No part of the candidate evidence in this exemplar material may be presented in an external assessment for the purpose of gaining credits towards an NCEA qualification.

91031





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# Level 1 Mathematics and Statistics, 2015 91031 Apply geometric reasoning in solving problems

9.30 a.m. Monday 9 November 2015 Credits: Four

A	Achievement	Achievement with Merit	Achievement with Excellence
Apply geome problems.	tric reasoning in solving	Apply geometric reasoning, using relational thinking, in solving problems.	Apply geometric reasoning, using extended abstract thinking, in solving problems.

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

You should attempt ALL the questions in this booklet.

Show ALL working.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–11 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

Merit
TOTAL 15

# **Annotated Exemplar Template**

Merit exemplar for 91031 2015			Total score	15	
Q	Grade score	Annotation			
1	M5	Candidate has correctly selected and used geometric concepts. They have answered a series of questions demonstrating an understanding of angle properties of isosceles triangles and trigonometric relationships in right angles triangles. To gain an E7 or E8 the candidate would need to use similar triangles to find lengths and compare areas.			
2	M6	Candidate has correctly selected and used geometric properties of angles, polygons and circles. They have clear reasons for the angles they have found. To gain an E7 or E8 the candidate would have needed to develop further a chain of logical reasoning. They were not able to fully prove that YR was equal to RZ in c). In 2b) iii) the candidate could not form a trigonometric relationship for NL using x and a.			
3	A4	Candidate has correctly selected and used geometric properties of angles and circles and trigonometric relationships. In a) iii) The student was not able to correctly interpret the solution in context. The candidate was not able to correctly find a correct total distance or bearing.			

#### **QUESTION ONE**

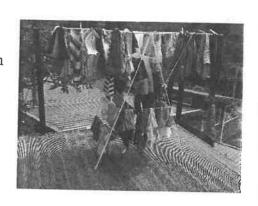
(a) A clothes drying rack has two horizontal levels on which the clothes can be hung as shown by lines AE and HI on the diagram below.

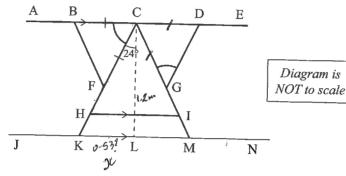
AE is parallel to HI and parallel to the ground JN.

The rack is symmetrical around the line CL.

$$BC = CF$$

Angle KCL =  $24^{\circ}$ 





(i) Find the size of angle BCF.

Justify your answer with clear geometric reasoning.

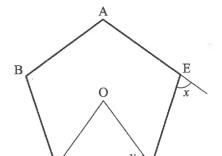
(ii) Find the size of angle DGC.

Justify your answer with clear geometric reasoning.

(iii) The height of AE above the ground is 1.2 m. SOH CAH TOA Pippa says the length KL is 0.53 m.

Show that she is correct.

## **QUESTION TWO**

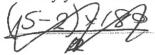


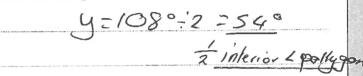
- ABCDE is a regular pentagon with centre O. (a)
  - Find the value of x and explain your answer. (i)

72° exf L's of pollygon = 360°

(ii) Find the value of y.

Justify your answer with clear geometric reasoning.





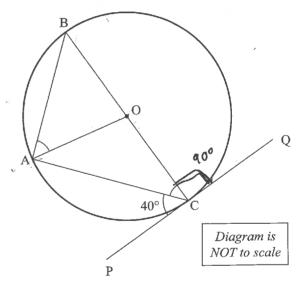
(n-2) ×180

(5-2)×180 : 500 = 108 int 28 pollygon

A, B, and C are on the circumference of a circle with centre O. BOC is a diameter.

QCP is a tangent to the circle.

Angle ACP =  $40^{\circ}$ .



Find the size of angle ACO. (i)

> Justify your answer with clear geometric reasoning.

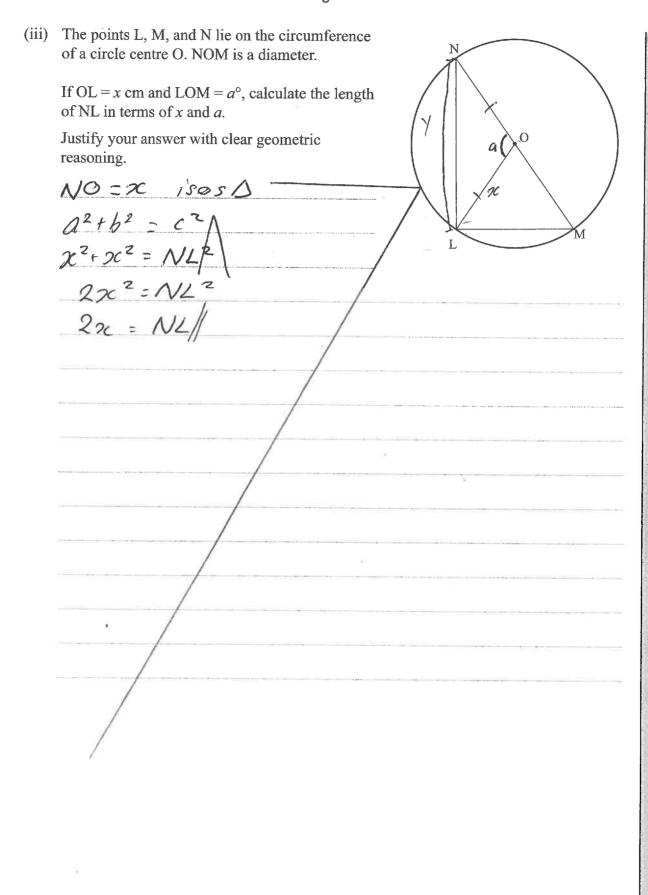
LACO= 90=40=500 rad 1 tot

Find the size of angle OAB. (ii)

