Simulation Study

```
library(survival)
library(glmnet)
## Loading required package: Matrix
## Loading required package: foreach
## Loaded glmnet 2.0-16
library(polspline)
library(knitr)
library(EnvStats)
##
## Attaching package: 'EnvStats'
## The following object is masked from 'package:Matrix':
##
##
       print
## The following objects are masked from 'package:stats':
##
##
       predict, predict.lm
## The following object is masked from 'package:base':
##
       print.default
library(tictoc)
library(abind)
library(bda)
```

Function for Simulating Survival Time from a Weibull or Lognormal Distribution

This function is based on simulate_data in https://cran.r-project.org/web/packages/rsimsum/vignettes/relhaz.html

```
#' Simulate survival times with censoring, based on a user-defined distribution

#'

"' This function simulates survival times with censoring, according to a specific

#' distribution that the user parameterizes. The survival times are

#' simulated for user-given covariates and coefficients, and the censoring times

#' are simulated for a user-given distribution.

#' @param dist distribution for the survival times, expected to be "weibull" or "lnorm"

#' @param x model matrix of covariate values

#' @param fcts_select subset of fcts from a hare object containing the coefficients of interest.

#' @param parameters scale and shape/sigma for the baseline hazard

#' @param FUN random generation function for the distribution of censoring times,

#' expected to be uniform, exponential, or weibull.

#' @param ... arguments for FUN, the random generation function for the

#' censoring distribution
```

```
#' Greturn dataframe appending survival time and censoring indicator to the model matrix x
#' @export
simulate_dist <- function(dist, x, fcts_select, params, FUN, ...) {</pre>
 n \leftarrow nrow(x)
  # extract unique list of covariates selected
  cov_nums <- sort(fcts_select[,1][fcts_select[,1] != 0])</pre>
  cov_names <- colnames(x)[cov_nums]</pre>
  x_select <- x[,cov_names]</pre>
  # extract the coefficient values from fcts_select
  betas <- fcts_select[,5][fcts_select[,1] != 0]</pre>
  betas <- betas[order(fcts_select[,1][fcts_select[,1] != 0])]</pre>
  # simulate survival times
  if (dist == "weibull") {
    # simulate survival times according to Bender et al. (2005)
    time <- (-log(u) / (params$scale * exp(x_select %*% betas)))^(1 / params$shape)
  } else if (dist == "lnorm") {
    z \leftarrow rnorm(n)
    time <- exp(params$scale + x_select %*% betas + params$sigma * z)</pre>
  } else {stop("Unrecognized Distribution")}
  # Winsorising tiny values for time (smaller than one day on a yearly-scale, e.g. 1 / 365.242),
  # and adding a tiny amount of white noise not to have too many concurrent values
  time <- ifelse(time < 1 / 365.242, 1 / 365.242, time)
  time[time == 1 / 365.242] <- time[time == 1 / 365.242] +
    rnorm(length(time[time == 1 / 365.242]), mean = 0, sd = 1e-4)
  # ...and make sure that the resulting value is positive
  time <- abs(time)</pre>
  # Censoring
  cid_time <- FUN(n, ...)</pre>
 cid <- ifelse(time < cid time, 1, 0)</pre>
 time <- pmin(time, cid_time)</pre>
 # return a dataframe
  data.frame(time, cid, x)
}
```

Setting up the requisite parameters for simulation

Generating example data set from the Weibull distribution

I calculate the Weibull shape parameter and use an arbitrary Weibull scale parameter to make the survival times and censoring rate be similar to those of the ACTG-175 data set.

Generating example data set from the Log-normal distribution

I use an arbitrary log-normal scale parameter and a calculated sigma parameter to make the survival times and censoring rate be similar to those of the ACTG-175 data set.

