
           pct_floodfactor3
## 15
           pct_floodfactor4
                                        Inf
## 16
           pct_floodfactor5
                                        Inf
## 17
           pct_floodfactor6
                                        Inf
           pct floodfactor7
## 18
                                        Inf
           pct floodfactor8
## 19
                                        Inf
## 20
           pct_floodfactor9
                                        Inf
## 21
          pct_floodfactor10
                                        Inf
## 22
                      EP_POV
                                  3.578009
## 23
                    EP_UNEMP
                                  1.858901
## 24
                      EP_PCI
                                  2.843404
## 25
                   EP_NOHSDP
                                  5.612552
## 26
                    EP_AGE65
                                  2.392680
## 27
                    EP_AGE17
                                  2.669909
```

```
## 28
                  EP DISABL
                                 2.851190
## 29
                  EP_SNGPNT
                                 2.594343
                                 3.757778
## 30
                  EP MINRTY
## 31
                  EP_LIMENG
                                 3.845793
## 32
                   EP_MUNIT
                                 2.000401
## 33
                  EP MOBILE
                                 1.668577
## 34
                   EP CROWD
                                 2.846717
                   EP_NOVEH
## 35
                                 3.260477
## 36
                  EP_GROUPQ
                                 1.394116
## 37
                 EP_UNINSUR
                                 2.448594
## 38
                                 9.168513
                         CO
## 39
                        no2
                                13.674682
## 40
                         о3
                                 2.967362
## 41
                       pm10
                                 3.810859
## 42
                       pm25
                                 5.265031
## 43
                                 2.740892
                         so2
## 44
                                 4.611565
                summer_tmmx
## 45
                                 5.370145
                winter_tmmx
## 46
                                 3.537477
                summer_rmax
## 47
                winter rmax
                                 3.314355
## 48
        Data_Value_CSMOKING
                                 6.151036
vifstep(X)
## 8 variables from the 48 input variables have collinearity problem:
## avg_risk_score_all pct_fs_risk_2050_500 pct_fs_risk_2020_500 pct_fs_risk_2050_5 avg_risk_fsf_2020_50
## After excluding the collinear variables, the linear correlation coefficients ranges between:
## min correlation ( EP_AGE65 ~ pct_floodfactor2 ): -0.0001046878
## max correlation ( avg_risk_fsf_2020_100 ~ avg_risk_score_2_10 ): 0.8776504
    ----- VIFs of the remained variables -----
##
##
                  Variables
## 1
         pct_fs_risk_2020_5 6.735162
## 2
         sd_risk_score_all 5.848256
## 3
          cv_risk_score_all 7.351120
## 4
        avg_risk_score_2_10 8.210073
      avg_risk_fsf_2020_100 5.996743
## 5
## 6
           pct_floodfactor2 1.436963
## 7
           pct_floodfactor3 1.515328
## 8
           pct_floodfactor4 1.552008
## 9
           pct_floodfactor5 1.428890
## 10
           pct_floodfactor6 1.985568
## 11
           pct floodfactor7 1.754579
## 12
           pct_floodfactor8 1.726176
## 13
           pct_floodfactor9 2.243287
## 14
          pct_floodfactor10 5.489516
## 15
                     EP_POV 3.553052
## 16
                   EP_UNEMP 1.925548
## 17
                     EP_PCI 2.792975
## 18
                  EP_NOHSDP 5.117330
## 19
                   EP_AGE65 2.377178
## 20
                   EP_AGE17 2.730325
## 21
                  EP_DISABL 2.730621
```

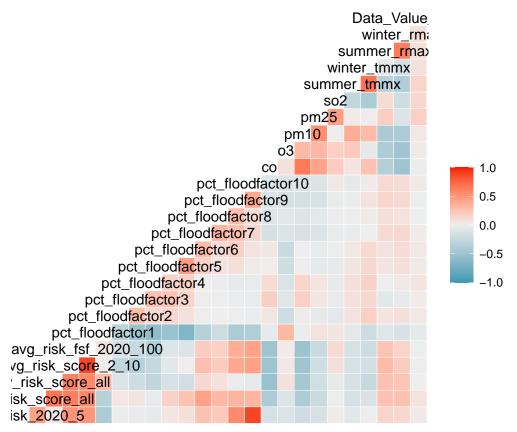
```
## 22
                  EP_SNGPNT 2.524202
## 23
                  EP_MINRTY 3.776391
## 24
                  EP_LIMENG 3.575261
## 25
                   EP_MUNIT 2.052669
## 26
                  EP_MOBILE 1.654346
                   EP_CROWD 2.506884
## 27
                   EP_NOVEH 2.828391
## 28
## 29
                  EP_GROUPQ 1.449686
## 30
                 EP_UNINSUR 2.433550
## 31
                          co 4.873870
                          o3 2.887367
## 32
## 33
                        pm10 3.643857
## 34
                        pm25 4.621878
## 35
                         so2 2.539562
## 36
                summer_tmmx 4.417985
## 37
                winter_tmmx 4.654570
## 38
                summer_rmax 3.635268
## 39
                winter_rmax 2.917975
## 40
        Data_Value_CSMOKING 5.851991
```

This procedure detects that the following variables have collinearity problems. Let's exclude these variables and then rerun the analysis.

