No part of the candidate evidence in this exemplar material may be presented in an external assessment for the purpose of gaining credits towards an NCEA qualification.

91267





# Level 2 Mathematics and Statistics, 2016 91267 Apply probability methods in solving problems

KIA NOHO TAKATŪ KI TŌ ĀMUA AO!

9.30 a.m. Thursday 24 November 2016 Credits: Four

Achievement	Achievement with Merit	Achievement with Excellence
Apply probability methods in solving problems.	Apply probability methods, using relational thinking, in solving problems.	Apply probability methods, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

### You should attempt ALL the questions in this booklet.

Make sure that you have Formulae Sheet L2-MATHF.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–15 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.º

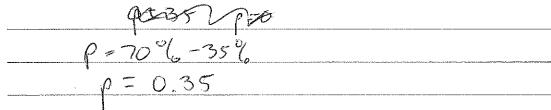
Achievement
TOTAL 12

(a) The trees in Brookhaven apple orchard are harvested twice a year, as the apples ripen at different times.

Records from previous years have shown that during the first harvest, 70% of apples are picked, while the rest are left. At the second harvest, 35% of the remaining apples are picked, while the rest are not picked.

All the apples that are picked go to the packing shed. From each harvest, 9% are selected to be sent for export; 31% are sent for sale on the local market; the rest are sent to a factory to be made into sauce.

(i) Find the probability that a randomly selected apple will not be picked.



(ii) What proportion of apples will be sent to the factory to be made into sauce?

from the first harvest?
P = D.666
There are 120 apples in an export carton.
If 172 export cartons are produced, then how many apples were there in the total crop?
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At the Pipsy Galore orchard only two varieties of apple, Jazz and Beauty, are grown. (b)

Twice as many Jazz apples as Beauty apples are grown.

Table 1 below shows the proportions of each variety of apple that have been picked after both harvests have been completed.

Table 1

Picked		Not picked	
Jazz	0.85	0.15	
Beauty	0.95	0.05	

Table 2 shows the proportion of picked apples for each variety that are exported, sold locally, or sent to the factory.

Table 2

	Export	Local	Factory
Jazz	0.12	0.58	0.3
Beauty	0.15	0.7	0.15

What is the probability that an apple selected at random from the total crop will be of (i) the Jazz variety and will be sent to the factory?

$$\rho = 0.255$$

ulations to s	support your answer, determine if this condition can be made
0 - 29	94 - 20.41
c Jih	condition can be met.
STAVES	be beauty apple at the
at in	higher than exerts for Jazz
<u>/                                    </u>	15 = Beauty
1.2	0.12 = Jaz
	- 1
_	

MI

ASSESSOR'S USE ONLY Crisp Orchard has two blocks of land where apples are grown. Apples from the larger block are grown by conventional methods, while in the other block they are grown organically.

A random sample of 1200 apples is taken over both blocks and tested for disease. The results are summarised in Table 3 below.

Table 3

	Conventional	Organic	Total
Diseased	122	58	180
Not diseased	518	502	1020
Total	640	560	1200

(a)	(i)	What proportion	of apples in the	e sample were	diseased?

180/1200

= 0.15

(ii) What proportion of the diseased apples were conventionally grown?

= 0.677

(iii) If there was a total of 171 000 organic apples grown, then based on this sample, how many apples would be expected to be grown conventionally and be diseased?

171,000 = 560 = 305.357 Convertional total = 640 x 305.357 = 195, 128

122=640 = 0.19

total diseased conventional = 195,428 x 0.19 = 37,131.32

(iv) It is claimed that apples that are conventionally grown are at least twice as likely to be diseased as apples that are grown organically.

State whether you agree with this claim, showing full calculations to support your answer.

Conventional = 122/640 = 0.19

organic = 58 ÷ 560 = 0.10

from the sample of results from table 3

it is seen that the probability of a

conventional apple being diseased is 0.19

where as for organic it is 0.1. The

conventional is just off 2 x as likely to be

otiseased as the organic apple I agree with

this claim because it is very close to being

right.

(b) Jazz and Beauty varieties are grown in both blocks.

From the same sample of 1200 apples in part (a), 890 apples were of the Jazz variety.

It was also found that 182 of the Beauty variety were not diseased.

Table 3 from part (a) is repeated here to help you answer the questions that follow.

Table 3

	Conventional	Organic	Total	
Diseased	122	58	180	1
Not diseased	518	502	1020	7 2
Total	640	560	1200	٦ \.

(i) What proportion of apples in the sample were of the Jazz variety and diseased?

