L2-MATHMF







Te Pāngarau me te Tauanga, Kaupae 2, 2014

2.00 i te ahiahi Rāapa 19 Whiringa-ā-rangi 2014

PUKA TIKANGA TĀTAI

mō 91261M, 91262M, 91267M

Tirohia tēnei pukaiti hei whakautu i ngā pātai o ō pukapuka Whakautu, Pātai hoki.

Tirohia mehemea kei roto nei ngā whārangi 2–3 e raupapa tika ana, ā, kāore hoki he whārangi wātea.

KA TAEA TĒNEI PUKA TE PUPURI HEI TE MUTUNGA O TE WHAKAMĀTAUTAU.

Whārite pūrua

Mēnā
$$ax^2 + bx + c = 0$$

kāti $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
ā $\Delta = b^2 - 4ac$

Taupū kōaro

Mēnā
$$y = b^x$$
 kāti $x = \log_b y$
 $\log_b (x^n) = n \log_b x$
Mēnā $y = e^x$ kāti $x = \log_e y (= \ln y)$

Tuanaki

$$\frac{\mathrm{d}}{\mathrm{d}x}\left(x^{n}\right) = nx^{n-1}$$

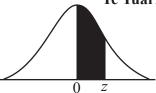
$$\mathrm{M\bar{e}n\bar{a}} f'(x) = x^{n}, \, \mathrm{k\bar{a}ti} \, f(x) = \frac{x^{n+1}}{n+1} + c$$

Tūponotanga

$$z = \frac{x - \mu}{\sigma}$$

2

Te Tuaritanga Hangarite Aro Whānui



$$\left(z = \frac{x - \mu}{\sigma}\right)$$

Ko ia tau e whakaatu ana i te tūponotanga ka noho mai te taurangi matap \bar{o} kere hangarite aro wh \bar{a} nui o te Z ki waenganui i te 0 me te z. Huatango

					wachganari te o me te z.							Huatango							
z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
0.0	0000	0040	0080	.0120	0160	0199	0239	0279	0319	0359	4	8	12	16	20	24	28	32	36
0.1				.0517							4	-	12		20				36
	1			.0910							4		12		19				35
0.2	1			.1293							4		11		19				34
0.3	1			.1664							4		11		18			29	
											+			14	10	22	23	29	32
0.5	1			.2019							3		10		17			27	-
0.6				.2357							3		10		16	-		26	-
0.7	1			.2673							3	6	9		15			24	
0.8				.2967							3	6	8		14		-	22	
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389	3	5	8	10	13	15	18	20	23
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	2	5	7	9	12	14	16	18	21
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	2	4	6	8	10	12	14	16	19
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015	2	4	5	7	9	11	13	15	16
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177	2	3	5	6	8	10	11	13	14
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319	1	3	4	6	7		10	11	13
1.5	1332	1315	1357	.4370	1382	1391	1106	1/118	1120	4441	1	2	4	5	6	7	Q	10	11
1.6	1			.4484							1	2	3	4	5	6	7	8	9
1.0				.4582							1	2	3	3	4	5	6	7	
1.8	1			.4664							1	1	2	3	4	4	5	6	
1.9	1			.4732							1	1	2	2	3	4	4	5	
											1	•	_	_			-		
2.0				.4788							0	1	1	2	2	3	3	4	
2.1				.4834							0	1	1	2	2	2	3	3	4
2.2	1			.4871							0	1	1	1	2	2	2	3	3
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916	0	0	1	1	1	2	2	2	2
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936	0	0	1	1	1	1	1	2	2
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	0	0	0	1	1	1	1	1	1
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	0	0	0	0	1	1	1	1	1
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	0	0	0	0	0	1	1	1	1
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981	0	0	0	0	0	0	0	0	1
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986	0	0	0	0	0	0	0	0	1
3.0	1987	1087	1027	.4988	1088	1080	1080	1080	1990	1990	0	0	0	0	0	0	0	0	0
3.1				.4991							0	0	0	0	0	0	0	0	
3.2				.4994		–					0	0	0	0	0	0	0	0	
3.3				.4996							0	0	0	0	0	0	0	0	
3.4				.4997							0	0	0	0	0	0	0	0	
											ľ								
3.5				.4998							0	0	0	0	0	0	0	0	
3.6				.4999							0	0	0	0	0	0	0	0	
3.7				.4999							0	0	0	0	0	0	0	0	
3.8				.4999							0	0	0	0	0	0	0	0	-
3.9	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	0	0	0	0	0	0	0	0	0