```
\verb|collin_var_names| <- c("avg_risk_score_all", "pct_fs_risk_2050_500", "pct_fs_risk_2020_500", "avg_risk_flower_all", "pct_fs_risk_2050_500", "pct_fs_risk_2050_500", "avg_risk_flower_all", "pct_fs_risk_2050_500", "avg_risk_flower_all", "pct_fs_risk_2050_500", "pct_fs_risk_2050_500", "avg_risk_flower_all", "pct_fs_risk_2050_500", "pct_fs_risk_2050_500", "avg_risk_flower_all", "avg_risk_flower_all", "pct_fs_risk_2050_500", "avg_risk_flower_all", "
```

Correlations among climate related variables: flood risk, pollution, and GRIDMET variables

```
Excluding variables in collin_var_names
climate_var_idx <- c(fr_index, 57:66)
climate_var_idx_exclude <- climate_var_idx[-which(names(fhs_model_df)[climate_var_idx] %in% collin_var_s
ggcorr(data = fhs_model_df[, c(climate_var_idx_exclude, ncol(fhs_model_df))])</pre>
```



 $\verb|climate_cor <- cor(fhs_model_df[complete.cases(fhs_model_df[, c(climate_var_idx_exclude, ncol(fhs_model_df[, c(climate_var_idx_exclude, ncol(flat_df[, c(climate_var_idx_exclude,$

climate_cor[nrow(climate_cor),] # correlation with dependent variable

```
##
      pct_fs_risk_2020_5
                              sd_risk_score_all
                                                      cv_risk_score_all
##
            0.0299804997
                                    0.0889601742
                                                           0.0060502492
##
                                                       pct_floodfactor1
     avg_risk_score_2_10 avg_risk_fsf_2020_100
##
           -0.0004361047
                                   -0.0112722648
                                                          -0.0665488462
##
        pct_floodfactor2
                               pct_floodfactor3
                                                       pct_floodfactor4
##
            0.0356060183
                                    0.0220103942
                                                           0.0620835478
##
        pct_floodfactor5
                               pct floodfactor6
                                                       pct floodfactor7
            0.0324997455
                                    0.0407283782
                                                           0.0287804262
##
        pct_floodfactor8
                               pct_floodfactor9
                                                      pct_floodfactor10
##
           -0.0048493860
                                   -0.0112121004
                                                           0.0349543674
##
##
                                                                   pm10
##
           -0.0196370204
                                    0.0226626739
                                                           0.0405151007
##
                     pm25
                                                            summer_tmmx
##
            0.1832766126
                                    0.1537557332
                                                           0.1454940393
##
             winter_tmmx
                                     summer_rmax
                                                            winter_rmax
##
            0.0731103518
                                    0.0944951518
                                                           0.0855385378
##
        Data_Value_MHLTH
            1.000000000
```

For each variable, I take the summary of its correlations with other variables, not including itself.