Coxph Simulation

Weibull distributed survival times

```
phm_sim_mat <- coxph(Surv(time, cid) ~ ., data = sim_mat)</pre>
summary(phm_sim_mat)
## Call:
## coxph(formula = Surv(time, cid) ~ ., data = sim_mat)
##
##
    n= 2139, number of events= 556
##
##
                   coef exp(coef)
                                     se(coef)
                                                   z Pr(>|z|)
## trtZDV.ddi -6.803e-01 5.065e-01 1.271e-01 -5.352 8.68e-08 ***
## trtZDV.ZAL -4.565e-01 6.335e-01 1.284e-01 -3.556 0.000376 ***
## trtddi
             -4.939e-01 6.103e-01 1.237e-01 -3.992 6.55e-05 ***
             -1.212e-02 9.880e-01 5.561e-03 -2.180 0.029282 *
## age
             -2.314e-03 9.977e-01 3.275e-03 -0.707 0.479837
## wtkg
             -2.068e-01 8.132e-01 1.690e-01 -1.224 0.221099
## hemo1
## drugs1
             -1.629e-01 8.497e-01 1.371e-01 -1.189 0.234634
## karnof
              1.866e-03 1.002e+00 8.117e-03 0.230 0.818147
## oprior1
             -4.414e-02 9.568e-01 2.830e-01 -0.156 0.876049
              5.042e-04 1.001e+00 1.006e-04 5.010 5.43e-07 ***
## preanti
             -1.926e-02 9.809e-01 1.043e-01 -0.185 0.853435
## race1
## gender1
              9.918e-03 1.010e+00 1.395e-01 0.071 0.943329
## symptom1
              4.581e-01 1.581e+00 1.145e-01 4.002 6.28e-05 ***
             -8.817e-01 4.141e-01 1.015e-01 -8.686 < 2e-16 ***
## offtrt1
## cd40
              3.779e-02 1.039e+00 1.359e-03 27.803 < 2e-16 ***
## cd80
              4.250e-04 1.000e+00 9.724e-05 4.370 1.24e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
             exp(coef) exp(-coef) lower .95 upper .95
                                               0.6497
## trtZDV.ddi
                0.5065
                           1.9745
                                     0.3948
```

```
## trtZDV.ZAL
                 0.6335
                            1.5786
                                      0.4926
                                                 0.8147
## trtddi
                 0.6103
                            1.6386
                                      0.4789
                                                 0.7777
## age
                 0.9880
                            1.0122
                                      0.9772
                                                 0.9988
## wtkg
                 0.9977
                            1.0023
                                      0.9913
                                                 1.0041
## hemo1
                 0.8132
                            1.2297
                                      0.5839
                                                 1.1325
## drugs1
                 0.8497
                            1.1769
                                      0.6495
                                                 1.1115
## karnof
                            0.9981
                                      0.9861
                 1.0019
                                                1.0179
## oprior1
                 0.9568
                            1.0451
                                      0.5495
                                                 1.6660
## preanti
                 1.0005
                            0.9995
                                      1.0003
                                                 1.0007
## race1
                 0.9809
                            1.0195
                                      0.7996
                                                 1.2034
## gender1
                 1.0100
                            0.9901
                                      0.7683
                                                 1.3276
## symptom1
                                                 1.9786
                 1.5810
                            0.6325
                                      1.2633
## offtrt1
                 0.4141
                            2.4149
                                      0.3394
                                                 0.5052
## cd40
                 1.0385
                            0.9629
                                      1.0358
                                                 1.0413
## cd80
                 1.0004
                            0.9996
                                      1.0002
                                                 1.0006
##
## Concordance= 0.914 (se = 0.005)
## Rsquare= 0.512
                    (max possible= 0.938)
## Likelihood ratio test= 1536 on 16 df,
                                            p = < 2e - 16
                        = 786.3 on 16 df,
## Wald test
                                             p=<2e-16
## Score (logrank) test = 1130 on 16 df,
                                            p=<2e-16
cox.zph(phm_sim_mat)
                          chisq
                   rho
## trtZDV.ddi 0.03319 6.12e-01 0.4342
## trtZDV.ZAL -0.03747 7.89e-01 0.3743
```

```
## trtddi
              0.00426 1.01e-02 0.9199
              0.01451 1.13e-01 0.7365
## age
## wtkg
              0.08006 3.49e+00 0.0618
             -0.05042 1.55e+00 0.2136
## hemo1
## drugs1
             -0.00714 3.14e-02 0.8594
## karnof
             -0.05259 1.72e+00 0.1894
## oprior1
             -0.00073 2.95e-04 0.9863
## preanti
             -0.00977 5.67e-02 0.8118
## race1
              0.06856 2.70e+00 0.1001
## gender1
             -0.00179 1.84e-03 0.9658
             -0.02961 4.87e-01 0.4852
## symptom1
## offtrt1
              0.03329 6.27e-01 0.4284
## cd40
              0.00461 1.23e-02 0.9119
## cd80
              0.04935 1.54e+00 0.2143
                   NA 2.04e+01 0.2046
## GLOBAL
```

