L2-MATHMF



See back cover for an English translation of this cover





Te Pāngarau me te Tauanga, Kaupae 2, 2012

2.00 i te ahiahi Rāhina 19 Whiringa-ā-rangi 2012

PUKA TIKANGA TĀTAI mō 91261M, 91262M, 91267M

Tirohia tēnei puka hei whakautu i ngā pātai o ō Pukapuka Whakautu, Pātai hoki.

Āta tirohia kua tāngia a muri o tēnei puka.

KA TAEA TĒNEI PUKA TE PUPURI HEI TE MUTUNGA O TE WHAKAMĀTAUTAU.

Whārite pūrua

Mēnā
$$ax^2 + bx + c = 0$$

kāti $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
ā $\Delta = b^2 - 4ac$

Taupū kōaro

Mēnā
$$y = b^x$$
 kāti $x = \log_b y$
 $\log_b (x^n) = n \log_b x$
Mēnā $y = e^x$ kāti $x = \log_e y (= \ln y)$

Tuanaki

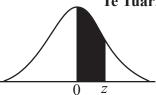
$$\frac{\mathrm{d}}{\mathrm{d}x}\left(x^n\right) = nx^{n-1}$$

Mēnā
$$f'(x) = x^n$$
, kāti $f(x) = \frac{x^{n+1}}{n+1} + c$

Tūponotanga

$$Z = \frac{X - \mu}{\sigma}$$

Te Tuaritanga Hangarite Aro Whānui



2

$$\left(Z = \frac{X - \mu}{\sigma}\right)$$

Ko ia tau e whakaatu ana i te tūponotanga ka noho mai te taurangi matapōkere hangarite aro whānui o te Z ki

0 0 0

waenganui i te 0 me te z. Huatango 4 5 6 7 8 9 0.0 | .0000 | .0040 | .0080 | .0120 | .0160 | .0199 | .0239 | .0279 | .0319 | .0359 4 8 12 16 20 24 28 32 36 0.1 | .0398 | .0438 | .0478 | .0517 | .0557 | .0596 | .0636 | .0675 | .0714 | .0754 8 12 16 20 24 28 32 36 0.2 | .0793 | .0832 | .0871 | .0910 | .0948 | .0987 | .1026 | .1064 | .1103 | .1141 4 8 12 15 19 22 27 31 35 15 19 22 26 30 34 0.3 | .1179 | .1217 | .1255 | .1293 | .1331 | .1368 | .1406 | .1443 | .1480 | .1517 8 11 0.4 | .1554 .1591 .1628 .1664 .1700 .1736 .1772 .1808 .1844 .1879 4 7 11 14 18 22 25 29 32 .1915 .1950 .1985 .2019 .2054 .2088 .2123 .2157 .2190 .2224 14 17 21 24 27 31 3 7 10 6 10 0.6 | .2258 .2291 .2324 .2357 .2389 .2422 .2454 .2486 .2518 .2549 13 16 19 23 26 29 12 15 18 21 24 27 .2580 .2612 .2642 .2673 .2704 .2734 .2764 .2794 .2823 .2852 6 9 0.8 | .2881 | .2910 | .2939 | .2967 | .2996 | .3023 | .3051 | .3078 | .3106 | .3133 3 6 8 11 14 17 19 22 25 0.9 | .3159 .3186 .3212 .3238 .3264 .3289 .3315 .3340 .3365 .3389 3 5 8 10 13 15 18 20 23 1.0 | .3413 | .3438 | .3461 | .3485 | .3508 | .3531 | .3554 | .3577 | .3599 | .3621 2 5 7 9 12 14 16 18 21 2 8 10 12 14 16 19 1.1 | .3643 | .3665 | .3686 | .3708 | .3729 | .3749 | .3770 | .3790 | .3810 | .3830 4 6 2 4 5 1.2 | .3849 | .3869 | .3888 | .3907 | .3925 | .3944 | .3962 | .3980 | .3997 | .4015 7 9 11 13 15 16 2 3 5 6 8 10 11 13 14 1.4 | .4192 | .4207 | .4222 | .4236 | .4251 | .4265 | .4279 | .4292 | .4306 | .4319 1 3 4 6 7 8 10 11 13 1.5 | .4332 | .4345 | .4357 | .4370 | .4382 | .4394 | .4406 | .4418 | .4429 | .4441 2 4 5 6 2 3 1.6 | .4452 | .4463 | .4474 | .4484 | .4495 | .4505 | .4515 | .4525 | .4535 | .4545 5 7 8 9 1.7 | .4554 | .4564 | .4573 | .4582 | .4591 | .4599 | .4608 | .4616 | .4625 | .4633 2 3 6 1 1 2 1.8 | .4641 | .4649 | .4656 | .4664 | .4671 | .4678 | .4686 | .4693 | .4699 | .4706 5 1.9 .4713 .4719 .4726 .4732 .4738 .4744 .4750 .4756 .4761 .4767 1 1 2 2 3 .4772 .4778 .4783 .4788 .4793 .4798 .4803 .4808 .4812 .4817 2.1 | .4821 | .4826 | .4830 | .4834 | .4838 | .4842 | .4846 | .4850 | .4854 | .4857 0 1 1 2 2 3 3 4 2 1 2 2 3 3 .4861 .4864 .4868 .4871 .4875 .4878 .4881 .4884 .4887 .4890 0 1 1 .4893 .4896 .4898 .4901 .4904 .4906 .4909 .4911 .4913 .4916 0 0 2 2 2 2 1 1 2.4 | .4918 | .4920 | .4922 | .4925 | .4927 | .4929 | .4931 | .4932 | .4934 | .4936 0 0 0 0 .4938 .4940 .4941 .4943 .4945 .4946 .4948 .4949 .4951 .4952 0 .4953 .4955 .4956 .4957 .4959 .4960 .4961 .4962 .4963 .4964 0 1 1 1 1 .4965 .4966 .4967 .4968 .4969 .4970 .4971 .4972 .4973 .4974 0 0 0 0 1 1 1 2.8 .4974 .4975 .4976 .4977 .4977 .4978 .4979 .4979 .4980 .4981 0 0 0 0 0 0 0 1 2.9 | .4981 | .4982 | .4982 | .4983 | .4984 | .4984 | .4985 | .4985 | .4986 | .4986 0 0 0 0 0 0 0 1 0 0 0 0 .4987 .4987 .4987 .4988 .4988 .4989 .4989 .4989 .4990 0 0 0 0 3.1 | 4990 | 4991 | 4991 | 4992 | 4992 | 4992 | 4992 | 4993 | 4993 3.2 .4993 .4993 .4994 .4994 .4994 .4994 .4994 .4995 .4995 .4995 0 0 0 0 0 0 0 0 3.3 | .4995 | .4995 | .4995 | .4996 | .4996 | .4996 | .4996 | .4996 | .4997 0 0 0 0 0 0 0 0 0 0 0 3.4 | .4997 | .4997 | .4997 | .4997 | .4997 | .4997 | .4998 | .4998 | 0 0 0 0 0 0 0 0 0 0 0 0 .4998 .4998 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 .4999 0 0 0 0 0 0 0 0 0 0 0 .4999 .4999 .4999 .4999 .4999 .4999 .5000 .5000 .5000 0 0 0 0 0 .5000 .5000 .5000 .5000 .5000 .5000 .5000 .5000 .5000 .5000 0 0 0 0 0 0