```
diag(climate_cor) <- NA
summary(climate_cor)</pre>
```

```
pct_fs_risk_2020_5 sd_risk_score_all cv_risk_score_all avg_risk_score_2_10
   Min. :-0.40902
##
                               :-0.3474
                                                  :-0.44990
                       Min.
                                          Min.
                                                              Min.
                                                                      :-0.45656
    1st Qu.:-0.05581
                        1st Qu.:-0.1228
                                           1st Qu.:-0.26268
                                                               1st Qu.:-0.17685
##
    Median: 0.03657
                        Median : 0.1166
                                          Median :-0.04901
                                                              Median: 0.04197
##
    Mean
          : 0.11607
                        Mean
                               : 0.1228
                                          Mean
                                                  :-0.01306
                                                              Mean
                                                                      : 0.08615
##
    3rd Qu.: 0.27656
                        3rd Qu.: 0.3371
                                           3rd Qu.: 0.11207
                                                              3rd Qu.: 0.29873
                               : 0.5955
    Max.
           : 0.88042
                        Max.
                                          Max.
                                                  : 0.58195
                                                              Max.
                                                                      : 0.87512
    NA's
                        NA's
##
           :1
                               :1
                                           NA's
                                                  :1
                                                              NA's
                                                                      :1
##
    avg_risk_fsf_2020_100 pct_floodfactor1
                                               pct floodfactor2
##
    Min.
           :-0.50351
                           Min.
                                  :-0.68385
                                               Min.
                                                      :-0.333951
    1st Qu.:-0.16835
                           1st Qu.:-0.38829
                                               1st Qu.:-0.051353
    Median: 0.04115
                           Median :-0.17383
                                               Median: 0.013113
##
##
    Mean
           : 0.07535
                           Mean
                                  :-0.19129
                                               Mean
                                                      :-0.001026
                                               3rd Qu.: 0.078299
##
    3rd Qu.: 0.28041
                           3rd Qu.:-0.03059
##
    Max.
           : 0.87512
                           Max.
                                  : 0.44949
                                               Max.
                                                      : 0.301375
##
    NA's
           :1
                           NA's
                                  :1
                                               NA's
                                                      :1
##
                                                                 pct_floodfactor6
    pct_floodfactor3
                         pct_floodfactor4
                                             pct_floodfactor5
    Min.
           :-0.522389
                         Min.
                                :-0.57674
                                             Min.
                                                    :-0.53652
                                                                 Min.
                                                                        :-0.6838548
                                             1st Qu.:-0.04306
    1st Qu.:-0.052386
                                                                 1st Qu.:-0.0004318
##
                         1st Qu.:-0.04865
##
    Median: 0.003107
                         Median :-0.01916
                                             Median: 0.04986
                                                                 Median: 0.0689923
##
    Mean
           : 0.002413
                         Mean
                                :-0.02058
                                             Mean
                                                    : 0.03239
                                                                 Mean
                                                                        : 0.0400112
    3rd Qu.: 0.150393
                         3rd Qu.: 0.13801
                                             3rd Qu.: 0.14366
                                                                 3rd Qu.: 0.1535915
                                                    : 0.46674
##
    Max.
           : 0.310142
                                : 0.31014
                                                                 Max.
                                                                        : 0.4667402
                         Max.
                                             Max.
    NA's
                         NA's
                                             NA's
                                                                 NA's
##
           :1
                                :1
                                                    :1
                                                                        :1
##
    pct floodfactor7
                        pct floodfactor8
                                            pct floodfactor9
                                                                pct floodfactor10
    Min.
           :-0.35804
                        Min.
                               :-0.27042
                                            Min.
                                                   :-0.42623
                                                                Min.
                                                                       :-0.38138
##
    1st Qu.:-0.02109
                        1st Qu.:-0.02231
                                            1st Qu.:-0.05628
                                                                1st Qu.:-0.06516
##
    Median: 0.04330
                        Median: 0.03359
                                            Median: 0.03625
                                                                Median: 0.02956
##
    Mean
           : 0.07881
                               : 0.07684
                                                  : 0.09221
                                                                       : 0.08918
                        Mean
                                            Mean
                                                                Mean
    3rd Qu.: 0.21338
                        3rd Qu.: 0.16632
                                            3rd Qu.: 0.28783
                                                                3rd Qu.: 0.14090
##
    Max.
           : 0.45756
                        Max.
                               : 0.45756
                                            Max.
                                                   : 0.58777
                                                                Max.
                                                                       : 0.88042
##
    NA's
           :1
                        NA's
                               :1
                                            NA's
                                                   :1
                                                                NA's
                                                                       :1
##
                              о3
                                                 pm10
                                                                     pm25
          co
           :-0.49037
                        Min.
                                                                Min. :-0.22305
##
                               :-0.50981
                                                   :-0.50351
    Min.
                                            Min.
##
    1st Qu.:-0.18352
                        1st Qu.:-0.13751
                                            1st Qu.:-0.23089
                                                                1st Qu.:-0.13091
    Median :-0.05265
##
                        Median :-0.09970
                                            Median :-0.02814
                                                                Median :-0.03210
##
    Mean
          :-0.04405
                        Mean
                               :-0.04017
                                            Mean
                                                  :-0.02623
                                                                Mean : 0.03357
##
    3rd Qu.: 0.11930
                        3rd Qu.: 0.08466
                                            3rd Qu.: 0.17628
                                                                3rd Qu.: 0.09245
##
    Max.
           : 0.62502
                        Max.
                               : 0.34745
                                            Max.
                                                   : 0.62502
                                                                Max.
                                                                       : 0.54279
##
    NA's
                        NA's
                                            NA's
                                                                NA's
           :1
                               :1
                                                   :1
                                                                       :1
##
         so2
                         summer tmmx
                                              winter tmmx
                                                                  summer rmax
##
           :-0.41123
                               :-0.354306
                                                    :-0.41123
                                                                        :-0.39896
    Min.
                        Min.
                                             Min.
                                                                 Min.
    1st Qu.:-0.04441
                                                                 1st Qu.:-0.03477
##
                        1st Qu.:-0.148715
                                             1st Qu.:-0.13020
##
    Median: 0.02180
                        Median :-0.010138
                                             Median: 0.01709
                                                                 Median: 0.08962
    Mean
           : 0.01892
                        Mean
                               : 0.001591
                                             Mean
                                                    : 0.02280
                                                                 Mean
                                                                        : 0.04483
##
    3rd Qu.: 0.11396
                        3rd Qu.: 0.072685
                                             3rd Qu.: 0.14145
                                                                 3rd Qu.: 0.14923
##
    Max.
           : 0.46857
                        Max.
                               : 0.692370
                                             Max.
                                                    : 0.69237
                                                                 Max.
                                                                        : 0.59653
##
    NA's
                        NA's
                                             NA's
           :1
                               : 1
                                                    :1
                                                                 NA's
                                                                        :1
##
     winter_rmax
                         Data_Value_MHLTH
##
    Min.
           :-0.509809
                         Min.
                                :-0.066549
##
                         1st Qu.: 0.004429
    1st Qu.:-0.132134
##
    Median: 0.079918
                         Median: 0.033727
##
    Mean :-0.007747
                         Mean : 0.044439
    3rd Qu.: 0.111153
                         3rd Qu.: 0.076217
```

```
## Max. : 0.596532 Max. : 0.183277
## NA's :1 NA's :1
```

Climate variables other than flood risk are not too correlated.

Non-spatial modeling

```
Y <- fhs_model_df$Data_Value_CHD
X <- fhs_model_df[, 19:(ncol(fhs_model_df) - 4)]</pre>
X <- X[, names(X) != "pct_floodfactor1"]</pre>
# exclude some more variables selected by vifstep, to account for multicollinearity
# excluding all of the pct_fs_risk variables, as well as 3 of the avg_risk_score variables
collin_var_names <- c("avg_risk_score_all", "pct_fs_risk_2050_500", "pct_fs_risk_2020_500", "avg_risk_f
X <- X[, !(names(X) %in% collin_var_names)]</pre>
# # also removing avg_risk_score_sfha due to large numbers of NAs
\# X \leftarrow X[, names(X) != "avg_risk_score_sfha"]
            <- scale(X) # Scale covariates
X[is.na(X)] \leftarrow 0
                        # Fill in missing values with the mean
# if I do mean imputation (which may be problematic), all the counties
# will have neighbors in W
\# X \leftarrow data.frame(X)
fhs_lm \leftarrow lm(Y \sim X)
summary(fhs_lm)
##
## Call:
## lm(formula = Y ~ X)
##
## Residuals:
                1Q Median
                                3Q
## -9.8599 -0.4803 -0.0189 0.4575 17.7353
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                           ## Xpct_fs_risk_2020_5
                           0.0041458 0.0086312
                                                   0.480 0.630996
## Xsd_risk_score_all
                           0.0552776 0.0077439
                                                   7.138 9.54e-13 ***
                                                   1.892 0.058538 .
## Xcv_risk_score_all
                           0.0141664 0.0074888
## Xavg_risk_score_2_10
                          -0.0320944 0.0075740
                                                 -4.237 2.26e-05 ***
## Xavg_risk_fsf_2020_100  0.0064095  0.0064859
                                                 0.988 0.323050
```