Log-normal distributed survival times

```
phm_sim_mat_lnorm <- coxph(Surv(time, cid) ~ ., data = sim_mat_lnorm)

summary(phm_sim_mat_lnorm)

## Call:
## coxph(formula = Surv(time, cid) ~ ., data = sim_mat_lnorm)

##
## n= 2139, number of events= 580
##</pre>
```

```
##
                    coef
                          exp(coef)
                                      se(coef)
                                                     z Pr(>|z|)
                                                 6.718 1.84e-11 ***
## trtZDV.ddi 0.9188650
                         2.5064439 0.1367729
## trtZDV.ZAL 1.0654428 2.9021238 0.1265975
                                                 8.416 < 2e-16 ***
## trtddi
              0.8143017
                         2.2575986
                                    0.1285474
                                                 6.335 2.38e-10 ***
## age
               0.0105286 1.0105842
                                    0.0055209
                                                 1.907 0.05651
## wtkg
              -0.0002270 0.9997730 0.0031204 -0.073 0.94200
## hemo1
              0.1042017 1.1098243 0.1620453
                                                 0.643 0.52020
## drugs1
              0.1467529 1.1580677 0.1353055
                                                 1.085 0.27810
              -0.0159226   0.9842035   0.0068964   -2.309   0.02095 *
## karnof
## oprior1
              0.4690807 1.5985240 0.2392082
                                                 1.961 0.04988 *
## preanti
              -0.0011414   0.9988593   0.0001103   -10.348   < 2e-16 ***
## race1
              -0.3257693 0.7219717
                                               -3.173 0.00151 **
                                    0.1026675
## gender1
              0.2151600 1.2400602 0.1313460
                                                 1.638 0.10140
             -0.3039862 0.7378710 0.1053642
## symptom1
                                               -2.885 0.00391 **
## offtrt1
              1.2134183 3.3649675
                                    0.0953360 12.728 < 2e-16 ***
## cd40
              -0.0546852 0.9467832
                                     0.0017639 -31.003
                                                       < 2e-16 ***
## cd80
              -0.0009773 0.9990232 0.0001085 -9.006 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
              exp(coef) exp(-coef) lower .95 upper .95
## trtZDV.ddi
                 2.5064
                            0.3990
                                      1.9171
## trtZDV.ZAL
                 2.9021
                            0.3446
                                      2.2644
                                                3.7194
## trtddi
                 2.2576
                            0.4429
                                      1.7548
                                                2.9045
## age
                 1.0106
                            0.9895
                                      0.9997
                                                1.0216
## wtkg
                 0.9998
                           1.0002
                                      0.9937
                                                1.0059
## hemo1
                 1.1098
                            0.9010
                                                1.5247
                                      0.8078
## drugs1
                 1.1581
                           0.8635
                                      0.8883
                                                1.5098
## karnof
                           1.0161
                                      0.9710
                 0.9842
                                                0.9976
## oprior1
                 1.5985
                           0.6256
                                      1.0002
                                                2.5547
## preanti
                 0.9989
                            1.0011
                                      0.9986
                                                0.9991
## race1
                 0.7220
                           1.3851
                                      0.5904
                                                0.8829
## gender1
                 1.2401
                            0.8064
                                      0.9586
                                                1.6041
## symptom1
                            1.3553
                 0.7379
                                      0.6002
                                                0.9071
## offtrt1
                 3.3650
                            0.2972
                                      2.7915
                                                4.0563
## cd40
                 0.9468
                            1.0562
                                      0.9435
                                                0.9501
## cd80
                 0.9990
                            1.0010
                                      0.9988
                                                0.9992
##
## Concordance= 0.979 (se = 0.001)
## Rsquare= 0.738
                   (max possible= 0.98)
## Likelihood ratio test= 2864 on 16 df,
                                            p = < 2e - 16
## Wald test
                        = 1010 on 16 df,
                                            p = < 2e - 16
## Score (logrank) test = 1335 on 16 df,
                                            p = < 2e - 16
cox.zph(phm sim mat lnorm)
##
                          chisq
                   rho
## trtZDV.ddi 0.15089
                       19.2296 1.16e-05
## trtZDV.ZAL
              0.09262
                         5.0994 2.39e-02
## trtddi
               0.07147
                         3.1417 7.63e-02
## age
               0.19228
                       27.8444 1.31e-07
              0.03185
                         0.6032 4.37e-01
## wtkg
              -0.03097
                         0.5708 4.50e-01
## hemo1
## drugs1
             -0.06752
                         3.1470 7.61e-02
## karnof
              0.12501 10.1582 1.44e-03
```

```
## oprior1
              -0.02810
                         0.4754 4.91e-01
              -0.01580
## preanti
                         0.1802 6.71e-01
## race1
               0.03004
                         0.5869 4.44e-01
## gender1
              -0.00789
                         0.0451 8.32e-01
## symptom1
             -0.14284
                        13.9136 1.91e-04
## offtrt1
                       41.8670 9.77e-11
               0.22695
## cd40
              -0.35096 159.0881 1.79e-36
## cd80
              -0.12101
                         8.7352 3.12e-03
## GLOBAL
                    NA 247.0840 2.05e-43
```

