Exercises Higher Order Functions

This exercise sheet is all about higher order functions (functions that take functions as a parameter), the most important ones that you will get to understand are `map, filter, foldr, foldl`, and along with them you will sometimes have to use lambda functions. At the time of writing, there are no exercises explicitly for practicing lambdas.

1 It begins

1.1 Map

`map` is often used in conjunction with a function that makes some transformation on an element. Use `map` to solve the following exercises. When a helper function is needed, you can write a function like normal or use a lambda function.

- Get a list of square roots, from a list of numbers.

- Get a list of lengths, from a list of strings.

- Add your favorite number to a list of numbers.

- Double the numbers in a list unless they exceed some threshold.

- Given a list, make a list of lists (each element is its own list).

- Using `fizzbuzz` from the second exercise sheet (if you made it), make a list of the first few (e.g. 20) "numbers" in FizzBuzz.

1.2 Filter

Remember that `filter` keeps the elements that match the predicate, rather than exclude them. Use `filter` to solve the following exercises.

- Get a list of numbers below some threshold, from a list of numbers.

- Come up with your own function that returns a bool and use it with `filter`.

- Recreate quicksort.

- Make a function that given a number finds all the positive integers that are a factor of it (evenly divides it).

    - Use it to make a naïve `isPrime` function.

1.3 Fold

To better understand what `foldr` and `foldl` does, try expanding the following expressions by hand, according to the pseudo definitions:

```
foldr f z [x1, x2, ..., xn] == x1 'f' (x2 'f' ... (xn 'f' z)...)
foldl f z [x1, x2, ..., xn] == (...((z 'f' x1) 'f' x2) 'f'...) 'f'
xn
```

- `foldr (||) False [False, True, False]`

- `foldl mod 1337 [1166, 86, 43]`

Now try to use `foldr` or `foldl` to solve the following exercises.

- Make your own `sum` function.

- Make your own `maximum` function, you may use `max`. Hint: assume numbers are $>= 0$.

- Make your own `reverse` function. Hint: use `flip`.

- Make `last` using `foldl1`.

The following is an attempt to make a function `isSorted` that checks if a list is sorted:

```
isSorted ls = foldr1 (<=) ls
```

but using it throws an error. Why is that? What should it do instead? Implement it.

For an additional challenge try to implement it in one line (it need only work for lists with at least 2 elements). Hint: One way is to at least use a combination of `foldr, map, zip, tail` and a lambda function. Another solution combines the functionality of the `map, zip` and lambda, in `zipWith`.

2 Modules Beginning

If you haven't already, start reducing the amount of parentheses you use, by instead using function composition and application (the '.' and '$').

2.1 Usage

Make a function that checks whether a string contains all the letters of the English alphabet. Import `Data.Char` to get the function `toLower :: Char -> Char`. For the string `"The quick brown fox jumps over the lazy dog"` it should return `True`.

Make yet another version of quicksort using `partition` from `Data.List`.

Make a `length` function using a fold.

Make an `elem` function using a `map` and a fold. Remake it using `any`.

Use `takeWhile` to find out how many numbers that squared are less than some threshold.

Use `find` and `elemIndices` to find a string with, for example more than 5 e's, in a list of strings.

2.2   (Dis-)Qualified

Complete the previous exercise in a file if you haven't already.

- Write your own `partition` function, and make sure it is not being imported from `Data.List`.

- Import `find` and `elemIndices` explicitly.

    - Make the imports qualified and update your program accordingly.

2.3   Define your own

Export some of your cool new functions as a module. Note: you should use the same name for your file as your module, e.g. you export a module `MyFuncs`, that file should be named `MyFuncs.hs`.

Import and use your functions in another file. If you named your files correctly, you should be able to something like `import MyFuncs`.

3   Your own types

It's time to start making your own types, here are some ideas for some types you can make, but you are welcome to try something else if you want. Remember to go read in LYH if you forgot something.

3.1   Shapes

Go through the shapes example in LYH.

A shape is either a cirle or a rectangle.

- Circles are defined by x and y coordinates and a radius.

- Rectangles are defined by their upper left corner and lower right corner.

- Optional: Update so points are represented by their own class.

- Make functions that calculate the surface area of a shape.

- Make functions that move the shapes around.

- Come up with other things to do with shapes.

3.2 Students

A student has: name, exam number, list of enrolled courses, list of grades.

- Make the value constructor.

- Make functions that can add or remove courses from the enrolled list.

- Make a function to add a grade.

  - Optional: Only allow grading for courses already enrolled.

3.2.1 Persons

Rather than students directly, make a class for persons.
A person has a name, gender and age.

- Make gender a type similar to `Bool`, choose whatever genders you like.

- Replace name with person in student, and update the program accordingly.

- Make some functions for persons, e.g. greetings based on name, gender and/or age.

- Update the constructors for students and persons with record syntax

- Come up with more functions to use on students and/or persons. E.g.:

  - Given a list of persons, return a list of persons with voting rights.

  - Given a list of students, return a list of students with at least some average grade.

    * Make courses into a type as well, where courses have a name and a weight. Update the average to take the weight into account.