Quadratics

If
$$ax^2 + bx + c = 0$$

then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
and $\Delta = b^2 - 4ac$

Logarithms

If
$$y = b^x$$
 then $x = \log_b y$

$$\log_b (x^n) = n \log_b x$$
If $y = e^x$ then $x = \log_e y (= \ln y)$

Calculus

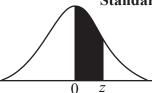
$$\frac{\mathrm{d}}{\mathrm{d}x}\left(x^n\right) = nx^{n-1}$$

If
$$f'(x) = x^n$$
, then $f(x) = \frac{x^{n+1}}{n+1} + c$

Probability

$$Z = \frac{X - \mu}{\sigma}$$

_ Standard Normal Distribution



3

$$\left(Z = \frac{X - \mu}{\sigma}\right)$$

Each entry gives the probability that the standardised normal random variable Z lies between 0 and z.

Differences

														D_{111}	CIC	IICC.	,		
Z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359	4	8	12	16	20	24	28	32	36
0.1				.0517							4	8	12	l	20				36
0.2				.0910							4		12		19				35
0.3				.1293							4		11		19				34
0.4				.1664							4	-	11		18				32
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224	3	7	10	14	17	21	24	27	31
0.6	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549	3	6	10	13	16	19	23	26	29
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852	3	6	9	12	15	18	21	24	27
0.8	.2881	.2910	.2939	.2967	.2996	.3023	.3051	.3078	.3106	.3133	3	6	8	11	14	17	19	22	25
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389	3	5	8	10	13	15	18	20	23
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	2	5	7	9	12	14	16	18	21
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	2	4	6	8	10	12	14	16	19
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015	2	4	5	7	9	11	13	15	16
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177	2	3	5	6	8	10	11	13	14
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319	1	3	4	6	7	8	10	11	13
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441	1	2	4	5	6	7	8	10	11
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545	1	2	3	4	5	6	7	8	9
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633	1	2	3	3	4	5	6	7	8
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706	1	1	2	3	4	4	5	6	6
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767	1	1	2	2	3	4	4	5	5
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817	0	1	1	2	2	3	3	4	4
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857	0	1	1	2	2	2	3	3	4
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890	0	1	1	1	2	2	2	3	3
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916	0	0	1	1	1	2	2	2	2
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936	0	0	1	1	1	1	1	2	2
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	0	0	0	1	1	1	1	1	1
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	0	0	0	0	1	1	1	1	1
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	0	0	0	0	0	1	1	1	1
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981	0	0	0	0	0	0	0	0	1
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986	0	0	0	0	0	0	0	0	1
3.0				.4988							0	0	0	0	0	0	0	0	0
3.1				.4991							0	0	0	0	0	0	0	0	0
3.2				.4994							0	0	0	0	0	0	0	0	0
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997	0	0	0	0	0	0	0	0	0
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998	.4998	0	0	0	0	0	0	0	0	0
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	0	0	0	0	0	0	0	0	0
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	0
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	0
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.5000	.5000	.5000	0	0	0	0	0	0	0	0	0
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	0	0	0	0	0	0	0	0	0

L3-STATMF

English translation of the wording on the front cover

Level 2 Mathematics and Statistics, 2012

2.00 pm Monday 19 November 2012

FORMULAE SHEET for 91261M, 91262M, 91267M

Refer to this sheet to answer the questions in your Question and Answer booklets.

Check that this sheet is printed on the back.

YOU MAY KEEP THIS SHEET AT THE END OF THE EXAMINATION.