Preanti instead of offtrt was determined to be the covariate violating the proportional hazards assumption.

Weibull model (to compare with Coxph), (Weibull distributed survival times)

Weibull Distributed Survival Time

The Weibull model should be more powerful (with less variance in the coefficient estimates) than the Cox Proportional Hazards model, as the data is from a Weibull distribution. The coefficient estimates themselves should be similar.

```
summary(survreg(Surv(time, cid) ~ ., data = sim_mat))
## Warning in survreg.fit(X, Y, weights, offset, init = init, controlvals =
## control, : Ran out of iterations and did not converge
##
## Call:
## survreg(formula = Surv(time, cid) ~ ., data = sim_mat)
                   Value Std. Error
## (Intercept) -1.70e-01
                           0.00e+00 - Inf < 2e-16
## trtZDV.ddi
               2.34e-03
                           0.00e+00 Inf <2e-16
## trtZDV.ZAL -3.09e-02
                           0.00e+00 - Inf < 2e-16
## trtddi
                7.25e-02
                           0.00e+00 Inf <2e-16
               -2.04e-03
                           0.00e+00 - Inf < 2e-16
## age
## wtkg
               2.04e-03
                           0.00e+00 Inf <2e-16
## hemo1
                5.59e-03
                           0.00e+00 Inf <2e-16
                                     Inf <2e-16
## drugs1
                4.08e-02
                           0.00e+00
## karnof
                2.08e-03
                           0.00e+00 Inf <2e-16
## oprior1
                1.07e-01
                           0.00e+00
                                    Inf <2e-16
                           0.00e+00 Inf <2e-16
## preanti
                5.89e-05
## race1
               -2.10e-02
                           0.00e+00 - Inf < 2e-16
## gender1
                5.06e-02
                           0.00e+00 Inf <2e-16
## symptom1
                7.40e-02
                           0.00e+00 Inf <2e-16
## offtrt1
               -3.47e-02
                           0.00e+00 - Inf < 2e-16
## cd40
               -2.03e-04
                           0.00e+00 - Inf < 2e-16
## cd80
                5.13e-05
                           0.00e+00 Inf <2e-16
## Log(scale) -4.08e+00
                           0.00e+00 - Inf < 2e-16
##
## Scale= 0.017
##
## Weibull distribution
## Loglik(model) = -253954
                            Loglik(intercept only) = 752.9
```

```
## Chisq= -509413.8 on 16 degrees of freedom, p= 1
## Number of Newton-Raphson Iterations: 30
## n= 2139
```