```
-0.0175671 0.0036160
                                                   -4.858 1.19e-06 ***
## Xpct_floodfactor2
## Xpct_floodfactor3
                           -0.0116605 0.0038324
                                                   -3.043 0.002346 **
                           -0.0112754
                                                   -3.058 0.002229 **
## Xpct floodfactor4
                                      0.0036872
                           -0.0025495 0.0037888
## Xpct_floodfactor5
                                                   -0.673 0.501012
## Xpct_floodfactor6
                           -0.0077272 0.0042902
                                                   -1.801 0.071688
## Xpct floodfactor7
                           -0.0002381 0.0039344
                                                   -0.061 0.951752
## Xpct floodfactor8
                           -0.0081307
                                      0.0041329
                                                   -1.967 0.049152 *
## Xpct_floodfactor9
                           -0.0099330
                                      0.0044657
                                                   -2.224 0.026133 *
## Xpct_floodfactor10
                           0.0252324
                                       0.0077199
                                                    3.268 0.001082 **
## XEP_POV
                           0.3390289
                                       0.0059369
                                                   57.105 < 2e-16 ***
## XEP_UNEMP
                           0.0157048
                                      0.0043573
                                                    3.604 0.000313 ***
## XEP_PCI
                           -0.0258376
                                       0.0052305
                                                   -4.940 7.84e-07 ***
## XEP_NOHSDP
                           0.2126295
                                       0.0074081
                                                   28.702
                                                          < 2e-16 ***
## XEP_AGE65
                           1.4712867
                                       0.0047719
                                                  308.324
                                                           < 2e-16 ***
## XEP_AGE17
                                                   62.398
                           0.3361792
                                       0.0053876
                                                           < 2e-16 ***
## XEP_DISABL
                           0.3453552
                                       0.0051798
                                                   66.673
                                                           < 2e-16 ***
## XEP_SNGPNT
                                                  -19.953
                          -0.1013951
                                      0.0050818
                                                           < 2e-16 ***
## XEP MINRTY
                          -0.0666869
                                                  -11.159
                                       0.0059761
                                                           < 2e-16 ***
## XEP_LIMENG
                           -0.0073262
                                                   -1.177 0.239195
                                      0.0062244
## XEP MUNIT
                           -0.0592066
                                      0.0044919
                                                  -13.181
                                                           < 2e-16 ***
## XEP_MOBILE
                           0.0416902 0.0039966
                                                   10.431
                                                           < 2e-16 ***
## XEP CROWD
                          -0.0675969
                                      0.0053378
                                                  -12.664
                                                          < 2e-16 ***
## XEP_NOVEH
                                                    8.095 5.80e-16 ***
                           0.0455598
                                      0.0056279
## XEP_GROUPQ
                           -0.0756168
                                      0.0038800
                                                  -19.489
                                                           < 2e-16 ***
## XEP_UNINSUR
                           0.1515184
                                      0.0048360
                                                   31.331
                                                           < 2e-16 ***
## Xco
                           0.0175963
                                      0.0071454
                                                    2.463 0.013796 *
## Xo3
                           -0.0628817
                                       0.0050313
                                                  -12.498 < 2e-16 ***
## Xpm10
                           -0.0072726
                                      0.0062277
                                                   -1.168 0.242902
## Xpm25
                           -0.0073628
                                      0.0064447
                                                   -1.142 0.253268
## Xso2
                                                   15.829
                           0.0821766
                                      0.0051917
                                                           < 2e-16 ***
## Xsummer_tmmx
                           0.1184252
                                       0.0066269
                                                   17.870
                                                           < 2e-16 ***
## Xwinter_tmmx
                                       0.0066074
                                                    9.588
                                                           < 2e-16 ***
                           0.0633490
## Xsummer_rmax
                           0.0599815
                                       0.0062598
                                                    9.582
                                                           < 2e-16 ***
                                                   14.569
                                                           < 2e-16 ***
## Xwinter_rmax
                           0.0821721
                                       0.0056402
                           0.8362653
                                                  110.447
## XData_Value_CSMOKING
                                       0.0075716
                                                           < 2e-16 ***
##
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.84 on 71794 degrees of freedom
     (702 observations deleted due to missingness)
## Multiple R-squared: 0.8553, Adjusted R-squared: 0.8552
## F-statistic: 1.061e+04 on 40 and 71794 DF, p-value: < 2.2e-16
->
```

PCA

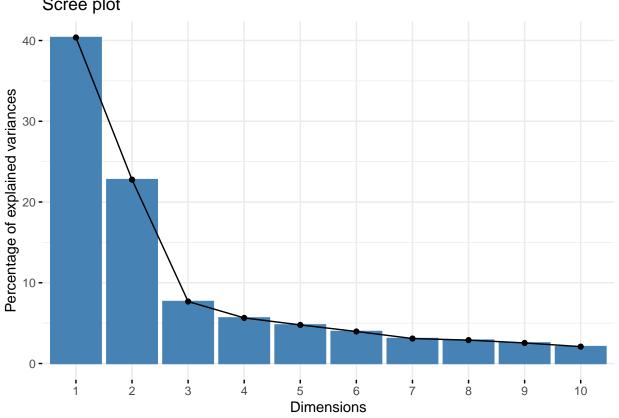
PCA with Centering and Scaling beforehand

Conduct PCA on the correlated flood risk variables

```
first_var <- 19
```

```
fr_index <- first_var:(first_var + 21)</pre>
flood_risk <- fhs_model_df[, fr_index]</pre>
fr_pca <- prcomp(flood_risk[complete.cases(flood_risk),], center = T, scale. = T)</pre>
fr_loadings <- fr_pca$rotation</pre>
fviz_eig(fr_pca)
```

Scree plot



