L2-MATHMF



See back cover for an English translation of this cover

2



Te Pāngarau me te Tauanga, Kaupae 2, 2022

TE PEPA TURE TĀTAI mō 91261M, 91262M, 91267M

Tirohia tēnei pepa hei whakaoti i ngā tūmahi i ō Pukapuka Tūmahi.

Tirohia mēnā e tika ana te raupapatanga o ngā whārangi 2 – 3 kei roto i tēnei pukapuka, ka mutu, kāore tētahi o aua whārangi i te takoto kau.

E ĀHEI ANA TŌ PUPURI I TĒNEI PUKAPUKA HEI TE MUTUNGA O TE WHAKAMĀTAUTAU.

Ngā Whārite Pūrua

Mēnā ka pēnei $ax^2 + bx + c = 0$

kātahi ka pēnei
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\bar{a}$$
, $\Delta = b^2 - 4ac$

Ngā Pūkōaro

Mēnā ka pēnei $y = b^x$ kātahi ka pēnei $x = \log_b y$

$$\log_b(xy) = \log_b(x) + \log_b(y)$$

$$\log_b \left(\frac{x}{y}\right) = \log_b(x) - \log_b(y)$$

$$\log_b(x^n) = n\log_b x$$

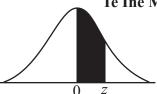
Mēnā ka pēnei $y = e^x$ kātahi ka pēnei $x = \log_e y$ $(= \ln y)$

Te Tuanaki

$$\frac{\mathrm{d}}{\mathrm{d}x}\left(x^n\right) = nx^{n-1}$$

Mēnā ka pēnei $f'(x) = x^n$, kātahi ka pēnei $f(x) = \frac{x^{n+1}}{n+1} + c$

Te Ine Mahora



$$\left(z = \frac{x - \mu}{\sigma}\right)$$

Kei ia tau te tūponotanga o te takoto ine mahora o tētahi taurangi matap \bar{o} kere, Z, ki waenga i te 0 me z.

Ngā rerekētanga	Ν	gā	rere	kētai	nga
-----------------	---	----	------	-------	-----

														Nga	. 1 (1	CKC	ung	,a	
z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
	0000	0040	0000	0120	0160	0100	0220	0270	0210	0250		0	1.2	1.0	20	2.4	20	22	26
0.0			.0080								4		12		20			32	
0.1	1		.0478								4		12		20			32	
0.2			.0871								4		12	ı	19			31	
0.3	l .		.1255								4		11	1	19			30	
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879	4	7	11	14	18	22	25	29	32
0.5			.1985								3		10		17			27	
0.6			.2324								3		10	_	16			26	
0.7	1		.2642								3	6	9	12	15	18		24	
0.8			.2939								3	6	8		14			22	
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389	3	5	8	10	13	15	18	20	23
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	2	5	7	9	12	14	16	18	21
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	2	4	6	8	10	12	14	16	19
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015	2	4	5	7	9	11	13	15	16
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177	2	3	5	6	8	10	11	13	14
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319	1	3	4	6	7	8	10	11	13
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441	1	2	4	5	6	7	8	10	11
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545	1	2	3	4	5	6	7	8	9
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633	1	2	3	3	4	5	6	7	8
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706	1	1	2	3	4	4	5	6	6
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767	1	1	2	2	3	4	4	5	5
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817	0	1	1	2	2	3	3	4	4
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857	0	1	1	2	2	2	3	3	4
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890	0	1	1	1	2	2	2	3	3
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916	0	0	1	1	1	2	2	2	2
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936	0	0	1	1	1	1	1	2	2
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	0	0	0	1	1	1	1	1	1
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	0	0	0	0	1	1	1	1	1
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	0	0	0	0	0	1	1	1	1
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981	0	0	0	0	0	0	0	0	1
2.9			.4982								0	0	0	0	0	0	0	0	1
3.0	4987	4987	.4987	4988	4988	4989	4989	4989	4990	4990	0	0	0	0	0	0	0	0	0
3.1			4991								0	0	0	0	0	0	0	0	0
3.2			.4994		–	=	–	=			0	0	0	0	0	0	0	0	0
3.3			.4995									0	0	0	0	0	0	0	0
3.4			.4997								0	0	0	0	0	0	0	0	0
3.5	4998	4998	.4998	4998	4998	4998	4998	4998	4998	4998	0	0	0	0	0	0	0	0	0
3.6			.4999								0	0	0	0	0	0	0	0	0
3.7			.4999									0	0	0	0	0	0	0	0
3.8			.4999								0	0	0	0	0	0	0	0	0
3.9			.5000								0	0	0	0	0	0	0	0	0
L ^{J,}	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	ட்	J	U	"	J	v	J	J	