Has an error: "Ran out of iterations and did not converge."

Log-normal Distributed Survival Time

```
summary(survreg(Surv(time, cid) ~ ., data = sim_mat_lnorm))
## Call:
## survreg(formula = Surv(time, cid) ~ ., data = sim_mat_lnorm)
                  Value Std. Error
                                       Z
## (Intercept) -1.08e+01
                          5.73e-01 -18.91 < 2e-16
## trtZDV.ddi -2.58e-01
                                   -2.53 0.01149
                          1.02e-01
## trtZDV.ZAL -6.41e-01
                          9.12e-02 -7.02 2.2e-12
## trtddi
              -4.08e-01
                          9.20e-02 -4.44 9.1e-06
## age
              -8.33e-03
                          3.78e-03 -2.20 0.02759
## wtkg
              1.18e-03
                          2.43e-03
                                   0.48 0.62785
## hemo1
               3.43e-03
                          1.21e-01 0.03 0.97750
## drugs1
               3.93e-01
                          1.07e-01
                                     3.69 0.00023
                                   4.42 9.9e-06
## karnof
               2.24e-02 5.06e-03
## oprior1
              -2.25e-01
                          1.78e-01 -1.26 0.20656
## preanti
              6.34e-04
                          7.57e-05
                                   8.38 < 2e-16
## race1
               1.38e-01
                          7.51e-02
                                     1.84 0.06595
## gender1
              -4.52e-02
                          9.52e-02 -0.47 0.63489
## symptom1
              -5.07e-02
                          7.62e-02 -0.67 0.50600
## offtrt1
              -6.26e-01
                          6.71e-02 -9.33 < 2e-16
                          4.80e-04 57.70 < 2e-16
## cd40
               2.77e-02
## cd80
               7.05e-04
                          8.32e-05
                                    8.47 < 2e-16
## Log(scale) -2.97e-01
                          2.94e-02 -10.09 < 2e-16
##
## Scale= 0.743
##
## Weibull distribution
## Loglik(model) = 926
                       Loglik(intercept only) = -389.6
## Chisq= 2631.29 on 16 degrees of freedom, p= 0
## Number of Newton-Raphson Iterations: 10
## n= 2139
```

For some reason Surveg works with the log-normal distributed survival times but not the Weibull-distributed survival times, ironically enough.

Glmnet Simulation

Weibull distributed survival times

```
coef(cv_phmnet, s = cv_phmnet$lambda.1se)
## 16 x 1 sparse Matrix of class "dgCMatrix"
## trtZDV.ddi -0.1333040691
## trtZDV.ZAL .
## trtddi
## age
             -0.0014868067
## wtkg
## hemo1
## drugs1
## karnof
## oprior1
              0.0002301603
## preanti
## race1
## gender1
## symptom1
              0.1737496563
## offtrt1 -0.5842351610
## cd40
            0.0297878005
## cd80
              0.0002183763
Log-normal distributed survival times
cv_phmnet_lnorm <- cv.glmnet(as.matrix(sim_mat_lnorm[-c(1,2)]),</pre>
                            Surv(sim_mat_lnorm$time, sim_mat_lnorm$cid),
                            family = "cox", alpha = .95)
coef(cv_phmnet_lnorm, s = cv_phmnet_lnorm$lambda.1se)
## 16 x 1 sparse Matrix of class "dgCMatrix"
##
## trtZDV.ddi 0.1459767101
## trtZDV.ZAL 0.3081062364
## trtddi 0.0314056288
## age
              0.0001826153
## wtkg
## hemo1
## drugs1
## karnof
            -0.0016872316
## oprior1
## preanti
            -0.0005571752
## race1
             -0.0939491403
## gender1
## symptom1 -0.0377871247
## offtrt1 0.7344315562
```