```
summ_pca <- summary(fr_pca)</pre>
summ_pca$importance[,1:10]
```

```
##
                               PC1
                                        PC2
                                                 PC3
                                                          PC4
                                                                    PC5
                                                                              PC6
## Standard deviation
                          2.980165 2.238176 1.299683 1.114667 1.025496 0.9341738
## Proportion of Variance 0.403700 0.227700 0.076780 0.056480 0.047800 0.0396700
## Cumulative Proportion 0.403700 0.631400 0.708180 0.764660 0.812460 0.8521300
                                PC7
                                          PC8
                                                   PC9
## Standard deviation
                          0.8249525 0.7983534 0.748906 0.6784936
## Proportion of Variance 0.0309300 0.0289700 0.025490 0.0209300
## Cumulative Proportion 0.8830600 0.9120300 0.937530 0.9584500
```

We started out with 22 variables. Including five PC scores would include 80% of the variance.

Including eight PC scores would include 90% of the variance.

Printing out the loadings, from most negative to least

```
# First PC Score
fr_loadings[, 1]
```

```
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
              -0.24042633
                                     -0.26657190
                                                            -0.31448378
##
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
              -0.31380335
                                     -0.29916654
                                                            -0.29619111
##
      avg_risk_score_all
                              sd_risk_score_all
                                                      cv_risk_score_all
##
             -0.33168172
                                     -0.17484099
                                                             0.08495769
##
     avg_risk_score_2_10
                          avg_risk_fsf_2020_100
                                                 avg_risk_fsf_2020_500
##
             -0.11957319
                                     -0.09942242
                                                            -0.12471527
##
        pct_floodfactor1
                               pct_floodfactor2
                                                       pct_floodfactor3
##
              0.29616865
                                     -0.04683405
                                                            -0.07886906
##
        pct_floodfactor4
                               pct_floodfactor5
                                                       pct_floodfactor6
##
             -0.09763011
                                     -0.14143760
                                                            -0.19907514
##
        pct_floodfactor7
                               pct_floodfactor8
                                                       pct_floodfactor9
##
             -0.16323272
                                     -0.14190186
                                                            -0.22217802
##
       pct_floodfactor10
             -0.21807090
```

The first PC score is very interpretable. Only the loading for pct_floodfactor1 is positive.

Second PC Score fr_loadings[, 2]

```
pct_fs_risk_2020_100
##
      pct fs risk 2020 5
                             pct_fs_risk_2050_5
##
              0.18936889
                                      0.15849267
                                                            -0.01897480
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
##
             -0.07046075
                                     -0.17012069
                                                            -0.19136490
##
      avg_risk_score_all
                              sd_risk_score_all
                                                      cv_risk_score_all
##
             -0.03653999
                                                             0.32161350
                                      0.21123041
##
     avg_risk_score_2_10 avg_risk_fsf_2020_100 avg_risk_fsf_2020_500
##
              0.38327527
                                      0.37692053
                                                             0.37889776
##
        pct_floodfactor1
                               pct_floodfactor2
                                                       pct_floodfactor3
##
              0.19143421
                                     -0.14797990
                                                            -0.23221303
##
        pct_floodfactor4
                               pct_floodfactor5
                                                       pct_floodfactor6
##
             -0.26037249
                                     -0.16487957
                                                            -0.16615218
##
                               pct floodfactor8
        pct floodfactor7
                                                       pct floodfactor9
##
              0.05646518
                                      0.08178865
                                                             0.12622288
##
       pct_floodfactor10
##
              0.15921169
```

Less interpretable—more of a mix of positive and negative loadings.

Third PC Score fr_loadings[, 3]

```
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
           -3.127449e-01
                                  -3.277179e-01
                                                          6.653306e-05
##
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
            1.561162e-02
                                   5.586528e-02
                                                          7.239793e-02
##
      avg_risk_score_all
                              sd_risk_score_all
                                                     cv_risk_score_all
##
           -6.145985e-02
                                   3.825294e-01
                                                          3.797622e-01
##
     avg risk score 2 10 avg risk fsf 2020 100 avg risk fsf 2020 500
##
            1.100369e-01
                                   9.448015e-02
                                                           1.166077e-01
##
        pct floodfactor1
                               pct floodfactor2
                                                      pct floodfactor3
```