840 - 1200 = 0.742 180 - 1028 = 0.176  $0.742 \times 0.176 = 0.13$ 

(ii)	It is claimed that apples are more likely to be diseased depending on their variety than whether they have been conventionally or organically grown.
	Can this claim be supported?
	Give calculations of absolute and relative risks to support your answer.
	Yes this claim can be true.
	There are 310 Beauty apples and 182
	are not diseased this leaves 128 apples
	to be diseased This is well over half
	the total diseased apples.
	128-180-0.71 71% of the
	diseases apples are Beauty apples

#### **QUESTION THREE**

Apples are sent to a factory to be made into sauce, then bottled.

Testing has shown that, when the bottling machine is operating correctly, the weight of sauce dispensed into a bottle can be taken to be normally distributed, with mean 310 grams and standard deviation 4.5 grams.

(a) (i) Find the probability that a randomly selected bottle will contain between 310 and 316 grams of sauce.

16 grams of sauce.  $\frac{310 - 316}{2}$ 

= 1338

P = 0.409

(ii) The label on the sauce bottle states that the contents weigh 300 grams. Bottles that contain less than 300 grams are considered to be under-weight.

What percentage of bottles would be expected to be under-weight?

Z = 310 -300\_ 4.5

7.5053 × 10 - 03

we would expect 0.001

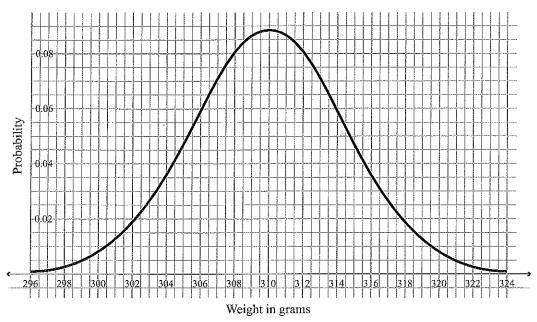
0.001 bottles to

(iii)	A quality control process identifies bottles of sauce that have contents that are overweight.
	When the machine is functioning correctly, no more than one bottle in 20 is overweight.
	If more than one in 20 bottles are over-weight, then the machine must be adjusted.
	How many grams of sauce will a bottle contain before it is considered over-weight?
	$0.05 = \frac{300M}{4.5}$
	315 8 8
	$M = \frac{310 + 0.05}{4.5}$
	= 315 q
(iv)	The quality control process involves taking a random sample of three successive bottles and measuring the weights of their contents. If more than one of the bottles is found to
(iv)	
(iv)	and measuring the weights of their contents. If more than one of the bottles is found to
(iv)	and measuring the weights of their contents. If more than one of the bottles is found to be over-weight or under-weight, then the machine is checked for possible adjustment.
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(b) If the bottling machine was operating correctly, the weight of sauce dispensed into a bottle would have a probability distribution similar in shape to the one in Figure 1 below.

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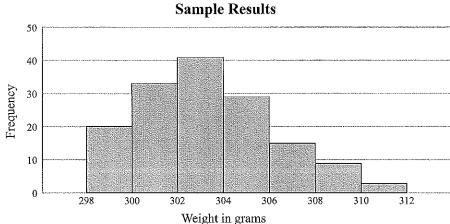




A new bottling machine is installed.

A random sample is taken of the contents of 150 bottles to test the new machine. The results are shown in the frequency histogram in Figure 2 below.

Figure 2



(i) What proportion of bottles in the sample had contents that were under-weight (i.e. the contents weighed less than 300 grams)?

i)	Compare the probability distribution with the frequency histogram that was obtained from the results of the sample.	ASSESSOR'S USE ONLY
	In your answer, you should consider the shape, centre, and spread of both distributions and provide numerical evidence.	
	With figure 1 the mean seems to be	
	directly in the centre over 310g the spread is	
	also even as it extends 14g either way. W Figure 2 the mean spens to be around 302 an	
	304 grows. The histogram looks very out of	<u>a</u>
	shape and uneven with a skew to the right	
	The spread is also only 14g. The proportion	
	to be greater the the projection figure 2 apple	
	The new bottle marking does not seem to be	
	operating correctly with the men being totally	
	off and having many underweight bothes //	
	·	

## Achieved exemplar 2016

Sub	ject:	Mathe	ematics	Standard:	61267	Total score:	12
Q		rade core	Annotation				
1	1 N1 1(b)(i) Di		1(a)(iv) No progress 1(b)(i) Did not recogn 1(b)(ii) Little progress				
2	M6 2(a)(iv) Altern		2(a)(iii) Logic is correct 2(a)(iv) Alternative ap 2(b)(ii) Little progress	proach. Doul	oles the absolute ri	sk. Incorrect cond	clusion
3			3(b)(ii) Four points bu	it only one co	mparative stateme	nt	