Quadratic Equations

If
$$ax^2 + bx + c = 0$$

then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
and $\Delta = b^2 - 4ac$

Logarithms

If
$$y = b^x$$
 then $x = \log_b y$

$$\log_b(xy) = \log_b(x) + \log_b(y)$$

$$\log_b\left(\frac{x}{y}\right) = \log_b(x) - \log_b(y)$$

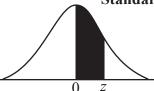
$$\log_b\left(x^n\right) = n\log_b x$$
If $y = e^x$ then $x = \log_e y$ (= ln y)

Calculus

$$\frac{\mathrm{d}}{\mathrm{d}x}\left(x^n\right) = nx^{n-1}$$

If
$$f'(x) = x^n$$
, then $f(x) = \frac{x^{n+1}}{n+1} + c$

Standard Normal Distribution



3

$$\left(z = \frac{x - \mu}{\sigma}\right)$$

Each entry gives the probability that the standardised normal random variable Z lies between 0 and z.

Differences

														Diff	ere	nces	•		
z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359	4	8	12	16	20	24	28	32	36
0.1				.0517							4		12		20		l	32	
0.2				.0910							4		12		19			31	
0.3				.1293							4		11		19			30	
0.4				.1664							4	-	11		18			29	-
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	2190	.2224	3	7	10	14	17	21	24	27	31
0.6				.2357							3		10		16		l	26	
0.7	2580	2612	2642	.2673	2704	2734	2764	2794	2823	2852	3	6	9	12	15	18	21	24	2
0.8				.2967							3	6	8		14	-		22	
0.9				.3238							3	5	8		13			20	
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	2	5	7	9	12	14	16	18	2
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	2	4	6	8	10	12	14	16	1
1.2				.3907							2	4	5	7	9	11	13	15	1
1.3				.4082							2	3	5	6	8	10	11	13	1
1.4				.4236							1	3	4	6	7	8	l	11	
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441	1	2	4	5	6	7	8	10	1
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545	1	2	3	4	5	6	7	8	
1.7				.4582							1	2	3	3	4	5	6	7	
1.8				.4664							1	1	2	3	4	4	5	6	
1.9				.4732							1	1	2	2	3	4	4	5	
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817	0	1	1	2	2	3	3	4	
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857	0	1	1	2	2	2	3	3	
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890	0	1	1	1	2	2	2	3	
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916	0	0	1	1	1	2	2	2	
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936	0	0	1	1	1	1	1	2	
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	0	0	0	1	1	1	1	1	
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	0	0	0	0	1	1	1	1	
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	0	0	0	0	0	1	1	1	
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981	0	0	0	0	0	0	0	0	
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986	0	0	0	0	0	0	0	0	
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990	0	0	0	0	0	0	0	0	
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993	0	0	0	0	0	0	0	0	
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995	0	0	0	0	0	0	0	0	
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997	0	0	0	0	0	0	0	0	
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998	.4998	0	0	0	0	0	0	0	0	
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	0	0	0	0	0	0	0	0	
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.5000	.5000	.5000	0	0	0	0	0	0	0	0	
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	0	0	0	0	0	0	0	0	

L2-MATHMF

English translation of the wording on the front cover

Level 2 Mathematics and Statistics 2022

FORMULAE SHEET for 91261M, 91262M, 91267M

Refer to this sheet to answer the questions in your Question and Answer Booklets.

Check that this booklet has pages 2–3 in the correct order and that none of these pages is blank.

YOU MAY KEEP THIS SHEET AT THE END OF THE EXAMINATION.