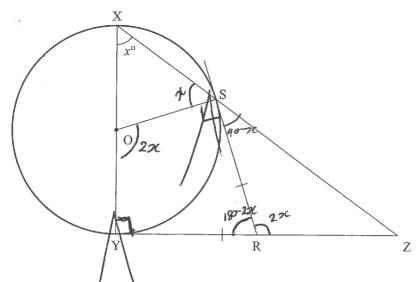
Justify your answer with clear geometric reasoning.

/AOC = 180-50-50-80° sum of isos A LBOA = 180° L's on a Line.

LOAB = 180-100 = 40° Sam of isos A



(c)



The points S, X, and Y are on the circumference of a circle centre O.

XY is a diameter of the circle.

YZ and SR are tangents to the circle.

RS = RY

Angle  $YXZ = x^{\circ}$ 

Prove that YR = RZ

[XSS= x° base L'S 1805 ] [XOS=180-2x Sum of 1505 ] LYRS=360-180-2x =180-2x Sum of []

> M6 M6

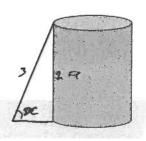
### **QUESTION THREE**

(a) (i) A farmer wants to climb a ladder to check the water in a tank.

He uses a 3 metre ladder and places it so that the top of the ladder just reaches the top of the tank.

The top of the tank is 2.9 metres from the ground.

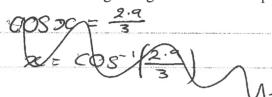
He wants the angle of the ladder to the ground to be less than  $80^{\circ}$ .



ASSESSOR'S USE ONLY

Diagram is NOT to scale

Is the ladder long enough to meet this requirement?



 $Sin x = \frac{2.7}{3}$   $x = Sin^{-1}\left(\frac{2.9}{3}\right)$ 

2-75.16% Yes the
Ladder is
long enough

(ii) How far is the foot of this ladder from the base of the tank?

Assume that the tank is sitting on level ground.

$$a^{2} + b^{2} = c^{2}$$

$$c^{2} - a^{2} = b^{2}$$

$$3^{2} - 2 \cdot 9^{2} = b^{2}$$

$$9-8.41=6^{2}$$
 $\sqrt{0.59}=6$ 

ase 5200 Jan 6=0.77

(iii) If the farmer places the ladder at 80° to the ground, how much of the ladder is above the top of the tank?

72 2.9

$$\frac{2 \times \sin 80}{\sin 80} = 2.9$$

$$\frac{\sin 80}{\sin 80} = \frac{2.9}{\sin 80}$$

$$2 = 2.9$$

$$2 = 8.1080$$

There

none it is below the tank

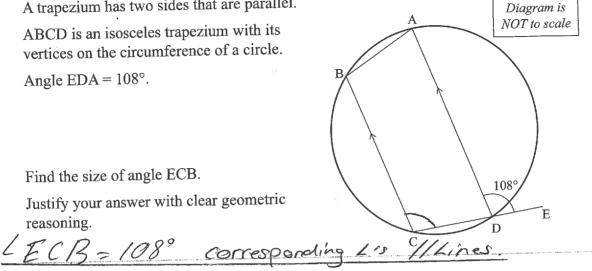
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A trapezium has two sides that are parallel. (i) (b) ABCD is an isosceles trapezium with its vertices on the circumference of a circle.

Angle EDA =  $108^{\circ}$ .

Find the size of angle ECB.

Justify your answer with clear geometric reasoning.

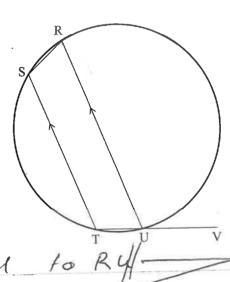


RSTU is any trapezium with its vertices on the (ii) circumference of a circle.

> Determine any geometrical facts about RSTU and prove that these are true for all such trapeziums.

Justify your answers with clear geometric reasoning.

& trapeziums have 2 Lines that are parallel ST is parallel to Ry



The plane then heads directly to airstrip D, which is 135 km due north of its starting point at airstrip A.

For the final leg of the flight path of the plane, how far does it need to fly, and what is the bearing of the final leg of the flight path?

LCB A = 130° co-int L's // lines.

\$\frac{47}{97} + \b^2 \\

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The plane flys 69.42km on me lost leg of its or ght.

Z SOA Sin 2 = 60.2A 30.6 Z = Sin (22.2A)

COS 50 = 2 × 4

EAH

AH AC

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