cd40

cd80

-0.0377602313

-0.0005874636

PH HARE Simulation

Weibull distributed survival times

```
phm_hare <- hare(sim_mat$time, sim_mat$cid, as.matrix(sim_mat[-c(1,2)]), prophaz = TRUE)</pre>
(fcts <- phm_hare$fcts)</pre>
      dim1 knot1 dim2 knot2
##
                                       beta
## 1
         0
               0
                    NA
                          NA
                              4.810484e+00 1.697890e-01
## 2
         0
               1
                    NA
                          NA -7.798423e+01 2.609708e+00
## 3
        15
               0
                   NA
                              3.708781e-02 1.294960e-03
## 4
        14
               0
                   NA
                          NA -9.184653e-01 9.630566e-02
## 5
        10
               0
                   NA
                          NA 4.645391e-04 9.555504e-05
## 6
        13
               0
                   NA
                          NA 4.330778e-01 1.114339e-01
## 7
                   NA
                              3.559056e-04 9.396533e-05
        16
               0
                          NA
## 8
         1
               0
                   NA
                          NA -6.494517e-01 1.247080e-01
## 9
         3
               0
                   NA
                          NA -5.211305e-01 1.221323e-01
## 10
         2
                          NA -4.659746e-01 1.246135e-01
```

Log-normal distributed survival times

```
beta
##
      dim1 knot1 dim2 knot2
                                                      SE
## 1
         0
               0
                   NA
                             9.376086e+00 7.083705e-01
## 2
        15
               0
                   NA
                         NA -8.013158e-03 3.409217e-03
## 3
        15
               1
                   NA
                         NA -5.987225e-02 4.159880e-03
## 4
        14
                   NA
                             2.798081e+00 3.670815e-01
         0
## 5
               3
                   NA
                         NA -1.320843e+00 2.983359e-01
## 6
         0
               1
                   NA
                         NA -6.959544e+03 1.107726e+03
         0
               2
                   NA
## 7
                         NA -1.666111e+01 1.655523e+00
                         NA 1.318860e+00 1.287100e-01
## 8
         1
               0
                   NA
## 9
         2
               0
                   NA
                             1.138402e+00 1.266781e-01
                         NA
## 10
         3
               0
                   NA
                         NA
                             8.543355e-01 1.269481e-01
                         NA -5.797461e-01 1.048808e-01
               0
                   NA
## 11
        13
## 12
         4
               0
                   NA
                             3.908264e-02 7.251078e-03
## 13
         4
               0
                   14
                          0 -3.560878e-02 9.715485e-03
```

non-PH HARE Simulation

Weibull distributed survival times

```
nphm_hare_sim <- hare(sim_mat$time, sim_mat$cid, as.matrix(sim_mat[-c(1,2)]))
(fcts <- nphm_hare_sim$fcts)</pre>
```

```
##
      dim1 knot1 dim2 knot2
                                      beta
## 1
         0
               0
                         NA 4.810484e+00 1.697890e-01
                   NΑ
## 2
         0
                   NA
                         NA -7.798423e+01 2.609708e+00
                             3.708781e-02 1.294960e-03
## 3
        15
               0
                   NA
## 4
        14
               0
                   NA
                         NA -9.184653e-01 9.630566e-02
## 5
                  NA
        10
               0
                         NA 4.645391e-04 9.555504e-05
                         NA 4.330778e-01 1.114339e-01
## 6
        13
               0
                  NA
## 7
        16
               0
                   NA
                         NA
                             3.559056e-04 9.396533e-05
## 8
         1
               0
                   NA
                         NA -6.494515e-01 1.247080e-01
## 9
         3
               0
                   NA
                         NA -5.211303e-01 1.221323e-01
## 10
         2
               0
                         NA -4.659744e-01 1.246135e-01
# Which covariates have an interaction with time (or a knot of it)?
unique(fcts[fcts[,1] == 0 & !is.na(fcts[,3]), 3])
## numeric(0)
```