```
##
           -7.242690e-02
                                    6.525560e-02
                                                           1.011418e-01
                               pct_floodfactor5
##
        pct_floodfactor4
                                                       pct_floodfactor6
##
            2.101051e-02
                                    2.505114e-01
                                                           2.561423e-01
                               pct_floodfactor8
                                                       pct_floodfactor9
##
        pct_floodfactor7
##
            3.122515e-01
                                    1.516808e-01
                                                          -1.739074e-01
##
       pct floodfactor10
##
           -3.974122e-01
# Fourth PC Score
fr loadings[, 4]
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
             0.121314451
                                     0.036713873
                                                           -0.179542754
##
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
            -0.152650065
                                     0.006693033
                                                            0.124019886
##
      avg_risk_score_all
                              sd_risk_score_all
                                                      cv_risk_score_all
##
                                                            0.202762749
            -0.017134527
                                     0.250355627
     avg_risk_score_2_10
                          avg_risk_fsf_2020_100
                                                 avg_risk_fsf_2020_500
##
##
            -0.007181716
                                     0.161299133
                                                            0.075307417
##
        pct_floodfactor1
                               pct_floodfactor2
                                                       pct floodfactor3
##
            -0.124261583
                                                            0.467353486
                                     0.511960031
##
        pct floodfactor4
                                                       pct floodfactor6
                               pct floodfactor5
##
             0.135511378
                                    -0.022257200
                                                           -0.260406423
##
        pct_floodfactor7
                               pct_floodfactor8
                                                       pct_floodfactor9
##
            -0.277781005
                                    -0.281315502
                                                           -0.110473643
##
       pct_floodfactor10
##
             0.161271275
# Fifth PC Score
fr_loadings[, 5]
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
             -0.03398928
                                     -0.12115849
                                                             0.03411119
    pct_fs_risk_2050_100
##
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
               0.11255958
                                      0.09349197
                                                             0.02552728
##
                              sd risk score all
                                                      cv risk score all
      avg risk score all
##
               0.03486906
                                      0.01664289
                                                             0.05708426
##
     avg risk score 2 10 avg risk fsf 2020 100 avg risk fsf 2020 500
##
              0.18644632
                                      0.08098052
                                                             0.13769357
        pct_floodfactor1
##
                               pct floodfactor2
                                                       pct floodfactor3
##
             -0.02532959
                                     -0.40980031
                                                            -0.15375374
##
        pct_floodfactor4
                               pct_floodfactor5
                                                       pct floodfactor6
##
              0.20952684
                                      0.19187611
                                                             0.25781763
##
        pct_floodfactor7
                               pct_floodfactor8
                                                       pct_floodfactor9
##
                                     -0.59925282
                                                            -0.22463544
              -0.36985923
       pct_floodfactor10
##
##
               0.10070678
round(fr_loadings[, 1:5], digits = 2)
##
                            PC1
                                  PC2
                                         PC3
                                               PC4
                                                      PC5
                          -0.24
                                 0.19 -0.31
                                              0.12 -0.03
## pct_fs_risk_2020_5
                          -0.27
                                 0.16 - 0.33
                                              0.04 - 0.12
## pct_fs_risk_2050_5
## pct_fs_risk_2020_100
                          -0.31 -0.02
                                        0.00 - 0.18
## pct_fs_risk_2050_100
                          -0.31 - 0.07
                                        0.02 - 0.15
                                                    0.11
## pct_fs_risk_2020_500
                          -0.30 -0.17
                                        0.06 0.01
                                                    0.09
```

```
## pct_fs_risk_2050_500
                         -0.30 -0.19 0.07 0.12
                          -0.33 -0.04 -0.06 -0.02
                                                   0.03
## avg_risk_score_all
## sd risk score all
                          -0.17
                                0.21
                                       0.38
                                             0.25
                                                   0.02
## cv_risk_score_all
                          0.08
                                0.32
                                            0.20
                                                   0.06
                                       0.38
## avg_risk_score_2_10
                          -0.12
                                0.38
                                       0.11 -0.01
                                                   0.19
## avg risk fsf 2020 100 -0.10
                                0.38
                                       0.09
                                            0.16
## avg risk fsf 2020 500 -0.12
                                0.38
                                       0.12
                                            0.08
## pct floodfactor1
                          0.30
                                0.19 -0.07 -0.12 -0.03
## pct_floodfactor2
                          -0.05 -0.15
                                       0.07
                                             0.51 - 0.41
## pct_floodfactor3
                         -0.08 -0.23
                                       0.10
                                             0.47 - 0.15
## pct_floodfactor4
                         -0.10 -0.26
                                       0.02
                                            0.14 0.21
## pct_floodfactor5
                                       0.25 - 0.02
                         -0.14 - 0.16
                                                   0.19
## pct_floodfactor6
                         -0.20 - 0.17
                                       0.26 - 0.26
                                                  0.26
## pct_floodfactor7
                         -0.16
                                0.06
                                       0.31 - 0.28 - 0.37
## pct_floodfactor8
                         -0.14
                                0.08 0.15 -0.28 -0.60
## pct_floodfactor9
                          -0.22
                                0.13 -0.17 -0.11 -0.22
## pct_floodfactor10
                         -0.22 0.16 -0.40 0.16 0.10
round(fr_loadings[, 1:8], digits = 2)
                                                    PC5
                                                                       PC8
##
                           PC1
                                  PC2
                                        PC3
                                              PC4
                                                          PC6
                                                                 PC7
## pct_fs_risk_2020_5
                          -0.24
                                 0.19 - 0.31
                                             0.12 - 0.03
                                                         0.00 - 0.05
                                                                      0.23
## pct_fs_risk_2050_5
                          -0.27
                                0.16 - 0.33
                                             0.04 - 0.12
                                                         0.06 -0.05 -0.02
## pct_fs_risk_2020_100
                          -0.31 -0.02
                                       0.00 - 0.18
                                                  0.03
                                                         0.05
                                                               0.12
## pct_fs_risk_2050_100
                          -0.31 -0.07
                                       0.02 -0.15
                                                   0.11
                                                         0.00
                                                                0.10 -0.04
## pct_fs_risk_2020_500
                          -0.30 - 0.17
                                       0.06
                                             0.01
                                                   0.09 - 0.14
                                                                0.02 - 0.01
## pct fs risk 2050 500
                         -0.30 -0.19
                                       0.07
                                             0.12
                                                   0.03 -0.05
                                                                0.00 - 0.04
## avg risk score all
                          -0.33 -0.04 -0.06 -0.02
                                                   0.03
                                                         0.02
                                                                0.00
                                             0.25
## sd_risk_score_all
                          -0.17
                                0.21
                                       0.38
                                                   0.02 - 0.09
                                                                0.02
                                                                      0.17
## cv risk score all
                          0.08
                                0.32
                                       0.38
                                            0.20
                                                   0.06 -0.10
                                                                0.05
## avg_risk_score_2_10
                          -0.12
                                0.38
                                       0.11 -0.01
                                                   0.19 -0.06
                                                                0.02 -0.13
## avg_risk_fsf_2020_100 -0.10
                                 0.38
                                       0.09
                                             0.16
                                                   0.08
                                                         0.04 -0.07 -0.15
## avg_risk_fsf_2020_500 -0.12
                                0.38
                                       0.12
                                            0.08
                                                   0.14
                                                         0.01
                                                               0.03 - 0.17
## pct_floodfactor1
                          0.30
                                0.19 -0.07 -0.12 -0.03
                                                         0.05
                                                                0.00
## pct_floodfactor2
                         -0.05 -0.15
                                       0.07
                                             0.51 - 0.41
                                                         0.35
                                                               0.58 - 0.13
## pct_floodfactor3
                         -0.08 -0.23
                                             0.47 -0.15 -0.06 -0.62
                                       0.10
## pct_floodfactor4
                         -0.10 -0.26
                                       0.02
                                             0.14
                                                   0.21 - 0.68
                                                                0.19 - 0.21
## pct_floodfactor5
                         -0.14 - 0.16
                                       0.25 - 0.02
                                                   0.19
                                                         0.48 - 0.37 - 0.14
## pct_floodfactor6
                         -0.20 - 0.17
                                       0.26 - 0.26
                                                   0.26
                                                         0.28
                                                               0.17
## pct floodfactor7
                          -0.16
                                0.06
                                       0.31 -0.28 -0.37 -0.10
                                                               0.08
## pct floodfactor8
                          -0.14
                                0.08
                                      0.15 -0.28 -0.60 -0.19 -0.19 -0.25
## pct_floodfactor9
                         -0.22
                                0.13 -0.17 -0.11 -0.22
                                                         0.04 -0.08 -0.51
## pct_floodfactor10
                         -0.22
                                0.16 -0.40 0.16 0.10 0.04 0.00
```

PCA with Centering but no Scaling beforehand

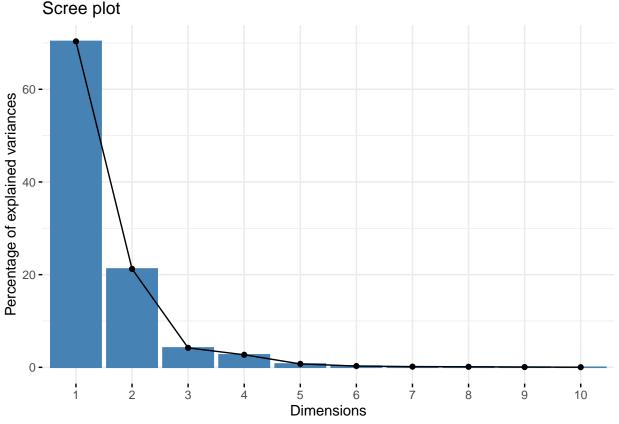
Do PCA without scaling beforehand, and use biplots, etc. to compare results with those in the last section. I think just scaling all covariates once, after PCA, will lead to more interpretable results

Conduct PCA on the correlated flood risk variables