Quadratics

If
$$ax^2 + bx + c = 0$$

then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
and $\Delta = b^2 - 4ac$

Logarithms

If
$$y = b^x$$
 then $x = \log_b y$

$$\log_b (x^n) = n \log_b x$$
If $y = e^x$ then $x = \log_e y (= \ln y)$

Calculus

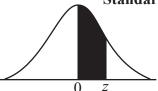
$$\frac{\mathrm{d}}{\mathrm{d}x}\Big(x^n\Big) = nx^{n-1}$$

If
$$f'(x) = x^n$$
, then $f(x) = \frac{x^{n+1}}{n+1} + c$

Probability

$$z = \frac{x - \mu}{\sigma}$$

_ Standard Normal Distribution



3

$$\left(z = \frac{x - \mu}{\sigma}\right)$$

Each entry gives the probability that the standardised normal random variable Z lies between 0 and z.

Differences

												Differences							
Z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
0.0	0000	0040	0080	.0120	0160	0199	0239	0279	0319	0359	4	8	12	16	20	24	28	32	36
0.1				.0517							4	-	12	-	20		-	32	
0.2	1			.0910							4	-	12		19		-	31	
0.3				.1293							4		11	-	19			30	
0.4	1			.1664							4		11		18			29	
0.5	.1915	1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224	3	7	10	14	17	21	24	27	31
0.6	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549	3	6	10		16		23	26	29
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852	3	6	9	12	15	18	21	24	27
0.8				.2967							3	6	8		14			22	
0.9	1			.3238							3	5	8		13			20	
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	2	5	7	9	12	14	16	18	21
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	2	4	6	8	10	12	14	16	19
1.2				.3907							2	4	5	7	9	11	13	15	16
1.3				.4082							2	3	5	6	8	10	11	13	14
1.4				.4236							1	3	4	6	7	8		11	
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441	1	2	4	5	6	7	8	10	11
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545	1	2	3	4	5	6	7	8	9
1.7				.4582							1	2	3	3	4	5	6	7	8
1.8	l .			.4664							1	1	2	3	4	4	5	6	6
1.9				.4732							1	1	2	2	3	4	4	5	5
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817	0	1	1	2	2	3	3	4	4
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857	0	1	1	2	2	2	3	3	4
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890	0	1	1	1	2	2	2	3	3
2.3				.4901							0	0	1	1	1	2	2	2	2
2.4				.4925							0	0	1	1	1	1	1	2	2
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	0	0	0	1	1	1	1	1	1
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	0	0	0	0	1	1	1	1	1
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	0	0	0	0	0	1	1	1	1
2.8	4974	4975	4976	.4977	4977	4978	4979	4979	4980	4981	0	0	0	0	0	0	0	0	1
2.9				.4983							0	0	0	0	0	0	0	0	1
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990	0	0	0	0	0	0	0	0	0
3.1	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993	0	0	0	0	0	0	0	0	0
3.2	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995	0	0	0	0	0	0	0	0	0
3.3	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997	0	0	0	0	0	0	0	0	0
3.4	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998	.4998	0	0	0	0	0	0	0	0	0
3.5	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	0	0	0	0	0	0	0	0	0
3.6	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	0
3.7	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	0	0	0	0	0	0	0	0	0
3.8	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.5000	.5000	.5000	0	0	0	0	0	0	0	0	0
3.9				.5000							0	0	0	0	0	0	0	0	0
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English translation of the wording on the front cover

Level 2 Mathematics and Statistics, 2014

2.00 pm Wednesday 19 November 2014

FORMULAE SHEET for 91261, 91262, 91267

Refer to this sheet to answer the questions in your Question and Answer booklets.

Check that this booklet has pages 2–3 in the correct order and that none of these pages is blank.

YOU MAY KEEP THIS SHEET AT THE END OF THE EXAMINATION.