The results here seem to be exactly the same as those for the PH HARE model

Log-normal distributed survival times

```
nphm_hare_sim_lnorm <- hare(sim_mat_lnorm$time, sim_mat_lnorm$cid, as.matrix(sim_mat_lnorm[-c(1,2)]))
(fcts <- nphm_hare_sim_lnorm$fcts)</pre>
##
      dim1 knot1 dim2 knot2
                                     beta
## 1
         0
                             4.061998e+00 1.010650e+00
                             2.022812e-02 5.830756e-03
## 2
        15
               0
                   NA
                         NA
## 3
        15
               1
                   NA
                         NA -7.912540e-02 5.534135e-03
## 4
        14
               0
                   NA
                         NA 1.482998e+00 9.121504e-02
## 5
         0
               2
                  NA
                         NA 1.006587e+02 1.887440e+01
## 6
                         NA -7.807387e+03 1.174774e+03
         0
                  NA
               1
## 7
        0
               2
                  15
                          0 -6.238626e-01 9.628516e-02
## 8
        13
               0
                 NA
                         NA -5.308365e-01 1.042583e-01
## 9
         1
               0
                  NA
                         NA 1.196092e+00 1.257502e-01
         2
## 10
               0
                   NA
                         NA
                             1.157569e+00 1.263454e-01
## 11
         3
               0
                   NA
                         NA 8.161224e-01 1.263709e-01
## 12
               3
                   NA
                         NA -3.843820e+00 7.976292e-01
# Which covariates have an interaction with time (or a knot of it)?
unique(fcts[fcts[,1] == 0 & !is.na(fcts[,3]), 3])
```

[1] 15

Simulating N = 100 Times

```
#' Select and calculate coefficient estimates for Cox PH, penalized PH, HARE PH,
#' and HARE non-PH models based on N simulated data sets.
#'
#' This function calls the simulation function for the distribution of interest N
#' times and calculates the corresponding regression coefficient estimates for
#' each simulated data set.
#' @param N number of simulated data sets to fit the models to.
```

```
#' Oparam p number of covariates in original dataset
#' @param ... arguments for simulate_dist
#' Greturn p x 5 x N array containing the coefficient estimates for variables
#' selected among p initial variables by 4 models fitted on N data sets,
#' as well as variables that the non-PH HARE model selects as having
#' an interaction with time (violation of proportional hazards)
#' @export
simulate_regression <- function(N, p, ...) {</pre>
 res \leftarrow array(NA, dim = c(p, 5, N))
 for (i in 1:N) {
    sim_mat <- simulate_dist(...)</pre>
    # Cox Proportional Hazards model
    phm_sim_mat <- coxph(Surv(time, cid) ~ ., data = sim_mat)</pre>
    s_phm_sim_mat <- summary(phm_sim_mat)</pre>
    # only storing the coefficient values for which the p-value is <= .05
    res[s_phm_sim_mat$coefficients[,5] <= .05, 1, i] <-</pre>
      phm_sim_mat$coefficients[s_phm_sim_mat$coefficients[,5] <= .05]</pre>
    # Penalized Proportional Hazards model
    cv phmnet <- cv.glmnet(as.matrix(sim mat[-c(1,2)]),
                            Surv(sim_mat$time, sim_mat$cid),
                            family = "cox", alpha = .95)
    selected_coef <- as.numeric(coef(cv_phmnet, s = cv_phmnet$lambda.1se))</pre>
    res[selected_coef != 0, 2, i] <- selected_coef[selected_coef != 0]</pre>
    # PH HARE model
    phm_hare <- hare(sim_mat$time, sim_mat$cid,</pre>
                      as.matrix(sim_mat[-c(1,2)]), prophaz = TRUE)
    # extracting the coefficients for basis functions
    # that do not correspond to time, knots, and/or tensor products
    fcts <- phm hare$fcts</pre>
    fcts select <- fcts[fcts[,1] != 0 \& fcts[,2] == 0 \& is.na(fcts[,3]),]
    res[fcts_select[,1], 3, i] <- fcts_select[,5]</pre>
    # non-PH HARE model
    nphm_hare <- hare(sim_mat$time, sim_mat$cid, as.matrix(sim_mat[-c(1,2)]))</pre>
    # extracting the coefficients for basis functions
```