```
first_var <- 19
fr_index <- first_var:(first_var + 21)</pre>
```

```
flood_risk <- fhs_model_df[, fr_index]
fr_pca <- prcomp(flood_risk[complete.cases(flood_risk),], center = T, scale. = F)
fr_loadings <- fr_pca$rotation
fviz_eig(fr_pca)</pre>
```

0 1



```
summ_pca <- summary(fr_pca)
summ_pca$importance[,1:10]</pre>
```

```
PC1
                                        PC2
                                                  PC3
                                                             PC4
                                                                       PC5
##
## Standard deviation
                          2.156094 1.184867 0.5271685 0.4232675 0.2213399
## Proportion of Variance 0.703430 0.212440 0.0420500 0.0271100 0.0074100
## Cumulative Proportion 0.703430 0.915870 0.9579200 0.9850300 0.9924500
##
                                PC6
                                          PC7
                                                     PC8
                                                                PC9
                                                                          PC10
## Standard deviation
                          0.1354879 0.1002485 0.08885766 0.0664214 0.04515333
## Proportion of Variance 0.0027800 0.0015200 0.00119000 0.0006700 0.00031000
## Cumulative Proportion 0.9952200 0.9967400 0.99794000 0.9986100 0.99891000
```

We started out with 22 variables. Including two PC scores would include >90% of the variance. Perhaps I can also look at the top 5 PCs, to get >99% variance explained.

Printing out the loadings, from most negative to least

```
# First PC Score
fr_loadings[, 1]
```

```
##
      pct_fs_risk_2020_5
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
            -0.021240339
                                   -0.026200603
                                                           -0.027287959
##
    pct fs risk 2050 100
                           pct fs risk 2020 500
                                                  pct fs risk 2050 500
##
            -0.025890403
                                   -0.012937437
                                                           -0.011239303
##
      avg_risk_score_all
                              sd_risk_score_all
                                                     cv_risk_score_all
##
            -0.206655116
                                   -0.224161348
                                                           -0.065925907
##
     avg_risk_score_2_10 avg_risk_fsf_2020_100 avg_risk_fsf_2020_500
##
            -0.581194182
                                    -0.477386598
                                                           -0.577512216
##
        pct_floodfactor1
                               pct_floodfactor2
                                                      pct_floodfactor3
##
             0.011215117
                                    0.002775862
                                                            0.006705547
##
        pct_floodfactor4
                               pct_floodfactor5
                                                      pct_floodfactor6
##
                                                           -0.001712055
             0.010804712
                                    0.000436761
        pct_floodfactor7
##
                               pct_floodfactor8
                                                      pct floodfactor9
##
                                   -0.001119415
                                                           -0.010331553
            -0.003673378
##
       pct_floodfactor10
##
            -0.015101598
```

The first PC score is very interpretable. Only the loadings for the first five pct_floodfactor variables are positive.

