## Assessment Schedule – 2012

## Mathematics and Statistics: Apply probability methods in solving problems (91267)

|   |   | <b>Expected Covera</b>  | ge     |                                 |            |  |                 |               |          |      |                       |
|---|---|---|--------|---------------------------------|------------|--|-----------------|---------------|----------|------|-----------------------|
| Q   | whe   | swers will vary depenether the candidate us<br>les or a graphing calculate  | es the | Achie                           | vement (u) |  | ľ               | Merit (r)     |          | Exce | ellence (t)           |
| ONE (a)   | 0.43  | 3319  |        | Probabilit                      | y found.   |  |                 |               |          |      |                       |
| (b)   | 10.5  | 56%   |        | Percentage found.               |            |  |                 |               |          |      |                       |
| (c)   | (40.33,41.67)   |   |        | ONE end point.                  |            |  | BOTH given.     |               |          |      |                       |
| (d)   | Prob = 0.1056<br>1900<br>10.56% less than 40 g<br>0.1056 × 18 000 = 1900                                    |   |        | Percentage or equivalent found. |            |  | Expec<br>found. |               |          |      |                       |
| (e)(i)  | The proportion weighing less than 40 g is 10.56%, which is considerably larger than the 4% claimed setting. |   |        | Comment appropriate.            |            |  |                 |               |          |      |                       |
| (ii)  | $Z =$ 1.75 Fix 1.75 $\mu =$ Fix 1.75 $\sigma =$ Mea   | probability = 0.04<br>-1.75<br>$5 = \frac{\mu - 40}{\sigma}$<br>$\sigma = 0.8$<br>$5 \times 0.8 = \mu - 40$<br>41.401 g<br>$\mu = 41$<br>$5\sigma = 41 - 40$<br>= $\frac{1}{1.75}$<br>an 41.401 g<br>SD = 0.571 |        |                                 |            |  | Correct for Z.  | ct value four | Mea      |      | R standar<br>n found. |
| (f) The data is not bell shaped (not symmetrically distributed about a mean).  It is bi-modal.  Mean and median not the same.  Most of the data is within 2 standard deviations.  The mean is not 41. |   |   |        |                                 | given      | l description<br>with TWO<br>nt comments | give            |               | cription |      |                       |
| NØ  | •   | N1  | N2     | A3                              | A4         |  | M5              | M6            | E7       |      | E8                    |
| o response  |   | Attempt at one question   | 1 of u | 2 of u                          | 3 of u     | 2  | e of r          | 3 of r        | 1 of     | t    | 2 of t                |

| Q  | Expected Cover  | age                                   | Achievement (u) |                             |                         |      | Merit (r)         |        | Excellence (t) |             |
|--|---|---------------------------------------|-----------------|-----------------------------|-------------------------|------|-------------------|--------|----------------|-------------|
| TWO (a)(i)   | $0.95 \times 0.93 = 0.8835$   | Correct solution.                     |                 |                             |                         |      |                   |        |                |             |
| (ii)   | $1 - 0.25 \times 0.05 = 0.987$<br>OR $0.95 + 0.05 \times 0.75$<br>= 0.9875<br>May be found by adding probabilities. | ONE probability correctly calculated. |                 |                             | Probability calculated. |      |                   |        |                |             |
| (iii)  | $0.25 \times 0.6 = 0.15$  |                                       |                 |                             |                         |      |                   | Correc | t probability. |             |
| (b)(i)   | 0.084   | Correct probability.                  |                 |                             |                         |      |                   |        |                |             |
| (ii)   | $0.12 \times 0.3 = 0.036$<br>$0.036 \times 250\ 000$<br>= 9000 customers  | Probability calculated.               |                 | Expected number calculated. |                         |      |                   |        |                |             |
| (iii)(A)   | 0.084 + 0.88x = 0.1Probability (x) = 0.01818  |                                       |                 | Equation set up.            |                         |      | ability<br>lated. |        |                |             |
| (B) Probability complained and left = $0.12 \times 0.7$ = $0.084$ Probability a person left = $0.1$ Probability that if they had left they had complained = $\frac{0.084}{0.1} = 0.84$ |   |                                       |                 |                             |                         | Mino | or error.         |        | Correc         | t solution. |
| NØ   | N1  | N2                                    | A3              | A4                          | N                       | M5   | M6                |        | E7             | E8          |
| No response; relevant evider   |   | 1 of u                                | 2 of u          | 3 of u                      | 2                       | of r | 3 of r            |        | l of t         | 2 of t      |

| Q            |   | Expected Coverage Achievement (u) |        |                             |                                    | nt (u)                     | Merit (r  | ;)                | Excellence (t)                                    |   |        |
|--------------|---|-----------------------------------|--------|-----------------------------|------------------------------------|----------------------------|---|-------------------|---|---|--------|
| THREE (a)(i) | $\frac{572}{800} = 0.715$   |                                   |        | Accept unsimplified answer. |                                    |                            |   |                   |   |   |        |
| (ii)         | $\frac{33}{228} = 0.1447$   |                                   |        |                             |                                    | accept unsimplified nswer. |   |                   |   |   |        |
| (iii)        | $\frac{228}{800} \times 2000 = 570$   |                                   |        |                             |                                    |                            | Correct solution.                                   |                   |   |   |        |
| (iv)         | Risk = $\frac{228}{800}$<br>= 0.285<br>2 in 7 is 0.2857<br>So risk is very close to 2 in 7.   |                                   |        |                             | Correct risk.                      |                            |   | Valid comparison. |   |   |        |
| (v)          | Female risk = $\frac{195}{600}$ = 0.325<br>Male risk = $\frac{33}{200}$ = 0.165<br>Relative risk = 1.97<br>So newspaper report is wrong – risk is almost twice for female than male.  |                                   |        |                             | rrect risk fo<br>nder.             | r one                      | both and insufficient is                            |                   | both<br>suffi                                     | Correct risks for both and sufficient conclusion. |        |
| (b)(i)       | $\frac{107}{501} = 0.214$   |                                   |        |                             | Co                                 | rrect risk.                |   |                   |   |   |        |
| (ii)         | Person under 40 risk = $\frac{107}{501}$ = 0.214  Person over 40 risk = $\frac{121}{299}$ = 0.404  Relative risk = 1.89  The risk is significantly higher for a person over 40 years old. About twice the risk. Claim is valid. |                                   |        |                             | Risk for one age group calculated. |                            | Correct risks for both and insufficient conclusion. |                   | Correct risks for both and sufficient conclusion. |   |        |
| NØ           |   | N1                                | N2     | A3                          |                                    | A4                         | M5  | M6                | Е   | E7  | E8     |
| No respon    | ise; no<br>vidence  | Attempt at one question           | 1 of u | 2 of u                      |                                    | 3 of u                     | 2 of r  | 3 of r            | 1 (   | of t  | 2 of t |

## **Judgement Statement**

|             | Not Achieved | Achievement | Achievement with Merit | Achievement with Excellence |  |  |
|-------------|--------------|-------------|------------------------|-----------------------------|--|--|
| Score range | 0 – 8        | 9 – 14      | 15 – 19                | 20 – 24                     |  |  |