Exercises Higher Order Functions

This exercise sheet is all about higher order functions (functions that take functions as a parameter), the most important ones that you will get to understand are map, filter, foldr, foldl.

1 It begins

map is often used in conjunction with a function that makes some transformation on an element. Use map to solve the following exercises, possibly using a helper function.

- Get a list of square roots, from a list of numbers.
- Get a list of lengths, from a list of strings.
- Add your favorite number to a list of numbers.
- Double the numbers in a list unless they exceed some threshold.
- Given a list, make a list of lists (each element is its own list).
- Using fizzbuzz from the second exercise sheet (if you made it), make a list of the first few (e.g. 20) "numbers" in FizzBuzz.

Remember that filter keeps the elements that match the predicate, rather than exclude them. Use filter to solve the following exercises.

- Get a list of numbers below some threshold, from a list of numbers.
- Come up with your own function that returns a bool and use it with filter.
- Recreate quicksort.

To better understand what foldr and foldl does, try expanding the following expressions by hand, according to the pseudo definitions:

```
foldr f z [x1, x2, ..., xn] == x1 'f' (x2 'f' ... (xn 'f' z)...) foldl f z [x1, x2, ..., xn] == (...((z 'f' x1) 'f' x2) 'f'...) 'f' xn
```

• foldr (||) False [False, True, False]

• foldl mod 1337 [1166, 86, 43]

Now try to use foldr or foldl to solve the following exercises.

- Make your own sum function.
- \bullet Make your own maximum function, you may use max. Hint: assume numbers are >=0.
- Make your own reverse function. Hint: use flip.