```
# Second PC Score
fr_loadings[, 2]
```

```
pct_fs_risk_2020_5
##
                             pct_fs_risk_2050_5
                                                  pct_fs_risk_2020_100
##
             0.030877735
                                    0.048298401
                                                            0.110524027
##
    pct_fs_risk_2050_100
                           pct_fs_risk_2020_500
                                                  pct_fs_risk_2050_500
##
             0.130411155
                                     0.162847406
                                                            0.176634178
##
      avg_risk_score_all
                              sd_risk_score_all
                                                     cv_risk_score_all
##
             0.882803822
                                                           -0.127097694
                                    0.144210669
##
     avg_risk_score_2_10
                          avg_risk_fsf_2020_100
                                                 avg_risk_fsf_2020_500
##
            -0.130010196
                                   -0.161871141
                                                           -0.117887932
##
        pct_floodfactor1
                               pct_floodfactor2
                                                      pct_floodfactor3
##
            -0.176663004
                                    0.006636052
                                                            0.019301215
##
        pct_floodfactor4
                               pct_floodfactor5
                                                      pct_floodfactor6
##
             0.035596848
                                    0.012790780
                                                            0.048754950
##
        pct_floodfactor7
                               pct_floodfactor8
                                                      pct_floodfactor9
##
             0.007900621
                                    0.001889291
                                                            0.018931063
##
       pct_floodfactor10
             0.024862184
```

The second PC score only has negative loadings for pct_floodfactor1 and some of the avg_risk_score variables.

round(fr loadings[, 1:2], digits = 2)

```
PC1
                                  PC2
## pct_fs_risk_2020_5
                          -0.02
                                 0.03
## pct_fs_risk_2050_5
                          -0.03
                                0.05
## pct_fs_risk_2020_100
                         -0.03
                                0.11
## pct_fs_risk_2050_100
                         -0.03
                                0.13
## pct_fs_risk_2020_500
                         -0.01
                                0.16
## pct_fs_risk_2050_500
                          -0.01
                                 0.18
## avg_risk_score_all
                          -0.21
                                 0.88
## sd_risk_score_all
                          -0.22 0.14
## cv_risk_score_all
                          -0.07 -0.13
## avg_risk_score_2_10
                         -0.58 -0.13
```

```
## avg_risk_fsf_2020_100 -0.48 -0.16
## avg_risk_fsf_2020_500 -0.58 -0.12
## pct floodfactor1
                         0.01 - 0.18
## pct_floodfactor2
                         0.00 0.01
## pct floodfactor3
                         0.01 0.02
                         0.01 0.04
## pct floodfactor4
## pct floodfactor5
                         0.00 0.01
## pct floodfactor6
                         0.00 0.05
## pct floodfactor7
                         0.00
                              0.01
## pct_floodfactor8
                         0.00 0.00
## pct_floodfactor9
                        -0.01 0.02
## pct_floodfactor10
                        -0.02 0.02
round(fr_loadings[, 1:8], digits = 2)
                          PC1
                                     PC3
                                           PC4
                                                 PC5
                                                       PC6
                                                            PC7
                                                                  PC8
##
                               PC2
## pct_fs_risk_2020_5
                        -0.02
                              0.03
                                    0.02 -0.02 -0.02
                                                      0.23 -0.04 -0.24
## pct_fs_risk_2050_5
                        -0.03
                              0.05
                                    0.04 -0.02 -0.02
                                                      0.30
                                                           0.02 - 0.25
## pct_fs_risk_2020_100
                                         0.04 -0.02
                        -0.03
                              0.11
                                    0.02
                                                     0.07
                                                           0.11
## pct_fs_risk_2050_100
                        -0.03
                              0.13 0.03
                                         0.04 0.01 -0.10
                                                          0.07
## pct_fs_risk_2020_500
                        -0.01
                              0.16 -0.01 0.02 -0.06 -0.39 -0.01 -0.03
## pct_fs_risk_2050_500
                        -0.01
                              ## avg_risk_score_all
                        -0.21 0.88 0.16 -0.06 -0.05 0.20 0.16 -0.06
                        -0.22 0.14 -0.93 0.07 0.01 0.10 -0.23 0.03
## sd_risk_score_all
## cv_risk_score_all
                        -0.07 -0.13 -0.25
                                         0.06 -0.04 -0.09 0.93 -0.17
## avg_risk_score_2_10
                        -0.58 -0.13 0.17
                                          0.52 -0.56 -0.08 -0.08 -0.03
## avg_risk_fsf_2020_100 -0.48 -0.16
                                   0.02 -0.83 -0.23 -0.06
                                                          0.00
## avg risk fsf 2020 500 -0.58 -0.12 0.14 0.14 0.78 0.03
                                                           0.00
## pct_floodfactor1
                         0.01 -0.18 0.02 0.03 -0.08 0.44
                                                           0.04
                                                                 0.11
## pct_floodfactor2
                         0.00
                              0.01 -0.01 -0.02
                                                0.05 -0.03
                                                           0.00 - 0.04
                         0.01 0.02 -0.02 -0.03
                                               0.04 -0.13 -0.05 -0.17
## pct_floodfactor3
## pct_floodfactor4
                         0.01
                              0.04 0.00
                                         0.02
                                                0.01 -0.37 -0.10 -0.36
                         0.00 0.01 0.00 0.00
                                                0.01 -0.05
## pct_floodfactor5
                                                           0.00
                                                                 0.08
## pct floodfactor6
                         0.00
                              0.05 0.00
                                         0.02
                                                0.01 - 0.15
                                                           0.07
## pct_floodfactor7
                         0.00 0.01 -0.01 0.00 0.00 0.01
                                                           0.01
                                                                 0.06
## pct_floodfactor8
                         0.00 0.00 0.00 0.00 0.00 0.00
                                                           0.00
## pct_floodfactor9
                                    0.01 -0.01 -0.01
                              0.02
                                                     0.09
                                                           0.04 -0.03
                        -0.01
## pct_floodfactor10
                        -0.02 0.02 0.02 -0.01 -0.02 0.20 -0.02 -0.21
```