Weibull distributed survival times

2880.832 sec elapsed

Proportion of times each covariate is selected across the four models fitted on simulated survival times from the Weibull distribution (this will be Table 5a in the manuscript)

```
load("sims500.RData")
prop_weibull <- matrix(0, nrow = 16, ncol = 5)

for (i in 1:16) {
    for (j in 1:5) {
        prop_weibull[i,j] <- sum(!is.na(sims[i, j,])) / dim(sims)[3]
    }
}
prop_weibull</pre>
```

```
## [,1] [,2] [,3] [,4] [,5]
```

```
[1,] 1.000 0.986 0.992 0.992 0.008
## [2,] 1.000 0.978 0.982 0.980 0.004
## [3,] 0.992 0.786 0.966 0.962 0.006
## [4,] 0.938 0.968 0.826 0.826 0.014
## [5,] 0.046 0.178 0.004 0.004 0.000
## [6,] 0.030 0.210 0.010 0.010 0.002
## [7,] 0.072 0.260 0.012 0.012 0.000
## [8,] 0.056 0.190 0.008 0.008 0.000
## [9,] 0.044 0.186 0.008 0.008 0.000
## [10,] 1.000 1.000 0.986 0.986 0.006
## [11,] 0.052 0.202 0.010 0.010 0.000
## [12,] 0.076 0.224 0.008 0.008 0.000
## [13,] 0.962 0.972 0.866 0.868 0.000
## [14,] 1.000 1.000 1.000 1.000 0.008
## [15,] 1.000 1.000 1.000 1.000 0.028
## [16,] 1.000 1.000 0.984 0.984 0.014
```

Log-normal distributed survival times

4112.399 sec elapsed

Proportion of times each covariate is selected across the four models fitted on simulated survival times from the Log-normal distribution (this will be Table 5b in the manuscript)

```
load("sims_lnorm500.RData")
prop_lnorm <- matrix(0, nrow = 16, ncol = 5)

for (i in 1:16) {
    for (j in 1:5) {
        prop_lnorm[i,j] <- sum(!is.na(sims[i, j,])) / dim(sims)[3]
    }
}
prop_lnorm</pre>
```

```
## [,1] [,2] [,3] [,4] [,5]
## [1,] 1.000 0.486 0.998 0.998 0.052
## [2,] 1.000 0.816 0.998 0.998 0.052
## [3,] 1.000 0.418 0.998 0.998 0.042
```

```
## [4,] 0.862 0.484 0.922 0.922 0.024
## [5,] 0.058 0.042 0.024 0.024 0.004
## [6,] 0.086 0.034 0.064 0.066 0.004
## [7,] 0.442 0.088 0.070 0.064 0.002
## [8,] 0.624 0.408 0.030 0.030 0.002
## [9,] 0.054 0.042 0.036 0.034 0.002
## [10,] 1.000 0.936 0.812 0.812 0.044
## [11,] 0.264 0.122 0.040 0.040 0.004
## [12,] 0.108 0.026 0.054 0.054 0.000
## [13,] 0.994 0.602 0.998 0.998 0.050
## [14,] 1.000 1.000 1.000 1.000 0.348
## [15,] 1.000 0.994 0.464 0.464 0.024
```

Update to do later?: track how many times the tensor product with time (indicating violation of proportional hazards) was selected for a specific covariate (ideally Offtrt)